

# **Diminishing America's Demographic Dilemma Through Pre-Funding Social Security**

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**Abstract.** Financing Social Security benefits at current levels implies significant increases in payroll taxes within the next 20 years under current U.S. demographic developments. Using a general-equilibrium overlapping-generations model with realistic patterns of fertility and lifespan extension, this study shows that future generations would be harmed during the demographic transition due to rising payroll taxes and declining real wages. A faster rate of technological progress would mitigate only some of the payroll tax increase and would not prevent the decline in real wages. Addressing the problem by reducing Social Security benefits as needed or by raising the eligibility age imposes major welfare losses on current or near term retirees. By contrast, pre-funding Social Security through consumption taxes more evenly spreads the welfare losses across generations, and it helps future generations, especially the poor, by stimulating capital formation.

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## 1. Introduction

How will the United States economy fare in 30 years when 77 million baby boomers will have retired? By that time, twice the number of elderly will rely on only 15 percent more workers for financial support primarily delivered through Social Security and Medicare.

Based on “intermediate” economic and demographic assumptions, the government’s Trustees project that Social Security is one-fifth short of the resources needed to pay benefits over the next 75 years. These estimates, though, understate the long-run problem: extending the projection horizon beyond 75 years triples the present value shortfall.<sup>1</sup> Medicare, which provides health care to retirees, faces even larger long-run shortfalls.<sup>2</sup> Eliminating the imbalances in both programs beyond the 75-year horizon and without reducing benefits would require doubling the payroll taxes levied on employees and employers, thereby reducing labor supply incentives.

These demographic forecasts, however, are partial equilibrium calculations and, therefore, may miss important general equilibrium effects during the demographic transition. An aging society could theoretically lead to capital deepening and, therefore, higher real wages as the number of retirees with capital rises relative to the number of workers supplying labor (Auerbach et al., 1989; Bohn, 2001). Higher real wages could then limit the payroll tax increases necessary to balance Social Security. However, capital deepening is not guaranteed since the larger payroll taxes themselves also reduce the potential for saving.

Using a new general-equilibrium life-cycle model, this paper analyzes the economic impact of demographic changes and explores the economic and welfare impact of potential

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<sup>1</sup> See the 2004 Social Security Trustees’ Report, Table IV.B7.

<sup>2</sup> See the 2004 Medicare Trustees’ Report, Table II.B11, Table II.C16, and Table II.C22.

reforms. This study builds on the literature that followed Feldstein's (1974) article contending that Social Security lowers national saving, including Kotlikoff (1979), Auerbach and Kotlikoff (1983), and Seidman (1986). More recent papers have considered the importance of land, earnings uncertainty, political economy considerations, liquidity constraints and different options for funding Social Security. These studies include Hubbard and Judd (1987), Imrohoroglu, Imrohoroglu, and Joines (1995, 1999), Kotlikoff (1996), Huang, Imrohoroglu, and Sargent (1997), Huggett and Ventura (1998), Cooley and Soares (1999a, 1999b), De Nardi, Imrohoroglu, and Sargent (1999), Kotlikoff, Smetters and Walliser (1998a, 1998b, 1999, and 2002), Raffelhüschen (1989, 1993), Bohn (2001) and Smetters and Walliser (2004).

While the model herein builds on the model of Auerbach and Kotlikoff (1987), it adds five critically important features for studying the impact of demographic changes: i) more realistic demographics that allows the model to better capture the population-age distribution and distribution of bequests; ii) cohort-specific longevity to reflect the important impact of rising longevity on the age distribution; iii) multiple earnings groups within each cohort to capture the impact that reforms have on different lifetime income groups;<sup>3</sup> iv) the ability to simulate the model from non steady-state initial conditions in order to start the simulations with the prevailing age distribution; and v) a close calibration of the model to U.S. fiscal conditions and institutions.

The paper by De Nardi, Imrohoroglu, and Sargent (1999) is the closest antecedent to ours. Their model includes demographic change as well as idiosyncratic shocks to earnings and longevity. It is limited, though, to quadratic preferences, omits most of the other US tax and transfer programs, lacks intra-generational heterogeneity as well as consumption by children, and

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<sup>3</sup> Intra-generational heterogeneity was also included in Fullerton and Rogers's (1993) important study of fundamental tax reform.

distributes all bequests at the beginning of adulthood. Their baseline simulation, like ours, shows a major increase over time in payroll tax rates. But their long-run payroll tax increase is much larger, and in contrast to our work they generate some modest long-run capital deepening.

Under our baseline simulation where taxes rise to maintain Social Security benefits, macroeconomic conditions exacerbate rather than mitigate fiscal problems. Lower wages require other taxes to rise to maintain discretionary spending. A faster rate of technical progress relative to our baseline would expand the wage base at a faster rate and somewhat reduce payroll tax increases. But it would still leave a major problem under current law because Social Security benefits at retirement are linked to average wage growth and thus grow with productivity.

As an alternative to increasing tax rates, we consider several reforms including reducing benefits as needed over time as well as increasing the retirement age. Our simulations show that these potential reforms impose major welfare losses on current or near term retirees. We also simulate pre-funding Social Security by paying off the liabilities accrued under the existing system with a tax levied on either wages or consumption. While pre-funding is far from being a free lunch for living generations, it spreads the pain more evenly than the other options and entails major welfare gains for future generations, particularly those with very low incomes.

The paper is organized as follows. Section 2 presents our model and calibration, paying particular attention to how we incorporate fertility and lifespan extension. Section 3 presents our baseline simulations under the demographic transition as well as the macroeconomic results from different potential reforms including reducing scheduled benefits over time as well as pre-funding Social Security. The welfare implications of these reforms across generations and between income classes within generations are then discussed in Section 4. Section 5 concludes.

## 2. The Model

This section describes our model as well as its calibration and solution method. Our life-cycle general equilibrium model builds, in part, upon the stationary-demographics model of Altig et al. (2001) that focused on tax reform. Since our federal tax system and production sector are same as in Altig et al., we provide only a brief sketch of those sectors. We instead focus our description on how we incorporate more-realistic demographics into the model.

### 2.1. The Household's Problem

#### 2.1.1. Preferences

Following Fullerton and Rogers (1993) and Altig et al. (2001), we sort households into 12 “full lifetime” earnings classes, that is, by the present value of lifetime income if households worked the maximum time allotment throughout their lifetime. Income groups 1 and 12 comprise the bottom and top two percent of lifetime wage income earners, respectively, while groups 2 and 11 represent the remaining eight percent of the top and bottom deciles. Income groups 3 - 10 cover the remaining population with each group representing one decile.

The household representing lifetime income class  $m$  becomes an independent economic actor at age 21 and maximizes utility over its lifespan extending to age  $d$ .<sup>4</sup> Lifetime utility is derived from (i) parents' lifetime consumption vector,  $c_p$ , and lifetime leisure vector,  $l_p$ ; (ii) the consumption and leisure vectors of children,  $c_k$  and  $l_k$ , below age 20 residing with their parents; and (iii) a bequest  $b^m$  per child. Household utility is additive with  $V(\cdot)$ ,  $H(\cdot)$ , and  $Z()$  representing the sub-utility functions for consumption and leisure by parents and children, and from bequests:

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<sup>4</sup> As described later in the calibration section, the lifespan,  $d$ , is indexed to the cohort's birth year in order to account for improvements in mortality. We don't show the time index on variables to avoid unwieldy notation.

$$(1) \quad U^m = V(c_p^m, l_p^m) + H(c_k^m, l_k^m) + Z(b^m)$$

To closely represent the actual heterogeneity in parental ages within a cohort, we assume that the household representing that cohort has “fractional children” of varying ages. We define a function “kid weight,”  $kw(i, j)$ , as the fraction of children of age  $i \in [1, 20]$  with a parent age  $j$ . For example, if  $kw(7, 35) = 0.05$ , 5 percent of seven year-olds have parents who are age 25. We also assume that children must be at least 20 years younger than their parents and that parents older than 45 do not give birth to more children, which makes some kidweights equal to zero.

The sub-utility functions for adults and children are specified as constant elasticity of substitution (CES), where  $\rho$  represents the intratemporal elasticity of substitution between consumption and leisure,  $\gamma$  represents the intertemporal elasticity of substitution,  $\alpha$  gives the weight on leisure, and  $\delta$  is the pure rate of time preference:

$$(2) \quad V(, ) = \frac{1}{1 - \frac{1}{\gamma}} \sum_{j=21}^d \left( \frac{1}{1 + \delta} \right)^{j-21} \left[ c_{p,j,m}^{1-\frac{1}{\rho}} + \alpha l_{p,j,m}^{1-\frac{1}{\rho}} \right]^{\frac{1-\frac{1}{\gamma}}{1-\frac{1}{\rho}}}$$

and

$$(3) \quad H(, ) = \frac{1}{1 - \frac{1}{\gamma}} \sum_{j=21}^d \left( \frac{1}{1 + \delta} \right)^{j-21} \sum_{i=1}^{20} \phi_i kw(i, j) \frac{P(i)}{P(j)} \left[ c_{k,i,m}^{1-\frac{1}{\rho}} + \alpha l_{k,i,m}^{1-\frac{1}{\rho}} \right]^{\frac{1-\frac{1}{\gamma}}{1-\frac{1}{\rho}}}$$

The CES formulation allows for varying consumption-leisure shares over the life cycle and more realistic labor supply elasticities. However, it does not accommodate simple analytical solutions.

The utility a parent enjoys from children is the sum of the welfare of all the children living in a parent's household at each age of the parent.  $\phi_i$  is the adult-equivalency scale for age- $i$

children and  $P(i)$  is the size of cohort aged  $i$ . Children's consumption is expressed in per-capita terms of adults by correcting children's consumption by the ratio of children to adults,  $P(i)/P(j)$ .

The utility for bequests is derived as the sum of utility derived from bequests made to all "fractional" children at the end of life, expressed in per-capita terms of the bequeathing cohort:

$$(4) \quad Z( ) = \left( \frac{1}{1+\delta} \right)^{d-21} \left( \sum_{i=21}^d kw(i,d) \frac{P(i)}{P(d)} \right) \mu^m [b^m]^{1-\frac{1}{\gamma}},$$

where  $\mu$  is the preference for bequests differing by income. We assume that each cohort aged  $j$  receives a share of these bequests per capita that is equal to its weight  $kw$  of the children of the dying cohort. Smoothing the receipt of bequests throughout the life-cycle instead of concentrating them at a single point in time allows for a more plausible life-cycle distribution of assets. Bequests are assumed to be passed to members of the same lifetime income group.

### 2.1.2. Budget Constraints

Lifetime utility maximization by a 21 year-old born in year  $t$  is subject to the following budget constraint (where, again, we do not subscript variables by time for notational simplicity):

$$(5) \quad \begin{aligned} & \sum_{j=21}^d [w_{j,m}(E-l_{p,j,m}) - c_{p,j,m} - T_{j,m}] \prod_{s=1}^{j-21} \frac{1}{1+r_{t+s-1}} \\ & - \sum_{j=21}^d \sum_{i=1}^{20} \left( kw(i,j) \frac{P(i)}{P(j)} c_{k,j,m} \right) \prod_{s=1}^{j-21} \frac{1}{1+r_{t+s-1}} \\ & + \sum_{j=21}^d kw(j,d) b^m \prod_{s=1}^{j-21} \frac{1}{1+r_{s-1}} \\ & = b_d^m \sum_{i=21}^d kw(i,d) \frac{P(i)}{P(d)} \prod_{j=1}^{d-21} \frac{1}{1+r_{j-1}} \end{aligned}$$

The first term in equation (5) includes the present value of the household's labor income derived from total time endowment  $E$  net of leisure  $l$ , multiplied with wage rates  $w$ . We have implicitly assumed that a child's prospective wage rate is zero and, hence, does not work. The variable  $r$  is the interest rate. This budget constraint says that the present value of labor income and all bequests a household receives over the lifetime (the third line of the budget constraint) must pay for parental consumption  $c_{p,j,m}$  and net tax payments  $T_{j,m}$  (first line), consumption by children  $c_{p,j,m}$  (second line), and bequests  $b_d^m$  left to decedents (right hand side of the budget constraint). Net taxes  $T$  include consumption, capital income, labor income, and net social insurance taxes as well as old-age transfers. As discussed below, factor prices, taxes, and benefits levels are derived from general equilibrium conditions and the government's budget constraint.

### 2.1.3. Calibration of Preferences

In line with the previous literature, the pure time preference rate,  $\delta$ , is set to .02, and the intratemporal and intertemporal substitution elasticities,  $\rho$  and  $\gamma$ , are set to .4 and .25, respectively. The parameter  $\alpha$  is chosen so that agents devote, on average, 40 percent of their available time endowment (16 hours per day) to labor during their prime working years (ages 21-55). As discussed by Altig et al. (2001), these parameter choices generate a Frisch elasticity of labor supply (MaCurdy, 1981) of 0.465, which is in line with the labor supply literature.<sup>5</sup> The bequest parameters  $\mu^j$  are for each earnings class  $j$  are calibrated such that the ratio of the bequest to economy-wide mean income corresponds to the ratio originally estimated by Menchik and David (1982), as updated by Fullerton and Rogers (1993), and inflation-adjusted to the year 2000. Bequests range from \$20,000 to \$450,000 for earnings group eight through group twelve.

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<sup>5</sup> See Browning, Hansen, and Heckman (1998), Blundell, Meghir and Neves (1993), Mulligan (1998), and Ziliak and Kniesner (1999).

## 2.2. Technological Change

Given our use of flexible CES preferences, the standard assumption of labor-augmenting technological change is not compatible with reaching a steady state. In particular, households' demand for leisure would increase across cohorts, eventually exceeding the time endowment. As discussed in Auerbach et al. (1989), we therefore use a different type of labor-augmenting technological change by assuming that technical progress causes the time endowment of each successive generation to grow at rate  $\lambda$ . This increasing endowment can be interpreted as a rising human capital endowment that allows agents born later in time to reach both higher income and leisure levels. Because the endowment grows at a steady rate, there is no underlying time trend imparted to the economy-wide real wage per unit of human capital at time  $t$ ,  $w_t$ .

## 2.3. Wage Profiles

To capture different skills by age and lifetime income group we apply an efficiency parameter  $\epsilon_j^m$  to the basic wage rate  $w_t$ . The wage rate for an agent of type  $m$  and age  $j$ ,  $w_{j,m,t} = \epsilon_j^m w_t$ , is determined through the following function:

$$(6) \quad \epsilon_j^m = e^{a_0^m + a_1^m j + a_2^m j^2 + a_3^m j^3} (1 + \lambda)^j h_j$$

with parameters  $a_1$  to  $a_3$  fitted from panel data as described in Altig et al. (2001). Secular growth in real wages, not captured in  $a$ , is explicitly added through the technological growth factor  $\lambda$ . We assume a 1 percent value for  $\lambda$ , the rate of technological change consistent with long-run patterns for the US. By introducing equal growth in the lifetime time endowment and in real wages over the life cycle we replicate two key features of traditional labor-augmenting technical

change: in steady state, real lifetime earnings grow at the rate of technical change, and the age-wage profile is steepened by this same rate of technical change. The final factor determining real wage growth in equation (6) is the variable  $h_t$ , an old-age productivity factor that helps generate realistic old-age labor supply by reducing productivity at age 62 (sensitivity analysis is performed in Section 3). Wage rates derived from equation (6) result in peak hourly wages valued in 2000 dollars of \$4.00, \$14.70, and \$79.50 for individuals in lifetime income classes 1, 6, and 12, respectively, generating annual incomes between \$9,000 and \$130,000.

#### 2.4. *Government*

Government in our model collects taxes and issues debt to finance government purchases of goods and services at time  $t$  ( $G_t$ ), interest payments on the existing stock of debt, and old-age and disability transfers. Government goods and services are assumed to be unproductive and generate no utility to households.<sup>6</sup> Per capita values of government purchases and government debt are held constant throughout our simulations, and income tax rates are adjusted endogenously to finance these expenditures.

##### 2.4.1. *Tax system*

Our benchmark tax system approximates the salient features of the 2000 U.S. federal, state, and local tax system, as described in Altig et al. (2001). It features separate wage and capital income taxes, and a consumption tax, with an adjustment of the tax bases to capture tax evasion. Including the federal tax system is important because reforms to Social Security will influence the size of the various tax bases – and hence the tax rates – required to finance  $G$ .

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<sup>6</sup> Since  $G$  remains fixed in all of our experiments, incorporating  $G$  into the utility function is unimportant.

\_\_\_\_\_The wage-income tax structure has four elements: i) a progressive marginal rate structure based on the 2000 federal statutory tax rates for individuals; ii) a standard deduction of \$4000 and exemptions of \$5660 (assuming about 1.2 children per agent, consistent with population growth assumption); iii) using estimates from the *Statistics of Income*, an approximation of itemized deductions which are applied only when they exceed the amount of the standard deduction; and iv) adjustments to earnings-ability profiles to reflect non-pension components of labor compensation consistent with tax return data. The marginal (average) labor income tax rates of 24 (14) percent and 18 (11) percent generated by the model for the highest and average income group, respectively, are close to empirical estimates.

Based on Auerbach (1996), the capital income tax rate is set at 20 percent and 20 percent of new capital may be expensed, generating a 16 percent effective tax rate on new capital. In addition to the federal taxation, capital and wage income are subject to a linear state income tax of 3.7 percent, which produces the correct share of total revenue raised at the state level in 2000.

We impose an 8.8 percent tax on consumption expenditures consistent with the level of business and excise taxes in the national accounts. However, because contributions to both defined benefit and defined contribution pension plans receive consumption tax treatment, we levy an additional 2.5 percent tax on household consumption expenditures to account for the consumption-tax treatment of labor compensation in the form of pension benefits (Auerbach, 1996). This 2.5 percent tax replaces the wage tax that otherwise would apply to the pension benefit component of labor compensation, which is not included in our wage tax base.

#### 2.4.2. *Social Security, Medicare, and Disability*

The model closely reflects US old-age and social insurance system programs, notably

Old-Age and Survivors Insurance (OASI), Disability Insurance (DI), and Medicare (HI). OASI, is a defined-benefit program that pays pension income to retirees and their survivors based on a progressive benefit formula. In particular, OASI determines each retiree's level of retirement benefits based on a measure of average indexed monthly earnings (AIME) over a 35-year work history subject to a wage ceiling. Wages exceeding this ceiling are not counted as contributions nor reflected in benefits. The AIME is converted into a primary insurance amount according to a progressive bend-point formula that determines initial monthly pension payments.

The model closely reproduces these settings by generating a model-based AIME that indexes past covered earnings to the growth in the economy-wide real wage per unit of human capital. In doing so, it excludes earnings above the model's maximum taxable earnings. Pension benefits in the model replace between 25 and 75 percent for the lifetime richest and lifetime poorest, respectively. Since approximately 50 percent of OASI benefits are paid to survivors and spouses, we multiply benefits by a factor of two. The model also reflects the fact that Social Security's eligibility age will slowly increase from 65 to 67 over time under current law. Finally, in our simulations of different policies, we adjust OASI benefits for changes in consumption tax rates, reflecting the fact that they are indexed to consumer price inflation.

Medicare and disability insurance are modeled in a straightforward way. Medicare benefits accrue as a fixed benefit to all households above the Medicare eligibility age. The total Medicare bill thus fluctuates with the size of the elderly population. Should demand for medical care rise faster than the number of eligible households, our model could underestimate the economic effects generated by Medicare's imbalance in the long run. Similarly, disability is modeled as a fixed benefit to the households below the eligibility age for OASI benefits. To

finance the government's transfer programs, we distinguish between OASI, DI, and HI payroll taxes. The annual values for the payroll tax rates are determined endogenously to finance the aggregate value of the benefits paid by each of these programs. Households in our model understand the link between the OASI payroll tax and future benefits. As a result, the effective marginal tax rate on OASI contributions is less than the statutory rate, and it differs by age and income class, except for agents with earnings above the taxable ceiling who face a zero marginal tax.<sup>7</sup> DI and HI taxes are pure wage taxes since their future benefits are not linked to contributions. DI is levied on payroll below the taxable ceiling whereas HI is levied on all earnings.

## 2.5. *Demographics*

We calibrate the model's demographics using population data and projections from the Social Security Administration. An initial population-age distribution is used to fill  $P(i)$  for the year in which we start our projections. Projected birth rates are then used to fill  $P(i)$  for future years. The distribution of births among living generations is used to calibrate the kidweight function  $kw$ , which we assume to stay constant over time. The Social Security population projections extend through 2075, after which we assume birth rates stabilize. The life expectancy,  $d$ , is estimated using the Social Security Administration's unisex life expectancy table conditional on reaching age 65. Life expectancy equals 82 for the initial year 2000 and,

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<sup>7</sup> In particular, young households face relatively larger effective tax rates on their contributions since the difference between market interest rate and Social Security's lower internal rate of return is compounded over many years. Households in higher income classes also face larger effective tax rates due to the progressivity of benefits.

based on Social Security's projections, increases to 83 by 2010, 84 by 2030, and 85 by 2060.<sup>8</sup>

Table 1 compares our model's predicted population totals as well as population shares with those forecast by the Social Security Administration. Our population totals line up quite well over the next 30 years, but understate projected population growth thereafter. In 2030, the model predicts there will be 22.8 percent more Americans alive than are now living. The comparable Social Security figure is 22.6 percent. The model also does a very good job tracking population shares. In 2075, the model predicts that 23 percent of the population will be 65 and older – the same share predicted by Social Security. In that year the model's and Social Security's predicted shares of those under age 20 differ by only 1 percentage point. Note that the U.S. population is predicted by both Social Security and our model to get old and stay old. Thus, unless policy is changed, the economic implications of America's aging will be here to stay.

Since we begin our simulations during a transition rather than from a steady state, our model requires an initial level and distribution of assets by age and earnings class. To obtain these initial conditions, we calculated the average net worth by age of household head in the 1998 Survey of Consumer Finances. The asset profile for the 12 earnings classes is then derived by assuming net assets are proportional to lifetime incomes, as approximated with earnings at age 40. We scale this initial allocation of net worth by age and earnings class by a constant factor until the model produces a realistic year-2000 national saving rate.

## 2.6. *Production*

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<sup>8</sup> As discussed by Fullerton, Coronado and Glass (2002), assuming all members of a given cohort die at the expected age of life misses some of the redistributive properties of Social Security arising (i) from lower-income households with shorter life expectancy offsetting to some extent the progressive benefit formula and (ii) from the provision of survivor and children's benefits as well as the dispersion of death dates.

We assume that output (net of depreciation) is produced by identical competitive firms using a standard Cobb-Douglas production function, with a capital coefficient equal to 0.25. The aggregate supply of capital at a point in time is obtained from summing over individual asset holdings less the value of government debt. The aggregate supply of labor at each point in time is calculated by summing together the effective labor supplies of all agents, given by the time endowment less leisure, multiplied by the efficiency parameter calculated from equation (6).

## 2.7. *General Equilibrium and Solution Method*

Starting from the initial calibration of the economy, the model uses a Gauss-Seidel algorithm to solve the perfect foresight general-equilibrium transition path to a new steady state over a period of 275 years. The calculation starts with a guess for the time-paths of the aggregate supplies of capital and labor (and thus factor prices) and then iterates on those variables until a convergence criterion is met. Factor price time-paths in conjunction with time-paths of tax rates (including payroll taxes) and certain shadow prices determine the household sector's supplies, over time, of labor and capital. Household choices are derived from first-order conditions of the utility function subject to budget constraints. In optimizing household choices, the model includes the constraint that leisure not exceed the endowment of time and solves the problem of the kinked budget constraint arising from standard deductions from taxable income.<sup>9</sup> We also address the non-convexity in the budget constraint due to the maximum taxable earnings for OASI and DI taxes by simply assuming that earnings groups 8 through 12 face no marginal payroll tax on their labor supply, but only an inframarginal payroll tax equal to the payroll tax

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<sup>9</sup> Auerbach and Kotlikoff (1987) derive a complete set of first-order conditions for the utility function used in the KSW model. Altig et al. (2001) describe the strategy for solving the kinked budget constraint.

rate times the payroll tax ceiling. This treatment results in very minor misalignments of marginal tax rates for income groups 7 and 8 at certain ages, without impact on our results.

Although we have no proof for the uniqueness of generated transition paths, Laitner (1984) has proved uniqueness in a linearized version of the original Auerbach-Kotlikoff model for the same utility- and production-function parameter values used herein. Also, we arrive at the same long-run steady state from a wide range of initial conditions.

The initial equilibrium matches key characteristics of the US economy. In addition to demographic characteristics it features a realistic national saving rate of 4.6 percent, a pre-tax return to capital of 7.5 percent, and an aggregate OASDHI payroll tax of 13.7 percent, which is within 0.6 percentage points of the current cost rate for these programs. The capital-output ratio of 3.3 is within the lower range of recent estimates based on market valuations of assets. The model's characterization of the tax system also generates average marginal tax rates and aggregate tax revenues values close to observable figures (see Altig, et al., 2001).

### **3. Macroeconomic Effects of Demographic Transition and Reforms**

This section presents the macroeconomic developments during the demographic transition under our baseline calibration discussed above and explores their sensitivity to changes in assumptions of longevity, productivity in old age, and technological change. We then consider two reforms of the existing pay-as-you-go OASI program that would limit the required increases in the OASI tax rate. Lastly, we analyze policies that fully pre-fund the OASI system, but differ with respect to the method of financing benefits accrued under the old system.

### 3.1. *The Demographic Transition: Baseline Calibration*

The first panel in Table 2 shows how key macroeconomic variables evolve in our base-case transition in which OASDHI tax rates are adjusted through time to finance the benefits of those programs on a strictly pay-as-you-go basis. Note that, due to increases in technological progress, the total *effective* labor supply continues to increase despite the aging of society. By 2030, labor supply is almost 60 percent larger than its initial value; it is projected to grow by only 24 percent absent technological change. However, capital accumulation increases by only 37 percent. Since the capital-labor ratio falls, the real wage in 2030 is 3.7 percent lower than in 2000 and the real return to capital rises by almost 100 basis points. Over the century, real wages decline by almost 9.8 percent, and the return to capital rises by 300 basis points.

One reason for these developments is the presence of the Social Security and Medicare programs. As the last column of Table 2 shows, between 2000 and 2030 the endogenous OASDHI payroll tax projected by the model rises by 77 percent, from 13.7 to 24.3 percent, with most of the increase occurring between 2010 and 2030.<sup>10</sup> This increase is within the vicinity of the 68 percent rise projected by the Social Security Administration (SSA), which does not take into account general equilibrium effects on labor supply and output. In 2075, the model's and SSA's projected cost rates are almost identical.<sup>11</sup> As the payroll tax rises, it significantly reduces the national saving rate and thus the amount of capital accumulation that occurs in these two decades. The payroll tax also stays very high for the rest of the century, reaching 26.5 percent in 2100, and preventing a recovery of saving rates later.

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<sup>10</sup> Recall that our model's 13.7 percent value for the tax rate in 2000 is lower than the actual 15.3 percent OASDHI tax rate because we incorporate payroll taxes in excess of benefit costs as part of general revenue finance.

<sup>11</sup> Recall that our model's 13.7 percent value for the tax rate in 2000 is lower than the actual 15.3 percent OASDHI tax rate because we incorporate payroll taxes in excess of benefit costs as part of general revenue finance.

A second factor that reinforces capital shallowing in our model is the increase over time in general revenue taxation. As previously mentioned, the federal income tax is modeled as a combination of a flat capital income tax, a progressive wage tax, and a flat consumption tax. Along the economy's baseline transition path, we adjust the intercept of the marginal wage tax rate function to generate enough revenue to finance a fixed level of government consumption per capita over time. With shrinking real wages, wage tax rates must rise to maintain government consumption, and the average labor income tax rate (excluding payroll taxes) increases from 11.3 percent in 2000 to 12.3 percent in 2030, further diminishing worker's disposable income.

A third possible reason for capital shallowing is that the economy is not starting its aging process from a stable ratio of capital per effective unit of labor. If, for historic reasons, including past fiscal policy and high asset valuations in 2000, the capital-labor ratio is unusually high, the country may already be embarked on a transition path toward a lower capital-labor ratio.

### 3.2. *The Demographic Transition: Sensitivity Analysis*

Table 3 summarizes the results for varying the baseline assumptions for longevity, productivity in old age, and the rate of technological change. SSA longevity projections tend to be more pessimistic than latest forecasts by demographers. The more optimistic Lee-Carter projection (updated from Lee and Carter, 1992) foresees 65 year-old Americans in 2050 living to age 86 – three years longer than SSA predicts. Using the Lee-Carter assumptions, the payroll tax generated by our model would be 0.6 percentage points higher in 2030 than in our baseline case, and exceed the baseline by 2.6 percentage points in 2100. However, the need to save for a longer

retirement stimulates some additional capital accumulation as well as more labor supply. In the long-run, the economy's capital-labor ratio and real wage are, therefore, essentially unchanged.

Table 3 also shows the effect of assuming that workers remain fully productive through age 65 --by adjusting the productivity factor  $h$  in equation (6) – rather than through age 62 under the baseline. Aggregate labor supply increases by 60.7 percent by 2030 relative to 58.7 percent under the baseline. Young and middle-aged agents, anticipating their longer productive work lives, work less at younger ages, offsetting some of the labor supply increases of older cohorts. Higher productivity in old age also reduces capital accumulation at younger ages and reduces the capital-labor ratio. In 2030, for example, the real wage is 4.2 percent lower than its initial value, compared with 3.7 percent lower in the base case. The slightly higher labor supply and the slightly lower wages essentially offset each other, leaving the payroll tax rate largely unchanged.

Finally, Table 3 shows that doubling of the rate of technological change from one to two percent per year helps mitigate some of the increase in payroll taxes along the transition. This dampening occurs because, while Social Security benefits are wage-indexed before retirement, they are only CPI-indexed after retirement under both current law and in our model. A faster rate of technological change, therefore, increases the size of the tax base relative to aggregate Social Security benefits paid. In 2030, the OASDHI tax rate, for example, is 24.3 percent in the base case, but only 21.7 percent with 2 percent technological progress. The corresponding tax rates in 2100 are 26.5 and 19.7 percent. Still, even under a sustained doubling of technological progress, the payroll tax would have to rise by 6 percentage points by the end of the century. Moreover, capital shallowing still occurs over the transition because the increase in saving does not keep pace with the faster rise in effective units of labor. The real wage per unit of effective labor is

9.1 percent lower than its initial value, not too different from the 9.8 percent in the base case.

### 3.3. *A 50-Percent Benefit Cut*

To help limit the rise in payroll taxes over time, we first consider a 50-percent reduction in OASI benefits over time. The cut is phased in over the next 30 years, with benefits for each year's *new* set of retirees declining an additional one thirtieth of 50 percent. Under this policy, OASDHI tax rates in 2030 and 2100 are 2.0 and 3.5 percentage points, respectively, above the 2000 level.

Table 2 shows that limiting the growth in payroll tax rates limits the extent of capital shallowing. Indeed, through 2030, the capital-labor ratio is the same as in 2000. However, thereafter, the supply of capital does grow more slowly than labor supply. In the long run, wages decline by 2.5 percent, compared with a 9.8 percent decline under the baseline. Evidently, the containment of taxes under this scenario increases the disposable income of younger cohorts and, by limiting old-age transfers, also increases their incentive to save, thus stimulating significantly more capital formation than under the base case. However, as mentioned above, two forces – the rise in the payroll tax, albeit muted compared to the base case, and historical circumstances (the initial conditions) – still prevent capital-labor ratios from rising under this scenario.

### 3.4. *Increasing Social Security's Eligibility Age*

Another way to partially contain rising payroll taxes is to raise the eligibility age for Social Security. In addition to the two-year increase to age 67 already in the baseline, we

consider an additional three-year increase to age 70, thereby reducing outlays by an additional 17 percent (Table 2). Not surprisingly, although the OASDHI tax hike is mitigated, the effect is smaller relative to the 50-percent benefit cut. Capital shallowing is also larger, and the long-run real wage decline is more pronounced. In sum, even a significant increase in the OASI eligibility age would not suffice to prevent major increases in the rate of payroll taxation.

### 3.5. *Pre-Funding Social Security*

Our next two simulations shown in Table 2 contemplate a more dramatic change to the OASI program, namely completely pre-funding it *at the margin* by paying out only those benefits accrued under the current system. To be precise, the simulations pay the OASI benefits of current retirees in full, and then linearly phase out OASI benefits for future retirees over a 45-year period starting in 2000, giving each future retiree a value roughly equal to the amount they have already accrued under Social Security. In addition, each pre-funding policy immediately eliminates the OASI tax rate and finances transitional OASI benefits with a new tax. After the transition is completed, workers finance all their retirement spending out of their own saving and no longer receive OASI transfers. Since workers in our model are not liquidity constrained, the results do not depend on any institutional arrangements attendant to the new policy.

#### 3.5.1. *Paying for the Transition with a Consumption Tax*

Consider first using a specially dedicated consumption tax to finance the transition.<sup>12</sup> The required consumption tax rate is initially 10.1 percent. It rises to 13.6 percent in 2020 and then gradually declines to zero over time, reaching zero in 2062 when Social Security has been fully

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<sup>12</sup> Recall that Social Security benefits are adjusted for inflation which includes the consumption tax.

phased out.<sup>13</sup> The remaining payroll tax for DI and HI is reduced to 4.7 percent, and grows by 3.4 percentage points over time as the demographics also raise the cost rate for the HI program.

This reform leads to considerable capital *deepening* over the transition, reversing the trend toward shallowing under the baseline. By 2030, the capital stock is 22.5 percent larger than under the baseline, and by 2100, it is 77.6 percent larger. Although long-run labor supply is somewhat smaller than under the baseline, the stimulus to capital formation leads to 11.1 percent more output than under the baseline by 2100, and the real wage is 15.1 percent larger. However, these gains arrive slowly. By 2030, the real wage is only 5.3 percent larger than it would have been in the absence of pre-funding. This relatively slow adjustment is not surprising given the enormous overhang of accrued OASI benefits that need to be paid off.

### 3.5.2. *Paying for the Transition with a Wage Tax*

Table 2 also shows the macroeconomic effects of paying for the transition with a new dedicated tax on (uncapped) wages. The long-run macroeconomic effects are identical to the consumption tax case since Social Security is fully pre-funded in both cases and both dedicated taxes eventually return to zero.<sup>14</sup> However, the macroeconomic gains from wage-tax financing arrive more slowly; in fact, there is no capital deepening over the next 30 years.

Consumption tax financing produces relatively faster macroeconomic gains because it places more of the transitional tax burden on older workers and retirees – especially the wealthy

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<sup>13</sup> Social Security is fully phased out in 2062 rather than in 45 years because the youngest worker alive in 2000, who will collect a partial Social Security retirement benefit someday, will live about 17 years in retirement.

<sup>14</sup> Table 2 shows that the economies under both financing methods are almost, but not yet fully, converged by 2100. The simulations, however, calculate all macroeconomic variables until 2275 to ensure convergence.

– whose consumption of non-Social Security wealth is exposed to higher after-tax prices. In contrast, the wage tax falls largely on younger households with relative higher marginal propensities to save. A consumption tax also represents, in part, a lump-sum tax on the economy’s initial wealth. Because lump-sum taxes are non-distortionary, the consumption tax provides workers with better overall incentives to work and save than the wage tax.

#### **4. Welfare and Distributional Effects of Reforms**

As suggested above, invariably some generations will be negatively affected by demographic change either under the baseline or under various policy reforms. Tradeoffs exist both between and within generations. Our model attempts to capture both dimensions.

Table 4 shows the welfare implications of different policies across three lifetime income classes – 1, 6, and 12 – and across several generations for the reforms described in Section 3. The welfare changes are measured as the equal percentage increase in both consumption and leisure that is needed by an agent in each remaining year of life under the baseline transition to achieve the same level of remaining lifetime utility as under the new policy. This measure is known as the “equivalent variation” of the policy change.

##### *4.1. Reducing Benefits*

The welfare effects from the gradual 50 percent reduction in OASI benefits are fairly benign on the oldest elderly at the time of the reform whose benefits are unchanged. But the reform is beneficial for all agents born in the long run, especially the poorest (class 1) whose welfare increases by almost 11 percent. The poor especially gain from reducing benefits over time because they are taxed fully by the payroll tax and most of their pre-reform retirement

wealth is in the form of Social Security which, despite the progressivity of the current system, produces a lower rate of return relative to capital markets.

However, this cut imposes rather large welfare losses on initial middle-aged and low-income agents who are close to retirement and experience most of the benefit cut without reaping the economic gains in the form of lower payroll taxes and a larger capital stock. The poorest agents who are age 60 at the time of the reform face a 7.0 percent loss. Their highest-earning contemporaries (class 12) have a much smaller welfare decline, 0.935 percent, because they have a comparatively small stake of their retirement wealth in Social Security.

The pattern of these welfare changes is similar if scheduled benefits are instead reduced through increasing Social Security's eligibility age by three years. However, because benefits are cut by a smaller percentage under this reform relative to the 50-percent benefit cut, the losses to older generation and gains to future generations are relatively smaller.

#### *4.2. Prefunding Benefits*

Pre-funding, either with a consumption tax or a wage tax, generates larger welfare gains for low- and middle-income agents born in the long run than the benefit cuts discussed above. Class 1 and class 6, for example, experience welfare gains of 21 and 19 percent, respectively. By contrast, class 12 only gains 5 percent. These gains are the result of a significant increase in real wages (15 percent) and a decline in payroll taxes (20 percentage points) relative to the baseline.

Pre-funding avoids the large welfare losses for middle-aged to older generations alive at the time of the reform that we found with benefit cuts. Instead, burdens are more evenly spread throughout the transition. Although we phase out all OASI benefits, welfare losses never exceed

3 percent for any household; with wage tax financing, losses never exceed 2 percent. For example, while households in income class 1 who are age 60 at the time of the reform lose 7 percent in welfare under a 50-percent reduction in benefits, they lose only 1.5 percent with pre-funding financed by a consumption tax and just 0.27 percent with wage tax financing.

With consumption tax financing, the initial elderly are largely protected by the indexation of Social Security benefits to prices which includes the new consumption tax. Thus, their losses are limited to their consumption out of their own saving, and among those age 70, for example, lower-income retirees are affected less than higher-income retirees. Retirees can also avoid some of the consumption taxes by leaving larger bequests. Among workers aged 30 to 50 welfare losses are more pronounced since they pay higher consumption taxes for most of their lives. As a result, the reform is slightly regressive for these workers since the phase-out of progressive benefits is not compensated quickly enough by capital deepening and rising wage levels. However, given the speed with which economic gains are generated, the 20 year-olds alive at the reform, who are about to enter the labor force, gain from reform except for the highest-income groups -- this despite the fact that 20 year-olds will pay higher consumption taxes for an extended period.

With wage-tax financing of the transition, the initial elderly and those about to retire at the time of the reform face only small welfare declines since they earn little if any wage income. Older workers are also fare better under the wage tax relative to a consumption tax. For example, the welfare of 50 year-olds at the time of the reform in income class 6 declines by 1.3 percent whereas it declined by 2.6 percent under the consumption tax. However, younger workers at the time of the reform mostly fare worse with wage-tax financing. For example, the

initial 20 year-olds in class 6 lose 1.12 percent in welfare whereas they gained 1.26 percent under consumption-tax financing. Similarly, those in class 6 born 5 years after the reform gain only 4.8 percent under wage-tax finance but 8.5 percent under consumption tax finance. In sum, wage tax financing of the transition protects higher-income elderly and distributes the losses during the transition among more generations, but at the cost to some young workers who suffer from the slower rise in incomes.

## **5. Conclusion**

Our simulation model tracks the nation's aging process well. Although it abstracts from several features of economic reality, it gives new insights into the general equilibrium feedback effects of the demographic transition. The sharp run-up in the payroll tax over the next three generations under the baseline reduces saving and dissipates what could otherwise be a process of capital deepening stemming from an aging population. Labor is projected to grow more rapidly than capital throughout the next century, thereby leaving the real wage per effective labor unit in 2100 about 10 percent lower than its current value. Preventing payroll taxes from dramatically rising by reducing Social Security's scheduled benefits would impose major welfare losses on middle-aged and older generations alive at the time of the reform.

As an alternative to reducing scheduled benefits, we also examine the option to pre-fund retirement saving. Our simulations show that it could avoid the payroll tax hike and generate major benefits for future generations. However, paying off the accrued liabilities of the old system imposes burdens of their own on generations alive at the time of the reform. Still, the welfare losses tend to be spread out much more evenly between generations and produce much

larger long-run gains relative to either the baseline or relative to cutting scheduled benefits. The economic benefits of pre-funding for future generations arise more quickly under consumption- than wage-tax finance, however at the cost of somewhat higher welfare losses for middle-aged generations.

Our model could also be questioned because of its stylized nature. It abstracts from the choice of education (see Heckman, et al., 1998), uncertainty, international trade, monetary policy, borrowing constraints, and a number of other aspects of economic reality. Whether the inclusion of those factors would materially alter our conclusions is a question for future research. However, we believe that the pending demographic change is severe enough that most models of the economy would generate a similar fiscal dilemma.

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**Table 1****Comparing the Model's and Social Security's Population Projections**

Year	Social Security Population Projections				The Model's Population			
	Total Population Index (100 in 2000)	Population Shares			Total Population Index (100 in 2000)	Population Shares		
		0-19	20 - 64	65 +		0-19	20 - 64	65 +
2000	100.0	0.29	0.59	0.12	100.0	0.29	0.59	0.12
2005	104.1	0.28	0.60	0.12	104.6	0.27	0.60	0.13
2010	108.1	0.27	0.60	0.13	108.6	0.26	0.59	0.15
2020	116.0	0.25	0.58	0.16	116.0	0.25	0.57	0.18
2030	122.6	0.25	0.56	0.20	122.8	0.24	0.54	0.22
2050	131.2	0.24	0.56	0.21	124.2	0.23	0.53	0.23
2075	140.3	0.23	0.54	0.23	125.8	0.24	0.53	0.23

Table 2 Summary Simulation Results

	Year	National Income	Capital Stock	Effective Labor Supply	National Saving Rate	Real Pre- Tax Wage	Interest Rate	OASDHI Cost Rates	
								Model	SSA
<b>Baseline Case</b>	2000	1.000	1.000	1.000	.046	1.000	.075	.137	.131
	2005	1.091	1.064	1.101	.044	.992	.077	.145	.136
	2010	1.191	1.137	1.209	.047	.985	.079	.158	.147
	2020	1.361	1.271	1.393	.030	.977	.081	.197	.183
	2030	1.529	1.366	1.587	.011	.963	.084	.243	.220
	2050	1.889	1.500	2.039	.015	.926	.095	.257	.237
	2075	2.479	1.845	2.736	.023	.906	.101	.264	.262
	2100	3.303	2.421	3.663	.027	.902	.103	.265	na
<b>50-percent Benefit Cut</b>	2000	1.000	1.000	1.000	.065	1.000	.076	.136	.131
	2005	1.096	1.094	1.096	.062	.999	.076	.135	.136
	2010	1.200	1.198	1.201	.063	.999	.076	.138	.147
	2020	1.387	1.403	1.382	.048	1.004	.075	.148	.183
	2030	1.578	1.578	1.578	.029	1.000	.076	.156	.220
	2050	1.967	1.886	1.995	.027	.986	.079	.167	.237
	2075	2.602	2.423	2.665	.033	.976	.082	.171	.262
	2100	3.472	3.218	3.561	.035	.975	.082	.171	na
<b>Raise Eligibility Age by 3 More Years</b>	2000	1.000	1.000	1.000	.059	1.000	.076	.136	.131
	2005	1.094	1.084	1.097	.055	.997	.076	.137	.136
	2010	1.196	1.177	1.203	.057	.995	.077	.141	.147
	2020	1.381	1.356	1.389	.042	.994	.077	.156	.183
	2030	1.557	1.500	1.577	.020	.987	.079	.192	.220
	2050	1.934	1.721	2.011	.021	.962	.085	.204	.237
	2075	2.551	2.166	2.694	.028	.947	.089	.209	.262
	2100	3.401	2.861	3.603	.031	.944	.090	.209	na

Table 2 Summary Simulation Results

	Year	National Income	Capital Stock	Effective Labor Supply	National Saving Rate	Real Pre- Tax Wage	Interest Rate	OASDHI Cost Rates	
								Model	SSA
<b>Consumption-Tax</b>	2000	1.000	1.000	1.000	.063	1.000	.076	.047	.131
<b>Pre-Funding</b>	2005	1.096	1.093	1.098	.062	.999	.076	.051	.136
	2010	1.201	1.199	1.202	.066	.999	.076	.056	.147
	2020	1.396	1.434	1.383	.059	1.009	.074	.068	.183
	2030	1.598	1.674	1.574	.046	1.016	.072	.081	.220
	2050	2.056	2.230	2.001	.051	1.027	.070	.081	.237
	2075	2.753	3.145	2.633	.048	1.045	.066	.081	.262
	2100	3.684	4.299	3.499	.046	1.053	.065	.081	na
<b>Wage-Tax</b>	2000	1.000	1.000	1.000	.052	1.000	.074	.044	.131
<b>Pre-Funding</b>	2005	1.094	1.070	1.102	.054	.993	.076	.048	.136
	2010	1.198	1.162	1.211	.062	.990	.076	.052	.147
	2020	1.350	1.309	1.364	.035	.991	.076	.064	.183
	2030	1.548	1.451	1.582	.027	.979	.079	.077	.220
	2050	2.044	1.894	2.096	.053	.975	.080	.080	.237
	2075	2.808	2.977	2.753	.057	1.020	.070	.081	.262
	2100	3.774	4.243	3.630	.048	1.040	.066	.081	na

**Table 3 Sensitivity of Baseline Results**

	<b>Year</b>	<b>National Income</b>	<b>Capital Stock</b>	<b>Effective Labor Supply</b>	<b>National Saving Rate</b>	<b>Real Pre-Tax Wage</b>	<b>Interest Rate</b>	<b>OASDHI Cost Rate</b>	<b>Cost Rates SSA</b>
<b>Lee-Carter Life Expectancy</b>	<b>2000</b>	<b>1.000</b>	<b>1.000</b>	<b>1.000</b>	<b>.051</b>	<b>1.000</b>	<b>.076</b>	<b>.136</b>	<b>.131</b>
	<b>2030</b>	<b>1.541</b>	<b>1.403</b>	<b>1.590</b>	<b>.014</b>	<b>.969</b>	<b>.083</b>	<b>.249</b>	<b>.220</b>
	<b>2100</b>	<b>3.358</b>	<b>2.480</b>	<b>3.715</b>	<b>.026</b>	<b>.904</b>	<b>.102</b>	<b>.291</b>	<b>n/a</b>
<b>Higher Productivity Through Age 65</b>	<b>2000</b>	<b>1.000</b>	<b>1.000</b>	<b>1.000</b>	<b>.041</b>	<b>1.000</b>	<b>.076</b>	<b>.137</b>	<b>.131</b>
	<b>2030</b>	<b>1.539</b>	<b>1.353</b>	<b>1.607</b>	<b>.011</b>	<b>.958</b>	<b>.086</b>	<b>.241</b>	<b>.220</b>
	<b>2100</b>	<b>3.330</b>	<b>2.408</b>	<b>3.711</b>	<b>.026</b>	<b>.898</b>	<b>.105</b>	<b>.263</b>	<b>n/a</b>
<b>2% Rate of Technical Progress</b>	<b>2000</b>	<b>1.000</b>	<b>1.000</b>	<b>1.000</b>	<b>.051</b>	<b>1.000</b>	<b>.087</b>	<b>.140</b>	<b>.131</b>
	<b>2030</b>	<b>1.753</b>	<b>1.509</b>	<b>1.843</b>	<b>.022</b>	<b>.951</b>	<b>.101</b>	<b>.217</b>	<b>.220</b>
	<b>2100</b>	<b>7.453</b>	<b>5.593</b>	<b>8.202</b>	<b>.047</b>	<b>.909</b>	<b>.115</b>	<b>.197</b>	<b>n/a</b>

**Table 4 Welfare Effects of Selected Policies**

(base-case percentage change in remaining lifetime consumption and leisure needed to achieve policy-induced utility level)

Generation's Year of Birth Relative to Policy Start Year	50-percent Benefit Cut			Increase Eligibility Age by 3 More Years			Consumption Tax Financed Pre-Funding			Wage Tax Financed Pre-Funding		
	Class 1	Class 6	Class 12	Class 1	Class 6	Class 12	Class 1	Class 6	Class 12	Class 1	Class 6	Class 12
-81	.020	.025	.018	.012	.015	.011	-.121	-.493	-.622	-.041	-.053	-.038
-70	-3.701	-2.585	-.735	-3.088	-2.292	-.639	-.574	-.978	-1.271	-.150	-.214	-.214
-60	-7.049	-4.599	-.935	-6.179	-3.985	-.776	-1.502	-1.972	-1.507	-.272	-.513	-.263
-50	-5.180	-3.288	-.787	-4.423	-2.417	-.558	-2.858	-2.598	-1.605	-.551	-1.349	-.277
-40	-3.136	-1.748	-.640	-1.631	-.917	-.376	-2.935	-2.294	-1.813	-.797	-1.945	-.888
-30	-.467	-.246	-.419	.148	.100	-.224	-1.641	-1.177	-1.810	.217	-1.822	-1.700
-20	1.871	1.494	.142	1.612	1.241	.149	.876	1.258	-1.125	2.506	-1.121	-3.037
5	8.468	7.176	1.583	5.317	4.556	1.013	9.407	8.480	.941	9.194	4.782	-1.568
30	10.320	9.483	2.383	6.219	5.778	1.459	17.982	16.019	3.994	16.399	14.082	3.004
55	10.795	10.221	2.735	6.473	6.283	1.673	20.172	18.353	4.994	19.589	17.828	4.754
80	10.959	10.450	2.823	6.561	6.420	1.725	20.692	18.921	5.221	20.551	18.794	5.165