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QUANTIFYING THE HIGH-FREQUENCY TRADING "ARMS RACE"

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ABSTRACT

We use stock exchange message data to quantify the negative aspect of high-frequency trading, known as “latency arbitrage.” The key difference between message data and widely-familiar limit order book data is that message data contain attempts to trade or cancel that fail. This allows the researcher to observe both winners and losers in a race, whereas in limit order book data you cannot see the losers, so you cannot directly see the races. We find that latency-arbitrage races are very frequent (about one per minute per symbol for FTSE 100 stocks), extremely fast (the modal race lasts 5-10 millionths of a second), and account for a remarkably large portion of overall trading volume (about 20%). Race participation is concentrated, with the top 6 firms accounting for over 80% of all race wins and losses. The average race is worth just a small amount (about half a price tick), but because of the large volumes the stakes add up. Our main estimates suggest that races constitute roughly one-third of price impact and the effective spread (key microstructure measures of the cost of liquidity), that latency arbitrage imposes a roughly 0.5 basis point tax on trading, that market designs that eliminate latency arbitrage would reduce the market's cost of liquidity by 17%, and that the total sums at stake are on the order of \$5 billion per year in global equity markets alone.

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Online Appendices are available at <http://www.nber.org/data-appendix/w29011>

“The market is rigged.” – Michael Lewis, Flash Boys (Lewis, 2014)

“Widespread latency arbitrage is a myth.” – Bill Harts, CEO of the Modern Markets Initiative, an HFT lobbyist (Michaels, 2016)

1 Introduction

As recently as the 1990s and early 2000s, human beings on trading floors, pits and desks intermediated the large majority of financial market transactions. Now, financial markets across most major asset classes—equities, futures, treasuries, currencies, options, etc.—are almost entirely electronic. This transformation of financial markets from the human era to the modern electronic era has on the whole brought clear, measurable improvements to various measures of the cost of trading and liquidity, much as information technology has brought efficiencies to many other sectors of the economy. But this transformation has also brought considerable controversy, particularly around the importance of speed in modern electronic markets.¹

At the center of the controversy over speed is a phenomenon called “latency arbitrage”, also known as “sniping” or “picking off” stale quotes. In plain English, a latency arbitrage is an arbitrage opportunity that is sufficiently mechanical and obvious that capturing it is primarily a contest in speed. For example, if the price of the S&P 500 futures contract changes by a large-enough amount in Chicago, there is a race around the world to pick off stale quotes in every asset highly correlated to the S&P 500 index: S&P 500 exchange traded funds, other US equity index futures and ETFs, global equity index futures and ETFs, etc. Many other examples arise from other sets of highly correlated assets: treasury bonds of slightly different durations, or in the cash market versus the futures market; options and the underlying stock; ETFs and their largest component stocks; currency triangles; commodities at different delivery dates; etc. Perhaps the simplest example is if the exact same asset trades in many different venues. For example, in the US stock market, there are 16 different exchanges and 50+ alternative trading venues, all trading the same stocks—so if the price of a stock changes by enough on one venue, there is a race to pick off stale quotes on all the others. These races around the world involve microwave links between market centers, trans-oceanic fiber-optic cables, putting trading algorithms onto hardware as opposed to software, co-location rights and proprietary data feeds from exchanges, real estate adjacent to and even on the rooftops of exchanges, and, perhaps most importantly, high-quality human capital. Just a decade ago, the speed race was commonly measured in milliseconds (thousandths of a second); it is now measured in microseconds (millionths) and even nanoseconds (billionths).²

¹See MacKenzie (2021) for a history of the transformation of financial markets from the human-trading era to the modern electronic era, with detailed documentation of many different aspects of the speed race and numerous additional references. See Hendershott, Jones and Menkveld (2011), Angel, Harris and Spatt (2015), and Frazzini, Israel and Moskowitz (2018) for key studies on the decline of trading costs. Most of the declines appear to be concentrated in the early years of the transformation, specifically the mid to late '90s and early to mid '00s; see especially Figure 20 of Angel, Harris and Spatt (2015) and Figure IA.8 of Hagströmer (2021). See Jones (2013), Biais and Foucault (2014), O'Hara (2015), and Menkveld (2016) for surveys of the literature on high-frequency trading.

²Please see the working paper version of this paper, Aquilina, Budish and O'Neill (2020), for detailed references. The latest salvo, reported April 1, 2021 in what at first seemed like an April Fools' joke, is dedicated satellite links

In theoretical terms, Budish, Cramton and Shim (2015, henceforth BCS) define latency arbitrage as arbitrage rents from symmetrically-observable public information signals, as distinct from the asymmetrically-observable private information signals that are at the heart of classic models of market microstructure (Kyle, 1985; Glosten and Milgrom, 1985). We are all familiar with the idea that if you know something the rest of the market doesn't know, you can make money. BCS showed that, in modern electronic markets, even information seen and understood by many market participants essentially simultaneously creates arbitrage rents—because of the underlying market design used by modern financial exchanges. The issue is the combination of (i) treating time as continuous (infinitely divisible), and (ii) processing requests to trade serially (one-at-a-time). These aspects of modern exchange design trace back to the era of human trading, which also used versions of limit order books and price-time priority. But, to a computer, serial processing and time priority mean something much more literal than to a human. Even in the logical extreme in which many market participants observe a new piece of information at *exactly* the same time, and respond with *exactly* the same technology, somebody gets a rent. BCS showed that these arbitrage rents lead to a socially-wasteful arms race for speed, to be ever-so-slightly faster to react to new public information, and harm investors, because the rents are like a tax on market liquidity—any firm providing liquidity has to bear the cost of getting sniped. A subtle change to the market design can eliminate the rents—preserving the useful functions of modern algorithmic trading while eliminating latency arbitrage and the arms race.

Unfortunately, empirical evidence on the overall magnitude of the latency arbitrage problem has been scarce. BCS provide an estimate for one specific trade, S&P 500 futures-ETF arbitrage, and find that this specific trade is worth approximately \$75 million per year. Aquilina et al. (2016) focus on stale reference prices in UK dark pools and estimate potential profits of approximately GBP4.2 million per year. The shortcoming of the approach taken in these studies is that it is unclear how to extrapolate from the profits in specific latency arbitrage trades that researchers know how to measure to an overall sense of the magnitudes at stake. Another notable study is Ding, Hanna and Hendershott (2014), who study the frequency and size of differences between prices for the same symbol based on exchanges' direct data feeds and the slower data feed in the U.S. known as the consolidated tape, which is sometimes used to price trades in off-exchange trading (i.e., dark pools). However, as the authors are careful to acknowledge, they do not observe which of these within-symbol price differences are actually exploitable in practice—not all are because of both noise in timestamps and physical limitations due to the speed at which information travels. Wah (2016) and Dewhurst et al. (2019) study the frequency and size of differences between prices for the same symbol across different U.S. equity exchanges. This is conceptually similar to and faces the same challenge as Ding, Hanna and Hendershott (2014), in that neither study observes which within-symbol price discrepancies are actually exploitable. For this reason, the magnitudes obtained in Wah (2016) and Dewhurst et al. (2019) are best understood as upper bounds on the within-symbol subset of latency arbitrage. Brogaard, Hendershott and Riordan (2014) and Baron et al. (2019) compute a large set of HFT firms' overall profits on specific exchanges (in NASDAQ data and Swedish data,

between market centers in North America, Europe, and Asia (Osipovich, 2021).

respectively), and Baron et al. (2019) show that relatively faster HFTs earn significantly greater profits, but neither paper provides an estimate for what portion of these firms’ trading profits arise due to latency arbitrage.³

In the absence of comprehensive empirical evidence, it is hard to know how important a problem latency arbitrage is and hence what the benefits would be from market design reforms, such as frequent batch auctions, that address it. If the magnitudes are sufficiently large then Michael Lewis’s claim that the market is “rigged for the benefit of insiders”, cited at the beginning of the paper, is reasonable if perhaps a bit conspiratorial. Conversely, if the magnitudes are sufficiently small then the HFT lobby’s claim that latency arbitrage is a “myth”, also cited above, is reasonable if perhaps a bit exaggerated. Notably, while numerous regulators around the world have investigated HFT in some capacity (e.g., the FCA, ESMA, SEC, CFTC, US Treasury, NY AG), and in a few specific instances have been required to rule specifically on speed bump proposals designed to address latency arbitrage, there is not a broad consensus on what if any regulatory rules or interventions are appropriate.⁴

This paper uses a simple new kind of data and a simple new methodology to provide a comprehensive measure of latency arbitrage. The data are the “message data” from an exchange, as distinct from widely familiar limit order book datasets such as exchange direct feeds or consolidated datasets like TAQ (Trades and Quotes) or the SEC’s MIDAS dataset. Limit order book data provide the complete play-by-play of one or multiple exchanges’ limit order books—every new limit order that adds liquidity to the order book, every canceled order, every trade, etc.—often with ultra-precise timestamps. But what is missing are the messages that *do not affect the state of the order book, because they fail*.⁵

For example, if a market participant seeks to snipe a stale quote but fails—their immediate or cancel (IOC) order is unable to execute immediately so it is instead just canceled—their message never affects the state of the limit order book. Or, if a market participant seeks to cancel their order, but fails—they are “too late to cancel”—then their message never affects the state of the limit order book. But in both cases, there is an electronic record of the participant’s *attempt* to snipe, or *attempt* to cancel. And, in both cases, there is an electronic record of the exchange’s response to the failed message, notifying the participant that they were too late.

Our method relies on the simple insight that these failure messages are a direct empirical sig-

³Other papers with empirical evidence that relates to the benefits and costs of HFT include Menkveld (2013), Brogaard et al. (2015), Foucault, Kozhan and Tham (2016), Shkilko and Sokolov (2020), Brogaard et al. (2018), Malinova, Park and Riordan (2018), Weller (2018), Van Kervel and Menkveld (2019), Breckenfelder (2019), and Indriawan, Pascual and Shkilko (2020).

⁴For regulatory investigations of HFT, please see Financial Conduct Authority (2018), Securities and Exchange Commission (2010), European Securities Market Authority (2014), Commodity Futures Trading Commission (2015), Joint Staff Report (2015), and New York Attorney General’s Office (2014). Specific speed bump proposals include Cboe EDGA (2019), ICE Futures (2019), London Metals Exchange (2019), Chicago Stock Exchange (2016), and Investors’ Exchange (2015).

⁵To our knowledge, ours is the first study (either academic, regulatory, or industry) to use exchange message data, defined as the full back-and-forth message traffic between market participants and the exchange. There have been several other studies of HFT with data that goes beyond TAQ or exchange direct feeds, such as participant identifiers or additional information on order types, but none, to our knowledge, with the complete call-and-response data that is key to our study.

nature of speed-sensitive trading. If multiple participants are engaged in a speed race to snipe or cancel stale quotes, then, essentially by definition, some will succeed and some will fail. The essence of a race is that there are winners and losers—but conventional limit order book data doesn't have any record of the losers. This is why it has been so hard to measure latency arbitrage. You can't actually see the race in the available data.

We obtained from the London Stock Exchange (by a request under Section 165 of the Financial Service and Markets Act) all message activity for all stocks in the FTSE 350 index for a 9 week period in Fall 2015.⁶ The messages are time-stamped with accuracy to the microsecond (one-millionth of a second), and as we will describe in detail, the timestamps are applied at the right location of the exchange's computer system for measuring speed races (the "outer wall"). Using this data, we can directly measure the quantity of races, provide statistics on how long races take, how many participants there are, the diversity and concentration of winners/losers, etc. And, by comparing the price in the race to the prevailing market price a short time later, we can measure the economic stakes, i.e., how much was it worth to win.

Our main results are as follows:

- Races are frequent. The average FTSE 100 symbol has 537 latency-arbitrage races per day. That is about one race per minute per symbol.
- Races are fast. In the modal race, the winner beats the first loser by just 5-10 microseconds, or 0.000005 to 0.000010 seconds. In fact, due to small amounts of randomness in the exchange's computer systems, about 4% of the time the winner's message actually arrives to the exchange slightly later than the first loser's message, but nevertheless gets processed first.
- A remarkably large proportion of daily trading volume is in races. For the FTSE 100 index, about 22% of trading volume and 21% of trades are in races. Cochrane (2016) describes that trading volume is "The Great Unsolved Problem of Financial Economics."⁷ Our results suggest that latency arbitrage is a meaningful piece of the puzzle. Indeed, in our most inclusive sensitivity scenario, with an up-to 3 millisecond race window, races constitute 44% of all FTSE 100 trading volume.
- Races are worth just small amounts each. The average race is worth a bit more than half a tick, which on average comes to about 2GBP. Even at the 90th percentile of races, the races are worth just 3 ticks and about 7GBP. There is also a fair amount of noise: about 20% of races have strictly negative profits one second ex-post.⁸

⁶The FTSE 350 is an index of the 350 highest capitalization stocks in the UK. It consists of the FTSE 100, which are the 100 largest stocks, and roughly analogous to other countries' large-cap stock indices (e.g., the S&P 500 index), and the FTSE 250, which are the next 250 largest, and roughly analogous to other countries' small-cap stock indices (e.g., the Russell 2000 index).

⁷See also Hong and Stein (2007) who write that "Some of the most interesting empirical patterns in the stock market are linked to volume," and provide numerous additional references.

⁸Robert Mercer, former co-CEO of the quantitative trading firm Renaissance Technologies, described quantitative investing as "We're right 50.75 percent of the time ... you can make billions that way." (Zuckerman, 2019, pg. 272) Similarly, high-frequency trading firm Virtu's CEO Doug Cifu indicated that around 51-52% of their trades are profitable (Mamudi, 2014). Our figures suggest that trading in races is closer to pure arbitrage than 51/49 but still a healthy distance from 100/0.

- Race participation is concentrated. The top firms disproportionately snipe. The top 3 firms win about 55% of races, and also lose about 66% of races. For the top 6 firms, the figures are 82% and 87%. In addition to documenting concentration, we also find that the top 6 firms are disproportionately aggressive in races, taking about 80% of liquidity in races while providing about 42% of the liquidity that gets taken in races. Market participants outside the top 6 firms take about 20% of liquidity in races while providing about 58%. Thus, on net, much race activity consists of firms in the top 6 taking liquidity from market participants outside of the top 6. This taking is especially concentrated in a subset of 4 of the top 6 firms who account for a disproportionate share of stale-quote sniping relative to liquidity provision.⁹
- In aggregate, these small races add up to a significant proportion of price impact and the effective spread, key microstructure measures of the cost of liquidity. We augment the traditional bid-ask spread decomposition suggested by Glosten (1987), which is widely utilized in the microstructure literature (e.g., Glosten and Harris, 1988; Hasbrouck, 1991*a,b*; Stoll, 2000; Hendershott, Jones and Menkveld, 2011), to separately incorporate price impact from latency-arbitrage races and non-race trading. Price impact from trading in races is about 31% of all price impact, and about 33% of the effective spread. This suggests latency arbitrage deserves a place alongside traditional adverse selection as one of the primary components of the cost of liquidity.¹⁰
- Market designs that eliminate latency arbitrage could meaningfully reduce the market’s cost of liquidity. We find that the latency arbitrage tax, defined as the ratio of daily race profits to daily trading volume, is 0.42 basis points if using total trading volume, and 0.53 basis points if using only trading volume that takes place outside of races. The average value-weighted effective spread paid in our data is just over 3 basis points. We show formally that the ratio of the non-race latency arbitrage tax to the effective spread is the implied reduction in the market’s cost of liquidity if latency arbitrage were eliminated; that is, if liquidity providers did not have to bear the adverse selection costs associated with being sniped. This implies that market designs that eliminate latency arbitrage, such as frequent batch auctions, would reduce investors’ cost of liquidity by 17%. As a complementary analysis, we also show that the liquidity provider’s realized spread in races is significantly negative whereas it is

⁹In the equilibria studied in BCS, fast trading firms provided all liquidity. Races consisted of some fast trading firms trying to snipe and other fast trading firms trying to cancel. Here, in Appendix F, we show that there exists another equilibrium of the BCS model in which both fast and slow firms provide liquidity. If a slow firm provides liquidity and there is a race, they get sniped with probability one. The key insight is that the same bid-ask spread that leaves fast trading firms indifferent between liquidity provision and stale-quote sniping (either way, earning $1/N$ of the sniping prize, where N is the number of fast firms in the race) is the zero-profit spread for slow trading firms.

¹⁰There are many different strands of literature on the broader importance of liquidity for financial markets. One strand explores the connection between the specific kinds of microstructure measures of liquidity we study and asset pricing—good starting points include Amihud (2002), Pástor and Stambaugh (2003), and Acharya and Pedersen (2005). This literature finds that liquidity is a factor in asset pricing returns, which in turn implies that reforms that improve the market’s liquidity reduce required equilibrium returns and hence increase the level of asset prices. Diamond and Dybvig (1983) and a large subsequent literature highlight the role of liquidity in reducing the likelihood of bank runs. Shleifer and Vishny (1992, 1997, 2011), Brunnermeier and Pedersen (2009), Hanson, Kashyap and Stein (2011), and many others have studied connections between liquidity and various aspects of financial stability.

modestly positive in non-race liquidity provision. This pattern holds whether or not the liquidity provider is one of the fastest firms. This is direct evidence that latency arbitrage races impose a tax on liquidity provision.¹¹

- These small races add up to a meaningful total “size of the prize” in the arms race. The relationship between daily latency-arbitrage profits and daily volume is robust, with an R^2 of about 0.81, and indeed the latency-arbitrage tax on trading volume is roughly constant in our data. Adding daily volatility to the relationship further improves the fit, albeit only slightly. Using these relationships, we find that the annual sums at stake in latency arbitrage races in the UK are about GBP 60 million. Extrapolating globally, our estimates suggest that the annual sums at stake in latency-arbitrage races across global equity markets are on the order of \$5 billion per year.¹²

Discussion of Magnitudes Whether the numbers in our study seem big or small may depend on the vantage point from which they are viewed. As is often the case in regulatory settings, the detriment per transaction is quite small: the average race is for just half a tick, and a roughly 0.5 basis point tax on trading volume certainly does not sound alarming. But, because of the large volumes, these small races and this seemingly small tax on trading add up to significant sums. A 17% reduction in the cost of liquidity is undeniably meaningful for large investors, and \$5 billion per year is, as they say, real money—especially taking into account the fact that our results only include equities, and not other asset classes that trade on electronic limit order books such as futures, treasuries, currencies, options, etc.

In this sense, our results are consistent with aspects of both the “myth” and “rigged” points of view. The latency arbitrage tax does seem small enough that ordinary households need not worry about it in the context of their retirement and savings decisions. Yet at the same time, flawed market design drives a significant fraction of daily trading volume, significantly increases the trading costs of large investors, and generates billions of dollars a year in profits for a small number of HFT firms and other parties in the speed race, who then have significant incentive to preserve the status quo.

Organization of the Paper The remainder of this paper is organized as follows. Section 2 describes the message data in detail. Section 3 describes our methodology for detecting and measuring latency-arbitrage races. Section 4 presents the main results. Section 5 discusses sensitivity analyses and robustness checks. Section 6 extrapolates to an annual size of the prize for the UK and global equity markets. Section 7 concludes.

¹¹Market design research often involves a mix of economic theory, empirical evidence, and institutional detail working together to help bring useful economic ideas from theory to practice. Roth (2002) has called this “The Economist as Engineer.” Other examples from outside of finance include the design of matching markets (Roth, 2008), spectrum auctions (Milgrom, 2021), kidney exchange mechanisms (Roth, Sönmez and Ünver, 2004), school choice procedures (Pathak, 2017), course allocation procedures (Budish et al., 2017), and accelerating Covid-19 vaccination (Castillo et al., 2021). See Kominers et al. (2017) and Roth (2018) for recent surveys.

¹²Over a variety of sensitivity analyses, with race windows ranging from 50 microseconds to 3 milliseconds, our range of estimates is \$2.3 - \$8.4 billion per year in global equities markets. In 2020, which was a particularly high-volume and high-volatility year due to the Covid-19 pandemic, our point estimate is \$7 billion and our range is \$3.1 - \$11.4 billion. We discuss caveats for this extrapolation exercise in detail in Section 6.3.

2 Message Data

The novel aspect of our data is that it includes all messages sent by participants to the exchange and by the exchange back to participants. Importantly, this includes messages that inform a participant that their request to trade or their request to cancel was not successful—such messages would not leave any empirical trace in traditional limit order book data. Also fundamental to our empirical procedure is the accuracy and location of the timestamps, which, as we will describe in detail below, are applied at the “outer wall” of the exchange’s network and therefore represent the exact time at which a market participant’s message reached the exchange. This timestamp location is ideal for measuring races, even more so than matching engine timestamps, as it represents the point at which messages are no longer under the control of market participants.¹³

We obtained these message data from the London Stock Exchange, following a request by the FCA to the LSE under Section 165 of the Financial Services and Markets Act. Our data cover the 44 trading days from Aug 17 – Oct 16 2015, for all stocks in the FTSE 350 index. We drop one day (Sept 7th) which had a small amount of corrupted data. This leaves us with 43 trading days and about 15,000 symbol-day pairs. In total, our data comprise roughly 2.2 billion messages, or about 150,000 messages per symbol-day.

2.1 Overview of a Modern Stock Exchange

The continuous limit order book is at heart a simple protocol.¹⁴ We guess that most undergraduate computer science students could code one up after a semester or two of training. Yet, modern electronic exchanges are complex feats of engineering. The engineering challenge is not the market design per se, but rather to process large and time-varying quantities of messages with extremely low latency and essentially zero system downtime.

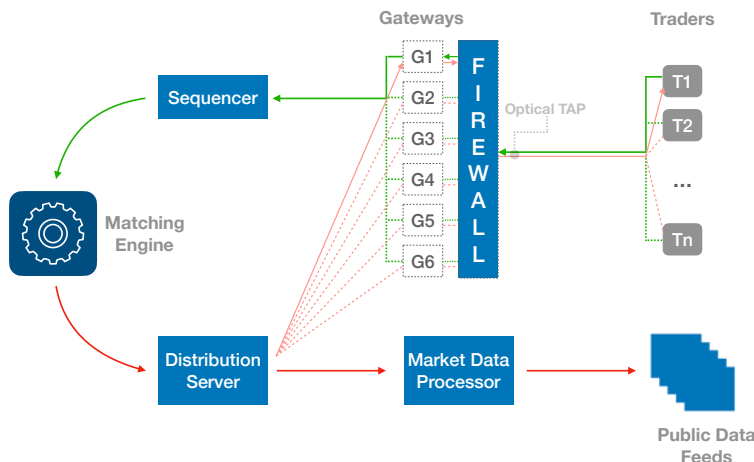
In this sub-section we provide a stylized description of a modern electronic exchange, illustrated in Figure 2.1. We do this both because it is a necessary input for understanding our data, and because we expect it will be useful per se to both academic researchers and regulators who seek a better understanding of the detailed plumbing of modern financial markets.

The core of a modern exchange, and likely what most people think of as the exchange itself, is

¹³We emphasize though that our methodology could be replicated in other contexts using matching engine timestamps, so long as the researcher has the full set of messages including failed cancels and failed IOCs and the timestamps are sufficiently precise. We think of the full message activity as a “must have” for the method and the specific location of the timestamps as more of a “nice to have.”

¹⁴We assume most readers are already familiar with the basics of a limit order book market but here is a quick refresher. The basic building block is a limit order, which consists of a symbol, price, quantity and direction. Market participants interact with the exchange by sending and canceling limit orders, and various permutations thereof (e.g., immediate-or-cancel orders, which are limit orders combined with the instruction to either fill the order immediately or to instead cancel it). Trades occur whenever the exchange receives a new order to buy at a price greater than or equal to one or more outstanding orders to sell, or a new order to sell at a price less than or equal to one or more outstanding orders to buy. If this happens, the new order executes at the price of the outstanding order or orders, executing up to the new order’s quantity, with the rest remaining outstanding. If there are multiple outstanding orders the new order could execute against, ties are broken based first on price (i.e., the highest offer to buy or lowest offer to sell) and then based on time (i.e., which outstanding order has been outstanding for the most time). Market participants may send new limit orders, or cancel or modify outstanding limit orders, at any moment in time. The exchange processes all of these requests, called “messages”, continuously, one-at-a-time in order of receipt.

Figure 2.1: Exchange Schematic



Notes: Please see the text of Section 2.1 for a discussion of the overall system architecture depicted in this figure. Green arrows depict the flow of inbound messages and red arrows depict the flow of outbound messages. Please see the text of Section 2.2 for discussion of the optical traffic analysis point (TAP) where our message data are recorded and timestamped (depicted in faded gray in the figure).

the *matching engine*. As the name suggests, this is where orders are matched and trades generated. A bit more fully, one should think of the matching engine as the part of the exchange architecture that executes the limit order book protocol. For each symbol, it processes messages serially in order of receipt and, for each message, both economically processes the message and disseminates relevant information about the outcome of the message. For example, if the message is a new limit order, the matching engine will determine whether it can execute (“match”) the order against one or more outstanding orders, or whether it should add the order to the book. It will then disseminate information back to the participant about whether their order posted, executed, or both; to any counterparties if the order executed; and to the public market data feeds about the updated state of the order book.

However, the matching engine is far from the only component of a modern exchange, and market participants do not even interact with the matching engine directly, in either direction. Rather, market participants send messages to the exchange via what are known as *gateways*, which verify the integrity of messages, perform risk checks, and translate messages from the participant interface language into a language optimized for the matching engine.¹⁵ Gateways in turn pass messages on to a *sequencer*, which in essence translates input from many parallel gateways into, for each symbol, a single sequence of messages that is passed on to the matching engine. The matching engine, once it does its work, transmits information back to a *distribution server*, which in turn passes private messages back to participants via the gateways, and public information to the market as a whole

¹⁵There intrinsically is a small amount of randomness in this piece of the systems architecture, because how long a particular gateway takes to process a particular message is stochastic. This randomness will manifest in our data below in Figure 4.1. We did not find any evidence in our data of firms attempting to exploit this randomness, e.g., by sending the same message to multiple gateways via multiple accounts. Our best guess why this behavior would be easy for the LSE to detect.

via the *market data processor*.

A fuller description of each of these components is in the working paper version of this paper (Aquilina, Budish and O’Neill, 2020). Here, we briefly emphasize the overall rationale for this system architecture. The matching engine must, given the limit order book market design, process all messages that relate to a given symbol serially, in order of receipt. This serial processing is therefore a potential computational bottleneck. For a stark example, if a million messages arrived at precisely the same moment for the same symbol, the matching engine would have to process these million messages one-at-a-time.¹⁶ Therefore, it is critical for latency to take as much of the work as possible “off of the shoulders” of the matching engine, and instead put it on to other components of the system.

2.2 Where and How Messages are Recorded and Timestamped

As just described, participants send messages to the exchange, and receive messages from the exchange, via gateways. Between the participants’ own systems and the exchange gateways is a firewall, through which all messages pass, in both directions. Our data are recorded and timestamped on the external side of this firewall using an optical TAP (traffic analysis point); please refer to Figure 2.1. This is the ideal timestamping location for measuring race activity because it records the time at which the participant’s message reaches the “outer wall” of the exchange’s system. Participant speed investments affect the speed with which their messages reach this outer wall, but once a message reaches this point it is out of the participant’s hands and in the exchange’s hands. Therefore, the outer wall is the right way to think about what is the “finish line” in a race.

Messages are timestamped to 100 nanosecond (0.1 microsecond or 0.0000001 second) precision, at this point of capture, by a hardware clock. Importantly, all messages are timestamped by a single clock. Therefore, while the clock may drift slightly over the course of the trading day, the relative timestamps of different messages in a race can be compared with extreme accuracy. Based on our discussions with the LSE we are comfortable treating our data as accurate to the microsecond.

Please note that the optical TAP timestamps we observe in our data are not seen by market participants.

2.3 Translating Message Data into Market Events

Any action by a market participant generates at least two messages: one on the way into the exchange, and one or more on the way out of the exchange. For example, a new limit order that both trades against a resting order and posts the remainder to the book will have a single inbound message with the new order, an outbound message to the user whose order was passively executed, and an outbound message to the user who sent the new limit order reporting both the quantity/price traded and the quantity/price that remains and is posted to the book.

An important piece of our code is to classify sets of such messages into what we call market events—for instance, a “new order - executed in full” event, or a “resting order - passive execution”

¹⁶Computational backlogs associated with such bursts of messages were thought to play a role in the U.S. Treasury Market Flash Crash of October 15, 2014. See Joint Staff Report (2015)

event. In this section we first describe the contents of inbound and outbound messages, and then describe how we classify messages into market events. For more complete details, please see the data appendix.

2.3.1 Inbound Messages

Each inbound message contains the following kinds of information:

- Identifiers. These fields contain the symbol and date the message is associated with; the UserID of the participant who submitted the message; and a participant-supplied ID for the message. Additionally, if the message is a cancel or modification of an existing order, then the message contains identifying information for the existing order.
- Message Type Information. Each message indicates what type of message it is, economically: for instance, a new limit order, a cancel, a cancel-replace, or an immediate-or-cancel order.
- Price/Quantity/Side Information. Last, if a message is a new order or a modification of an existing order, it will of course indicate the price, quantity, and direction (buy/sell).

2.3.2 Outbound Messages

Each outbound message contains the following kinds of information:

- Identifiers. These fields typically contain all of the same information as the inbound message, with the addition, for new orders, of a matching-engine-supplied OrderID. That is, for new orders, on the way in they just have the participant-supplied ID, but on the way out they contain both the participant-supplied ID and the matching-engine-supplied ID.
- Message Outcome Information. Outbound messages contain several fields that provide information on the outcome of an inbound message just submitted. One field reports on what type of activity the matching engine just executed: for instance, a post to the book, a trade, or a failed immediate-or-cancel request. A second field indicates the current status of the order: the main status options are new, filled, partially filled, canceled, and expired. A third field specifically allows us to see if a cancel request failed; failed cancels require a special treatment because the order the user tried to cancel no longer exists in the matching engine's state.
- Trade Execution Reports. If a new order results in a trade, outbound messages will be sent to both parties in the trade with trade execution reports detailing the price, quantity, and side. If an order matches with multiple counterparties or at multiple prices there will be a separate pair of outbound messages for each such match.
- Price/Quantity/Side Status Information. Any outbound message that relates to an order that has not yet been fully executed or canceled will also report the order's price, side, and remaining quantity.

Table 2.1: **Classifying Inbound and Outbound Messages Into Events**

Event Name	Inbound Message Type	Outbound Message Type
New order posted to book	New Order (Limit)	New Order Accepted
New order aggressively executed in full	New Order (Limit)	Full Fill (Aggressive)
	New Order (IOC)	Partial Fill (Aggressive) - multiple such orders that sum to the full quantity
New order aggressively executed in part	New Order (Limit)	Partial Fill (Aggressive) - one or more that sum to less than the full quantity
	New Order (IOC)	Order Expire - for IOCs, not Limits which will post the remainder
Order passively executed in part	-	Partial Fill (Passive)
Order passively executed in full	-	Full Fill (Passive)
Cancel accepted	Cancel	Cancel Accept
Failed cancel	Cancel	Cancel Reject
Failed IOC	New Order (IOC)	Order Expire

Notes: Please see the text of Section 2.3.1 for a description of the contents of inbound messages, Section 2.3.2 for a description of the contents of outbound messages, and Section 2.3.3 for a description of event classification.

2.3.3 Event Classification

Combinations of inbound and outbound messages indicate market events, as listed in Table 2.1. In order to perform this classification, our code loops through all messages sequentially, and at each inbound message loops ahead to find all related outbound messages (using the information from both the participant-supplied and matching-engine supplied identifiers), to classify events as listed in the table. For complete details of this key piece of code please see the data appendix.

For all events other than passive fills, we define the time of the event based on the time of the inbound message timestamp; this timestamp is what will be relevant for race detection. For passive fills, we define the time of the event based on the time of the outbound message; this information is not related to race detection per se but will help us maintain the order book as discussed next.

2.3.4 Maintaining the Order Book

Observe that neither inbound nor outbound messages contain the state of the limit order book—i.e., the prices and quantities at the best bid and offer, and at other levels of the order book away from the best bid and offer. This is because conveying the state of the order book in each message, while convenient, would mean larger and hence slower messages. We thus have to build and maintain the state of the limit order book ourselves.

We maintain the state of the limit order book, for each symbol-date, on *outbound* messages. We use outbound messages rather than inbounds because outbound messages report what the matching engine actually did. Whenever we compute race statistics that rely on the order book, we utilize the state of the order book as of the first inbound message in the race. There are a few technical

details related to maintaining the order book with message data that we discuss in more detail in the data appendix, along with discussion of robustness checks.

3 Defining and Measuring Latency Arbitrage Races

The theory in BCS,¹⁷ and a modest extension we include as Appendix F.1, suggest that the empirical signature of a latency-arbitrage race in response to public information, as distinct from Kyle-Glosten-Milgrom-style informed trading based on private information, is:

1. Multiple market participants acting on the same symbol, price, and side
2. Either a mix of take attempts and cancel attempts (equilibrium emphasized in BCS), or all take attempts (if the liquidity provider is slow, see Appendix F.1)
3. Some succeed, some fail
4. All at the “same time.”

Of these, characteristics #1-#3 are relatively straightforward to define and implement. We structure the analysis so that our baseline is likely to be inclusive of all races and the alternatives filter down to more-conservative subsets of races.

Characteristic #4 is conceptually more difficult. In a theory model there is such a thing as the “same time” but in data no two things happen at *exactly* the same time. We structure the analysis so that the baseline method is conservative and then consider a wide range of sensitivity analyses.

Note that throughout, when we describe either actions or timestamps, we refer to the *inbound* messages and timestamps, enhanced with the event classification information described above in Section 2.3 using subsequent outbound messages. For example, if we refer to a failed IOC, we are referring to the inbound IOC message and its timestamp, having inferred from subsequent outbound messages that the IOC failed to execute.

3.1 Characteristic #1: *Multiple market participants act on the same symbol, price, and side*

The “same symbol, price, and side” aspect is straightforward. Every limit order message (including IOC’s, etc.) includes the symbol, price, and side of the order. We interpret a limit or IOC order to buy at p as relevant to any potential race at price p or lower, and similarly a limit or IOC order to sell at p as relevant to any race at price p or higher. Cancel messages can be linked to the price and side information of the order that the message is attempting to cancel. We count a cancel order of a quote at price p as relevant to races at price p only.¹⁸

¹⁷Please see Section 4.1 of the working paper version of this paper for a brief review of the relevant theory.

¹⁸For example, if we observed an IOC to buy at 20 and a cancel of an ask at 21 at the same time, we would not want to count that as a race at 20. Whereas, if we observed an IOC to buy at 21 and a cancel of an ask at 20 at the same time, we potentially would want to count that as a race at 20.

Our baseline definition of “multiple market participants” is 2+ unique UserIDs. Note that a particular trading firm might use different UserIDs for different trading desks. Our approach treats distinct trading desks within the same firm as potentially distinct competitors in a latency-sensitive trading opportunity.

In sensitivity analyses, we also consider larger minimum requirements for the number of participants in the race, especially 3+, and requiring that the FirmIDs are unique, not just UserIDs.

3.2 Characteristic #2: *Either a mix of take and cancel attempts, or all take attempts*

For our baseline, we require that a race consist of either a mix of take and cancel attempts (i.e., 1+ aggressors and 1+ cancelers) or all take attempts (i.e., 2+ aggressors and 0 cancelers).

In sensitivity analyses, we also consider requiring both an aggressor and a canceler (that is, excluding races with 2+ aggressors and 0 cancelers), and requiring 2+ aggressors.

3.3 Characteristic #3: *Some succeed, some fail*

For our baseline, we require 1+ success and 1+ fail, defined as follows.

Fails. A cancel attempt is a fail if the matching engine responds with a too-late-to-cancel error message. An immediate-or-cancel limit order is a fail if the matching engine responds with an “expired” message, indicating that the IOC order was canceled because it was unable to execute immediately. Note that an IOC order that trades any positive quantity will not count as a fail, even if the traded quantity is significantly less than the desired quantity.

In our baseline, we count a limit order as a fail in a race at price p if it was priced aggressively with respect to p (i.e., is an order to buy at $\geq p$ or an order to sell at $\leq p$) but obtains zero quantity at p . While most sniping attempts in our data are IOCs (over 90% in the baseline race analysis), in a race it can make sense to use limit orders instead of IOCs for two reasons. First, by using a limit order instead of an IOC, the participant posts any quantity he does not execute to the book, which in principle may yield advantageous queue position in the post-race order book. Second, at the LSE, there was a small (0.01 GBP per message) fee advantage to using plain-vanilla limit orders instead of IOC orders. This difference means that, technically, IOCs are often dominated by “synthetic IOCs” created by submitting a plain-vanilla limit order followed by a cancellation request.¹⁹

In sensitivity analysis, we consider an alternative in which only failed IOCs and failed cancel attempts count as fails, and plain-vanilla limit orders cannot count as fails. This sensitivity reflects the possibility that a limit order that obtains zero quantity at p and instead posts to the book may represent post-race liquidity provision reflecting the post-race value, as opposed to a failed

¹⁹At the time of our data and as of this writing, the LSE assessed an “Order management charge” of 0.01 GBP for non-persistent orders such as IOCs, whereas there was no order management charge for plain-vanilla limit orders (London Stock Exchange Group, 2015). An exception is if the trader has triggered the “High usage surcharge” by having an order-to-trade ratio of at least 500:1; such traders must pay a fee of 0.05 GBP per message, so the synthetic IOC would be nearly twice as expensive as an IOC (London Stock Exchange Group, 2015). Our understanding is that triggering this surcharge is rare.

attempt to snipe. We will emphasize this alternative, which we refer to as “strict fail”, especially in sensitivity analyses with longer time horizons where we are more concerned about the post-race liquidity provision issue.

Successes. For our baseline, we consider an IOC or a limit order to be successful in a race at price p if it is priced aggressively with respect to p (i.e., is an order to buy at $\geq p$ or an order to sell at $\leq p$) and obtains positive quantity at a price p or better (i.e., it buys positive quantity at a price $\leq p$ or sells positive quantity at a price of $\geq p$). We consider a cancel to be successful in a race at price p if the order being canceled is at price p and the cancel receives a cancel-accept response.

We note that this requirement is inclusive in two senses. First, it counts an IOC or a limit order as successful even if it trades only part of its desired quantity. However, the fact that an IOC or limit order trades only part of its desired quantity, in conjunction with the requirement that some *other message fails*—i.e., some other participant tried to cancel and received a too-late-to-cancel message, or some other participant tried to aggress at p but executed zero quantity—will typically mean that the full quantity available at price level p was contested and there were genuine winners and losers of the race. The possible exception is a successful IOC or limit for a subset of the available liquidity at price p , in conjunction with a failed cancel for part of that same subset of the available liquidity at price p .

Second, it counts a cancel as a success even if it cancels just a small quantity relative to the full quantity available at price level p . However, if the only success is a cancel, then since we also require a fail and 1+ aggressor, this implies that the full quantity available at price level p was contested and there were genuine winners and losers of the race.

In sensitivity analysis, we also consider requiring proof that 100% of depth at the race price is successfully cleared in the race. This can be satisfied in three ways: observing a failed IOC at the race price p ; observing a limit order at the race price p that posts to the book at least in part; or observing quantity traded plus quantity canceled of 100% of the displayed depth at the start of the race.

3.4 Characteristic #4: *all at the “same time.”*

Of the 4 characteristics, this last one is conceptually the hardest. In a theory model there can be a precise distinction between simultaneous and non-simultaneous actions, but in data no two things happen at *exactly* the same time if time is measured precisely enough. Indeed, even if a regulatory authority or exchange *intends* for market participants to receive a piece of information at exactly the same time, and even if the market participants have exactly the same technology and choose exactly the same response, there will be small measured differences in when they receive the information, and when they respond to the information, if time is measured finely enough.²⁰

We consider two different approaches to this issue.

²⁰Try to blink your left eye and right eye at exactly the same time, measured to the nanosecond. You will fail! Computers are better at this sort of task than humans are, but even they are not perfect. See, e.g., MacKenzie (2019).

Baseline Method: Information Horizon. Our baseline approach, which we call the Information Horizon method, requires that the difference in inbound message timestamps between the first and second participants in a race is small enough that we are essentially certain that the second participant is not reacting to the action of the first participant. Concretely, we measure the information horizon as:

$$\begin{aligned} \text{Information Horizon} = & \text{Actual Observed Latency : } M1 \text{ Inbound} \rightarrow M1 \text{ Outbound} \\ & + \text{Minimum Observed Reaction Time : } M1 \text{ Outbound} \rightarrow M2 \text{ Inbound} \end{aligned}$$

where: M1 refers to the first message in a race; M2 refers to the second message in the race; Actual Observed Latency M1 Inbound \rightarrow M1 Outbound refers to the actual measured time between M1’s inbound message’s timestamp and its outbound message’s timestamp, and Minimum Observed Reaction Time M1 Outbound \rightarrow M2 Inbound refers to the minimum time it takes a state-of-the-art high-frequency trader to respond to a matching engine update, as measured from the outbound message’s timestamp to the response’s inbound message timestamp.

Given this formula, if M2’s inbound message has a timestamp that follows M1’s inbound message by strictly less than the information horizon, then the sender of M2 logically cannot be responding to information about the outcome of M1. Whereas, if M2’s inbound message has a timestamp that follows M1 by more than the information horizon, it is logically possible that M2 is a response to M1. In this method, such a response would not be interpreted as the same time.

In our data we compute the Minimum Observed Reaction Time as 29 microseconds,²¹ and the median Actual Observed Latency is about 150 microseconds (90th percentile: about 300 microseconds). We provide further details in Appendix A. We also decided, in consultation with FCA supervisors, to place an upper bound on the information horizon of 500 microseconds. That is, if the sum of the observed matching engine latency and the minimum observed reaction time exceeds 500 microseconds, we use 500 microseconds as the race horizon instead. The reason for this upper bound is that our assumption that M1 and M2 are responses to the same (or essentially same) information set becomes strained if the observed matching engine latency is sufficiently long, because even though the sender of M2 would not be able to see M1, the sender of M2 might have seen new data from other symbols or from other exchanges. We would expect all of these parameters to be potentially different for different exchanges or different periods in time.

Alternative Method: Sensitivity Analysis. Our second approach to defining what it means for multiple participants to act at the “same time” is more agnostic. For a range of choices of T , we define “same time” as no further apart than T . Clearly, if we choose T to be the finest amount of time observable in our data (100 nanoseconds) there will be essentially no races, whereas if we choose T to be too long the results will be meaningless. We will conduct this analysis for T ranging

²¹This 29 microseconds reflects a combination of the minimum time it takes an HFT to react to a privately-received update from an outbound message, plus the difference in data speed between a private message sent to a particular market participant (M1 outbound) and data obtained from the LSE’s proprietary data feed, which is different from our message data. In fact, our analysis suggests that the 29 microseconds is comprised of about 17 microseconds from the first component and about 12 microseconds from the second component, as we describe in Appendix A.

from 50 microseconds to 3 milliseconds. A summary of the results are presented in Section 5.1 with full details in Appendix C.1. What T 's would be of interest we would expect to evolve over time as technology evolves.

A Note on Code Structure and Overlapping Races. If we observe a race at a price level of p starting at time t , we do not look for other races at p until at least either the information horizon or T amount of time has passed (in the baseline and sensitivities, respectively). That is, we do not allow for “overlapping” races at a single price level.

Relatedly, in the event of a latency-arbitrage race that occurs across multiple levels of the book (e.g., in the event of a large change in public information about the value of an asset), we structure our code so that it identifies races that satisfies the four characteristics described above at one price level at a time. That is, if p and p' are separate price levels in a multi-level race, our code will detect two single-level races, one at p , starting at say time t , and one at p' starting at say time t' .

4 Main Results

This section presents all of our main results under the baseline specification as described in Section 3. In the following section (Section 5) we will discuss various alternative specifications and sensitivity analyses. Section 4.1 presents results on race frequency, duration, and trading volume. Section 4.2 presents results on race participation patterns. Section 4.3 presents results on profits per race. Section 4.4 presents results on aggregate profits and the latency arbitrage tax. Section 4.5 presents two spread decompositions that explore what proportion of the cost of liquidity is the latency arbitrage component versus the traditional adverse selection component.

4.1 Frequency and Duration of Latency-Arbitrage Races

Races Per Day

The average FTSE 100 symbol in our sample has 537 races per day. Over an 8.5 hour trading day, this corresponds to a race roughly once per minute per symbol. There are fewer races for FTSE 250 symbols: the average FTSE 250 symbol has 70 races, or roughly one per 7 minutes. Also, while all FTSE 100 symbols have daily race activity (the minimum is 76 races per day), the bottom quartile of FTSE 250 symbols have zero or hardly any race activity. See Table 4.1, Panel A. Across all symbols in our data, there are on average about 71,000 races per day, of which 54,000 are FTSE 100 and 17,000 are FTSE 250. This total number of races per day ranges from a min of 48,000 to a max of 144,000. See Table 4.1, Panel B.

Race Durations

The average race duration in our data, as measured by the time from the first success message to the first fail message, is 79 microseconds, or 0.000079 seconds. Figure 4.1 depicts the distribution of race durations. The mode of the distribution is between 5-10 microseconds, and the median is

Table 4.1: **Races Per Day**

Panel A: Number of races per day across symbols

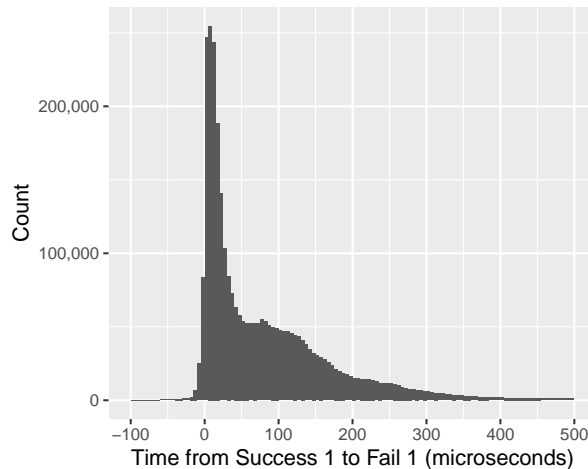
Description	Mean	sd	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99
FTSE 100	537.24	473.26	132	184	240	352	619	1,134	2,067
FTSE 250	70.05	93.53	0	0	2	44	104	166	404
Full Sample	206.03	340.73	0	1	14	87	239	511	1,814

Panel B: Number of races per day across dates

Description	Mean	sd	Min	Pct10	Pct25	Median	Pct75	Pct90	Max
FTSE 100	54,261	15,660	35,174	40,490	44,036	51,361	60,632	70,588	117,370
FTSE 250	17,232	3,856	11,536	13,444	14,800	16,125	19,404	23,326	26,613
Full Sample	71,493	19,223	48,175	54,264	58,698	64,516	79,429	93,914	143,752

Notes: Please see Section 3 for a detailed description of the baseline race-detection criteria and Section 2 for details of the message data including how we classify inbound messages and how we maintain the order book. This table reports the distribution of the number of races detected at the symbol level (Panel A) and at the date level (Panel B). The symbol level averages across all dates for each symbol. The date level sums across all symbols for each date.

Figure 4.1: **Duration of Races**



Notes: For each race detected by our baseline method we compute the difference in message timestamps between the first inbound message in the race that is a success and the first inbound message in the race that is a fail (success and fail are defined in Section 3.3). Denote these messages S1 and F1, respectively. The figure plots the distribution of F1’s timestamp minus S1’s timestamp in microseconds, that is, by how long did the first successful message in the race beat the first failed message. The histogram has a bin size of 5 microseconds.

46 microseconds. There is then steady mass in the distribution up until about 150 microseconds, the 90th percentile is about 200 microseconds, and there is a tail up to our truncation point of 500 microseconds. Appendix Table B.1 provides additional details on the distribution.

Sometimes the “Wrong” Message Wins

Interestingly, in Figure 4.1, there is a small amount of mass to the left of zero; that is, the first fail message arrives before the first success message. Recall from Section 2.2 that our timestamps are

Table 4.2: **Volume and Trades in Races**

Panel A: Percentage of volume (value-weighted) in races across dates

Description	Mean	sd	Min	Pct10	Pct25	Median	Pct75	Pct90	Max
FTSE 100	22.15	1.90	17.84	20.09	21.15	22.02	23.11	24.85	26.08
FTSE 250	16.90	1.78	11.58	14.73	15.71	17.07	18.19	19.21	20.13
Full Sample	21.46	1.75	17.63	19.70	20.50	21.41	22.53	24.02	25.02

Panel B: Percentage of number of trades in races across dates

Description	Mean	sd	Min	Pct10	Pct25	Median	Pct75	Pct90	Max
FTSE 100	20.69	1.59	16.91	18.62	19.83	20.80	21.58	22.93	23.51
FTSE 250	16.96	1.50	13.29	15.24	16.01	17.01	18.07	18.91	19.31
Full Sample	19.70	1.42	16.07	18.04	18.94	19.65	20.68	21.73	22.22

Notes: For each symbol-date in our dataset, we obtain all outbound messages in regular-hours trading that are aggressive fills (see fn. 23 for more detail). We then obtain the inbound message associated with each such outbound aggressive fill, and check whether the inbound is part of a race (as defined in Section 3). For Panel A, for each date, we then sum the quantity in GBP associated with all aggressive fills that are part of races, divided by the quantity in GBP associated with all aggressive fills, whether or not in race. For Panel B, for each date, we then sum the number of trades associated with all aggressive fills that are part of races, divided by the number of trades associated with all aggressive fills, whether or not in race.

obtained at the outer wall of the exchange’s system. It is therefore possible, if two race messages arrive to different gateways at nearly the same time, that they reach the matching engine in a different order from the order at which they reached the exchange’s outer perimeter. Thus, the “wrong” message wins the race about 4% of the time in our data.

We do not think the fact that the wrong message wins is necessarily that economically interesting; it is akin to one shopper choosing a slightly faster queue than another shopper at the supermarket. Rather, we think of the result as reinforcing just how fast races are: they are so fast that randomness in exchange gateway processing is sometimes the difference between winning and losing.²²

Significant Trading Volume in Races

For the average FTSE 100 symbol, races take up a total of 0.043 seconds per day, or about 0.0001% of the trading day. During this tiny slice of the trading day, an average of 21% of FTSE 100 trades take place corresponding to 22% of FTSE 100 daily trading volume (value-weighted).²³ For the average FTSE 250 symbol, races take up about 0.00002% of the trading day. During this time 17% of trades take place constituting 17% of daily trading volume. Please see Table 4.2.

²²Please also see a recent essay of MacKenzie (2019) on various aspects of randomness in high-frequency trading races.

²³We compute daily trading volume in our data by obtaining all outbound messages during regular hours that are aggressive fills — that is, that report a trade execution to a just-received inbound message that aggressed against a previous resting order. In the event classification table (Table 2.1), these are the events called “New order aggressively executed in full” and “New order aggressively executed in part.” We count just the aggressive side of the trade to prevent double counting.

Table 4.3: Number of Participants and Messages in Races

Panel A: Number of participants											
Description	Mean	sd	Min	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99	Max
Participants within 50 μ s	1.77	0.86	1	1	1	1	2	2	3	5	12
Participants within 100 μ s	2.08	0.97	1	1	1	1	2	2	3	5	13
Participants within 200 μ s	2.56	1.13	1	1	2	2	2	3	4	6	16
Participants within 500 μ s	3.27	1.56	2	2	2	2	3	4	5	9	23
Participants within 1000 μ s	3.64	1.94	2	2	2	2	3	4	6	11	26

Panel B: Number of take messages											
Description	Mean	sd	Min	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99	Max
Takes within 50 μ s	1.66	0.97	0	0	1	1	1	2	3	5	14
Takes within 100 μ s	1.93	1.08	0	0	1	1	2	2	3	5	15
Takes within 200 μ s	2.37	1.30	0	1	1	1	2	3	4	7	17
Takes within 500 μ s	3.07	1.78	1	1	1	2	3	4	5	9	29
Takes within 1000 μ s	3.45	2.19	1	1	1	2	3	4	6	11	40

Panel C: Number of cancel messages											
Description	Mean	sd	Min	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99	Max
Cancels within 50 μ s	0.17	0.41	0	0	0	0	0	0	1	1	8
Cancels within 100 μ s	0.22	0.47	0	0	0	0	0	0	1	2	8
Cancels within 200 μ s	0.30	0.56	0	0	0	0	0	1	1	2	12
Cancels within 500 μ s	0.40	0.70	0	0	0	0	0	1	1	3	14
Cancels within 1000 μ s	0.44	0.78	0	0	0	0	0	1	1	3	21

Notes: For each race detected by our baseline method we obtain the timestamp of the first inbound message and the price and side of the race. We then use the message data to obtain all messages within the next T microseconds, for different values of T as depicted in the table, that are race relevant, defined as either new orders that are aggressive at the race price and side or cancels at exactly the race price and side. Panel A depicts the distribution of the number of participants with at least one race-relevant message. Panel B depicts the distribution of the number of race-relevant take messages and Panel C depicts the distribution of race-relevant cancel messages.

4.2 Race Participation

Number of Participants

Table 4.3, Panel A provides data on the number of participants in races. Since the information horizon varies across races depending on the matching engine’s processing lag, to keep the measure consistent across races we report the distribution for varying amounts of time T after the start of the race, ranging from 50 microseconds to 1 millisecond. Note that 50 microseconds is shorter than the information horizon for nearly all races and 1 millisecond is longer than the information horizon for all races (which is capped at 500 microseconds). Focusing on the 500 microseconds row, the average race has about 3.3 participants; the median has 3 participants; the 25th percentile has 2 participants; and there is a right tail with a 99th percentile of 9 participants and a max of 23 participants.

Comparing the 500 microseconds row to the 50 and 100 microseconds rows, we see that at shorter time horizons there are fewer participants. This is consistent with heterogeneity in speed, whether across firms or across different kinds of public signals.

Number of Takes and Cancels

Panels B and C of Table 4.3 provide the distribution of the number of take messages and cancel messages in races, respectively. Focusing initially on the 500 microseconds row, we see that the 3.27 participants per race send an average of 3.47 messages of which 3.07 are takes and 0.40 are cancels. These figures tell us that in most races most of the activity is aggressive. This is consistent with equilibria of the BCS model in which the fastest traders primarily engage in sniping as opposed to liquidity provision, and substantial liquidity is provided by participants who are not the very fastest participants in the market (see Appendix F.1 for theoretical discussion of these equilibria). We will return to this pattern shortly.

Of these 3.07 take attempts, the large majority, 2.81, are immediate-or-cancel orders (IOCs) that are marketable at the race price, with the remainder, 0.25, being ordinary limit orders that are marketable at the race price. Please see Appendix Table B.5 for this and additional participation data.

Pattern of Winners and Losers

Figure 4.2 displays data on the pattern of winners and losers across races. The figure is sorted by firm based on the proportion of races in which they are the first successful message (S1). As can be seen, the top 3 firms are each either S1 or F1 (i.e., the first fail message) in over one-third of races, with firm 1 winning 21% of races while losing another 18% of races, firm 2 winning 18% of races while losing 27%, and firm 3 winning 15% of races while losing 19%. The next 3 firms then each win about another 9% of races each, and then there are another 4 firms that win between 2-4% of races each.

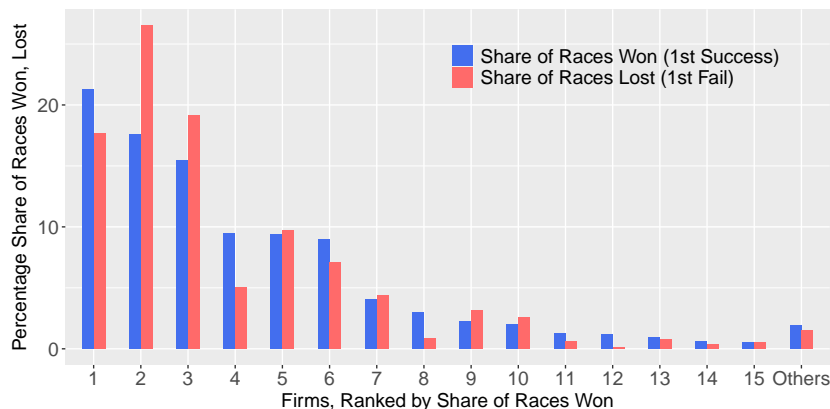
It is notable that there is clear concentration of winners, with the top 3 firms winning 54% of races, and the top 6 firms winning 82% of races. Yet, these same firms who win a lot of races also lose a lot of races. The top 3 winning firms lose 63% of races, and the top 6 lose 85%. These patterns are consistent with the BCS model in two ways. First, as the model suggests, fast trading firms “sometimes win, sometimes lose,” and indeed in any particular race who wins may be a bit random. Second, as the model suggests, firms not at the cutting edge of speed should essentially never be competitive in a race. Put differently, these facts are consistent with the idea that there is an arms race for speed, and that, at least in UK equity markets circa 2015, there are a relatively small number of firms competitive in this race.²⁴

Pattern of Takes, Cancels, and Liquidity Provision

Figure 4.3 Panel A shows that about 90% of races are won with a take (i.e., aggressive order or snipe attempt) with the remaining 10% won by a cancel. This makes sense in light of the data in Table 4.3 which showed that most of the message activity in races is take attempts as opposed to cancel attempts.

²⁴Around this time, a US high-frequency trading CEO described to one of the authors of this study that, in the US, there were 7 firms in what he called the “lead lap” of the speed race.

Figure 4.2: **Percentage of 1st Successful and 1st Failed Messages by Firm (FTSE 100 Races)**



Notes: For each race detected by our baseline method we obtain the FirmID of the participant who sends the first success message and the first fail message (i.e., S1 and F1, respectively, in Figure 4.1). We then compute, over all races for FTSE 100 symbols, for each FirmID that appears, the portion of races in which that FirmID is the first success message, and the portion of races in which that FirmID is the first fail message. The table sorts FirmIDs based on the proportion of races won. The “Others” bar sums all FirmIDs outside of the top 15.

Figure 4.3 Panel B provides data on the pattern of successful takes, successful cancels, and liquidity provision across firms. The top 6 firms, as defined by the proportion of races won as shown in Figure 4.2, account for about 80% each of race wins, liquidity taken in races, and liquidity successfully canceled in races. In contrast, these 6 firms account for about 42% of all liquidity provided in races — that is, of all of the trading volume in races, 42% is volume where the resting order had been provided by one of the top 6 firms.

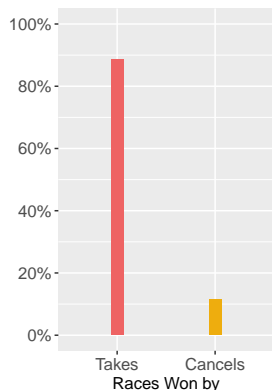
Within these top 6 firms there are two distinct patterns of race participation. 2 of the top 6 firms together account for 28% of race wins, 22% of liquidity taken, 61% of successful cancels in races, and 31% of all liquidity provided in races. These data suggest that these 2 firms engage in meaningful quantities of both stale-quote sniping and liquidity provision; their ratio of liquidity taken in races to liquidity provided in races is about 2:3. The remaining 4 of the top 6 firms together account for 54% of race wins, 57% of liquidity taken, 21% of successful cancels, and just 11% of all liquidity provided in races. These data suggest that these 4 firms engage in significantly more stale-quote sniping than liquidity provision; their ratio of liquidity taken in races to liquidity provided in races is 5:1. We therefore denote these two groups of firms as “Balanced in Top 6” and “Takers in Top 6”, respectively.²⁵

Market participants outside of the top 6 firms account for about 20% each of race wins, liquidity taken in races, and liquidity successfully canceled in races. Where they stand out is that they account for 58% of all liquidity provided in races; that is, they provide nearly 3 times as much

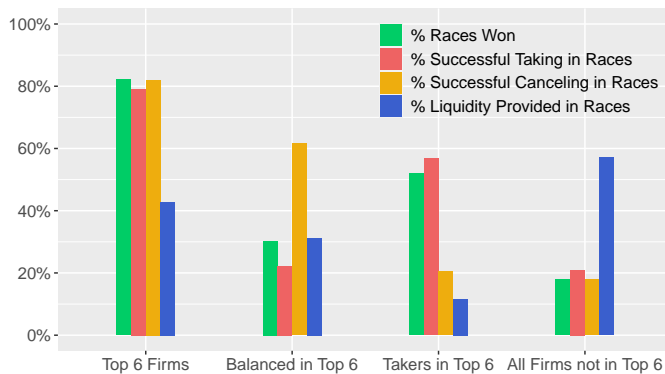
²⁵Previous studies that document heterogeneity across HFT firms with respect to their taking and liquidity provision behavior include Benos and Sagade (2016) and Baron et al. (2019). Benos and Sagade (2016) report that the most aggressive group of firms in their sample have an aggressiveness ratio of 82%, which means that 82% of their overall trading volume is aggressive, with the remaining 18% passive. Baron et al. (2019) report that the 90th percentile of firms in their sample have an aggressiveness ratio of 88%.

Figure 4.3: **Pattern of Takes, Cancels, and Liquidity Provision**

Panel A: Races Won by Takes vs. Cancels



Panel B: Analysis by Firm Group



Notes: Panel A: For each FTSE 100 race detected by our baseline method we obtain whether the first successful message (i.e., S1) is a take or a cancel. Panel B: The first bar, % Races won, reports the data depicted in Figure 4.2 aggregated by firm group, with the firm groups as described in the text. The second bar, % Successful Taking in Races, is computed by taking all trading volume in all FTSE 100 races and utilizing the FirmID associated with the aggressive order in each trade. The third bar, % Successful Canceling in Races, is computed by taking all successful cancels in FTSE 100 races and utilizing the FirmID associated with the cancel attempt. The fourth bar, % Liquidity Provided in Races, is computed by taking all trading volume in all FTSE 100 races and utilizing the FirmID associated with the passive side of each trade, i.e., the resting order that was taken by the aggressive order utilized in the % Successful Taking bar.

Table 4.4: **Liquidity Taker-Provider Matrix**

% of Race Volume by Taker-Provider Combination

		Provider		
		Takers in Top 6	Balanced in Top 6	Non-Top 6
Taker	Takers in Top 6	5.7	17.2	34.3
	Balanced in Top 6	2.5	6.4	13.3
	Non-Top 6	3.2	7.4	10.1

Notes: For each race detected by our baseline method we obtain all executed trades, and for each executed trade we obtain the FirmID of the participant who sent the take message that executed and the FirmID of the participant whose resting order was passively filled. The FirmIDs are classified into firm groups as described in the text. Each cell of the matrix reports the percentage of GBP trading volume associated with that particular combination of taker firm group and liquidity provider firm group.

liquidity in races as they take.

Thus, on net, much race activity consists of firms in the top 6 taking liquidity from market participants outside of the top 6. This taking is especially concentrated in a subset of the fastest firms who account for a disproportionate share of stale-quote sniping relative to liquidity provision. The modal trade in our race data consists of a Taker in Top 6 firm taking from a market participant outside the top 6 (34.3% of all race volume). This pattern seems more consistent with the “rigged” as opposed to “myth” point of view as discussed in the introduction.

There is also significant race activity that consists of the fastest firms taking from each other. This volume is especially likely to consist of a Taker in Top 6 firm sniping a Balanced in Top 6 firm

(17.2%). Please see Table 4.4 for a matrix of race trading volume organized by such taker-provider combinations.

Expected Number of Races By Chance

We can use the arrival rate of messages that could potentially be part of a race to compute the number of races we would expect to observe by chance if messages arrived Poisson randomly.²⁶ We say that a message is potentially-race-relevant if the message is either a marketable limit order (including marketable IOCs) or a cancel of a message at the best bid or offer. For each symbol-date, we compute the total number of such potentially-race-relevant messages per day to get an average arrival rate; to fix ideas, the average arrival rate for FTSE 100 symbols is a bit over 1 potentially-race-relevant message per second. We then use these arrival rates to compute the number of times per day we would expect to observe N such messages within T time on the same side of the order book.

For the mean FTSE 100 symbol-date, the number of times per day we should expect to see $N = 2$ such messages on the same side of the order book within $T = 200$ microseconds, about the mean information horizon in our data set, is 1.42. The number of times we would expect to see $N = 2$ such messages within $T = 500$ microseconds, the upper bound on the information horizon, is 3.55. For the mean FTSE 250 symbol-date, the figures are 0.02 and 0.04. The number of times we would expect to see $N = 3$ or more such messages arrive by chance in such a time window, for either FTSE 100 or FTSE 250, is 0.00. Please see Table 4.5.

Accounting for the fact that the rate of message arrivals is higher near the open and close of the UK trading day, and during the window that coincides with the U.S. open, increases these numbers only modestly. Even if we assume that the entire trading day is as busy as the symbol-date's busiest half-hour segment, the average number of times we would observe 2 messages that could possibly be racing, within 500 microseconds, is just 13.26 for FTSE 100 symbols and 0.21 for FTSE 250 symbols.

Keep in mind as well that all of these figures are *upper bounds* on the number of N -participant races that would occur by chance, because occurrences of messages on the same side of the order book at the same time only constitute a race if our other race criteria are satisfied (in particular, at least one message must fail).

The bottom line is that the number of races we would observe by chance is de minimis. For additional details, see Appendix B.2.

²⁶An influential paper by Engle and Russell (1998) provides more sophisticated econometric techniques to deal with the fact that messages arrive at time-varying rates. In the introduction they write: "Even more intriguing is the case of transactions that are generally infrequent but that may suddenly exhibit very high activity. This may be due to some observable event such as a news release or to an unobservable event which may best be thought of as a stochastic process." Our paper relates to Engle and Russell (1998) in that it relates to *why* messages sometimes arrive in bursts, and in particular in clusters in amounts of time that would have been difficult to fathom at the time of Engle and Russell (1998). For this reason, we use Poisson as a particularly simple benchmark to give a sense of how many races one might expect to observe by chance, and then use as a sensitivity an increased Poisson arrival rate, reflecting the kinds of higher arrival rates Engle and Russell (1998) had in mind at for instance the market's open and the close.

Table 4.5: **Expected Number of Potential Race Events By Chance**

	FTSE 100		FTSE 250	
	Average Rate	Busiest 30 Mins	Average Rate	Busiest 30 Mins
Expected Occurrences by Chance				
2+ within 50 μs	0.35	1.33	0.00	0.02
2+ within 100 μs	0.71	2.65	0.01	0.04
2+ within 200 μs	1.42	5.31	0.02	0.09
2+ within 500 μs	3.55	13.26	0.04	0.21
2+ within 1000 μs	7.09	26.49	0.08	0.43
3+ within 1000 μs	0.00	0.03	0.00	0.00
Actual Number of Races				
Baseline analysis		537.24		70.05
3+ within Info Horizon		228.98		30.68

Notes: For each symbol-date we calculate the arrival rate of potentially-race-relevant messages (see text for description) and use this to compute the expected number of occurrences of N such messages within T microseconds, on the same side of the order book, if messages arrive at this rate via a Poisson arrival process. For each symbol-date we also perform this calculation using the arrival rate of potentially-race-relevant messages during the busiest 30 minutes of the day for that symbol-date, assuming the entire day has this level of activity. We also report the actual number of races, both for the baseline and for the sensitivity in which we condition on there being at least 3+ participants within the information horizon.

4.3 Race Profits

Profits Per-Race

Table 4.6 presents statistics on per-race profits. As in BCS, we compute profits as the signed difference between the price in the race and the midpoint in the near future, which has the interpretation of the mark-to-market value for the asset in the race.²⁷ Our main results use the midpoint 10 seconds out, and we will report figures for horizons ranging from 1 millisecond to 100 seconds shortly.²⁸

The average FTSE 100 race is worth about half a tick per share (0.48 ticks), or about 1.20 basis points. This comes to about 2 GBP per race, measured either using all of the displayed depth at the start of the race (1.95 GBP) or all of the quantity traded or canceled during the race (1.84 GBP). For the FTSE 250, the figures are 0.77 ticks, 3.09 basis points, and GBP 1.55 per race based on displayed depth, and GBP 1.48 per race based on quantity traded or canceled. For the full sample, the figures are 0.55 ticks, 1.66 basis points, GBP 1.85, and GBP 1.76.

²⁷Note that while successful snipers must “cross the spread” in the trade that snipes a stale quote, they need not cross the spread in unwinding this position. This is both because trading firms that engage in sniping often also engage in liquidity provision, and because sniping opportunities are equally likely to be buys versus sells. Also note that it is appropriate to ignore trading fees in computing the size of the latency arbitrage prize, as long as exchanges’ marginal costs of processing trades are zero, because trading fees assessed on latency-arbitrage trades simply extract some of the sniping prize. In any event, LSE’s trading fees are small relative to average race profits: 0.15 basis points for aggressive orders from high-volume participants, and zero for orders that are passively executed.

²⁸Since our data include firm identifiers, it would seem possible to use the actual trades made by participants to realize their profits rather than using mark-to-market profits at a range of time horizons. However, in addition to concerns about exploring specific firms’ trading strategies in more detail than is necessary for this study, given that this is a privileged regulatory dataset obtained under a Section 165 request, there are two key limitations to this idea. First, we only have data from the London Stock Exchange, so do not observe when positions are closed by trades on other venues (see also Carrion, 2013, who notes the same concern). Second, firms may not unwind positions after each race, but may instead manage inventory risk on a portfolio basis (see, for example, Korajczyk and Murphy, 2019).

Table 4.6: **Detail on Race Profits (Per-Share and Per-Race) Marked to Market at 10s**

Panel A: FTSE 100									
Description	Mean	sd	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99
Per-share profits (ticks)	0.48	4.17	-7.00	-1.50	-0.50	0.00	1.00	2.50	10.00
Per-share profits (GBX)	0.16	1.61	-2.50	-0.50	-0.05	0.00	0.25	1.00	3.50
Per-share profits (basis points)	1.20	7.75	-13.95	-4.02	-1.18	0.00	3.42	6.31	20.32
Per-race profits displayed depth (GBP)	1.95	17.87	-22.99	-3.29	-0.42	0.00	2.37	7.99	45.50
Per-race profits qty trade/cancel (GBP)	1.84	17.07	-20.74	-3.06	-0.40	0.00	2.23	7.46	41.92

Panel B: FTSE 250									
Description	Mean	sd	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99
Per-share profits (ticks)	0.77	2.99	-4.50	-1.00	-0.50	0.50	1.50	3.00	11.00
Per-share profits (GBX)	0.20	0.99	-1.50	-0.25	-0.05	0.05	0.25	0.75	3.50
Per-share profits (basis points)	3.09	11.07	-18.12	-5.14	-1.70	1.37	6.12	13.28	38.78
Per-race profits displayed depth (GBP)	1.55	9.63	-9.13	-1.52	-0.20	0.09	1.67	5.25	27.68
Per-race profits qty trade/cancel (GBP)	1.48	9.34	-8.48	-1.40	-0.19	0.09	1.55	4.94	26.40

Notes: For each race detected by our baseline method we obtain the race price and side, the quantity in the book at that price and side as of the last outbound message before the initial race message, and the quantity traded and canceled in the race. Per-share profits in ticks, pence (GBX), and basis points are computed by comparing the race price to the midpoint price 10 seconds after the first race message (i.e., as of the last outbound message before 10 seconds after the timestamp of the first race message). Per-race profits are computed by multiplying per-share profits in GBX, times 1/100 to convert to GBP, times either the quantity displayed or the quantity traded and canceled.

There is of course significant variation in profitability across races. This reflects both that some races are more profitable ex ante than others, i.e., reflect larger jumps in public information, and that over a 10 second horizon other information can materialize, either positively or negatively, that affects realized race profits ex post. Across our full sample, a 90th percentile race is worth 3.00 ticks and 7.98 basis points; a 99th percentile race is worth 10 ticks and 27.02 basis points.

Table 4.7 presents statistics on average per-race profits for different mark-to-market time horizons. As can be seen, average per-race profits increase with the time horizon, eventually flattening out at around 10 seconds for the FTSE 100 and at around 60 seconds for the FTSE 250. Our finding that it takes non-zero time for race profits to materialize, and that with this time comes noise as well, is consistent with both discussions with practitioners as well as empirical evidence in Conrad and Wahal (2020) on what they call the “term structure of liquidity.”

Figure 4.4 complements Table 4.7 by presenting the distribution of race profits and price impact at different time horizons. The difference between the two measures is that race profits are the difference between the price paid in the race and the midpoint price in the future, whereas price impact compares the midpoint at the time of the first inbound message in the race (i.e., just prior to its effect on the order book) to the midpoint price in the future (i.e., price impact does not charge the winner of the race the half bid-ask spread). Focus first on 1ms. At this relatively short time horizon, many races have profits that are either a small positive amount or small negative amount per share, whereas nearly all races have weakly positive price impact. This pattern reflects that, at the moment of a first success in a race, the mark-to-market profits of the winner are typically negative. For example, if the market is at bid 10 – ask 12, so the midpoint is 11, and there is

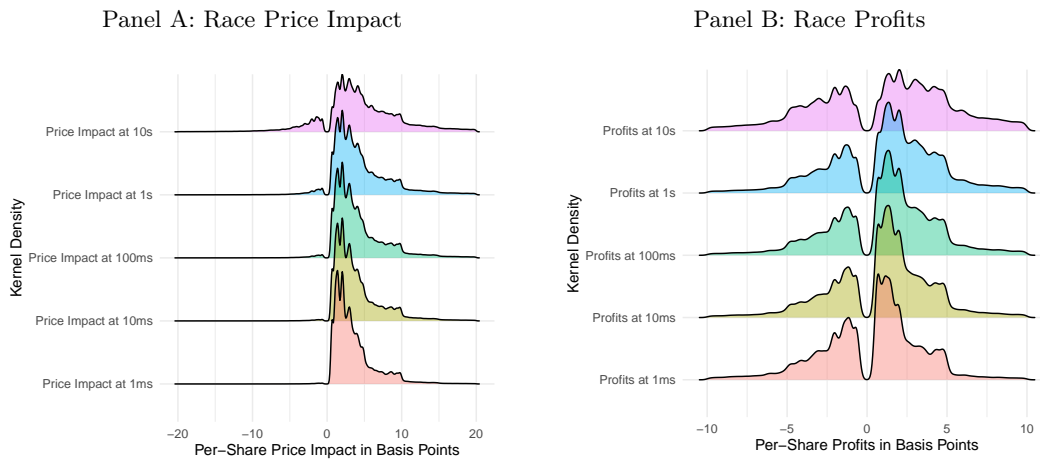
Table 4.7: Average Race Profits (Per-Share and Per-Race) for Different Mark to Market Horizons

Panel A: FTSE 100								
Description	1ms	10ms	100ms	1s	10s	30s	60s	100s
Mean per-share profits (ticks)	0.08	0.24	0.31	0.39	0.48	0.49	0.50	0.51
Mean per-share profits (GBX)	0.05	0.09	0.11	0.14	0.16	0.16	0.16	0.16
Mean per-share profits (basis points)	0.31	0.68	0.83	1.01	1.20	1.23	1.24	1.25
Mean per-race profits displayed depth (GBP)	0.40	1.14	1.42	1.72	1.95	1.89	1.86	1.82
Mean per-race profits qty trade/cancel (GBP)	0.43	1.10	1.35	1.62	1.84	1.78	1.74	1.70

Panel B: FTSE 250								
Description	1ms	10ms	100ms	1s	10s	30s	60s	100s
Mean per-share profits (ticks)	-0.10	0.12	0.24	0.43	0.77	0.94	1.04	1.06
Mean per-share profits (GBX)	-0.01	0.05	0.08	0.12	0.20	0.24	0.26	0.26
Mean per-share profits (basis points)	-0.26	0.64	1.09	1.78	3.09	3.74	4.14	4.24
Mean per-race profits displayed depth (GBP)	-0.09	0.41	0.65	0.97	1.55	1.79	1.92	1.93
Mean per-race profits qty trade/cancel (GBP)	-0.06	0.41	0.64	0.93	1.48	1.71	1.84	1.85

Notes: For each race detected by our baseline method and for each race profits measure described in Table 4.6, we re-compute the profits measure for different mark to market horizons, ranging from 1 millisecond to 100 seconds. That is, for each measure, we compute race profits by comparing the price and side in the race to the midpoint price T later, for T ranging from 1 millisecond to 100 seconds (Table 4.6 used $T = 10$ seconds). We then report the mean at each horizon.

Figure 4.4: Race Price Impact and Profits Distributions at Different Time Horizons



Notes: For each race detected by our baseline method we obtain per-share profits and price impact in basis points at different mark to market horizons ranging from 1 millisecond to 10 seconds. Profits at horizon T are defined as the signed difference between the race price and the midpoint price at time T , while price impact at horizon T is the signed difference between the midpoint price at the time of the first inbound message of the race (i.e., before that message affects the order book) and the midpoint price at time T . The figure plots the kernel density of the distribution of per-share price impact (Panel A) and per-share profits (Panel B), each in basis points, at different time horizons. To make the distributions readable, we drop all of the mass at exactly zero profits or price impact.

positive public news triggering a race to buy at 12, then a successful sniper buys at 12 while the midpoint is still 11 (or, if the market becomes bid 10 – ask 13, the midpoint becomes 11.5)—for a small mark-to-market loss. The figure shows that even by 1 millisecond, many races are profitable on a mark-to-market basis. As the figure progresses from 1 millisecond to 1 second, you can see visually that mass shifts to the right of the distribution (Table 4.7 reports the means), though there remains a meaningful mass of races with negative mark-to-market profits. Up to 1 second, nearly all races have weakly positive price impact.

Remark: Races with Negative Realized Profits. In principle, races with negative mark-to-market profits could either be spurious races that our method picks up but are not profitable, or they could be races based on public signals that multiple market participants expected to be profitable but turned out not to be profitable ex-post. Given the low likelihood of spurious races as discussed in Section 4.2 and Table 4.5, we suspect the latter interpretation is more quantitatively important. To give a sense of magnitudes, at each of the 10ms, 100ms, and 1s time horizons, about 80% of races are weakly profitable and about 20% of races have strictly negative realized profits. Conditional on race-profits being non-zero, about 70% have positive profits and 30% have negative profits. See further discussion in Section 5.2.

4.4 Aggregate Profits and the “Latency Arbitrage Tax”

Table 4.8 presents statistics on the total daily race profits in our sample. Panel A reports statistics at the symbol level, and Panel B reports statistics aggregated across all symbols in the FTSE 100, FTSE 250, and full sample. Note that all of these numbers are daily race profits in our data from the London Stock Exchange; we will extrapolate from these numbers to the full UK equities market and to global equities markets in Section 6.

Referring to Panel A, we see that the average symbol in the FTSE 100 has daily race profits of GBP 1,047, and the 99th percentile symbol has daily race profits of GBP 3,432. For the FTSE 250 the average and 99th percentile are GBP 108 and GBP 606, respectively. Referring to Panel B, we see that the average day in our data set has race profits of GBP 105,734 for the FTSE 100, GBP 26,643 for the FTSE 250, and GBP 132,378 for the full sample.

These aggregate profits numbers are difficult to interpret in isolation. A more interpretable measure is obtained by dividing race profits by daily trading volume, with both measures in GBP. We refer to this ratio as the “latency arbitrage tax,” since, following the theory in BCS, the prize in latency arbitrage races is like a tax on overall market liquidity. We consider two versions of this measure, the first based on all trading volume, and the second based on all non-race trading volume. The version based on all trading volume is both simpler to describe and more appropriate for out-of-sample extrapolation. However, the version based on all non-race trading volume more closely corresponds to the theory, which shows that latency arbitrage imposes a tax on non-race trading (both noise trading and non-race informed trading).

Table 4.9 reports that for the average symbol in the FTSE 100, the latency arbitrage tax is 0.492 basis points based on the all-volume measure, and 0.675 basis points based on the non-race-

Table 4.8: **Daily Profits in GBP**

Panel A: Daily Profits by Symbol									
Description	Mean	sd	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99
FTSE 100	1,046.9	729.6	199.7	340.5	526.6	909.3	1,410.5	1,967.2	3,431.8
FTSE 250	108.3	134.1	-0.7	0.5	7.6	67.1	160.8	257.2	606.3
Full Sample	381.5	590.7	-0.6	1.5	26.7	135.1	466.2	1,184.5	2,273.8

Panel B: Daily Profits by Date									
Description	Mean	sd	Min	Pct10	Pct25	Median	Pct75	Pct90	Max
FTSE 100	105,734	32,852	62,980	78,777	87,038	93,074	117,979	153,712	223,187
FTSE 250	26,643	8,592	14,667	19,501	21,376	23,100	30,392	40,100	49,066
Full Sample	132,378	40,266	82,391	99,363	108,706	116,636	147,814	183,227	272,253

Notes: For each race detected by our baseline method we take per-race profits in GBP based on displayed depth with prices marked to market at 10 seconds (see notes for Table 4.6). We then compute daily profits for each symbol-date, by summing all races for that symbol on that date. In Panel A, for each symbol, we compute its average daily race profits, and report the distribution across symbols. In Panel B, for each date, we compute total daily race profits summed across all symbols, and report the distribution across dates.

volume measure. For the average FTSE 250 symbol, the latency arbitrage tax is 0.562 based on the all-volume measure and 0.692 basis points based on the non-race-volume measure. Higher-volume symbols tend to have lower latency arbitrage taxes, so the overall value-weighted average daily latency arbitrage tax, for all symbols in the FTSE 350, is 0.419 basis points using the all-volume measure and 0.534 basis points using the non-race-volume measure.

An interpretation of the first figure is that for every GBP 1 billion that is transacted in the market overall, latency arbitrage adds GBP 41,900 to trading costs. An interpretation of the second figure is that for every GBP 1 billion that is transacted by participants not in latency-arbitrage races, latency arbitrage adds GBP 53,400 to trading costs.

Relationship between Profits, Volume and Volatility

Figure 4.5 presents scatterplots of latency arbitrage profits against trading volume (Panel A) and 1-minute realized volatility (Panel B). Each dot represents one day of our data. As can be seen, latency arbitrage profits are highly correlated to both volume and volatility. The R^2 of the relationship between profits and volume is 0.811 and the R^2 of the relationship between profits and 1-minute volatility is 0.661. These relationships are consistent with the theory in BCS, which suggests that the size of the latency arbitrage prize should be related to both volume and volatility.

Appendix Figure B.2 presents scatterplots of the latency arbitrage tax (Measure 1, all volume) against these same measures: trading volume (Panel A) and 1-minute realized volatility (Panel B). The figures show that once we divide latency arbitrage profits by daily trading volume, to obtain the latency arbitrage tax in basis points, the result is relatively flat across the days in our sample. We will report further details on these relationships in Section 6, where they will be used for the purpose of out-of-sample extrapolation.

Table 4.9: **Latency Arbitrage Tax**

Panel A: Distribution Across Symbols

Sub-Panel (i): Measure 1, Latency Arbitrage Tax based on All Trading Volume (basis points)

Description	Mean	sd	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99
FTSE 100	0.492	0.235	0.163	0.236	0.292	0.454	0.627	0.827	1.035
FTSE 250	0.562	0.393	-0.022	0.022	0.267	0.565	0.817	1.043	1.540
Full Sample	0.542	0.356	-0.014	0.054	0.283	0.519	0.774	0.960	1.508

Sub-Panel (ii): Measure 2, Latency Arbitrage Tax based on Non-Race Trading Volume (basis points)

Description	Mean	sd	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99
FTSE 100	0.675	0.362	0.200	0.303	0.387	0.587	0.870	1.180	1.595
FTSE 250	0.692	0.504	-0.028	0.024	0.287	0.678	1.029	1.304	2.042
Full Sample	0.687	0.466	-0.020	0.057	0.345	0.651	0.995	1.275	2.032

Panel B: Distribution Across Dates

Sub-Panel (i): Measure 1, Latency Arbitrage Tax based on All Trading Volume (basis points)

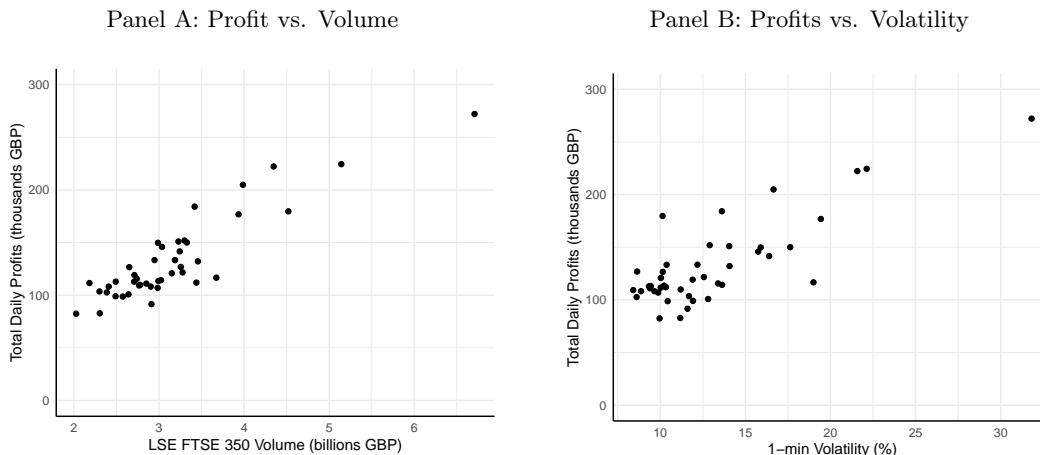
Description	Mean	sd	Min	Pct10	Pct25	Median	Pct75	Pct90	Max
FTSE 100	0.383	0.053	0.286	0.329	0.345	0.381	0.415	0.456	0.516
FTSE 250	0.663	0.099	0.495	0.552	0.591	0.653	0.725	0.790	0.912
Full Sample	0.419	0.053	0.313	0.360	0.382	0.416	0.450	0.495	0.537

Sub-Panel (ii): Measure 2, Latency Arbitrage Tax based on Non-Race Trading Volume (basis points)

Description	Mean	sd	Min	Pct10	Pct25	Median	Pct75	Pct90	Max
FTSE 100	0.493	0.075	0.351	0.418	0.443	0.487	0.533	0.603	0.656
FTSE 250	0.800	0.133	0.577	0.653	0.712	0.788	0.899	0.969	1.136
Full Sample	0.534	0.076	0.384	0.454	0.481	0.531	0.581	0.652	0.680

Notes: Panel A. For each symbol, we compute total race profits in GBP, summed over all dates in our sample, using per-race profits in GBP based on displayed depth with prices marked to market at 10 seconds (see notes for Table 4.6). We then compute total regular-hours trading volume in GBP, and total non-race regular-hours trading volume in GBP (see notes for Table 4.2). Panel A(i) reports the distribution across symbols of race profits divided by all trading volume. Panel A(ii) reports the distribution across symbols of race profits divided by non-race trading volume. Panel B is the same except at the date level (with race profits, all volume and non-race volume each summed across all symbols) instead of at the symbol level.

Figure 4.5: Latency Arbitrage Profits Correlation with Volume and Volatility



Notes: Panel A presents a scatterplot of daily race profits for the full sample, computed as in Table 4.8 (Panel B), against daily regular-hours trading volume (see notes for Table 4.2). Panel B presents a scatterplot of daily race profits for the full sample, against daily realized 1-minute volatility for the FTSE 350 index, computed using Thomson Reuters Tick History (TRTH) data.

4.5 Latency Arbitrage’s Share of the Market’s Cost of Liquidity

In this sub-section we quantify latency arbitrage as a proportion of the market’s overall cost of liquidity. We present two complementary approaches.

4.5.1 Approach #1: Traditional Bid-Ask Spread Decomposition

An influential decomposition of the bid-ask spread (e.g., Glosten, 1987; Stoll, 1989; Hendershott, Jones and Menkveld, 2011) is:

$$EffectiveSpread = PriceImpact + RealizedSpread \quad (4.1)$$

where *EffectiveSpread* is defined as the value-weighted difference between the transaction price and the midpoint at the time of the transaction, *PriceImpact* is defined as the value-weighted change between the midpoint at the time of the transaction and the midpoint at some time in the near future, and *RealizedSpread* is the remainder. *EffectiveSpread* is typically interpreted as the revenue to liquidity providers from capturing the bid-ask spread, *PriceImpact* as the cost of adverse selection, and *RealizedSpread* as revenues net of adverse selection.

The theory of latency arbitrage suggests two refinements to (4.1). First, we can decompose the price impact component of the spread into two components: one that reflects latency arbitrage and one that reflects traditional private information. Second, the theory shows that the equilibrium bid-ask spread also reflects the value of “losses avoided” by fast liquidity providers who successfully cancel in a latency arbitrage race. The intuition is that fast liquidity providers must earn a rent in equilibrium for being fast that is equal to the rent earned by fast traders who try to snipe; i.e., they earn the “opportunity cost of not sniping.”

Formally, we start with equation (3.1) of Budish, Lee and Shim (2019), which gives the equilibrium bid-ask spread in the continuous limit order book (CLOB) market as

$$\lambda_{invest} \frac{s^{CLOB}}{2} = (\lambda_{public} + \lambda_{private}) \cdot L\left(\frac{s^{CLOB}}{2}\right), \quad (4.2)$$

with the notation defined as follows. λ_{invest} , λ_{public} and $\lambda_{private}$ are, respectively, the Poisson arrival rates of investors who trade and thus pay the half-spread to a liquidity provider, publicly observed jumps in the fundamental value which cause a sniping race, and privately observed jumps in the fundamental value which lead to Glosten and Milgrom (1985) adverse selection. s^{CLOB} denotes the equilibrium bid-ask spread. $L\left(\frac{s^{CLOB}}{2}\right)$ denotes the expected loss to a liquidity provider, at this spread, if there is a jump in the fundamental value and they get sniped or adversely selected. In Appendix F.2 we show formally that equation (4.2) implies the spread decomposition:

$$EffectiveSpread = PriceImpact_{Race} + PriceImpact_{NonRace} + LossAvoidance + RealizedSpread \quad (4.3)$$

with terms defined as follows. *EffectiveSpread* is defined in the standard way, as the value-weighted absolute difference between the price paid in trades and the midpoint at the time of the trade (i.e., the value-weighted half-spread). *PriceImpact_{Race}* and *PriceImpact_{NonRace}* are, respectively, the value-weighted change between the midpoint at the time of the trade and the midpoint at some time in the near future (we will use 10 seconds), for trades in latency-arbitrage races and trades not in latency-arbitrage races. Last, *LossAvoidance* is defined as the value-weighted change between the race price and the midpoint in the near future for successful cancels in latency arbitrage races.

Table 4.10 gives details for decomposition (4.3) at the symbol level. For the average symbol in the FTSE 100, averaged over the days of our data set, the overall effective spread is 3.27 basis points, of which price impact is 3.62 basis points, loss avoidance is 0.01 basis points, and realized spread is -0.36 basis points. That price impact slightly exceeds the effective spread, so that the realized spread is slightly negative, is relatively common in modern markets, as noted in O’Hara (2015), and documented in Battalio, Corwin and Jennings (2016); Malinova, Park and Riordan (2018); Baron et al. (2019).²⁹ That loss avoidance is small is consistent with our finding earlier that most race activity is aggressive.

The FTSE 100 overall effective spread of 3.27 basis points reflects relatively similar effective spreads in races and outside of races, at 3.18 and 3.29 basis points, respectively. Price impact, in contrast, is meaningfully higher in races than not in races: 5.11 basis points versus 3.15 basis points. Consequently, the realized spread is -1.93 basis points in races versus +0.15 basis points not in races.³⁰ This result suggests that liquidity provision is modestly profitable in non-race trading

²⁹Realized spreads are slightly positive if price impact is measured at a shorter duration, such as 100ms or 1s rather than 10s (please see Appendix Tables B.13 and B.14). This is consistent with Conrad and Wahal (2020), who find that realized spreads decrease as the time interval decreases. Please note as well that at the LSE liquidity providers do not receive rebates, whereas in markets such as the US where rebates are common, this could lead to a negative realized spread being a rational feature of equilibrium liquidity provision (Battalio, Corwin and Jennings, 2016).

³⁰Note that the realized spread in races, multiplied by the roughly 22% of trading volume in races as reported in

Table 4.10: **Spread Decomposition**

Distribution Across Symbols (FTSE 100)

Description	Mean	sd	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99
Effective spread paid - overall (bps)	3.27	1.22	1.22	1.75	2.28	3.18	4.13	4.91	5.79
Effective spread paid - in races (bps)	3.18	1.22	0.99	1.70	2.21	3.17	4.05	4.89	5.98
Effective spread paid - not in races (bps)	3.29	1.22	1.25	1.78	2.30	3.17	4.15	4.96	5.71
Price impact - overall (bps)	3.62	1.36	1.40	1.92	2.52	3.56	4.52	5.55	6.99
Price impact - in races (bps)	5.11	1.83	2.02	2.85	3.48	4.90	6.50	7.56	8.81
Price impact - not in races (bps)	3.15	1.16	1.21	1.66	2.21	3.17	3.97	4.67	5.99
Loss avoidance (bps)	0.01	0.01	0.00	0.00	0.00	0.01	0.01	0.01	0.03
Realized spread - overall (bps)	-0.36	0.32	-1.07	-0.76	-0.55	-0.35	-0.17	0.01	0.39
Realized spread - in races (bps)	-1.93	0.70	-3.72	-2.83	-2.40	-1.79	-1.42	-1.11	-0.88
Realized spread - not in races (bps)	0.15	0.30	-0.35	-0.20	-0.05	0.08	0.34	0.56	0.90
PI in races / PI total (%)	33.16	6.09	19.99	24.88	29.53	32.13	37.23	41.72	44.72
PI in races / Effective spread (%)	36.90	7.18	19.79	27.73	33.06	36.59	41.97	46.44	51.67

Notes: Please see the text of Section 4.5 for definitions of Effective Spread, Price Impact (PI), Loss Avoidance, and Realized Spread.

but loses significant money in races. Note as well that this negative realized spread in races obtains even at the 99th percentile of FTSE 100 symbols (-0.88 basis points), which suggests that the finding is robust in the cross section of symbols.

Aggregated over all trading volume, price impact in races accounts for about 37% of the effective spread and 33% of all price impact in FTSE 100 stocks.

For symbols in the FTSE 250 (see Appendix Table B.12), overall effective spreads are higher, at 8.06 basis points, realized spreads are a bit less negative at -0.04 basis points, and loss avoidance remains small (0.01 basis points). Effective spreads are noticeably a bit narrower in races versus not in races, at 6.74 basis points in races versus 8.22 basis points outside of races. As with FTSE 100 stocks, price impact is significantly higher in races than in non-race trading (12.22 basis points versus 7.50 basis points), and consequently the realized spread is modestly positive in non-race trading (0.72 basis points) and meaningfully negative in races (-5.48 basis points). Aggregated over all trading volume, price impact in races accounts for about 22% each of the effective spread and of all price impact in FTSE 250 stocks.

In the full sample, value-weighted, the effective spread is 3.17 basis points, the realized spread is -1.83 basis points in races versus +0.23 basis points not in races, and price impact in races accounts for 30.58% of all price impact and 32.82% of the overall effective spread.

Overall, these results suggest that latency arbitrage deserves a place alongside traditional adverse selection as one of the primary components of the market's cost of liquidity.

The Realized Spread is Negative in Races for Both Fast and Slow Firms. Importantly, this negative realized spread in races does not appear to discriminate much by firm speed. For the top 6 firms as defined by the proportion of races won (see Figure 4.2) the realized spread in races

Table 4.2, corresponds roughly to the all-volume latency-arbitrage tax as reported in Table 4.9. (The relationship is not exact due to loss avoidance, which we count as part of the latency-arbitrage prize but does not count towards realized spreads, and some small differences in how the data are aggregated). Conceptually, the negative realized spread in races and the latency-arbitrage tax are two very similar ways of expressing the harm to liquidity providers.

Table 4.11: **Realized Spreads in Races by Firm Group**

Firm Group	Realized Spread (bps)			Cancel Attempt Rate (%)		
	Overall	Non-Race	Race	In Race	Within 1ms	Ever
All Firms	-0.209	0.236	-1.833	19.29	21.89	24.53
Fast vs. Slow						
Top 6	-0.086	0.347	-1.699	35.35	38.94	39.88
All Others	-0.302	0.152	-1.930	7.57	9.47	13.35
Within Fast						
Takers in Top 6	0.016	0.455	-1.493	45.16	47.56	47.82
Balanced in Top 6	-0.120	0.311	-1.775	30.97	35.09	36.33

Notes: Firm groups are as in Figure 4.3. The realized spread is calculated as described in the text and reported in Table 4.10. To calculate the cancel attempt rates we first compute, for each firm, the number of races in which they have a cancel attempt within the race horizon, the number of races in which they either have a cancel attempt within the race horizon or a cancel attempt within 1 millisecond of the start of the race for an order taken in the race, the number of races in which they either have a cancel attempt within the race horizon or a cancel attempt anytime after the race horizon for an order taken in the race, and the number of races in which they either have a successful cancel or provide liquidity (each is measured at the relevant price and side for the race). We then aggregate into the firm-group cancel rates by, for the numerator, summing the number of races with cancel attempts over all firms in the group (possibly counting the same race multiple times), and for the denominator, summing the number of races with either cancel attempts or liquidity provision over all firms in the group (possibly counting the same race multiple times).

is -1.699 basis points, versus -1.930 basis points for firms outside the top 6. The difference between the Takers and Balanced firms in the top 6 is small as well: -1.493 basis points versus -1.775 basis points. Please see Table 4.11.

Similarly, both fast and slow firms earn a modestly positive realized spread in non-race liquidity provision. For the top 6 firms the realized spread in non-race liquidity provision is 0.347 basis points versus 0.152 basis points for firms outside the top 6.

There is a more significant difference between faster and slower firms in their canceling behavior. The top 6 firms attempt to cancel in races about 35% of the time within the race horizon, and about 39% of the time within 1 millisecond of the starting time of the race. Within these top 6 firms, the maximum cancel rate is 66% within the race-horizon and 68% of the time within 1 millisecond. Firms outside of the top 6 attempt to cancel just 7.57% of the time within races and 9.47% of the time within 1 millisecond of the starting time of the race. If we look beyond 1 millisecond to include any failed cancel attempts of quotes taken in a race, the top 6 cancel attempt rate goes up to 40% and the cancel rate for firms outside of the top 6 goes up to 13.35%.³¹ Thus, fast firms are about five times more likely to attempt to cancel in a race than are slower firms.

Together, these results reinforce the idea that latency arbitrage imposes a tax on liquidity provision — it is expensive to be the liquidity provider who gets sniped in a race. The fastest firms are better than slower firms at avoiding this cost, but even they get sniped with significant probability if their quotes become stale.³²

³¹For firms in the top 6 essentially all of the incremental failed cancels come within 3 milliseconds after the race start (98.57% of all cancel attempts are within 3ms of the race start). For firms outside the top 6 the large majority of the incremental failed cancels come by 3 milliseconds after the race start (85.73%), and essentially all come by 1 second after the race start (99.43%).

³²Our best guess for why slower firms rarely attempt to cancel, and even fast firms sometimes do not attempt to cancel, is that, by the time the quote provider has figured out that their quote is stale and they should reprice,

4.5.2 Approach #2: Implied Reduction of the Bid-Ask Spread if Latency Arbitrage Were Eliminated

Our second approach asks what would be the proportional reduction in the market cost of liquidity if there were no latency arbitrage. Formally, we seek to empirically measure:

$$\frac{\frac{s^{CLOB}}{2} - \frac{s^{FBA}}{2}}{\frac{s^{CLOB}}{2}} \quad (4.4)$$

where s^{CLOB} is the bid-ask spread under the continuous limit order book (CLOB) and s^{FBA} is the bid-ask spread under a counterfactual market design, frequent batch auctions (FBA), which eliminates latency arbitrage. To turn (4.4) into something empirically measurable, we take the following steps. First, we multiply the numerator and denominator of (4.4) by $(\lambda_{invest} + \lambda_{private})$. Second, we use (4.2) to solve out for $\lambda_{invest} \frac{s^{CLOB}}{2}$ in the numerator. Third, we use equation (5.1) of Budish, Lee and Shim (2019),

$$\lambda_{invest} \frac{s^{FBA}}{2} = \lambda_{private} \cdot L\left(\frac{s^{FBA}}{2}\right) \quad (4.5)$$

where $L(\frac{s^{FBA}}{2})$ is the loss to the liquidity provider if there is a privately-observed jump of at least $\frac{s^{FBA}}{2}$ and they get adversely selected, to solve out for $\lambda_{invest} \frac{s^{CLOB}}{2}$ in the numerator of (4.4). Observe that the difference between the equilibrium bid-ask spread characterization for frequent batch auctions, (4.5), and the equilibrium bid-ask spread for continuous trading, (4.2), is the $\lambda_{public}L(\cdot)$ term; if there is a publicly-observed jump a liquidity provider in an FBA does not get sniped, unlike in the continuous market.

These manipulations and some algebra, included in Appendix F.3 for completeness, shows that equation (4.4) can be re-expressed as:

$$\frac{\frac{s^{CLOB}}{2} - \frac{s^{FBA}}{2}}{\frac{s^{CLOB}}{2}} = \frac{\lambda_{public}L\left(\frac{s^{CLOB}}{2}\right)}{(\lambda_{invest} + \lambda_{private})\frac{s^{CLOB}}{2}} \quad (4.6)$$

Both the numerator and denominator of the right-hand-side of (4.6) are directly measurable. The numerator is simply latency arbitrage profits (including both races where an aggressor wins and races where a cancel wins). The denominator is the non-race portion of the effective spread; that is, it is all of the bid-ask spread revenue collected by liquidity providers outside of latency arbitrage races. These objects can be measured either in GBP terms, or, by dividing both numerator and

they already have received the update that their quote has been executed. That is, if the information horizon is 200 microseconds, they “lose the race” by more than 200 microseconds. We note as well that, conditional on losing a race, the average cost is just half a tick, so this could easily be accounted for as a “cost of doing business”. To confirm this hypothesis would require data from a broker-dealer execution algorithm, for instance.

Table 4.12: **Percentage Reduction in Liquidity Cost, if Latency Arbitrage Eliminated**

Panel A: Symbol level									
Description	Mean	sd	Pct01	Pct10	Pct25	Median	Pct75	Pct90	Pct99
FTSE 100	19.95	5.29	8.87	13.30	16.79	19.69	23.58	26.50	32.54
FTSE 250	11.93	6.31	0.58	3.12	8.05	11.91	15.33	18.58	31.31
Full Sample	14.77	7.09	0.70	5.55	10.03	14.55	19.41	24.10	32.22

Panel B: Date level									
Description	Mean	sd	Min	Pct10	Pct25	Median	Pct75	Pct90	Max
FTSE 100	19.06	3.29	7.49	16.53	17.53	18.97	21.48	22.25	25.40
FTSE 250	11.39	1.66	8.27	9.43	10.22	11.17	12.45	13.36	16.18
Full Sample	16.73	2.57	7.88	14.57	15.19	16.82	18.66	19.17	21.58

Notes: For each symbol, we implement equation (4.7) by dividing total race profits in GBP, across all dates, and dividing by total non-race Effective Spread paid in GBP, across all dates. Race profits in GBP are as described in Table 4.8 and Effective Spread paid in GBP is as described in Table 4.10. Analogously, for each date, we implement equation (4.7) by dividing total race profits in GBP, across all symbols, and dividing by total non-race Effective Spread paid in GBP, across all symbols. We do both exercises separately for FTSE 100, FTSE 250, and full sample. In Panel A, we only include symbols that have at least 100 races summed over all dates; this drops about one-quarter of FTSE 250 symbols and does not drop any FTSE 100 symbols.

denominator by non-race trading volume, in basis points terms. Thus, we have the relationship:

$$\begin{aligned} \text{Proportional Reduction in Liquidity Cost} &= \frac{\text{Race Profits (GBP)}}{\text{Non-Race Effective Spread (GBP)}} \quad (4.7) \\ &= \frac{\text{Latency Arbitrage Tax (Non-Race Volume)}}{\text{Non-Race Effective Spread (bps)}} \end{aligned}$$

Table 4.12 presents our computation of (4.7). For the average symbol in the FTSE 100, eliminating latency arbitrage would reduce the cost of liquidity by 19.95%.³³ For the FTSE 250, the figure is 11.93%. Even though race profits are higher as a proportion of trading volume for the FTSE 250 (per Table 4.9), bid-ask spreads are several times wider for FTSE 250 symbols than for FTSE 100 symbols (see Appendix Tables B.10-B.12), so eliminating latency arbitrage would reduce the overall cost of liquidity by less for the FTSE 250 than for the FTSE 100.

For the market as a whole, value-weighted and averaging over all dates in our sample, eliminating latency arbitrage would reduce the cost of liquidity by 16.73%.³⁴

³³It may at first be confusing why eliminating latency arbitrage reduces the spread by about 20% for FTSE 100 stocks in this exercise, whereas price impact in latency arbitrage races constituted 37% of the effective spread in Table 4.10. The difference is that latency arbitrage profits charge the aggressor the half spread, whereas the price impact calculation in effect does not. Here is the rough back of envelope math. The effective spread is on average about 3 bps. Price impact in races is about 5bps and races constitute 23% of volume for the average FTSE 100 symbol (Appendix Table B.4). Therefore price impact in races as a proportion of the effective spread is $\frac{23\% \cdot 5bps}{3bps}$, which is about 37% as claimed. The latency arbitrage tax on non-race volume is $\frac{(5bps - 3bps) \cdot 23\%}{(100\% - 23\%)}$, which is about 0.60bps, or about 20% of the non-race effective spread, implying a roughly 20% reduction in the cost of liquidity as claimed.

³⁴Both equation 4.2 for the spread in the continuous market and equation 4.5 for the spread in the FBA market assume no tick-size constraints. A market design reform that both adopted FBA and eased tick-size constraints, as advocated by Yao and Ye (2018), Kyle and Lee (2017), and others, would, based on these estimates, reduce the cost of liquidity by more than 16.7%. If tick-size constraints bind, then the liquidity advantage of FBA relative to

5 Sensitivity Analysis and Robustness Checks

We performed a wide range of sensitivity analyses and robustness checks. First, we explored how our main results as presented in Section 4 vary as we modify each of the components of our race definition as presented in Section 3. The insights from this work are discussed in Section 5.1, with a summary table in the main text and full details in Appendix C. Second, we performed additional robustness analyses to better understand races in our data that do not fit as neatly within the paradigm of the BCS model: races with negative mark-to-market profits, and races where the best bid and offer (BBO) is volatile just before the race. This analysis is discussed in Section 5.2 with supporting details in Appendix D.

5.1 Sensitivity to Varying the Definition of a Race

As described in Section 3, for each of the four components of our race definition—multiple participants, at least some of whom are aggressive, at least some of whom succeed and some of whom fail, all at the “same time”—we performed our full analysis for both a baseline and alternatives. In this subsection we report the main insights from these alternative specifications. Table 5.1 then presents a range of sensitivity scenarios informed by this work.

Finding #1: Effect of Race Horizon. Our baseline method requires that a set of messages satisfying the baseline race requirements arrives within the “information horizon” of the first message of the race, which averages about 200 microseconds and is capped at 500 microseconds. In sensitivity analyses, we explored instead requiring that the set of messages satisfying the baseline race requirements arrives within a time window of T , with values of T ranging from 50 microseconds to 3 milliseconds. The longer horizons are intended to capture races among firms of varying technological sophistication that could still be considered racing one another.³⁵ We consulted with HFT industry contacts and FCA supervisors to agree on an appropriate horizon. Following these discussions, we determined 3 milliseconds would capture most of these additional potential races, though for races originating from signals far from London (e.g., Chicago) differences in speed between cutting-edge HFTs and relatively sophisticated firms could easily exceed that number. We will also miss races where, by the time the loser or losers of the race detect the signal, they can already tell from their representation of the order book that they are too late and hence do not bother to send a message; such cases can be understood as a gray area between asymmetric private information (because the winner understood the signal far enough in advance of the losers) and symmetric public information (because the time differences are still quite small).

continuous trading can manifest in greater depth as opposed to a narrower spread. There can be more liquidity at a given price while keeping the marginal unit of liquidity provision indifferent between providing and not, because there is no sniping.

³⁵Sources of speed loss for firms that are sophisticated but not at the cutting edge of speed include not using code and hardware that is optimized for speed, not utilizing the fastest co-location and connectivity options at exchanges, not using the fastest links to overseas markets such as the United States, and not using microwave connections where possible to do so.

The main pattern that emerges from this analysis is that the longer is T the more races we find, without much effect on the various measures of per-race profits. The increase is especially steep up through 500 microseconds. For example, with $T = 100\mu s$ the number of FTSE 100 races per symbol per day is 389, with $T = 500\mu s$ the number is 720, with $T = 1ms$ the number is 768, and with $T = 3ms$ the number is 800.³⁶

As a result, our measures of the effect of latency arbitrage on the cost of liquidity are all strongly increasing with the race horizon. At $T = 100\mu s$ the full-sample latency arbitrage tax is 0.26 bps, price impact is 19.2% of the effective spread, and the implied reduction in the market's cost of liquidity from eliminating latency arbitrage is 9.5%. At $T = 500\mu s$ the figures are 0.60bps, 50.8%, and 28.1%, respectively; at $T = 1ms$ the figures are 0.68bps, 59.3%, and 35.4%; and at $T = 3ms$ the figures are 0.74bps, 66.1%, and 41.6%. That is, if the race window is defined as 3 milliseconds instead of the information horizon, latency arbitrage constitutes about 65% of the effective spread and eliminating latency arbitrage would reduce the market's cost of liquidity by about 40%.

Finding #2: Number of Race Participants. Our baseline method requires that there are at least 2 race participants within the information horizon. In sensitivity analysis we consider requiring 3+ participants and 5+ participants. Given the large effect that the race's time horizon had on the number of races and the harm to market liquidity, we perform this sensitivity for both the baseline information horizon method and for fixed race horizons ranging from 50 microseconds to 3 milliseconds.

The main pattern that emerges from this sensitivity is that increasing the required number of race participants lowers the number of races found while increasing the various measures of profitability per race. For example, requiring 3+ participants reduces the number of races in the information horizon by about 60%, but increases per-race profits by about 60% as well. The net effect is that measures of total race profits and harm to liquidity fall by about one-third: the latency arbitrage tax is 0.29bps, race price impact's proportion of the spread is 20.5%, and the implied reduction in the market's cost of liquidity is 10.4%.

Increasing the race horizon increases the number of races detected, just as in the baseline case. The overall magnitudes for the total cost of latency arbitrage are similar among the baseline method, the sensitivity with 3+ participants within 500 microseconds, and the sensitivity with 5+ participants within 1 millisecond.

Finding #3: Takes and Cancels. Our baseline method defines a race to consist of either 1+ aggressors and 1+ cancels, or 2+ aggressors and 0 cancels. The former case corresponds to the equilibria studied in BCS, whereas the latter case, in which all race activity is aggressive, corresponds to equilibria in a modest extension of BCS presented in Appendix F.

There are two main findings that emerge from our sensitivity analysis of these criteria. First,

³⁶The numbers reported in Table 5.1 at horizons of 500 microseconds and longer all also reflect the sensitivity requirement that plain vanilla (non-IOC) limit orders cannot count as fails, i.e., only failed IOCs and failed cancels count as fails. See discussion below under Finding #4. The Appendix includes a version of the time horizon sensitivity without this requirement (Table C.1); the numbers are about 10-15% bigger.

requiring a cancel attempt within the race horizon significantly reduces the number of races and the associated harm to market liquidity. If we require at least 1 cancel within the information horizon, the number of races and the various harm to liquidity measures are each about 30% of the baseline. This is as expected given our findings in Section 4.2 that most of the message activity in races is aggressive. That said, if we consider races with 1+ cancel over a 3 millisecond time horizon, then the results are closer to baseline, at about 85% of the number of races and the various harm to liquidity measures.

Second, races with just a single take attempt (i.e., 1 aggressor and 1+ cancels) have meaningfully lower profitability than races with 2+ aggressors. As a consequence, imposing the requirement that there are 2+ aggressors in a race lowers the number of races by about 20% but lowers the latency arbitrage tax by closer to 10%.

Finding #4: Success and Fail Criteria. Reassuringly, in our baseline analysis, varying the definition of success and fail does not move the needle too much. At longer time horizons, whether or not we treat plain vanilla (non-IOC) limit orders as potential fails makes a bigger difference, affecting the number of races detected by on the order of 10-15%. This makes sense because at longer horizons we should be more concerned about mistaking limit orders that post to the book with the intent to provide liquidity as failed race attempts. For this reason, in the summary of sensitivity scenarios presented below as Table 5.1, we do not allow non-IOC limit orders to count as fails at time horizons of 500 microseconds and longer, i.e., at time horizons longer than the information horizon only failed IOCs and failed cancels count as fails.

Selected Sensitivity Scenarios. Based on what we have learned from the various sensitivity analyses, Table 5.1 highlights several specific scenarios that we feel give a sense of the overall range of estimates for race profits and the effect on liquidity.

As Low scenarios, since we learned that race profits are especially sensitive to the choice of race horizon and to stricter requirements on the level of participation, we highlight: 2+ within 50 microseconds, 2+ within 100 microseconds, and 3+ within the information horizon.

As Medium scenarios, we highlight: 2+ within 200 microseconds, 2+ within 500 microseconds, and 3+ within 500 microseconds.

As High scenarios, we highlight: 2+ within 1 millisecond, 2+ within 3 milliseconds, and 3+ within 3 milliseconds.

Over this set of scenarios, the latency arbitrage tax ranges from 0.20 to 0.74 basis points on the all-volume measure, and from 0.22 to 1.31 basis points on the non-race volume measure. Latency arbitrage as a percentage of trading volume ranges from 9.8% to 43.7%. Latency arbitrage as a percentage of the effective spread ranges from 13.8% to 66.1%. The potential reduction in the market's cost of liquidity ranges from 7.0% to 41.6%.

We acknowledge that this exercise is somewhat subjective. At the lower end, we know conceptually that if we reduce the race horizon sufficiently and/or increase the participation requirements sufficiently we can find a lower bound that is essentially zero (e.g., 5+ within 50 microseconds yields

Table 5.1: Sensitivity Analysis: Selected Scenarios

Measure	Baseline	Low Scenarios			Middle Scenarios			High Scenarios		
		2+, 50 μ s	2+, 100 μ s	3+, 1H	2+, 200 μ s	2+, 500 μ s	3+, 500 μ s	2+, 1ms	2+, 3ms	3+, 3ms
Frequency and Duration of Races										
Races per day	537.24	296.66	388.58	228.98	521.53	719.71	458.94	768.02	799.91	609.01
FTSE 100 - per symbol										
% of volume in races	21.46	9.77	13.32	12.30	19.21	34.89	26.42	40.03	43.72	38.14
Full Sample										
Per-Race Profits										
Per-share profits	0.55	0.54	0.53	0.71	0.51	0.52	0.60	0.54	0.55	0.64
ticks	0.17	0.16	0.16	0.23	0.16	0.16	0.19	0.16	0.16	0.19
GBX	1.66	1.68	1.63	2.24	1.57	1.59	1.90	1.64	1.64	1.92
basis points										
Per-race profits GBP	1.85	1.58	1.59	2.98	1.60	1.91	2.54	2.04	2.09	2.67
displayed depth	1.76	1.38	1.44	2.87	1.51	1.92	2.59	2.07	2.16	2.76
qty trade/cancel										
Aggregate Profits and LA Tax										
Daily Profits	132,378	63,573	83,233	91,506	111,722	187,989	158,444	215,794	232,457	221,526
Full Sample - aggregate (GBP)										
Latency Arbitrage Tax, All Volume (bps)	0.42	0.20	0.26	0.29	0.35	0.60	0.50	0.68	0.74	0.70
Full Sample										
Latency Arbitrage Tax, Non-Race Volume (bps)	0.53	0.22	0.30	0.33	0.44	0.92	0.70	1.14	1.31	1.14
Full Sample										
Spread Decomposition										
Price impact in races / All price impact %	30.58	12.84	17.89	19.13	25.69	47.38	37.08	55.27	61.61	55.54
Price impact in races / Effective spread %	32.82	13.77	19.19	20.54	27.57	50.84	39.61	59.31	66.11	59.61
Implied Reduction in Cost of Liquidity										
Full Sample - % Reduction	16.73	6.96	9.49	10.43	13.62	28.12	20.96	35.37	41.64	36.20

Notes: For descriptions of the sensitivity scenarios please see the text. Descriptions of each of the items in this table can be found in the following table notes in Section 4. Races per day: Table 4.1. % of Volume in Races: Table 4.2. Per-race profits: Table 4.6. Aggregate profits: Table 4.8. Latency Arbitrage Tax: Table 4.9. Spread decomposition: Table 4.10. Implied Reduction in Cost of Liquidity: Table 4.12. All scenarios with a time horizon of 500 microseconds or longer use the strict fails criterion in which non-IOC limit orders cannot count as fails, as discussed in the text.

very low numbers, see Appendix Table C.3). Similarly, at the high end, one could be even more inclusive (e.g., looking at horizons even longer than 3 milliseconds). Or, one could attempt to find a way to account for the gray-area case, between symmetric public information and asymmetric private information, where one firm’s response to a trading signal is sufficiently faster than others’ that, by the time other firms observe the signal, they can already tell from the order book that they are too late and hence don’t bother. Still, we think this exercise provides a useful sense for the range of magnitudes we find using our method. This range will inform our analysis in Section 6 where we provide extrapolations for the total sums at stake in latency-arbitrage races.

5.2 Additional Robustness Checks

We did additional robustness work to explore two aspects of the main results that do not fit neatly within the original BCS model.

Races with Negative Profits Ex-Post. In our main specification, 20% of races have strictly negative profits when marked to market at 100 milliseconds after the race, 22% when marked at 1 second after the race, and 29% when marked at 10 seconds after the race. While these numbers surely reflect some post-race noise, we find that 8% of races have strictly negative profits continuously for the 10 seconds after the race. (As seen in Figure 4.4, when a race is not profitable, typically the pattern is that price impact is weakly in the direction of the race but not by enough to recover the half-spread.)

Even in our most strenuous sensitivity test, which requires 5+ participants within 50 microseconds, 10% of races have strictly negative profits 100 milliseconds after the race, 11% at 1 second, 19% at 10 seconds, and 3% of races have strictly negative profits continuously for the 10 seconds after the race. For full details see Appendix D.1.

These results suggest to us that at least some races are based on noisy signals that turn out not to be profitable ex-post. While this squares with common intuitions about algorithmic trading more broadly, where it can of course be rational to trade on signals that are profitable in expectation but noisy—and our figures suggest that trading in races is a lot closer to pure arbitrage than the 51/49 odds described by Renaissance and Virtu³⁷—it is inconsistent with a literal interpretation of the BCS model in which the public signal that triggers races is perfectly correlated to the fundamental value of the asset.

Races Triggered by Order Book Activity. In the BCS model, races are triggered by jumps in a public signal, interpreted for example as a change in the price of a highly correlated asset or the same asset on another venue. A recent paper of Li, Wang and Ye (2020) extends the BCS model to incorporate both discrete price increments (i.e., tick-size constraints) and a stylized version of institutional investor execution algorithms, and finds that races can be triggered by both

³⁷See fn. 8 in the introduction on Renaissance and Virtu, and also see MacKenzie (2021) who discusses several different types of canonical HFT signals, some of which are closer to pure arbitrage and some of which are more statistical in nature.

public signals and by order-book activity by the execution algorithms. Specifically, if an execution algorithm places a limit order in the book that is sufficiently attractive (e.g., a new bid that is sufficiently close to the ask), and trading firms are sufficiently confident that this order does not reflect new information, the order could trigger a race.³⁸

We find some evidence for this pattern in our data. In about 14% of races there is a change in the race-side best bid or offer in the 100 microsecond window just prior to the race, and of these, nearly all of the price changes (89% of the subset, or 12% of the total) are in the direction consistent with Li, Wang and Ye (2020). These races have fewer cancelations than baseline races (0.24 versus 0.40) and a larger share of liquidity provided by non-top 6 firms (71% versus 58%), both of which also seem consistent with the theory in Li, Wang and Ye (2020).

That said, the large majority of races have stable prices leading up to the race. This suggests that most races are triggered by some public signal external to the symbol’s own order book, as in the BCS model. For full details see Appendix D.2.

6 Total Sums at Stake

6.1 Extrapolation Models

Figure 4.5 showed visually that daily latency arbitrage profits are highly correlated with market volume and volatility, as expected given the theory. Table 6.1 presents these same relationships in regression form for the purpose of out-of-sample extrapolation.

Columns (1)-(2) regress daily in-sample latency arbitrage profits on daily LSE regular-hours trading volume in GBP (10,000s). The coefficient of 0.421 in (2) is directly interpretable as the all-volume latency arbitrage tax in basis points. Including a constant term changes the coefficient only slightly, to 0.432. This single variable has an R^2 of 0.81.

Columns (3)-(4) regress daily in-sample latency arbitrage profits on daily realized 1-minute volatility.³⁹ To make the results interpretable in units of latency arbitrage tax, realized volatility in percentage points is multiplied by the sample-average of daily trading volume.⁴⁰ Here, including the constant term does provide a meaningfully better fit, which can also be seen visually in the scatterplot in Figure 4.5, Panel B. The coefficient of 0.023 in (3) means that every additional percentage point of realized volatility adds 0.023 basis points to that day’s latency arbitrage tax. This variable has lower explanatory power than volume, but still high, with an R^2 of 0.661.

Columns (5)-(6) present results for a two-variable model in which daily latency arbitrage profits are regressed on both trading volume and realized volatility. Again, to make the results interpretable, realized volatility is multiplied by average daily trading volume.⁴¹ Both variables are significant,

³⁸See also Foucault, Kozhan and Tham (2016) who call this “non-toxic arbitrage.”

³⁹In the Appendix we report regression results for 5-minute volatility and for a measure of volatility emphasized in BCS called distance traveled. 5-minute volatility has lower explanatory power than 1-minute volatility. Distance traveled actually has greater explanatory power than 1-minute volatility, but we emphasize the latter because it is more easily measurable across markets and over time, and more widely utilized in practice and in the literature.

⁴⁰That is, we regress $\text{LatencyArbProfits}_t = \alpha + \beta(\sigma_t \cdot \text{AvgDailyVolume})$ where σ_t is in percentage points and AvgDailyVolume is in GBP 10,000s.

⁴¹That is, we regress $\text{LatencyArbProfits}_t = \alpha + \beta\text{Volume}_t + \gamma(\sigma_t \cdot \text{AvgDailyVolume})$. We also considered the

Table 6.1: **Extrapolation Models**

	<i>Dependent variable:</i>					
	Latency Arbitrage Profits (GBP)					
	(1)	(2)	(3)	(4)	(5)	(6)
Volume (10,000 GBP)	0.4319*** (0.0326)	0.4213*** (0.0082)			0.3405*** (0.0544)	0.3354*** (0.0415)
Volatility (1 min) * Average Volume			0.0228*** (0.0025)	0.0313*** (0.0009)	0.0065** (0.0032)	0.0066** (0.0031)
Constant	-3,562 (10,611)		39,226*** (11,032)		-1,532 (10,263)	
Observations	43	43	43	43	43	43
R ²	0.811	0.810	0.661	0.567	0.829	0.829

*p<0.1; **p<0.05; ***p<0.01

Notes: The dependent variable in all regressions is daily race profits in GBP, for the full sample, as described in Table 4.8. Volume is daily regular-hours LSE trading volume in GBP, as first described in Table 4.2, in units of 10,000 GBP so that the coefficient is interpretable as a latency arbitrage tax in basis points. Volatility is realized 1-minute volatility for the FTSE 350 index in percentage points, using TRTH data, as described in Figure 4.5. Volatility in percentage points is multiplied by average daily volume in 10,000 GBP so that the coefficient has the interpretation of the effect of a 1 percentage point change in volatility on the latency arbitrage tax in basis points. Regressions are ordinary least squares. R^2 in the regressions without constant terms is computed according to the formula $1 - \text{Var}(\hat{\epsilon})/\text{Var}(y)$. P-values are computed using the student-t distribution.

and the two-variable model has higher explanatory power than the single-variable model, but the difference is modest, with an R^2 of 0.83 versus 0.81. The reason for this is that volume and volatility are highly correlated to each other, with an in-sample correlation of 0.82 in our data. The coefficients can be interpreted as follows. On a day with average 1-minute volatility (about 13% in our sample), the latency arbitrage tax is $0.3354 + 13 \cdot 0.0066 = 0.42$ basis points, the overall sample average. On a particularly high realized volatility day, say 25%, the latency arbitrage tax would be 0.50 basis points. On a relatively calm day, say 10% realized volatility, the latency arbitrage tax would be 0.40 basis points.

Before we turn to out-of-sample extrapolation, we emphasize that the standard errors on these coefficients are much smaller than the variation in the latency arbitrage tax we found in sensitivity analysis when we considered different specifications for race detection. Therefore, we will emphasize two kinds of out-of-sample results: (i) results based on the volume and volatility model presented in Column (6); and (ii) results based on the volume-only model in column (2), using both the baseline latency arbitrage tax and the range of latency arbitrage taxes across the various sensitivity analyses discussed in Section 5.1.

specification $\text{LATax}_t = \alpha + \beta \cdot \frac{\text{Volume}_t - \text{AvgDailyVolume}}{\text{AvgDailyVolume}} + \gamma\sigma_t$, that is, the latency arbitrage tax in basis points is the LHS variable. In this specification, the coefficient on volatility is roughly the same as in Column 6, at 0.0061, and the coefficient on volume is -0.0008 and statistically insignificant. These coefficients imply that on a day where trading volume is 10 percentage points higher than the average, holding volatility fixed, the latency arbitrage tax is -0.008 basis points lower than average.

Table 6.2: **Annual Latency Arbitrage Profits in UK Equity Markets (GBP Millions)**

Year	(1) Volume- Volatility	(2) Volume- Only	(3) Low Scenario	(4) High Scenario
2014	52.0	56.7	27.1	99.1
2015	58.9	61.6	29.4	107.7
2016	63.3	63.8	30.4	111.4
2017	51.0	57.5	27.4	100.4
2018	55.8	60.6	28.9	105.9

Note: We compute UK regular-hours trading volume by dividing LSE’s monthly reported regular-hours trading volume by LSE’s monthly reported regular-hours market share. We compute UK 1-minute realized volatility using TRTH data for the FTSE 350 index, computing the realized volatility on each day and then computing the root mean square. Model (1) uses the coefficients from Regression (6) in Table 6.1. Model (2) uses the coefficient from Regression (2) in Table 6.1. Model (3) and Model (4) use the min and max latency arbitrage taxes found in Table 5.1, of 0.20 bps and 0.74 bps, respectively.

6.2 Out-of-Sample Extrapolation: UK Equity Markets

Table 6.2 presents our estimates of the annual sums at stake in latency arbitrage races in the UK for the five year period 2014-2018. In Column (1) we present the estimate based on the volume and volatility regression model. For volume data we use LSE reports of their daily trading volume and monthly regular-hours market share to estimate total daily regular-hours trading volume. For volatility data, we compute daily one-minute realized volatility of the FTSE 350 index using Thomson Reuters data. In Column (2) we present the estimate based on the volume-only model. In Columns (3)-(4) we present the range of estimates implied by the sensitivity analyses discussed in Section 5.1; these are based on latency arbitrage taxes of 0.20 basis points in the lowest of the Low scenarios and 0.74 basis points in the highest of the High scenarios.

The volume-and-volatility model implies annual latency arbitrage profits in UK equity markets ranging between GBP 51.0 Million to GBP 63.3 Million per year. The volume-only model yields slightly higher estimates. At the low end of our sensitivity analyses the annual profits are about GBP 30 million and at the high end the annual profits are about GBP 100 million.

6.3 Out-of-Sample Extrapolation: Global Equity Markets

This section presents estimates of the annual sums at stake in latency arbitrage races in global equities markets. The goal is to get a sense of magnitudes for what our results using the LSE message data imply about the overall global size of the latency arbitrage prize. We emphasize that this extrapolation does not attempt to account for differences in equity market structure across countries that may affect the level of latency arbitrage (e.g., the level of fragmentation, role of ETFs, geography), nor does it include other asset classes besides equities. As we will further emphasize in the conclusion, we hope that other researchers in the future will use message data from other countries and additional asset classes to produce better numbers.

We use volume data from the World Federation of Exchanges (2021). The advantage of WFE data is that it covers nearly all exchange groups around the world, but a caveat is that there may be

Table 6.3: Annual Latency Arbitrage Profits in Global Equity Markets in 2018 (USD Millions)

Exchange Group	(1) Volume- Volatility	(2) Volume- Only	(3) Low Scenario	(4) High Scenario
NYSE Group	1,006	1,023	488	1,787
BATS Global Markets - U.S.	895	910	434	1,590
Nasdaq - U.S.	847	862	411	1,505
Shenzhen Stock Exchange	327	336	160	588
Japan Exchange Group	281	286	136	500
Shanghai Stock Exchange	260	268	128	468
Korea Exchange	118	120	57	209
London Stock Exchange Group**	109	119	57	207
BATS Chi-X Europe	110	119	57	207
Hong Kong Exchanges and Clearing	102	104	50	182
Euronext	89	96	46	168
Deutsche Börse Group	78	85	40	148
TMX Group	56	61	29	107
National Stock Exchange of India	47	49	24	86
SIX Swiss Exchange	40	43	21	76
Global Total (WFE Data Universe)	4,674	4,799	2,289	8,383

**London Stock Exchange Group includes London Stock Exchange as well as Borsa Italiana

Note: As discussed in the text, this analysis does not attempt to account for differences in market structure across countries and exchanges that may affect the level of latency arbitrage. Rather, its goal is to provide the reader with a sense of global magnitudes. Trading volume is from the World Federation of Exchanges (2021). Per guidance from the WFE, we sum the volume of listed symbols and exchange traded funds traded on electronic order books (“EOB Value of Share Trading” and “ETFs EOB Turnover”). Please note that there may be inconsistencies across exchanges in how they report data to WFE. The data is comprehensive and helps give a sense of the overall global magnitudes but for any particular exchange better volume data may be available. Volatility is computed using TRTH data for the following indices. NYSE, BATS and Nasdaq: S&P 500. Shenzhen and Shanghai: Shanghai composite. Japan: Nikkei225. Korea: KOSPI. LSE Group: FTSE 350. BATS Chi-X, Euronext, Deutsche Börse, Swiss: EuroStoxx600. Hong Kong: Hang Seng. India: SENSEX. Canada TMX Group: TSX Composite. The row denoted Global Total (WFE Data Universe) includes all exchange groups in the WFE data. All estimates reported in the table are computed analogously to Table 6.2 with the exception of the global total in Column (1): since we do not have volatility indices for all exchange around the world, we compute this as (Sum of Volume-and-Volatility Model Profits for Top 15 Exchange Groups) / (Sum of Volume-Only Model Profits for Top 15 Exchange Groups) * (Global Total Profits Based on Volume-Only Model).

some inconsistencies in how exchange groups report their data to the WFE. We consulted with the WFE to obtain their advice regarding how best to utilize their data. Unfortunately, exchange groups appear to be inconsistent about whether they include volume from opening and closing auctions, which ideally we would exclude. In the other direction, this data does not include electronic off-exchange trading volume (i.e., dark pools) that is vulnerable to latency arbitrage, and which is a significant share of equities trading volume in many countries. We compute volatility based on the one-minute realized volatility of regional equity market indices using Thomson Reuters data. As in Table 6.2 above, Table 6.3 Column (1) presents estimates based on the volume and volatility regression model, Column (2) presents estimates based on the volume-only model, and Columns (3)-(4) present the range implied by the sensitivity analyses.

Our main estimate of a latency arbitrage tax of 0.42 basis points implies annual latency arbitrage profits of \$4.8 billion in 2018 for global equities markets. The volume-and-volatility model yields a slightly lower estimate since volatility was lower in 2018 than in our sample period. At the low end of our sensitivity analyses the annual latency arbitrage profits for global equity markets are about

\$2.3 billion, and at the high end the annual profits are about \$8.4 billion.⁴²

Because of the COVID-19 pandemic, 2020 was an exceptionally high-volume and high-volatility year for financial markets. Our volume-only model applied to 2020 implies annual latency arbitrage profits in global equity markets of \$6.5 billion, while our volume-and-volatility model yields a slightly higher estimate of \$7.0 billion. At the low end of our sensitivity analyses the figure is \$3.1 billion and at the high end the figure is \$11.4 billion for global equity markets in 2020 (Appendix Table E.2).

7 Conclusion

We conclude by summarizing the paper’s contributions to the academic literature and discussing our hopes for future work.

The paper’s first contribution is methodological: utilizing exchange message data to measure latency arbitrage. The central insight of the method is simple: an important part of the activity that theory implies should occur in a latency arbitrage race will not actually manifest in traditional limit order book data—the *losers* of the race. To see the full picture of a latency arbitrage race requires seeing the full message traffic to and from the exchange, including the exchange error messages sent to losers of the race (specifically, failed IOCs and failed cancels). Armed with this simple insight and the correct data, it was conceptually straightforward, albeit human-time and computer-time intensive, to develop and implement the empirical method described in Section 3.⁴³

The paper’s second—and we think main—contribution is the set of empirical facts we document about latency arbitrage in Section 4. We show that races are very frequent and very fast, with an average of 537 races per day for FTSE 100 stocks, lasting an average of just 81 microseconds, and with a mode of just 5-10 microseconds, or less than 1/10000th of the time it takes to blink your eye. Over 20% of trading volume takes place in races. A small number of firms win the large majority of races, disproportionately as takers of liquidity. Most races are for very small amounts of money, averaging just over half a tick. But even just half a tick, over 20% of trading volume, adds up. The latency arbitrage tax, defined as latency arbitrage profits divided by trading volume, is 0.42 basis points based on all trading volume, and 0.53 basis points based on all non-race volume. This amounts to about GBP 60 million annually in the UK. Extrapolating from our UK data, our estimates imply that latency arbitrage is worth on the order of \$5 billion annually in global equity

⁴²As yet another approach to extrapolation: Virtu recently started publishing global bid-ask spreads data (Virtu, 2021). If we take the Virtu spreads data from Jan 2020, which is the one month in their data that is both globally comprehensive and pre-pandemic, and we use WFE global equity volumes from that same month, we obtain a global value-weighted effective spread of 3.78 basis points. If we then apply our 16.7% overall reduction in liquidity cost to the non-race effective spread paid, we get about \$6 billion per year instead of about \$5 billion per year.

⁴³The final run of our code, including all sensitivity analyses, required about 24 days of computer time on a 128-core AWS server (about 60 hours for data preparation and the baseline analysis, plus an additional 35 hours per sensitivity analysis). From initial receipt of data to first completed draft, the paper required about 3 years of work. The main reason the project has been time intensive, despite its conceptual simplicity, is that message data had never been used before for research (neither academic research nor, we think, industry research) and it took a lot of false starts and iterations to fully understand. We expect that future research using message data will be a lot more efficient than our study for at least two reasons. First, our study can be used as a blueprint. Second, some code re-optimization we are including in the code that will be disseminated publicly reduces the computational run time by about 75%.

markets alone.

A third contribution, more technical in nature but we hope useful to the literature, is the development of two new approaches to quantifying latency arbitrage as a proportion of the overall cost of liquidity. These new methods, used in conjunction with the results described above, show that latency arbitrage accounts for 33% of the effective spread, 31% of all price impact, and that market designs that eliminate latency arbitrage would reduce the cost of liquidity for investors by 17%.

One natural direction for future research is to utilize this paper’s method for detecting latency arbitrage races to then try to better understand their sources. One could imagine, for instance, trying to quantify what proportion of latency arbitrage races involve public signals from the same symbol traded on a different venue, what proportion involve a change in a correlated market index, what proportion involve signals from different asset classes or geographies, etc. Such a study could utilize machine learning methods, treating races as the outcome variable and then trying to understand what preceding market conditions explain the observed races, and would ideally utilize data across many different exchanges and asset classes to cast a wide net in the search for race triggers.

Our main hope for future research, however, is simply that other researchers and regulatory authorities replicate our analysis for markets beyond UK equities. Of particular interest would be markets like US equities that are more fragmented than the UK; and assets such as ETFs, futures, treasuries and currencies that have lots of mechanical arbitrage relationships with other highly-correlated assets. The “hard” part of such a study is obtaining the message data. Once one has the message data, applying the method we have developed in this paper is relatively straightforward.⁴⁴

To our knowledge, most regulators do not currently capture message data from exchanges, and exchanges seem to preserve message data somewhat inconsistently. We hope this will change. Limit order book data has historically been viewed as the official record of what happened in the market, but our study suggests that message data, and especially the “error messages” that indicate that a particular participant has failed in their request, are key to understanding speed-sensitive trading.

⁴⁴To this end, our codebase and a user guide will be made publicly available upon publication of this paper. Regulators and researchers interested in obtaining this codebase and user guide prior to publication should contact the authors.

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