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ABSTRACT

Data-intensive technologies, like AI, are increasingly widespread. We argue that the direction of innovation and growth in data-intensive economies may be crucially shaped by the state because: (i) the state is a key collector of data and (ii) data is sharable across uses within firms, potentially generating economies of scope. We study a prototypical setting: facial recognition AI in China. Collecting comprehensive data on firms and government procurement contracts, we find evidence of economies of scope arising from government data: firms awarded contracts providing access to more government data produce both more government and commercial software. We then build a directed technical change model to study the implications of government data access for the direction of innovation, growth, and welfare. We conclude with three applications showing how data-intensive innovation may be shaped by the state: both directly, by setting industrial policy; and indirectly, by choosing surveillance levels and privacy regulations.

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1 Introduction

Artificial intelligence and machine learning technologies (“AI” for brevity) are increasingly widespread. Because of their potential, they have attracted a great deal of attention from economists and others (see Agrawal et al., eds, 2019 for a review). Developing these technologies is *data-intensive*. The importance of data can be seen in recent breakthroughs from translation, to speech and facial recognition, to chess grand mastery: all of these were driven as much by access to massive amounts of data as by algorithmic advances.¹

Data differs from other inputs into innovation in two important ways. First, throughout history and up to the present, states have collected massive quantities of data to fulfill their primary objectives. From administrative data that make society “legible” (Scott, 1998) and allow the state to collect taxes; to surveillance data used to provide public security; to geographic and scientific data used for national defense, among others. Tellingly, “state” is at the root of the word “statistics.” Second, data can be shared across multiple uses within a firm. These two features may generate *economies of scope* from government data.² In particular, a firm gaining access to government data collected by the state could use that same data to develop new products for government uses as well as for commercial ones. Thus, government data collection and provision can potentially affect not only government product innovation, but also innovation targeting much larger commercial markets. In this paper, we argue that, because of these two features of data, the direction of innovation and growth in data-intensive economies may be crucially shaped by the state.

To examine the empirical relevance of the two features of data we have highlighted, we study a prototypical data-intensive sector in which the state has a significant interest: the facial recognition AI industry in China. We find evidence of economies of scope arising from government data: following the receipt of a government contract to supply AI software, firms produce more software both for *government* and *commercial* purposes when the contract provides access to more government data. To study the *aggregate* implications of firms’ access to government data, we build a general equilibrium directed technical change model where some firms choose to engage in data-intensive innovation, the state and private sector demand data-intensive software to produce “surveillance” services and consumption goods, respectively, and government data gives rise to economies of scope. We show that increasing the amount of government data provided to firms can indeed

¹See Sejnowski (2018). Kai-Fu Lee (former director of Microsoft Research Asia and president of Google China) has even argued that, as opposed to researchers, “... it is data that is crucial to the implementation of AI technologies ...” (<https://asiahouse.org/news-and-views/kai-fu-lee-age-ai-china-new-openc/>, last accessed July 10, 2020).

²The sharability of data across multiple uses within the firm is related to the non-rivalry of data across firms, which has been highlighted by Jones and Tonetti (2018), among others. Seminal work by Panzar and Willig (1981) shows how economies scope may arise in the presence of sharable inputs.

increase the economy's growth rate and bias the direction of private innovation towards data-intensive software. However, because innovation crowds-out resources from consumption, government data provision increases welfare only when economies of scope are sufficiently strong.³ We conclude with three applications which illustrate the varied ways that data-intensive innovation may be shaped by the state: both directly, by setting industrial policies; and indirectly, by choosing public surveillance levels as well as enacting privacy regulations. These applications demonstrate that the welfare implications of government data collection and provision are further complicated by potential misalignment between citizens' and states' preferences for surveillance and privacy.

Our paper begins by presenting a simple conceptual framework where economies of scope in data-intensive innovation arise from government data being sharable across multiple uses. We derive a key prediction that guides our subsequent empirical analysis: a government contract that results in an exogenous increase in the government data available to a firm will lead to increased production of *both* government and commercial software. Yet, we note that economies of scope may not arise even when government data can be shared across uses. For instance, firms may not increase commercial software production upon receipt of a government contract if, in order to fulfill it, the firm needs to reallocate substantial resources towards government software production and away from commercial software production.

The facial recognition AI industry in China is a uniquely suited empirical context to study this question. Firms developing facial recognition software require large datasets, in particular allowing the linkage of faces to personal identifiers. The Chinese state both collects huge amounts of personally identifiable data and demands facial recognition software for surveillance purposes.⁴ A firm receiving a government contract would thus receive access to government data which is not publicly available, using this data to develop the software it was contracted to produce. For example, when obtaining a contract with a municipal police department to produce surveillance software, it would receive access to video from street cameras and a database of labeled personal images. It would then develop surveillance software by training an AI algorithm that matches individuals in video to the database of labeled images. Crucially though, the detection of individuals from video (or photo) data is also key to any *commercial* facial recognition AI application, for

³These results, albeit different in context and mechanism, echo those in Barro (1990), who shows how optimal government provision of services (like infrastructure) trades-off direct increases in firm productivity and growth against the crowding-out of resources from consumption.

⁴To be precise, the Chinese state possesses administrative records that link faces to identities (i.e., it possesses large amounts of *identified* data) and it also collects huge amounts of facial data that can be linked to administrative records (i.e., it collects large amounts of *identifiable* data). Both identified and identifiable data are critical inputs into training facial recognition AI algorithms.

instance, facial recognition platforms for retail stores.⁵ Therefore, to the extent that the government data (or fine-tuned detection algorithm) is sharable across uses, there may exist economies of scope.

Reflecting this discussion, our empirical strategy compares changes in firm software output following the receipt of *data-rich* versus *data-scarce* government contracts. In order to operationalize it, we overcome three data challenges. First, linking AI firms to government contracts. To do so, we collect data on (approximately) the universe of Chinese facial recognition AI firms and link this data to a separate database of Chinese government contracts, issued by all levels of the government. Second, quantifying AI firms' software production and, as important, classifying firms' software by intended use. We do this by compiling data on all Chinese facial recognition AI firms' software development based on the digital product registration records maintained by the Chinese government. Using a Recurrent Neural Network model, we categorize software products based on whether they are directed towards the commercial market or government use. Third, measuring the amount of government data to which firms have access. To do this, we construct two proxies for the data-richness of an AI contract. We begin by distinguishing among government contract awarding agencies. Procurement contracts awarded by a public security agency are most likely to provide access to massive, linkable, personal data, collected for monitoring purposes, while contracts with other agencies likely provide access to less data.⁶ Thus, our first proxy for a data-rich contract is one that came from a public security agency, whereas a data-scarce contract is one that did not. We next distinguish among contracts within the set of public security contracts, identifying those that are likely to be especially rich in data. These are contracts with public security agencies possessing greater surveillance capacity, which we measure using prefectural government contracts for surveillance cameras. Thus, our second proxy for a data-rich contract is one that came from a public security agency located in a prefecture with above-median surveillance capacity at the time the contract was awarded, whereas a data-scarce contract is one coming from a public security agency located in a prefecture with below-median surveillance capacity. We prefer the second proxy as it allows us to make comparisons *within* a set of very similar public security contracts.

Using these newly constructed datasets, we use a triple differences design to estimate the effect of access to greater amounts of government data on facial recognition AI firms' subsequent software development. Specifically, we compare firms' software releases be-

⁵While the ultimate behaviors predicted for government and commercial purposes are likely to differ, the detection problem — and thus the benefit from access to larger amounts of government data — is shared.

⁶Non-public security agencies do not have access to large scale surveillance camera networks and cover narrower groups of individuals. For example, a bank, school, or hospital might hire an AI firm to provide facial recognition-based access to its facilities.

fore and after they receive their first government contract, controlling for firm and time period fixed effects. To help pin down the importance of access to *government data*, rather than other benefits of government contracts, such as capital, reputation, and political connections, we exploit variation in the type of contract: data-rich or data-scarce. We find that receipt of a data-rich contract *differentially* increases *both* government and commercial software production, relative to receipt of a data-scarce contract. Our evidence is thus consistent with the presence of economies of scope, reflecting crowding-*in* rather than crowding-out. Using our preferred proxy for data-richness, we find that in the three years after the receipt of a contract, data-rich contracts generate an *additional* 3 government software products (over and above the effects of a data-scarce contract), and an additional 2 commercial software products.

We provide a range of corroborating evidence for our proposed mechanism of access to government data contributing to product innovation. First, we observe lower bids (even controlling for firm fixed effects) for data-rich contracts, as well as more bidders overall. Second, we find that production of non-AI, data-complementary software (e.g., software supporting data storage and transmission) significantly, and differentially, increases after firms receive data-rich public security contracts. Finally, we find that firms that produce video facial recognition AI software for the government — a type of software that requires access to particularly large amounts of data — exhibit differentially large increases in data-complementary software production, and greater commercial and government AI software production as well.

We conclude our empirical analysis by evaluating a range of threats to identification and alternative mechanisms. First, we show that systematic firm selection into receiving contracts at a particular time is unlikely to drive our main results: our event-study estimates show no differential software production prior to receipt of a data-rich contract, and our findings are robust to allowing pre-contract firm characteristics to flexibly affect post-contract output. Second, we show that learning-by-doing is unlikely to be differentially stronger for data-rich contracts: data-rich contracts do not meaningfully differ from data-scarce ones in their content and we find that the types of government software produced after data-rich contracts are not different from those produced after data-scarce ones. Moreover, we show that controlling for pre-contract software production (a measure of how strong the potential for learning is) only slightly reduces the differential effects of a data-rich contract. Third, we show that the baseline results are not driven by the differential capital, signaling value, commercial opportunities, or connections to local government that may be provided by data-rich contracts, relative to the data-scarce ones.

Significant microeconomic consequences of economies of scope arising from government data do not necessarily imply that provision of government data would promote

aggregate innovation or increase welfare. To examine the macroeconomic implications of government data access, we develop a directed technical change model, building on Acemoglu (2002). We let innovator firms develop and supply differentiated varieties of data-intensive government and commercial software, as well as other, non-software varieties which do not use data as an input. Commercial software and non-software are used to produce a final good. Government software is purchased by the state to produce a government good, which we call “surveillance” for concreteness. There are two types of data in the economy: government and private. Government data is necessary for producing government software. We assume that the same government data could simultaneously be used for producing both government and commercial software, generating economies of scope. Government data is produced as a by-product of surveillance, whereas private data is a by-product of total private transactions (as measured by final good output). Both types of data are excludable, but only private data can be purchased in the market. As in our empirical context, government data can only be accessed by producing government software for the state after procuring a government contract. Finally, a representative household owns all firms and consumes the final good.

We show conditions under which there is a unique BGP equilibrium with free-entry of innovators and three types of firms being present: those producing both government and commercial software using government and private data, those producing private software using private data alone, and those producing non-software. Then, we study how government data access affects innovation and welfare. When commercial software and non-software are sufficiently substitutable, an increase in government data provided to firms increases the BGP rate of innovation and biases private innovation towards data-intensive software. However, the welfare effect is more ambiguous: while government data provision does lead to a direct positive effect on welfare through higher consumption growth, this is offset by a decrease in the level of consumption due to crowding-out by resources used in innovation. Thus, we consider a second-best problem where the state can only choose the level of government data provided to firms in order to maximize household welfare. We find that, even if neither the state nor the representative household derives utility from surveillance, it may be optimal for the state to produce it in order to provide firms with the government data that is generated as a by-product. This is because, in doing so, it can increase the rate of private software innovation and thus consumption growth when there are economies of scope. Importantly, such a policy is only justified when economies of scope are strong enough and, as a result, the increase in the growth rate is sufficiently large to compensate for the crowding-out of resources.

Finally, in three applications, we illustrate the varied ways that data-intensive innovation may be shaped by the state, both directly and indirectly, because of the features

of data that we highlight. First, we show that industrial policy in the form of government data provision can be justified on grounds which differ from those that motivate traditional industrial policy. Second, we show that surveillance states’ desire to monitor and control their citizens aligns with promoting data-intensive innovation and growth, but may reduce citizen welfare when states’ objectives and citizens’ preferences do not coincide. Third, we show that regulation limiting government data collection reduces data-intensive innovation and growth but may benefit citizens overall when they value privacy.

In what follows, we discuss the related literature and our contribution in Section 2. In Section 3, we present the simple conceptual framework on economies of scope arising from government data as an input, which provides testable predictions that guide our empirical exercise. Next, we present the empirical exercise examining the role of access to government data in shaping innovation in China’s facial recognition AI sector: first the empirical context and data sources in Section 4; then the empirical strategy and results in Section 5. In Section 6, we introduce a general equilibrium framework of directed technical change to study the macroeconomic implications of government data access. We discuss three applications of the framework in Section 7, and offer concluding thoughts in Section 8.

2 Related literature

Our work most directly contributes to an emerging literature on the economics of AI and data, particularly work that aims to understand the role of AI technology and data in fostering innovation, and firm and aggregate growth (see, e.g., Aghion et al., 2017; Agrawal et al., 2018; Farboodi et al., 2019). We contribute to this literature by examining direct and indirect ways in which data-intensive innovation may be shaped by the state, and identifying two crucial characteristics of data that shape the impact of the state on innovation. Our analysis complements a recent literature studying the effects of specific characteristics of information and data on innovation: Williams (2013) studies the non-excludability of government research on genes (in contrast with the excludability of private sector research); Simon and Sichelman (2017) studies the effects of data arising from innovations; and, Aghion et al. (2017) and Jones and Tonetti (2018) study non-rivalry of data across firms. We instead study economies of scope arising from the sharability of government data across government and commercial applications within a firm.

Our examination of the link between the state and the private sector AI industry builds on literatures on both industrial policy and innovation policy. Rodrik (2007) and Lane (2020) provide recent overviews of the industrial policy literature, with the latter highlighting quasi-experimental evidence of effective industrial policy.⁷ Recent research on

⁷Contexts in which industrial policy was shown to be effective include: the 19th century French textile

innovation policy also suggests an important role for the state in encouraging R&D — see Bloom et al. (2019).⁸ We make three primary contributions to these literatures. First, we study a frontier technology: the effects of the state on the development of modern AI innovation, a technology which has enormous economic potential, and which also may be particularly sensitive to state policy. Second, we conceptualize and empirically identify a specific within-firm mechanism underlying spillovers from government expenditure to private innovation in our setting. We highlight that economies of scope across government and commercial uses could generate consequences similar to those achieved by industrial policy and innovation policy, despite the incidental nature of the state’s engagement, for example, due to states’ demand for surveillance or due to citizens’ demand for privacy protection.⁹ Third, we provide a justification for government data provision that differs from that of traditional industrial policies. For example, Costinot et al. (2019) evaluate the case for industrial policy to correct for learning-by-doing externalities. We show that because states are key collectors of data, and because government data can give rise to economies of scope, it may be optimal to directly provide such data to data-intensive software producers, even in the absence of externalities. In this sense, we also contribute to a macroeconomic literature on the role of government spending in promoting economic growth (e.g., Rosenstein-Rodan, 1961, Murphy et al., 1989, Barro, 1990).

By placing our analysis of AI innovation within a model of directed technical change, we contribute to the body of work on these models (Hicks, 1932; Habakkuk, 1962; Acemoglu, 2002, 2007). The theoretical literature is well developed, including applications to: climate change and environmental policy (Acemoglu et al., 2012; Hemous, 2016), technology-skill complementarity (Acemoglu, 1998), the sources of cross-country productivity differences (Acemoglu et al., 2006b), migration (Lewis, 2013), and pharmaceutical innovation (Acemoglu and Linn, 2004). We add to this literature by studying a novel application —

industry, protected by the blockade of British competitors during the Napoleonic Wars (Juhász, 2018); 19th century UK and Great Lakes US shipbuilding (Hanlon, 2020); post-WWII Finland following industrialization imposed by the Soviet Union (Mitrinen, 2019); post-WWII US as a result of Office of Scientific Research and Development (OSRD) spending (Gross and Sampat, 2020); post-WWII Italy, as a result of the US Marshall Plan (Giorcelli, 2019); East Asia’s (and China’s) Growth Miracle (Lane, 2017; Liu, 2019); and, Chinese shipbuilding in the 2000s (Kalouptsi, 2017; Barwick et al., 2019). Bartelme et al. (2019) estimate the importance of sectoral economies of scale that are often used to justify industrial policy, finding that industrial policy may not be as effective as other policies (e.g., trade).

⁸Among others, Bronzini and Iachini (2014) find that R&D subsidies by the Italian government raise investment of small enterprises; Howell (2017) shows that the US Department of Energy’s funding helps financially constrained firms to attract future funding and innovate; Azoulay et al. (2018) demonstrate that public scientific grant funding increases private sector patenting among pharmaceutical and biotechnology firms; and, Moretti et al. (2019) show that defense-related R&D expenditures of OECD countries crowd in private sector R&D spending. In related work, Moser (2005) and Moser and Voena (2012) study the role of state policy on intellectual property rights in shaping patterns of innovation.

⁹Incidental industrial policy is also documented by Slavtchev and Wiederhold (2016). Our finding of a within-firm spillover to products *other than* those contracted on contrasts with firms’ tendency to specialize after a specific government demand shock, as seen in Clemens and Rogers (2020).

data-intensive innovation and the role of the state. Our empirical analysis contributes to a much smaller body of empirical work on directed technical change. Existing work has focused on the effect of energy prices on innovation in energy-saving technologies (Newell et al., 1999; Popp, 2002; Aghion et al., 2016), and the effect of demand forces on pharmaceutical innovation (Acemoglu et al., 2006a; Acemoglu and Linn, 2004; Costinot et al., 2019). An exception is Hanlon (2015), who documents that the reduction in the supply of American cotton to Britain due to the US Civil War induced innovation toward technologies complementing cotton varieties from other sources. We add to this literature by documenting how an increase in the supply of data, as a result of receiving a government contract, induces Chinese firms to develop (data-intensive) commercial applications of AI technologies.

Finally, we highlight the political dimension of data-intensive AI innovation. Data is valued — and thus accumulated — by modern surveillance states, particularly by autocratic states (Guriev and Treisman, 2019). In addition, a fundamental aim of AI technology — to make accurate predictions — is aligned with their surveillance and social control agenda (Zuboff, 2019). Therefore, AI is a technology that can buttress rather than threaten autocratic regimes. Combining these insights, our project contributes to our understanding of how political economy affects the rate and direction of technical change. Traditionally, scholars have emphasized limits on entrepreneurship under autocracies arising from the misaligned incentives facing entrepreneurs and political elites.¹⁰ In the domain of AI technology, however, surveillance states’ objectives and data collection, along with the economies of scope arising from data as an input, facilitate data-intensive innovation even for commercial applications. Thus, the alignment between the state and private sector could offset the expropriation risks and commitment problems traditionally faced by private entrepreneurs under autocracy, although, as we emphasize, such alignment may still be detrimental to citizens overall. Our analysis thus may also help explain the puzzle of China’s global leadership in AI innovation and more generally suggests that modern autocracy may be compatible with technical change along specific trajectories.¹¹

¹⁰The risk of *ex post* taxation or expropriation of entrepreneurs will mean *ex ante* less investment (North, 1991; North et al., 2009; Acemoglu and Robinson, 2012). Threats to elites arising from successful entrepreneurs will mean that elites may *ex ante* tax entrepreneurs to preserve their political rents (Acemoglu and Robinson, 2006). Corruption and other public sectors distortions will also discourage innovation and investment (Shleifer and Vishny, 1993, 2002).

¹¹A large literature studies the Chinese economy and its spectacular growth in the recent decades (e.g., Song et al., 2011; Khandelwal et al., 2013; Roberts et al., 2017; Cheng et al., 2019; Bai et al., 2019), as well as innovation in China more specifically (e.g., Wei et al., 2016; Bombardini et al., 2018). Much of the work on China’s political economy highlights institutional features — for example, competition for promotion (e.g., Li and Zhou, 2005; Jia et al., 2015), bureaucratic rules of evaluation and rotation (Li, 2019), or social norms (Tsai, 2007) — that allow China to grow *despite* the lack of institutional constraints on the Chinese Communist Party. In contrast, our work (along with others, like Bai et al., 2019) identifies a mechanism through which autocratic power can actually *promote* economic growth.

3 Economies of scope from government data as an input

This section discusses how government data can generate economies of scope and derives the key testable implication that guides our empirical approach in the following sections. We consider a setting that incorporates the two characteristics of data that we highlight: (i) the state is a key collector of data with no perfect private substitutes, and (ii) data can be shared across uses.

Suppose that a firm may develop data-intensive software for both the state and the private sector. Assume that developing software for the state uses government data d_g as an input. Imagine — as is the case in reality — that there exist types of government data that lack close substitutes (e.g., surveillance video which can be linked to administratively identified records) and that are not made publicly available. In order to obtain access to these government data, the firm must obtain a contract from the state to produce government software. Government software production also uses a number of other inputs, including other forms of data, which can be purchased in the market, and which we denote in vector form by x_g . Then, we let $F_g(d_g, x_g)$ be the production function of software for the government S_g .

Moreover, assume that if a firm has access to government data d_g , then it can use that *same* data to produce commercial software for the private sector. That is, government data can be *shared across uses*. We let $F_c(d_g, x_c)$ be the production function of commercial software S_c , where x_c is again a vector other types of inputs. As an example of government data and its shared uses, consider video from street surveillance cameras and administrative records with the names of individuals linked to images of their faces. This data is used to train an algorithm with the ability to *recognize* faces in video and identify individuals in administrative records. That trained identification algorithm may then also be part of a more complex software application that performs the *predictive* task of identifying potential security threats. That same data, though, is also a crucial input to train algorithms that perform a wide range of *commercial* recognition and prediction tasks, such as identifying a customer in video from cameras in a store or predicting a customer's purchases.¹²

Following Panzar and Willig (1981), it is possible that *economies of scope* arise when $\frac{\partial F_c}{\partial d_g} > 0$. Intuitively, this is because the firm obtaining more government data by producing government software could produce a given level of commercial software S_c with less of the other inputs, and thus at lower cost.¹³ This generates a testable implication about

¹²Note that an alternative plausible specification of the technologies would be one where government data is not shared across uses *per se*, but is instead used to train a “base algorithm,” which is used as an input to both government and private software. For the purposes of our paper, these two specifications are equivalent.

¹³Imagine that the firm splits in two: one only producing government software (with access to government data) and the other one only producing private software (without access to government data). Formally, let input prices be ω and let $C(S_g, S_c, d_g, \omega)$, $C_g(S_g, 0, d_g, \omega)$, and $C_c(0, S_c, 0, \omega)$ be the cost functions of the

the firm-level impact of obtaining a government contract that is richer in data, when there are economies of scope. Consider a firm that is already producing commercial software. Suppose it receives a government contract to produce government software, which provides access to government data (with $\frac{\partial F_c}{\partial d_g} > 0$). Then this firm could begin to produce not only more government software (using government data), but also more commercial software, because the government data to which it receives access can be used for commercial software production as well.

Note, however, that these economies of scope are not guaranteed. For instance, when a firm uses resources to produce more government software, this may *crowd-out* resources that would have been used for commercial software production. If such crowding-out effects are relatively strong, obtaining a government contract that is richer in government data would induce the firm to produce more government software but *less* commercial software. Observing increases in *both* government and commercial software production following receipt of a data-rich government contract would thus be strong evidence for economies of scope arising from government data, where the ability to share data across uses more than offsets any crowding out of resources.

In the next section, we test for this implication of economies of scope in the context of China’s AI industry:

Implication of economies of scope arising from government data: Obtaining a government contract that is richer in government data induces a firm to produce both more government and commercial software.

4 The state and China’s facial recognition AI: context and data sources

4.1 Empirical context

China’s facial recognition AI sector is a prototypical setting in which to examine the impact of access to government data on innovation and to provide evidence of economies of scope arising from such data. First, because facial recognition AI is extremely data-intensive: the development of the technology requires access to large datasets that allow the linkage of faces to personal identities. Second, because the Chinese state collects huge amounts of personally identifiable data and demands software in order to monitor citizens. The value of government data is clear to private sector entrepreneurs: in 2019, a founder of a leading Chinese AI firm stated, “The core reason why [Chinese] AI achieves such tremendous

firms producing both types of software and each type separately. Then, there are economies of scope when $C(S_g, S_c, d_g, \omega) < C_g(S_g, 0, d_g, \omega) + C_c(0, S_c, 0, \omega)$.

success is due to data availability and related technology. Government data is the biggest source of data for AI firms like us.”¹⁴ Importantly, data acquired privately are not currently a close substitute for government data: in 2019, the former premier, Li Keqiang, stated that, “At this time, 80% of the data in China is controlled by various government agencies.”¹⁵

Consider an example in which a private firm receives a procurement contract to provide facial recognition software to a municipal police department in China. The firm implicitly receives access to large quantities of government data which are not publicly available. Such data includes video from street surveillance cameras as well as labeled images with names and faces of individuals. The firm uses this data to train a “detection” AI algorithm: matching faces observed in cameras to the database of individuals. Then, economies of scope can arise from the government data being used to train a separate algorithm that results in a commercial AI product, for example, AI software designed for retail firms who may wish to detect and track individual shoppers throughout their stores, and then predict their consumption choices.

This context allows us to empirically test for economies of scope arising from access to government data. In particular, in the next section we exploit within-firm variation over time in the receipt of procurement contracts, together with variation in the data available to firms under different contracts. This allows us to estimate the effect of access to more government data on both government and commercial software production.

4.2 Data sources

Operationalizing our empirical analysis faces three data-related empirical challenges: first, the need to link AI firms to government contracts; second, the need to compile information on AI firms’ software production, and specifically the orientation of software toward government or commercial use; and, third, the need to measure the quantity of government data to which firms have access. We address these challenges by constructing a novel dataset combining information on Chinese facial recognition AI firms and their software releases, and information on local governments’ procurement of AI software and of surveillance cameras.¹⁶

Linking Chinese facial recognition AI firms to government contracts We identify (close to) all active firms based in China producing facial recognition AI using information from

¹⁴Source: Chinese People’s Political Consultative Conference official website: <http://www.rmzxb.com.cn/c/2019-06-13/2363368.shtml>, last accessed June 12, 2020.

¹⁵*Ibid.* It is important to note that Chinese government support of AI innovation is not limited to data provision, but also includes a range of subsidies. Industrial policy that broadly affects all firms (whether or not they receive government data) is thus an important characteristic of the setting we study. It is also more broadly a characteristic of AI innovation around the world.

¹⁶Appendix Table A.1 describes the core variables and their sources.

Tianyancha, a comprehensive database on Chinese firms licensed by the People’s Bank of China (i.e., China’s central bank).¹⁷ We extract firms that are categorized as facial recognition AI producers by the database, and we validate the categorization by manually coding firms based on their descriptions and product lists. We complement the *Tianyancha* database with information from *Pitchbook*, a database owned by Morningstar on firms and private capital markets around the world.¹⁸ Using the overlap between sources, we validate the coding of firms identified in the *Tianyancha* database. We also supplement the *Tianyancha* data by adding a small number of AI firms that are listed by *Pitchbook* but omitted by *Tianyancha*. Overall, we identify 7,837 Chinese facial recognition AI firms.¹⁹ We also collect an array of firm level characteristics such as founding year, capitalization, major external financing sources, as well as subsidiary and mother firm information.

We extract information on 2,997,105 procurement contracts issued by all levels of the Chinese government between 2013 and 2019 from the Chinese Government Procurement Database, maintained by China’s Ministry of Finance.²⁰ The contract database contains information on the good or service procured, the date of the contract, the monetary size of the contract, the winning bid, as well as the number of bidders for a subset of the contracts. To identify contracts procuring facial recognition AI, we match the contracts with the list of facial recognition AI firms, identifying 26,200 procurement contracts involving at least one facial recognition AI firm. Many firms receive multiple contracts; overall, 1,095 of the facial recognition AI firms in our dataset receive at least one contract.

Counting and classifying novel facial recognition AI software products We collect all software registration records for our facial recognition AI firms from China’s Ministry of Industry and Information Technology, with which Chinese firms are required to register new software releases and major upgrades. We are able to validate our measure of software releases (using a single large firm), by cross-checking our data against the IPO Prospectus of MegVii, the world’s first facial recognition AI company to file for an IPO.²¹ We find that our records’ coverage is comprehensive (at least in the case of MegVii): MegVii’s IPO Prospectus contains 103 software releases, all of which are included in our dataset.

We use a Recurrent Neural Network (RNN) model with tensorflow — a frontier method for analyzing text using machine learning — to categorize software products according to their intended customers and (independently) by their function. Our categorization by

¹⁷See Supplementary Figure S.1 for an example entry.

¹⁸See Supplementary Figure S.2 for an example entry.

¹⁹These firms fall into 3 categories: (i) firms specialized in facial recognition AI (e.g., Yitu); (ii) hardware firms that devote substantial resources to develop AI software (e.g., Hik-Vision); and (iii) a small number of distinct AI units within large tech conglomerates (e.g., Baidu AI).

²⁰See Supplementary Figure S.3 for an example contract.

²¹The prospectus was filed with the Hong Kong Stock Exchange. See <https://go.aws/37GbAZG>, last accessed June 22, 2020.

customer distinguishes between software products developed for the government (e.g., “smart city — real time monitoring system on main traffic routes”) and software products developed for commercial applications (e.g., “visual recognition system for smart retail”). We allow for a residual category of general application software whose description does not clearly specify the intended user (e.g., “a synchronization method for multi-view cameras based on FPGA chips”). By coding as “commercial” only those products that are specifically linked to commercial applications, and excluding products with ambiguous use, we aim to be conservative in our measure of commercial software products.

Our categorization by function first distinguishes between software products that are directly related to AI (e.g., “a method for pedestrian counting at crossroads based on multi-view cameras system in complicated situations”) and those that are data-complementary, involving data storage, data transmission, or data management (e.g., “a computer cluster for webcam monitoring data storage”). Within the category of AI software, we also separately identify a subcategory of software that is particularly data-intensive: video-based facial recognition, which (as opposed to static images) requires N-to-1 or even N-to-N matching algorithms that are extremely data demanding.²²

To implement the two dimensions of categorization using the RNN model, we manually label 13,000 software products to produce a training corpus. We then use word-embedding to convert sentences in the software descriptions into vectors based on word frequencies, where we use words from the full dataset as the dictionary. We use a Long Short-Term Memory (LSTM) algorithm, configured with 2 layers of 32 nodes. We use 90% of the data for algorithm training, while 10% is retained for validation. We run 10,000 training cycles for gradient descent on the accuracy loss function. The categorizations perform well in general: we are able to achieve 72% median accuracy in categorizing software customer and 98% median accuracy in categorizing software function in the validation data. Appendix Figure A.1 shows the summary statistics of the categorization output by customers and by function; and, Appendix Figure A.2 presents the confusion matrix (Type-I and Type-II errors) of the predictions relative to categorization performed by humans.²³

Measuring the quantity of government data to which firms have access We construct two proxies for access to greater amounts of government data. We begin by distinguishing among government contract awarding agencies. Procurement contracts awarded by

²²The differences in 1-to-1, N-to-1, and N-to-N matching in facial recognition are sometimes referred to as facial authentication versus facial recognition; see Gates (2011) for more details.

²³Supplementary Table S.1 presents the top words (in terms of frequency) used for the categorization and Supplementary Figure S.4 presents the density plots of the algorithm’s category predictions. The algorithm is very accurate in categorizing software for government purposes. The algorithm is relatively conservative in categorizing software products for commercial customers, and relatively aggressive in categorizing them as general purpose. In setting our categorization threshold for commercial software we again aim to be conservative in our measure of commercial software products.

a public security agency are most likely to provide access to massive, linkable, personal data, collected for monitoring purposes, while contracts with other agencies likely provide access to less data. Take, as an example from our dataset, a public security contract signed between an AI firm and a municipal police department in Heilongjiang Province to “increase the capacity of its identity information collection system” on August 29th, 2018. The contract specifies that the AI firm shall provide a facial recognition system that can store and analyze at least 30 million facial images — a substantial amount of data to which the firm obtains access. In contrast, consider a non-public security contract in our dataset signed between an AI firm and a provincial bank in Gansu Province to “establish its facial recognition system” on November 20th, 2018. The system is aimed at providing identification services for the bank’s clients, suggesting that the AI firm obtains access to a relatively small amount of data (i.e., identified faces) compared to a public security contract.

Our first empirical definition of a data-rich contract is a contract with a public security agency, the effects of which we compare to those of data-scarce procurement contracts, awarded by government agencies unrelated to public security (e.g., contracts with schools to monitor cheating during exams). Such non-public security contracts indicate a firm’s relationship with the government, but do not provide access to large amounts of personally identified facial data.²⁴

Our measure of public security contracts is comprehensive. We capture the following four types of contracts from the Chinese Government Procurement Database: (i) all contracts for China’s flagship surveillance/monitoring projects — *Skynet Project*, *Peaceful City Project*, and *Bright Transparency Project*; (ii) all contracts with local police departments; (iii) all contracts with the border control and national security units; and, (iv) all contracts with the administrative units for domestic security and stability maintenance, the government’s political and legal affairs commission, and various “smart city” and digital urban management units of the government.

We identify 28,023 public security procurement contracts involving at least one facial recognition AI firm. Many firms receive multiple contracts; overall, 7.2% (568 of 7,837) of the facial recognition AI firms in our dataset receive at least one public security procurement contract. We find that 12.6% (984 of 7,837) of the facial recognition AI firms in our dataset receive at least one non-public security contract, and 5.2% (408 of 7,837) of the facial recognition AI firms receive at least one contract of each type.

We next distinguish among contracts *within* the set of public security contracts, identifying those that are likely to be especially rich in data for facial recognition AI firms.

²⁴We identify 410,510 public security contracts in total. We present the cumulative number of procurement contracts of each type (public security and non-public security) in Supplementary Figure S.5, top panel; as well as the flow of new contracts signed in each month (bottom panel). Both the public security and non-public security contracts have steadily increased since 2013.



Figure 1: Each circle represents a prefecture in our dataset that has at least one surveillance camera contract as well as an AI contract that is some AI firm’s first government contract. Circle size indicates the number of first AI contracts awarded in the prefecture (larger circles indicate more contracts, log scale). Circle shading indicates the fraction of first AI contracts that were data-rich or data-scarce, where the within-prefecture variation comes from changes in the number of surveillance cameras in a prefecture over time (a larger fraction of dark shading indicates a larger fraction of prefecture contracts being data-rich).

In particular, we identify contracts with public security agencies possessing greater video surveillance capacity, which we measure using 5,837 prefectural government contracts for surveillance cameras.²⁵ We sum the number of cameras procured in each prefecture up to a certain date and divide this by the prefecture’s population to form a time-varying measure of the video surveillance capacity of a particular prefecture.²⁶ Our second — and preferred — empirical definition of a data-rich contract is one with a public security agency located in a prefecture that has above-median surveillance capacity (measured by cameras per capita) at the time the contract was awarded. Figure 1 shows the distribution of data-rich and data-scarce contracts across prefectures according to this second, preferred definition.²⁷ We compare the effects of these data-rich contracts to data-scarce public security contracts, now defined as contracts awarded by a public security agency, but located in a prefecture that has below-median surveillance capacity at the time the contract was awarded. We prefer this definition of a data-rich contract given the fineness of the comparison within a set of firms that selected into a similar set of public security contracts.

²⁵These contracts contain data including the quantity of cameras ordered, the total size of the contract, the unit price of cameras, as well as the locality and time in which the contract must be fulfilled; when data on price and quantity is (occasionally) missing, we use data from the same prefecture to impute values. There are on average 77 contracts per prefecture. In Supplementary Figure S.6, we present a time series plot of the number of cameras in our data over time.

²⁶This measure captures the stock of *newer* surveillance cameras at the time an AI procurement contract was awarded. While we do not observe the entire stock of surveillance cameras — including older ones — we believe that a focus on newer cameras is appropriate given their higher resolution and thus greater usefulness in identifying and matching faces. This is affirmed in the Chinese government’s directive “Several Opinions on Strengthening the Construction, Networking and Application of Public Security Video Surveillance.” Source: <https://bit.ly/3dqdjU0>, last accessed on June 22, 2020.

²⁷By measuring data-richness at the time of the contract, we ensure that secular trends in surveillance capacity do not skew our measure toward coding later contracts as data-richer.

Summary statistics In Appendix Table A.2, we present summary statistics describing the firms in our sample. One can see that firms receiving different types of contracts differ substantially from each other, so accounting for differences (both observable and unobservable) between the firms receiving data-rich and data-scarce contracts will be crucial to identify the effects of the contracts. Interestingly, some patterns of selection into contracts that are data-rich differ depending on the definition used: for example, firms receiving public security contracts are better capitalized than firms receiving non-public security contracts (40 vs. 13 million USD), but firms receiving public security contracts in high-surveillance prefectures are less well capitalized than firms receiving public security contracts in low-surveillance prefectures (13 vs. 61 million USD). This suggests that simple selection stories will not easily account for effects of data-rich contracts seen along both margins of comparison.

In Appendix Table A.3, we present summary statistics describing the contracts procuring AI services in our sample.²⁸ One can see that data-scarce and data-rich contracts differ on dimensions other than in the quantity of data to which firms receive access, so accounting for alternative mechanisms (other than data provision) through which data-rich contracts might affect software production will be crucial to identifying the causal effects of interest. However, it is worth noting that the differences observed between data-rich and data-scarce contracts often reverse depending on which definition of data-rich is used. For example, public security contracts are on average issued by a lower administrative unit than non-public security contracts (28% vs. 34% by provincial level or above), but public security contracts issued in prefectures with above-median surveillance capacity are issued by a higher administrative unit than public security contracts issued in prefectures with below-median surveillance capacity (31% vs. 14% by provincial level or above). Finding consistent effects of data-rich contracts across definitions will argue against simple alternative hypotheses regarding unobserved contract characteristics.

5 Analyzing the role of government data in Chinese facial recognition AI

5.1 Empirical model and identification strategy

We use a triple differences design to identify the effects of accessing government data on facial recognition AI firms' subsequent product development and innovation. The empirical strategy exploits variation across time and across firms in the receipt of a government

²⁸In Appendix Table A.4, we provide descriptive statistics for the prefectures where contracts were issued, again disaggregating by the type of agency and by surveillance capacity.

contract, and across types of government contracts that firms receive. Specifically, as in an event study design, we compare firms’ outcomes — their software releases — before and after they receive their first government contracts, controlling for firm and time period fixed effects. To help pin down the importance of access to *government data*, rather than other benefits of government contracts, such as capital, reputation, and political connections, we exploit variation in the type of the government contract received.

We test whether firms receiving data-rich contracts differentially increase their software production following receipt of the contract. To do so, we estimate the following empirical model:

$$y_{it} = \sum_T \beta_{1T} T_{it} Data_i + \sum_T \beta_{2T} T_{it} + \alpha_t + \gamma_i + \sum_T T_{it} X_i + \epsilon_{it}.$$

The outcome variable, y_{it} , is the cumulative number of software releases by firm i up to the semi-year period t . The explanatory variables of interest are the interaction terms between a set of dummy variables, T_{it} , indicating semi-year time periods before or since firm i received its first contract, and $Data_i$, a dummy variable indicating whether the firm’s first contract was data rich, as defined above.²⁹

The coefficients on the interaction terms (i.e., on $\sum T_{it} \times Data_i$) non-parametrically capture a firm’s differential production of new software approaching or following the arrival of initial data-rich contracts, relative to data-scarce ones. To account for time-varying sources of variation in software production common to all facial recognition firms (for example, government industrial policy promoting AI), we include time period fixed effects, α_t in all specifications. We also include firm fixed effects, γ_i , in all specifications, allowing us to control for all (observable or unobservable) time-invariant firm characteristics. Finally, in addition to estimating a parsimonious model without controls, we also estimate a model including a vector of pre-contract firm characteristics (X_i) interacted with time period fixed effects.³⁰ We allow the error term ϵ_{it} to be correlated not only across observations for a single firm, but also across observations for firms that are related by common ownership by a single mother firm.³¹

Our empirical strategy allows us to address important threats to identification. A particular concern is non-random assignment of contracts to firms. We account for fixed firm characteristics that may determine selection into data-rich contracts as well software production by including a full set of firm fixed effects. We can test whether firms produced different amounts of software *prior* to receipt of a data-rich contract by testing whether β_{1T}

²⁹We focus on the effect of the initial contract, because the receipt of subsequent contracts is endogenous to firms’ performance in their initial contracts.

³⁰Controls are firms’ year of establishment, capitalization, and pre-contract level of software production.

³¹We cluster standard errors at the mother firm-level to be conservative; clustering standard errors at the firm level allows us to make even more precise inferences.

differ from zero *prior* to contract receipt (that is, conducting a test of parallel pre-treatment trends). To address the possibility that *ex ante* firm characteristics shape selection into contracts and software production in a time-varying way, we control for firm characteristics interacted with time periods. A second important concern is that contract characteristics other than data may affect software production. Many of these (such as a signal of a firm’s connection to the government) are accounted for by differencing out the effects of data-scarce contracts, and we will also directly control for a contract’s monetary size and a prefecture’s GDP per capita interacted with time period fixed effects. In addition to including these controls, we will also present more direct evidence of data’s importance in generating the effects we observe, as well as evidence against alternative mechanisms.

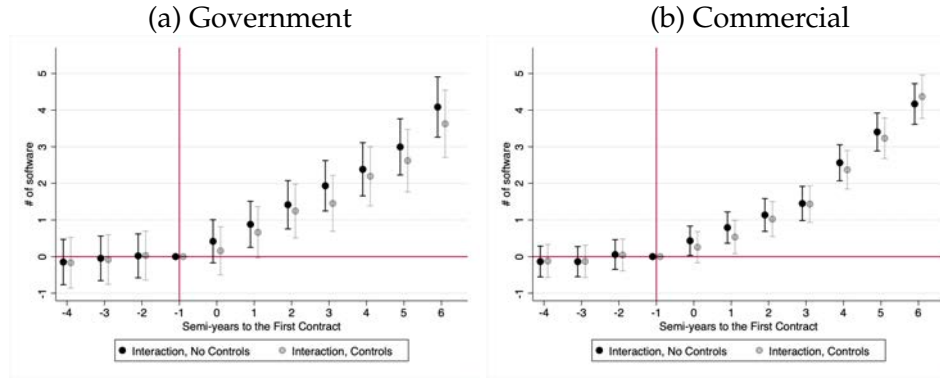
5.2 Results

We first present the baseline results in Section 5.2.1 following the empirical strategy described above; we then present evidence suggesting an important role of government data in firms’ innovation in Section 5.2.2; finally, in Section 5.2.3 we discuss alternative hypotheses and present evidence suggesting they are not driving our main results.

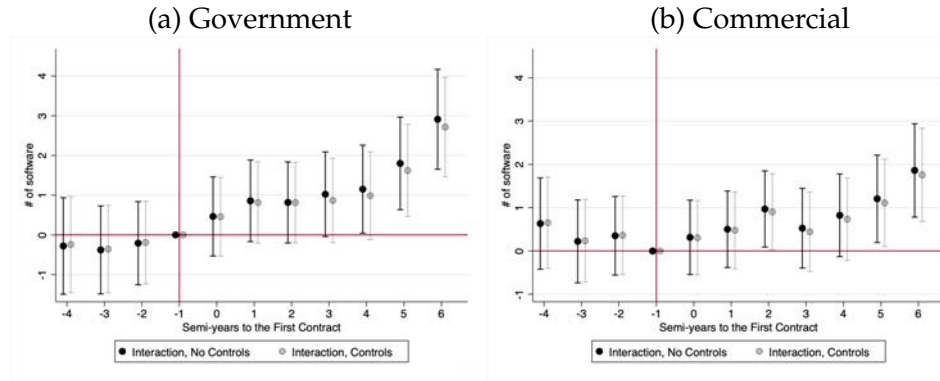
5.2.1 Baseline estimates and robustness checks

We first estimate our baseline specification, comparing the effects of public security contracts to non-public security contracts on firms’ production of software. In Figure 2, Panel A, we plot the coefficients β_{1T} , describing the *differential* software production around the time when a public security contract was received, relative to a non-public security contract (all coefficients are presented in Appendix Table A.5). We show 95% confidence intervals for all coefficients, from models with and without controls ($\sum_T T_{it}X_i$). In Panel A(a), one can see that receipt of a public security contract is associated with differentially more government software production than receipt of a non-public security contract. Suggesting a causal interpretation of the effect of a public security contract, we find no evidence of pre-contract differences in software production levels or trends. The inclusion of controls for time-varying effects of firm characteristics has little effect on our findings. In Panel A(b), one can see that receipt of a public security contract is also associated with differentially more *commercial* software production than receipt of a non-public security contract. Again supporting a causal interpretation of the effect of a public security contract, we find no evidence of pre-contract differences in software production levels or trends. The inclusion of controls for time-varying effects of firm characteristics has little effect on our findings.³²

³²One may wonder what are the overall effects of government contracts that underly the differential effects in Figure 2, Panel A. In Appendix Figure A.4, we plot the coefficients β_{2T} , describing software production around the time when a non-public security contract was received, and the sum of the coefficients, $\beta_{1T} +$



Panel A: Public security vs. non-public security contracts



Panel B: Public security contracts with high vs. low surveillance capacity prefectures

Figure 2: Differential software development intended for government (left column) or for commercial uses (right column), resulting from data-rich contracts, relative to data-scarce contracts, controlling for firm and time period fixed effects. Panel A defines data-rich contracts as all public security contracts, and presents their effects relative to non-public security contracts. Panel B defines data-rich contracts as public security contracts in prefectures with above-median surveillance capacity, and presents their effects relative to public security contracts in prefectures with below-median surveillance capacity. Translucent lines/markers additionally interact pre-contract firm characteristics with a full set of time-period fixed effects.

We next, in Figure 2, Panel B, plot regression coefficients analogous to those in Panel A, but now considering variation in data-richness *within* the set of public security contracts. Specifically, we compare the effects of public security contracts in prefectures with above-median surveillance capacity (data-rich contracts) with those that have below-median surveillance capacity (data-scarce contracts). All coefficients are presented in Appendix Table A.6. This is our preferred proxy of data-richness as it accounts for two potential concerns about our previous comparison between public and non-public security contracts. First, that firm selection into public and non-public security contracts may be different. Second, that public and non-public security contracts may differ beyond the quantity of government data

β_{2T} , describing software production around the time when a public security contract was received. We find that government software and commercial software *both* significantly increase after receipt of *both* non-public security and public security contracts, with effects being significantly greater in the latter.

the firms can access (e.g., the type of government software developed and its production process could also differ). We focus on our preferred proxy for data-richness in our subsequent empirical analyses, but results are qualitatively identical comparing public security and non-public security contracts instead.

In Figure 2, Panel B(a), we examine government software production. One can see that receipt of a data-rich public security contract is associated with differentially more government software production than receipt of a data-scarce public security contract. Suggesting a causal interpretation of the effect of a data-rich public security contract, we find no evidence of pre-contract differences in software production levels or trends. The inclusion of controls for time-varying effects of firm characteristics does not affect our findings. In Figure 2, Panel B(b), one sees that receipt of a data-rich public security contract is also associated with differentially more *commercial* software production than receipt of a data-scarce public security contract. Again supporting a causal interpretation, we find no evidence of pre-contract differences in software production levels or trends. The inclusion of controls for time-varying effects of firm characteristics has little effect on our findings. In terms of magnitudes, we see in Figure 2, Panel B, that receipt of a data-rich public security contract increases government software production by 2.9 and increases commercial software by 1.9 products over 3 years — on top of the effect of a data-scarce public security contract.³³

Interpretation As discussed in Section 3, the results presented above indicate economies of scope in AI innovation arising from government data being shared across commercial and government uses. In particular, the results imply that the benefits coming from access to government data outweigh any crowding-out of other resources from commercial software production, and that other sources of data (or other inputs, more generally) available in the private market must not be close substitutes for the government data firms are able to access. Importantly, our results are not merely capturing differentially less crowding out: we observe an overall positive effect of all types of government contracts on commercial software production, and differentially large effects of data-rich contracts (see Appendix Figure A.5).

The results presented thus far do not appear to be the result of differential selection by firms into data-rich contracts. First, we find no evidence of pre-contract differences in software production levels or trends, which one would expect if firms selected into data-rich government contracts as a function of their productivity trends. Second, by differenc-

³³We show the overall effects of data-rich and data-scarce public security contracts in Appendix Figure A.5. We plot the coefficients β_{2T} , describing software production around the time when a data-scarce public security contract was received, and the sum of the coefficients, $\beta_{1T} + \beta_{2T}$, describing software production around the time when a data-rich public security contract was received. We again find that government software and commercial software *both* significantly increase after receipt of *both* data-scarce and data-rich contracts, with effects being significantly greater in the latter.

ing out the effects of data-scarce contracts (either non-public security contracts or public security contracts in prefectures with below-median surveillance capacity), we account for time-varying selection into receiving either a government or public security contract. Third, by controlling for the time-varying effects of firms’ age and pre-contract software production, we address concerns about firms selecting into data-rich government contracts as a function of their potential production growth. Finally, by controlling for the time-varying effects of firms’ pre-contract capitalization, we account for selection into data-rich contracts on firms’ potential benefit from the capital provided by a government contract. We find evidence of economies of scope arising from government data even including this full range of controls. In Sections 5.2.2 and 5.2.3, we provide further evidence of the importance of government data.

Robustness Given the complex process of constructing our dataset, it is important to note that our findings are robust to varying several salient dimensions of our analysis. First, we assess the robustness of our results to the three key parameters of choice in the RNN algorithm that we use to categorize software — timestep, embedding, and nodes. We vary these three parameters, re-configure the RNN LSTM algorithm, re-categorize software, and re-estimate the baseline empirical specification. We find that these algorithm parameter choices have no impact on our results (see Appendix Table A.7). In addition, we evaluate the robustness of our results to adjustments of the LSTM classification threshold — the baseline specification sets the threshold as 50%. We re-categorize software using higher classification thresholds of 60% and 70%, and these adjustments have no impact on our results (see Appendix Table A.8). Next, we can vary the time-frame studied: we examine wider windows of time around the receipt of the first contract; and, we consider a balanced panel of firms within a narrow window (studying a balanced panel over too long a window substantially reduces the sample size). These changes have no impact on our findings (see Appendix Table A.9). Finally, we can vary the construction of the explanatory variable of interest, adjusting our classification of (data-rich) public security contracts to exclude any ambiguous government agencies (e.g., contracts with the government headquarters, and smart city management and administrative bureaux could be meant to provide security services just for the government office building). This, too, has no impact on our results (see Appendix Table A.10).

5.2.2 Additional evidence of the importance of data as an input

Our proposed mechanism of economies of scope arising from government data suggests that data-rich government contracts are more valuable to firms than data-scarce contracts. It is thus natural to test whether: (i) firms submit lower bids for data-rich contracts; and, (ii)

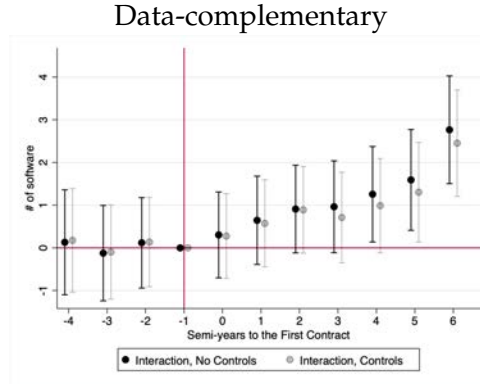


Figure 3: Differential data-complementary software development resulting from data-rich public security contracts, relative to data-scarce public security contracts, controlling for firm and time period fixed effects. Translucent lines/markers additionally interact pre-contract firm characteristics with a full set of time-period fixed effects.

more firms submit bids for data-rich contracts. While we do not have bidding information for all contracts, we use those contracts for which this information is available to estimate the relationship between bid values and local surveillance camera capacity at the time the contract was awarded, as well as the relationship between the number of bidders and local surveillance capacity. The patterns match what we expect (see Appendix Figure A.3): data-rich contracts are associated with lower bids — even controlling for bidding firm fixed effects (p-value = 0.13) — and with significantly more bidding firms (p-value = 0.05).

Under our proposed mechanism, firms receiving access to unprecedented quantities of data may need to develop tools to manage that data (e.g., software supporting data storage). We next test whether firms receiving data-rich contracts differentially produce data-complementary software. Importantly, these data-complementary software products are *distinct* from the AI software studied above. In Figure 3, we present estimates from the same specification as in Panel B of Figure 2, but now considering the outcome of data-complementary software products. One can see that the data-complementary software production *differentially* increases after the receipt of a data-rich public security contract.³⁴ We find no evidence of pre-contract differences in data-complementary software production levels or trends, suggesting a causal effect of data-rich public security contracts.³⁵

Our proposed mechanism suggests that access to government data will not only in-

³⁴We plot the coefficients β_{2T} , describing data-complementary software production around the time when a data-scarce public security contract was received, and the sum of the coefficients, $\beta_{1T} + \beta_{2T}$, describing data-complementary software production around the time when a data-rich public security contract was received, in Appendix Figure A.7. We find that data-complementary software increases after receipt of *both* data-scarce and data-rich contracts, with effects being significantly greater in the latter.

³⁵The production of data-complementary software can be seen as an alternative empirical proxy for firms' receiving access to particularly large quantities of data. Analogous to our previous comparison between high and low surveillance capacity public security contracts, one would expect differentially more government and commercial AI software production among firms that produced data-complementary software after receiving a public security contract. In Appendix Figure A.8, one can see that public security contracts that led to data-complementary software production within the first year of the contracts were associated with differentially more government *and* commercial software production. Again we find no evidence of pre-contract differences in software production levels or trends.

crease the quantity of software production, but also the quality. While we cannot directly observe differences in the quality of software produced as a result of receiving access to more government data, we can test whether data-rich contracts lead to increased production of the most demanding form of facial recognition AI: that using video. Indeed, we find significantly greater video facial recognition AI software production following receipt of a data-rich contract (see Appendix Figure A.6).³⁶

A final set of tests arises from an examination of firms that produced video facial recognition AI software for the government following receipt of a public security contract: this software is the most data-intensive facial recognition AI software, presumably requiring access to the greatest quantity of government data.³⁷ We examine whether these firms also differentially produce more government and commercial software after receiving a data-rich public security contract. One can see in Appendix Figure A.9 that indeed they do. Moreover, we note that the magnitudes of the coefficients when considering the post-contract production of government video AI as a proxy for the data-richness of the contract are nearly double those using our other proxies, consistent with the idea that video AI software is particularly data-intensive.

A range of tests, exploiting multiple margins of variation in access to government data, all point in the same direction: contracts providing access to more government data allow firms to produce more government and commercial software. Beyond other mechanisms through which contracts may affect output, access to government data plays a crucial role.

5.2.3 Evaluating alternative hypotheses

While a range of analyses suggest an important role for economies of scope arising from access to government data in shaping firms' production of AI software, it is important to consider alternative mechanisms, including alternative sources of economies of scope. For a parsimonious presentation of the varied empirical exercises to come, we plot regression coefficients and confidence intervals only for differential effects of data-rich contracts 3 years following contract receipt, in Figure 4. The figure plots these estimates specification-by-specification for a wide range of specifications. We also present more complete sets of coefficient estimates in tables provided in the Appendix.

Differences in the terms and tasks under data-rich contracts One naturally wonders whether firms receiving data-rich public security contracts are engaged in similar work to firms receiving data-scarce public security contracts. We first examine whether differences

³⁶This suggests a potential bias of technical change toward video facial recognition AI *within* the broader category of facial recognition AI technology.

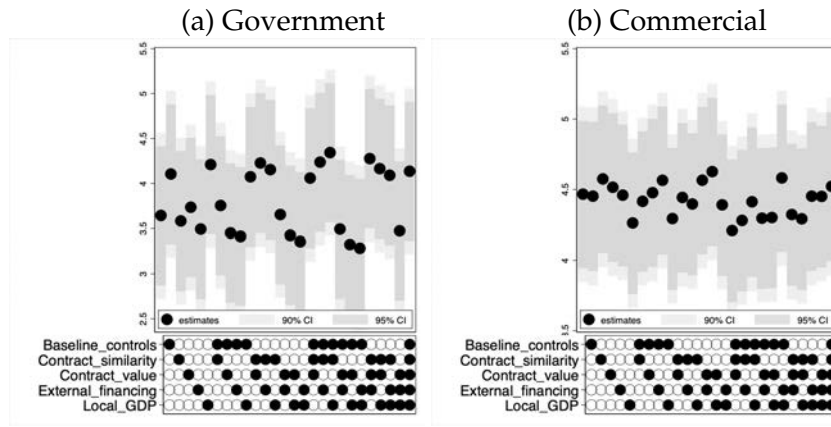
³⁷Firms that produce video facial recognition AI for the government after receiving a data-rich public security contract also differentially produce more data-complementary software post-contract. See Appendix Figure A.9.

in contractual terms may play a role in generating our results. To quantify the content of each public security contract (high or low capacity), we calculate the vector distance between the language of each public security contract in our dataset and a random sample of 500 non-public security contracts using Bidirectional Encoder Representations from Transformers (BERT; Devlin et al., 2018). We control for this contract-specific distance measure interacted with time period fixed effects, and find that it cannot fully explain our results (see Figure 4 and Table A.11, Panel B).

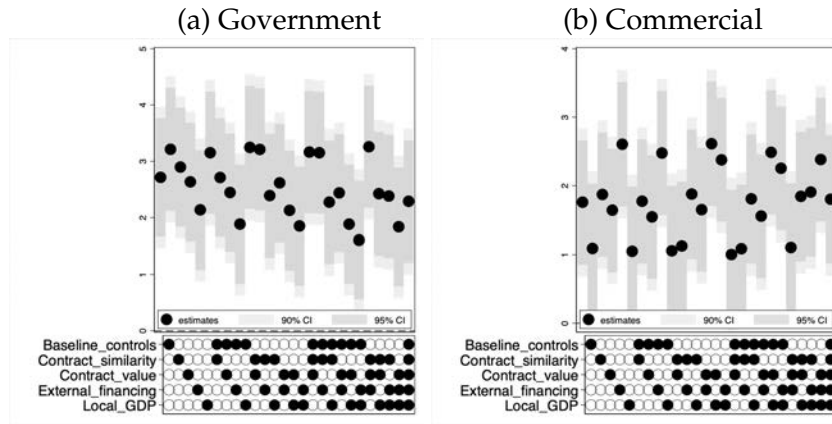
We next compare the registered descriptions of firms' government software produced immediately following receipt of a data-rich or data-scarce public security contract. To quantify the content of each government software product description, we calculate the vector distance between the language of the government software descriptions and a random sample of 500 commercial software product descriptions, again using BERT. We test whether receipt of a data-rich contract differentially affects the government software produced by a firm (relative to receipt of a data-scarce contract); we find a very tight null result (government software descriptions change by around 1% of a standard deviation, with a p-value of 0.89). These results suggest that our findings are not driven by differences in the content of government software produced under data-rich and data-scarce contracts.

Learning by doing It is possible that data-rich contracts generate more AI software not because of the data they provide, but because of firms' opportunities for learning by doing under these contracts. Two pieces of evidence suggest that learning by doing is not driving our main results. First, while learning by doing may certainly be important in explaining the overall effects of contracts on software production, for it to explain our *differential* effects between data-rich and data-scarce contracts, it would have to be that the potential for learning was positively correlated with data-richness. This may be more of a concern when we compare public and non-public security contracts, since the production processes for the associated government software may be different. Yet, for our preferred comparison within the set of public security contracts, we view such positive correlation as much less likely. In fact, we have shown above that the description of government software produced following the receipt of a data-rich public security contract is very similar to the software produced after the receipt of a data-scarce one, suggesting that the underlying production processes should be similar as well.

Second, the possibility of learning by doing should presumably be stronger for firms with lower levels of production prior to the receipt of a contract. The time-varying control for pre-contract software production in the specification with controls (estimated above) allows us to (imperfectly) account for this. In addition, we estimate our baseline specification, but now including pre-contract government software production, or software production in the corresponding category, or software production in the opposite category



Panel A: Public security vs. non-public security contracts



Panel B: Public security contracts with high vs. low surveillance capacity prefectures

Figure 4: Panel A: baseline results presented in Appendix Table A.5, adding various controls. Software development intended for government (left, (a)) and commercial (right, (b)) relative to the time of receiving initial procurement contract, controlling for firm and time period fixed effects. Coefficient on the interaction for public security contracts 3 years after contract receipt is presented. Panel B: baseline results presented in Appendix Table A.6, adding various controls. Software development intended for government (left, (a)) and commercial (right, (b)) relative to the time of receiving initial procurement contract, controlling for firm and time period fixed effects. Coefficient on the interaction for high surveillance capacity 3 years after contract receipt is presented. Solid dots indicate coefficients that are significant at the 10% level or better.

(e.g., controlling for government software production when examining commercial software production as outcomes). If learning by doing was the main driver our findings, then controlling for pre-contract software production in these sub-categories should substantially decrease the estimated impact of receiving a data-rich contract. We instead find that controlling for pre-contract sub-category software production only slightly reduces the estimated effect of a data-rich contract, which remains quantitatively large and statistically significant (see Appendix Table A.12).

Government contracts as sources of capital Another important consideration is that contracts may affect firms' software production through the provision of capital. We at-

tempted to account for this channel above by differencing out the impact of “data-scarce” contracts and by controlling for the time-varying effects of firms’ pre-contract capitalization, but we can also address this concern in two other ways. First, we can directly control for the monetary value of the contract interacted with time period fixed effects (formally $\sum_T T_{it} value_i$). We add these interactions to our baseline specification and find that they do not affect our results (see Figure 4 and Appendix Table A.11, Panel C). Second, we add to our baseline specification interactions between a firm’s pre-contract amount of external financing and the full set of time period fixed effects (formally $\sum_T T_{it} \times financing_i$). Again, adding this set of controls has no impact on our results (see Figure 4 and Appendix Table A.11, Panel D).

Government contracts as signals It is also possible that receipt of a data-rich contract may function as a signal of firm quality or potential: perhaps firms receiving a government contract receive additional benefits from local industrial policy, or attract additional external funding, human capital, or customers, all of which contribute to the production of software. To test whether the signaling value of data-rich contracts accounts for our findings, we first examine the effects of a firm’s first contract, but limiting our analysis to subsidiary firms belonging to a mother firm that has *already* received a government contract through a different subsidiary. Arguably, the signaling value of these first contracts should be lower (mother firm quality is already observed), while access to data remains potentially extremely valuable. In Appendix Table A.13, Panel B, one can see that within this sample of first contracts there is still a significant differential effect of receiving a data-rich contract on both government and commercial software production.

As an alternative approach, we can examine the effects of firms’ own *second* public security contracts: again, signaling effects should be much smaller for these contracts, but they should still provide access to valuable data. When we estimate our baseline specification, examining software production around the time of receiving a second contract, we continue to find significant effects of receiving a data-rich contract on government and commercial software production (see Appendix Table A.13, Panel C).

Different commercial opportunities associated with data-rich contracts A last important set of concerns is that contracts with governments in prefectures with high surveillance capacity may offer different commercial opportunities for reasons other than the additional data to which firms gain access. First, high-surveillance prefectures may also be richer commercial markets; a contract with a local government in a richer prefecture could affect software production. To evaluate this possibility, we control for the GDP per capita of the administrative unit where a firm’s first government contract was issued, interacted with time period fixed effects (formally $\sum_T T_{it} \times market_i$). Adding these interactions to our

baseline specification does not affect our results (see Figure 4 and Appendix Table A.11, Panel E). A second possibility is that contracts with two very specific high-surveillance prefectures may disproportionately affect our results: Beijing and Shanghai. Contracts with these powerful local governments may offer a range of political and economic opportunities that go beyond access to data. To rule out the possibility that our findings are distorted by contracts with these two local governments, we estimate our baseline specification, but excluding contracts with Beijing and Shanghai governments. Our findings are qualitatively unchanged (see Appendix Table A.14, Panel B). A third possibility is that contracts with a firm’s home-province government may give the firm some commercial advantage, beyond the effects of data. To rule this out, we estimate our baseline model, but excluding contracts signed between firms and any government in their home province. We again find that our results are unaffected (see Appendix Table A.14, Panel C).

Our empirical results thus paint a clear picture: after receiving government contracts that provide them with greater access to government data, firms are able to use that data to develop not only government software products, but also commercial software products. This is possible due to the economies of scope arising from government data, rather than other mechanisms. We next explore the macroeconomic implications of these findings.

6 Macroeconomic implications of firms’ access to government data

In our empirical analysis of Section 5, we have observed some of the firm-level consequences of access to government data: an increase in government data available to firms increases their data-intensive innovation. However, this evidence does not imply that such policy will shift the *aggregate* direction of innovation or the economy’s growth rate. There are two main reasons why the microeconomic and macroeconomic implications may diverge. The first is that increases in innovation by firms accessing government data may crowd-out resources from other innovating firms. The second is that, in general equilibrium, relative prices may change, thus affecting innovation as well. Moreover, even if the economy’s growth rate did increase, it would not necessarily imply that increasing firms’ access to government data would increase welfare. A higher consumption *growth rate* is offset by a lower *level* of consumption due to crowding-out of resources by innovation and government data production.

Thus, in this section, we examine how access to government data affects the direction of innovation, growth, and welfare in data-intensive economies, with these considerations taken into account. We start by building a directed technical change model (Acemoglu, 2002) with data as an input, where we incorporate the economies of scope implied by our evidence. We present the environment and characterize a balanced-growth path equilib-

rium in Section 6.1; we then discuss both positive and normative macroeconomic implications of government data provision in Section 6.2.

6.1 A directed technical change model with economies of scope from data

Model overview We model an economy in which firms innovate to develop and supply differentiated varieties of government and commercial (private) software — which require data in production — as well as other, non-software, varieties — which do not. Commercial software and non-software varieties are intermediate inputs into the production of a final good. A representative household consumes the final good and owns all firms. Government software varieties are purchased by the state as intermediate inputs to produce a government good. To be concrete, and to link the model to our empirical setting, we refer to this government good as “surveillance.”

As in Section 3, we assume that government data can be shared across uses within the firm. Specifically, government data is necessary for producing government software and the same data can simultaneously be used for producing commercial software — where it is not necessary and is instead a gross substitute with private data. Government data is supplied by the state and is produced as a by-product of surveillance. Private data is supplied by a representative firm as a by-product of all private transactions in the economy as measured by total output of the final good.³⁸ Furthermore, while both types of data are excludable, we assume that only private data can be purchased in the market. In contrast, as in Section 3, government data can only be accessed by obtaining a contract for producing government software varieties for the state.

The state chooses a policy that involves: a level of expenditures on surveillance (which determines the amount of government data produced), an amount of government data supplied to firms that obtain a contract to produce government software varieties, and the levels of lump sum taxes of, and transfers to, households. Given a state policy, potential entrants can choose to innovate on and supply new varieties of government software, commercial software, both types of software, or only non-software varieties. Firms will innovate and enter such that, in a balanced growth path equilibrium, all sectors grow at the same rate, and profits are equalized across sectors. We next describe this economy formally.

Goods production Consider an economy with three intermediate good sectors producing: commercial (private) software Y_c , government software Y_g , and other non-software

³⁸This corresponds, for instance, to information collected from consumers when performing online transactions. It is worth noting that, by giving the rights to selling private data to a representative firm owned by the representative household, we are ignoring a number of interesting issues regarding how to allocate property rights between firms and consumers whose transactions generate data as a by-product.

products Y_z . Within each sector i , there is a measure N_i of differentiated product varieties j of quality $q_i(j)$. A representative sectoral firm has production technology:

$$Y_i = \frac{1}{1 - \frac{1}{\chi}} \int_0^{N_i} q_i(j)^{1 - \frac{1}{\chi}} dj. \quad (1)$$

We assume the firm is competitive and maximizes static profits taking sectoral prices p_i and product variety prices $p_i(j)$ as given. This gives inverse demand schedules:

$$p_i(j) = p_i q_i(j)^{-\frac{1}{\chi}}. \quad (2)$$

A representative firm then combines private software and non-software to produce a final good Y using a CES aggregator:

$$Y = \left[a Y_z^{\frac{\epsilon-1}{\epsilon}} + (1-a) Y_c^{\frac{\epsilon-1}{\epsilon}} \right]^{\frac{\epsilon}{\epsilon-1}}. \quad (3)$$

We again assume the firm is competitive and maximizes static profits given sectoral prices p_c and p_z , and the price of Y which we normalize to 1. This implies that prices satisfy:

$$1 = \left((a)^\epsilon (p_z)^{1-\epsilon} + (1-a)^\epsilon (p_c)^{1-\epsilon} \right)^{\frac{1}{1-\epsilon}}. \quad (4)$$

Innovators A software variety j is supplied by a monopolist “innovator.” As in Section 3, we assume that producing software of a higher quality is data-intensive.³⁹ Dropping the j index for notational convenience, government software production uses government data d_g and intermediate goods x_g to produce a variety of quality q_g . Commercial software production uses both government and private data, d_g and d_p , as well as intermediates x_c to produce a variety of quality q_c .

Specifically, we assume that the firms may produce government and commercial software using the following technologies (a special case of those in introduced in Section 3):

$$q_g(d_g, x_g) = (d_g)^\beta x_g^{1-\beta} \quad (5)$$

$$q_c(d_g, d_p, x_c) = \left(\alpha d_g^{\frac{\gamma-1}{\gamma}} + (1-\alpha) d_p^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \beta} x_c^{1-\beta}, \quad (6)$$

where $\alpha < 1$ governs the relative productivity of government vis-à-vis private data, and $\gamma > 1$ describes their gross substitutability in commercial software production.⁴⁰ With this specification, α is a key parameter governing the strength of economies of scope generated by government data.

³⁹For example, one measure of quality of AI facial recognition software is prediction accuracy. This is higher when larger datasets are used in training the AI algorithms.

⁴⁰The assumption of gross substitutability is important because, as will be seen below, it allows innovators to produce commercial software even without access to government data.

Next, we consider the profit maximization problem for a software variety of quality q . We assume that private data can be purchased in the market at price p_d . Moreover, we assume that intermediate goods x_g, x_c cost ϕ units of the final consumption good (whose price is normalized to 1) and that all product varieties never depreciate.⁴¹

These assumptions, together with demand schedules for a variety having constant elasticity χ imply that, for any sectoral price p_i and government data d_g , the flow of profits from a variety are:

$$\Pi_g(d_g, p_g) = \max_{x_g} p_g q_g(d_g, x_g)^{1-\frac{1}{\chi}} - \phi x_g \quad (7)$$

$$\Pi_c(d_g, p_c, p_d) = \max_{x_c, d_p} p_c q_c(d_g, d_p, x_c)^{1-\frac{1}{\chi}} - \phi x_c - p_d d_p, \quad (8)$$

and the corresponding input demand schedules are $d_p(d_g, p_c, p_d), x_c(d_g, p_c, p_d), x_g(d_g, p_g)$.

Next, we describe how new varieties are introduced. We assume that innovators can invest 1 unit of the final consumption good in R&D in order to produce μ_i new varieties in sector i — thus becoming the monopolist supplier of those varieties forever. Then, given total R&D spending R_i for sector i , new varieties accumulate according to:

$$\dot{N}_i = \mu_i R_i \quad (9)$$

The entry decision is somewhat nuanced due to the fact that government data can be shared across uses and that there is no market for such data. We assume the following sequence of events takes place. A software innovator can first decide whether to attempt to obtain a government contract or not by paying a cost F . If the innovator decides not to make an attempt, it can choose to introduce a new commercial software variety without access to government data ($d_g = 0$). If it decides to make an attempt, it obtains a government contract with probability λ . The contract commits the innovator to produce a new government software variety and provides the innovator with access to a fixed quantity of government data \bar{d}_g . The innovator can then choose to also introduce a new commercial software variety using government data in its production. Finally, if the innovator does not obtain the government contract, it can again choose to introduce a new commercial software variety without access to government data.

We consider a balanced growth path with constant interest rate r where there is free-entry of innovators. This implies that the expected present discounted value of profits net of the unit cost of R&D investment must be zero for both government and commercial software variety innovators. Given the assumptions above and setting $\mu_g = \mu_c = 1$, a balanced growth path equilibrium where both types of software producing firms are present requires:

⁴¹As in Acemoglu (2002), if varieties depreciate slowly, this would not change the balanced-growth path equilibrium — which will be our focus — but only the transitional dynamics.

$$F = \lambda \left(\frac{\Pi_g(\bar{d}_g, p_g)}{r} - 1 + \max \left\{ \frac{\Pi_c(\bar{d}_g, p_c, p_d)}{r} - 1, 0 \right\} \right) + (1 - \lambda) \max \left\{ \frac{\Pi_c(0, p_c, p_d)}{r} - 1, 0 \right\} \quad (10)$$

$$1 = \frac{\Pi_c(0, p_c, p_d)}{r} \quad (11)$$

Finally, for non-software innovators which do not require data as an input, the R&D investment yields new varieties with quality $q_z = x_z^{1-\beta}$, where x_z is again intermediate goods. This results in profits:

$$\Pi_z(p_z) = \max_{x_z} p_z q_z^{1-\frac{1}{\lambda}} - \phi x_z. \quad (12)$$

The free-entry condition for non-software innovators is then:

$$1 = \mu_z \frac{\Pi_z(p_z)}{r}. \quad (13)$$

Representative household We assume the existence of a representative household with CRRA flow utility $u(C) = \frac{C^{1-\theta}}{1-\theta}$, where C is consumption of final goods and θ is the inverse of the intertemporal elasticity of substitution. Then, given discount rate ρ , the present discounted utility is:

$$\int_0^\infty e^{-\rho t} u(C_t) dt \quad (14)$$

The household maximizes utility subject to the budget constraint:

$$C_t + \dot{A}_t \leq A_t r_t + \Pi_t - T_t, \quad (15)$$

where A_t are assets, Π_t are profits coming from all firms, and T_t are government taxes.

Data supply and the state The state purchases the government software aggregate Y_g at price p_g in order produce surveillance G with linear technology $G = Y_g$. Moreover, it sets lump sum taxes T on households such that budget balance holds at each point in time:

$$p_g G = T. \quad (16)$$

Aggregate government data D_g is produced as a by-product of government surveillance: specifically, one unit of surveillance, G , produces κ_g units of government data.⁴² Then, given a measure N_g of government software innovators and a dataset available to them \bar{d}_g , we have that:

$$N_g \bar{d}_g = D_g = \kappa_g G. \quad (17)$$

We assume that government data is not sharable *across* firms: this can correspond to a local

⁴²In our empirical context, this government data could correspond, for example, to the video feed from street cameras or individual administrative records. These are themselves produced as a consequence of the surveillance and other activities of governments.

government collecting its own surveillance data and contracting with a specific firm to analyze it, thus restricting its use to that firm. Allowing government data to be sharable across firms would magnify the importance of government data; by assuming non-sharable government data, we are able to focus on the positive and normative implications of the sharability of government data across uses *within* a firm (the consequences of non-rival private data across firms have been studied by, e.g., Jones and Tonetti, 2018).

We are now ready to formally define a state policy. Because we will consider a balanced growth path, we find it more useful to define the policy in terms of variables that are stationary. In particular, we divide the level of government software expenditures for surveillance and lump sum taxes by the level of private output. Then,

Definition 1 (State policy) *A state policy is a dataset available to government software innovators \bar{d}_g , government software expenditures for surveillance purposes relative to final good output $p_g G/Y$, and lump sum taxes relative to final good output T/Y that satisfy equations (16) and (17).*

Finally, we complete the description of the economy's environment with the production of private data. A representative firm produces D_p by "mining" data out of private transactions as measured by total private output Y .⁴³ Suppose it can mine $\kappa_p Y$ units of data out of Y , then the supply of private data is:⁴⁴

$$D_p = \kappa_p Y. \quad (18)$$

Equilibrium We now consider a balanced growth path equilibrium (BGP) where all variables grow at constant rate η . We denote by: \tilde{N}_c the total number of commercial software varieties produced by firms without a government contract, N_g the number produced by firms with a government contract (which is also the number of government software varieties), and N_z the number of non-software varieties.⁴⁵

Definition 2 (BGP Equilibrium) *Given a state policy $\{\bar{d}_g, p_g G/Y, T/Y\}$, a balanced-growth path equilibrium is a set of prices $\{p_c, p_z, p_g, p_d, r\}$, relative varieties \tilde{N}_c/N_z and N_g/N_z , and growth rate η such that firms and households are optimizing, there is free-entry of innovators, and all markets clear.*

⁴³In reality, private data production (and government data production) would involve the use of other intermediate inputs. We have explored this and found that it does not meaningfully change our analysis.

⁴⁴Note that this firm will be making positive profits in equilibrium, which are then redistributed to the households. One interpretation of these profits is that they are rents from ownership of a fixed factor that is needed in order to mine private data. For example, in reality, the fixed factor could be the "land" on which data centers are built.

⁴⁵We denote by \tilde{N}_c the *subset* of commercial software varieties produced by firms using *only* private data; we reserve the notation N_c to capture all types of commercial software varieties (as discussed below).

Because we endogeneize the production of data and new software varieties, it is possible that, for some parameterizations, no BGP equilibrium exists with entry of both types of software firms: i.e., those producing commercial software alone and those producing both government and the commercial software.⁴⁶ Proposition 1 in Appendix A.1 lays out sufficient conditions for a BGP to exist and be unique where all types of firms are present.

We now formally define two objects that will be of interest in the next section. The first is the economy's BGP growth rate η , which equals the rate of innovation in any sector i :

$$\eta = \frac{\dot{N}_i}{N_i}. \quad (19)$$

The second is the bias of private innovation towards data-intensive software, which we define as commercial software varieties relative to non-software varieties along the BGP:

$$n_c = \frac{N_c}{N_z}, \quad (20)$$

where N_c is an output-weighted average of commercial software varieties $N_c \equiv \tilde{N}_c \omega + N_g(1 - \omega)$, with $\omega = \frac{q_c(0, p_c, d_p)^{1-\frac{1}{\chi}}}{q_c(0, p_c, d_p)^{1-\frac{1}{\chi}} + q_c(\bar{d}_g, p_c, d_p)^{1-\frac{1}{\chi}}}$.

6.2 The effects of government data provision on innovation and welfare

Using the model of data-intensive technical change, we now focus on two questions, one positive and one normative: first, how does government data provision affect the rate and direction of innovation? Second, how does government data provision affect welfare?

How does government data provision affect the rate and direction of innovation? The next theorem shows the conditions under which policies that directly provide more government data to innovating firms increase the economy's growth rate and bias the direction of private innovation towards data-intensive software.

Theorem 1 (Government data provision and innovation) *Assume the sufficient conditions in Proposition 1 for a unique BGP equilibrium to exist hold. Then, an increase in government data provided to firms (\bar{d}_g) will increase the rate of innovation (η). Moreover, if $\epsilon \geq \frac{\chi + \beta(\chi - 1)}{1 + \beta(\chi - 1)}$, it will also bias private innovation towards data-intensive software (increase n_c).*

Proof. See Appendix A.2. ■

Beyond the formal proof, we also provide an intuitive discussion of the theorem in Appendix A.2. In brief, the higher profits earned by firms using government data will drive

⁴⁶This is the empirically relevant equilibrium: most AI firms produce commercial software *without* access to government data.

up the return on investment (r) under free-entry and, therefore, induce higher R&D spending and increase the rate of innovation on the BGP. Moreover, in equilibrium, innovators must be indifferent among developing software varieties using government data, developing commercial software without using government data, and developing non-software varieties. The necessary price adjustments for such indifference imply that commercial software sells at lower prices in the new equilibrium. If relative demand is sufficiently elastic ($\epsilon \geq \frac{\chi+\beta(\chi-1)}{1+\beta(\chi-1)}$), this implies that the new entry of commercial software innovators will be sufficient to bias private innovation towards data-intensive software.

Finally, we establish an equivalence between state policy choices which anticipates some of the results in Section 7: the indirect effects of a state's choice of surveillance levels and data collection will, in a BGP, be analogous to the direct effects of government data provision. A proof is provided in Supplementary Material B.1.

Remark 1 *In a BGP equilibrium, the consequences of an increase in \bar{d}_g are equivalent to those arising from an increase in surveillance spending $p_g G/Y$ or aggregate government data D_g/Y as a share of final good output.*

How does government data provision affect welfare? We showed above that increases in \bar{d}_g can lead to a higher growth rate η . Yet, there is no reason for the state to increase η *per se*. The appropriate objective for a benevolent state is to maximize household utility. Assuming $\rho - \eta(1 - \theta) > 0$ on a BGP (i.e., utility is bounded), the present discounted utility of the representative household is (aside from the initial level of output which we normalize to 1):

$$U = \frac{1}{1 - \theta} \left(\frac{C}{Y} \right)^{1 - \theta} \frac{1}{\rho - \eta(1 - \theta)}.$$

The increase in η leads to a direct positive effect on welfare, since the growth rate of consumption is higher. But, from the aggregate resource constraint (shown below), we see that there are two forces that may *offset* such increase by decreasing the consumption to output ratio $\frac{C}{Y}$ (and therefore welfare) following an increase in \bar{d}_g :

$$\frac{C}{Y} = 1 - \underbrace{\left(\left(2 + \frac{F}{\lambda} \right) \frac{\dot{N}_g}{Y} + \frac{\dot{N}_c}{Y} + \frac{1}{\mu_z} \frac{\dot{N}_z}{Y} \right)}_{\text{Resources used in innovation}} - \underbrace{\frac{\chi - 1}{\chi} (1 - \beta) \left(1 + \frac{p_g G}{Y} \right)}_{\text{Resources used in production}}.$$

First, the crowding-out of resources from consumption that are used instead for creating new varieties (i.e., innovation). Second, the crowding-out of resources from consumption that are used instead as intermediates for producing government surveillance.

Given this discussion, we next consider a second-best problem where the government

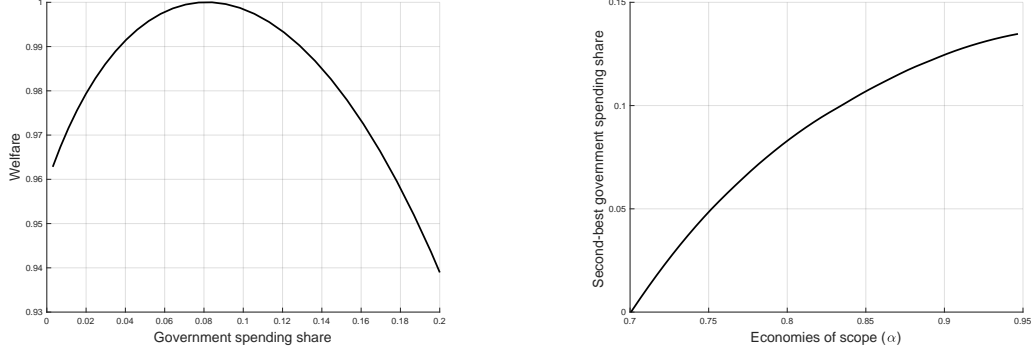


Figure 5: Left panel: government data provision and welfare; Right panel: Economies of scope and second-best government data provision.

chooses the level of government data provision to maximize household welfare.⁴⁷ Figure 5 shows how welfare changes when the share of government spending in total output $\frac{p_g G}{Y + p_g G}$ changes. These changes are brought about by different levels of government data provision \bar{d}_g . We report welfare in consumption equivalent units relative to the maximum attainable welfare. To make the analysis transparent, the benchmark parameterization underlying the figure is such that: (i) the economy is symmetric in the sense that the direction of innovation is unbiased ($\frac{\tilde{N}_c}{\tilde{N}_z} = \frac{N_g}{N_z} = 1$), all sectors have an identical share ($\frac{p_c Y_c}{Y + p_g G} = \frac{p_z Y_z}{Y + p_g G} = \frac{p_g G}{Y + p_g G} = 1/3$), and private and government data are identical ($\bar{d}_g = d_p(\bar{d}_g, p_c, p_d)$); and, (ii) economies of scope (as governed by α) are consistent with our benchmark estimates from the empirical section (to be precise, the relative elasticity of commercial to government software production of around two-thirds implies $\alpha = 0.82$).⁴⁸ Then, we vary the level of government data provision \bar{d}_g from this benchmark parameterization, keeping all other parameters fixed.

In Figure 5, left panel, one sees that, given our parameterization of the model, the second-best government data provision results in a government spending share of 8%. Moreover, one can see that deviations from this second-best can be rather costly. For example, when government data is relatively scarce and the government spending share is only 2%, then welfare is about 2% lower in consumption equivalent units. The reason is that the growth rate η is lower, and this is not sufficiently compensated by a reduction in the crowding-out of resources from consumption by innovation. The opposite is true when government data provision is too generous: in that case, there is significant crowding-out that outweighs the increase in η .

These results beg the question as to what determines the welfare maximizing government data provision. Is it always the case that an interior solution exists? Or, would it sometimes be optimal for the state not to provide government data because the increase in the economy's growth rate is not sufficient to compensate for the crowding out of re-

⁴⁷It is a second-best problem because of distortions coming from the monopoly power of innovators in the decentralized equilibrium.

⁴⁸See Supplementary Material B.3 for a more detailed description of the calibration.

sources? To answer this, Figure 5, right panel, shows how the welfare maximizing government spending share ($\frac{p_g G}{Y + p_g G}$) changes as economies of scope become stronger (as governed by α). We find that when α is below 0.7 then it is never optimal for the state to supply government data. Therefore, when economies of scope are sufficiently low, the second-best BGP equilibrium would only feature the production of commercial software using private data alone, and no production of government software or surveillance. As economies of scope become greater, so does the second-best government spending share, because a higher level of government data provision to firms causes larger changes in the economy's growth rate which compensate for the crowding out of resources from consumption. In fact, when economies of scope are sufficiently strong, the state would optimally choose to provide such a high level of government data that the only software producing firms that exist in a BGP are those that produce both government and commercial software.

7 Roles of the state in data-intensive economies

In this section, we present three applications which illustrate the varied ways that data-intensive innovation may be shaped by the state, both directly and indirectly. Specifically, we show that: (i) industrial policy in the form of government data provision can be justified on different grounds from traditional industrial policy; (ii) surveillance states' interest in monitoring and controlling their citizens is aligned with promoting data-intensive innovation and growth but may reduce citizen welfare; and, (iii) regulation limiting government data collection due to privacy concerns will reduce data-intensive innovation and growth but may increase welfare.

7.1 States' choice of industrial policy

Traditional forms of industrial policy entail giving direct production subsidies to a sector or subsidizing a key input. The stated goal of such policies is often to shift the relative size of sectors (and/or the direction of innovation) to correct for market failures. Alternatively, states sometimes directly provide key inputs that are used by private firms. These include, for example, infrastructure — such as transportation, water, or electric power — as well as public services that increase worker productivity — such as education or health.⁴⁹

Our evidence and model suggest another justification for industrial policy in the age of data-intensive innovation. Because states are key collectors of data and government data gives rise to economies of scope, in Section 6.2 we have shown that it may be optimal to directly provide such data to data-intensive software producers when they contract with

⁴⁹For example, see Barro (1990) for a canonical endogenous growth model with government provided goods as an input in production.

the government. The justification is even stronger when government services that produce data as a by-product (like surveillance in our model) are also directly valued by either the state or households.⁵⁰

Our model also suggests sources of variation in second-best policy choices that are particularly salient in data-intensive economies. The consequences of variation in economies of scope (e.g., due to the sectoral composition of an economy) have already been shown in Figure 5. In addition, the availability of good substitutes for government data and the productivity of data production can all determine whether government provision of data to firms should be larger or smaller (or even non-existent). Differences in production technologies can thus have large effects on second-best industrial policies.

Finally, we note that, even without intending to do so, different state policies may also have important industrial policy components. This echoes the argument of Rodrik (2007) that all policies, whether intended or not, can be considered as industrial policies. Our second and third applications present two such instances: the state's demand for surveillance to monitor the population, or regulations on government data collection or data sharing due privacy concerns will have important industrial policy components despite being pursued with very different objectives.

7.2 States' choice of surveillance level

All states engage in citizen monitoring for the preservation of public security, potentially generating massive surveillance datasets. At the extreme are autocratic states that aim to monitor and control their populations to maintain power (Guriev and Treisman, 2019). In the modern world, this need to monitor is likely to produce substantially greater data collection and data analysis — particularly using AI. Indeed, AI has been described by the *Wall Street Journal* as part of the autocrat's new tool kit, "A sophisticated new set of technological tools ... that will allow strongmen and police states to bolster their internal grip, undermine basic rights and spread illiberal practices beyond their own borders."⁵¹ China is one prototypical example of this phenomenon, leading the world in surveillance capacity: there will be around 560 million public surveillance cameras installed in China by 2021, versus approximately 85 million in the US.⁵²

⁵⁰Note that this logic is not limited to the Chinese context. For example, in the US, *Wired* writes that "the Pentagon believes AI has matured enough to become a central plank of America's national security ... The plan depends on the Pentagon working closely with the tech industry to source the algorithms and cloud computing power needed to run AI projects. Federal contracting records indicate that Google, Oracle, IBM, and SAP have signaled interest in working on future Defense Department AI projects." See <https://www.wired.com/story/pentagon-doubles-down-ai-wants-help-big-tech/>, last accessed March 25, 2020.

⁵¹The *Wall Street Journal* article is: "The Autocrat's New Tool Kit," by Richard Fontaine and Kara Frederick, March 15, 2019. Available online at: <https://on.wsj.com/2H1sIgu>, last accessed August 7, 2019.

⁵²Source: IHS Markit Technology Report, described by the *Wall Street Journal*, <https://on.wsj.com/2U0uuIJ>, last accessed on June 16, 2020. More generally, many democratic states have also expanded their

Our model and empirical results suggest a potential alignment between surveillance states and data-intensive innovation. Greater purchases of government software and surveillance production will not only increase the state’s political control, but also produce the government data (as a by-product) that fuels data-intensive innovation.

We consider an extension of our model where the flow utility is:

$$u(C) + \delta G. \quad (21)$$

This captures the social welfare function of a state that values both household utility and also G directly. For example, $\delta > 0$ can capture an autocratic state wanting higher G to better monitor the population or, alternatively, a representative household that cares about security provided by the government in democracies facing security threats.⁵³ Differences in δ across states will result in differences in government spending and, as a result, in growth rates and the bias of private innovation.

More concretely, consider the following thought experiment. Imagine that the only differences between the US and Chinese economies was their δ . Moreover, imagine that this fully explains why government spending on domestic security was 40% lower in the US than China in 2018.⁵⁴ We assume that the symmetric economy associated with our benchmark calibration was China. Holding all else fixed, we ask: what are the consequences of decreasing government surveillance ($\frac{p_s G}{Y + p_s G}$) by 40% in our model? We find that the annual growth rate (η) decreases from the benchmark 6% to 4.7% and that the bias of innovation (n_c) decreases from the benchmark 1 to 0.84.

These results show that surveillance states’ preferences for monitoring and controlling their population may result in an inherent advantage in data-intensive innovation by expanding surveillance spending and the provision of government data. While a previous literature (discussed in Section 2) has pointed out that more autocratic regimes may impose a “tax” on private innovation through the hold up or expropriation of entrepreneurs, our findings suggest that this autocratic tax may be offset by surveillance states’ advantage in data-intensive innovation. Note, however, that optimal government data provision to firms and surveillance levels chosen by the *state* could be very different from those preferred by *citizens* — states and citizens may have different values of δ . Thus, the state’s choice of large quantities of surveillance G may promote data-intensive innovation and

surveillance capacities, e.g., the United States since the enactment of the USA PATRIOT Act of 2001.

⁵³Even selfish autocrats may value $u(C)$ when the probability of sustaining political power increases with household utility.

⁵⁴US spending was 0.8% of GDP vis a vis 1.32% of GDP for China. Sources: “USA Spending.gov”, https://www.usaspending.gov/#/explorer/budget_function, last accessed on April 21, 2020 and “Keynote Speech by H.E. Liu Xiaoming, Chinese Ambassador to the UK, at the Meeting with the Defence Correspondents’ Association”, https://www.fmprc.gov.cn/mfa_eng/wjb_663304/zwjg_665342/zwbd_665378/t1695061.shtml, last accessed on April 21, 2020.

growth, but significantly reduce citizen welfare through violations of civil liberties.

7.3 States' choice of privacy protection

States not only collect and hold data, but also regulate the collection and exchange thereof. This regulation will — especially in democracies — often reflect citizen norms regarding privacy; personal data in particular have an element of “repugnance” (Roth, 2007), with many individuals expressing discomfort when private data — especially government data — are collected and commoditized.

While there is limited systematic evidence on citizens' privacy concerns globally, it appears that there exist large differences in consumers' willingness to pay to protect their data across the US, UK, Germany, China, and India.⁵⁵ On one end of the spectrum, Chinese consumers show low levels of privacy concerns.⁵⁶ On the other end of the spectrum, Germans exhibit substantial privacy concerns regarding a broad range of data, reflected in, for example, the EU's strict General Data Protection Regulation.⁵⁷

We focus here on restrictions on the state's collection and sharing of data, arising from norms of privacy. Our model suggests that the expression of norms regarding data's repugnance (ultimately reflected in regulation) can significantly affect the rate and direction of innovation. Consider an extension of our model where the flow utility is:

$$u(C) - \varphi D_g. \quad (22)$$

A positive φ captures households' repugnance towards government data production and data sharing. If households can enforce their preferences through regulations limiting data collection, production, or sharing, then a benevolent state would produce a lower level of aggregate government data in a BGP (i.e., a lower D_g/Y). As a result, if such preferences vary across economies, then the rate and direction of innovation will vary as well. Note that in our model, reduced government collection of data could be welfare-enhancing for citizens who value privacy, despite lower growth rates and less data-intensive innovation.

More concretely, we engage in the following thought experiment. Imagine that the symmetric economy associated with our benchmark calibration was again China. What would be the consequences of decreasing the amount of government data to the level observed in Germany? Specifically, we consider decreasing D_g/Y by 57% across BGP equilibria, which corresponds to the decrease from the number of cameras in China (14.36

⁵⁵Source: “Customer Data: Designing for Transparency and Trust”, <https://hbr.org/2015/05/customer-data-designing-for-transparency-and-trust>, last accessed on February 5, 2020.

⁵⁶Cultivating a tolerance for data collection might be an explicit aim of autocrats: this would align citizen attitudes with the monitoring objective of the state (and with the interests of innovators relying on data). For example, China's development of a “social score” provides individuals with incentives to be monitored.

⁵⁷See Aridor et al. (2020) for an examination of how GDPR affects the amount of data available to firms.

per 100 residents) to Germany (6.27 per 100 residents) in 2018.⁵⁸ We find that the annual growth rate (η) decreases from the benchmark 6% to 4% and that the bias of innovation (n_c) decreases from the benchmark 1 to 0.76.

8 Conclusion

In this paper, we analyzed direct and indirect ways in which data-intensive innovation may be shaped by the state, highlighting two features of data as an input: (i) historically, states have been key collectors of data, and (ii) data is sharable across multiple uses within firms, giving rise to economies of scope when firms can access government data and produce data-intensive software for government and commercial uses.

Our analysis suggests several directions for future research. First, we have provided a theoretical justification for government data provision as a policy to promote innovation, and evidence on one determinant of its consequences: economies of scope. Yet, many uncertainties remain about the implications of this policy, and a comprehensive quantitative assessment requires further measurement. For example, we know little about the substitutability of data with other inputs or the technologies for supplying and collecting data. Moreover, studying a broader range of countries and data-intensive technologies — e.g., for health care or mapping — will help us determine whether government data is as important elsewhere as it is in China’s facial recognition AI industry.

Second, we have studied the consequences of *government* data collection and provision to firms. One would also like to study the implications of *private* data collection and dissemination. Private firms’ possession of large datasets (e.g., those collected by Alibaba, Baidu, Facebook, or Google) should also generate significant economies of scope. Our analysis suggests that firm access to large private datasets (or lack thereof) will have important consequences for innovation, competition, and growth (see Aridor et al., 2020, and Jones and Tonetti, 2018). Empirically identifying the effects of large-scale private data collection and sharing on innovation is an important area for future work.

Finally, our analysis sheds new light on interrelationships among innovation, political institutions, and culture that require further study (see, e.g., Benabou et al., 2015; Besley and Persson, 2019). Our work suggests that the alignment between data-intensive innovation and the Chinese state’s surveillance interests, as well as permissive privacy norms, can help explain China’s rise to pre-eminence in AI.⁵⁹ However, we find that the normative

⁵⁸Source: “Top 10 Countries and Cities by Number of CCTV Cameras”, <https://www.aithority.com/news/top-10-countries-and-cities-by-number-of-cctv-cameras/>, last accessed on April 21, 2020.

⁵⁹Consider the facial recognition AI sector as an example: Supplementary Figure S.7 presents the companies with the top facial recognition algorithms, as ranked by the Face Recognition Vendor Test in 2018, organized by the National Institute of Standards and Technology, an agency of the US Department of Commerce. As one

implications of greater data-intensive innovation in surveillance states are complex, with higher economic growth potentially coming at a significant welfare cost to citizens. More research is therefore needed to understand the role of the state in determining economic, political, and social outcomes in the age of data-intensive innovation.

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can see, Chinese firms occupy all of the top 5 positions (see <https://bit.ly/20KL5Ze> for more details, last accessed on August 8, 2019). Lee (2019) documents China’s leadership in several sectors of the AI industry.

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ONLINE APPENDIX

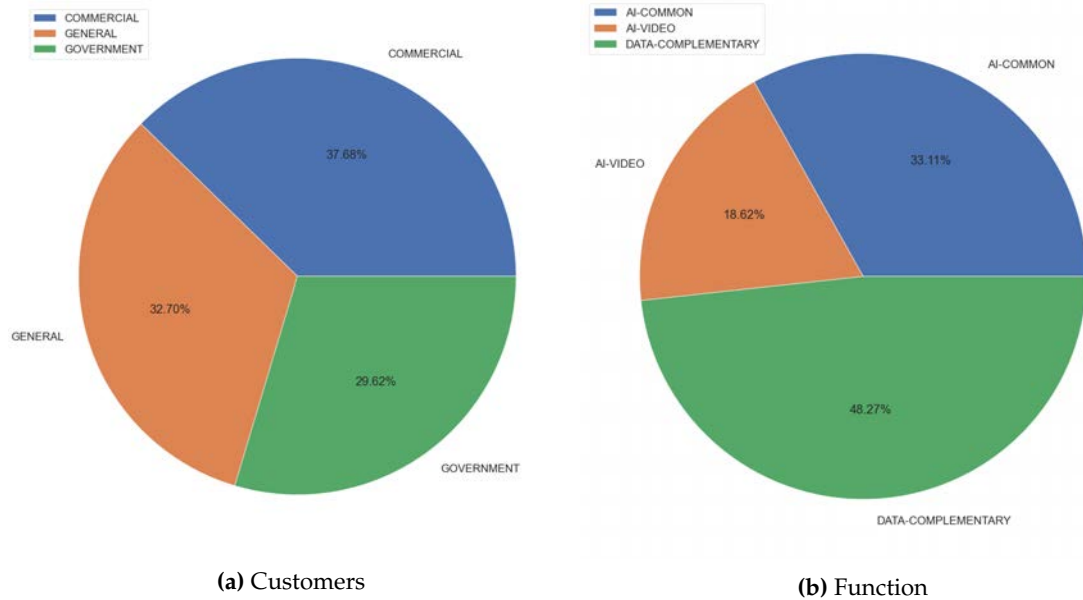


Figure A.1: Summary statistics of categorization outcomes for software categorizations based on Recurrent Neural Network with Long Short-Term Memory algorithm. Top panel shows categorization by customers; bottom panel shows categorization by function.

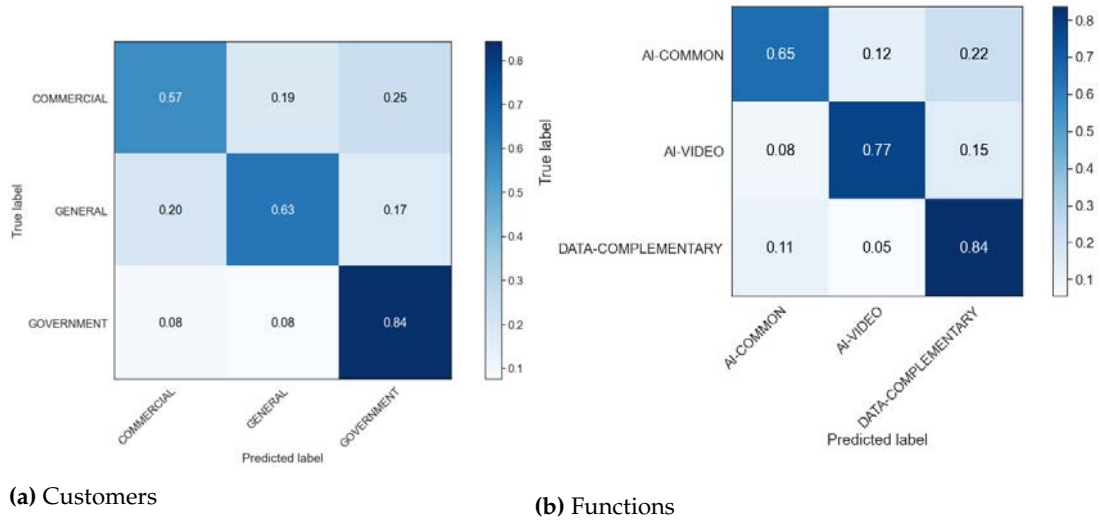


Figure A.2: Confusion matrix of categorization outcomes for software categorizations. True labels are based on training set constructed by human categorizations (performed by two individuals). Predicted labels are outputs based on Recurrent Neural Network with Long Short-Term Memory algorithm. Top panel shows categorization by customers; bottom panel shows categorization by function.

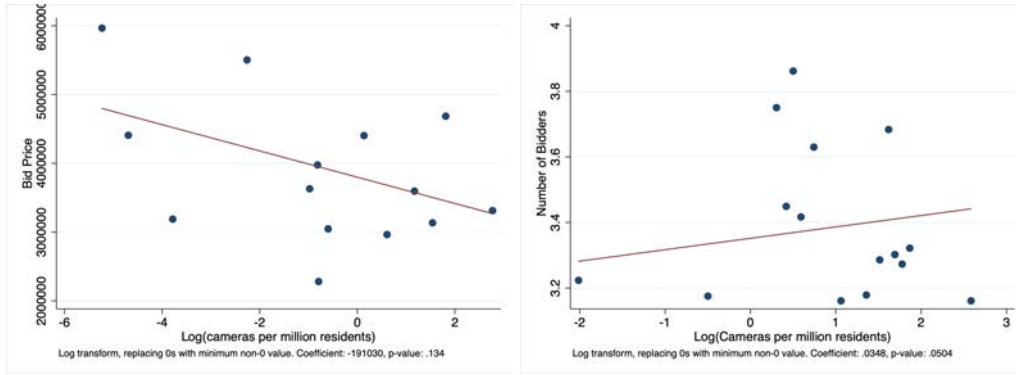


Figure A.3: Binned scatterplots of size of bid versus prefecture surveillance capacity, conditional on company fixed effects (left); and of number of bidders versus prefecture surveillance capacity (right).

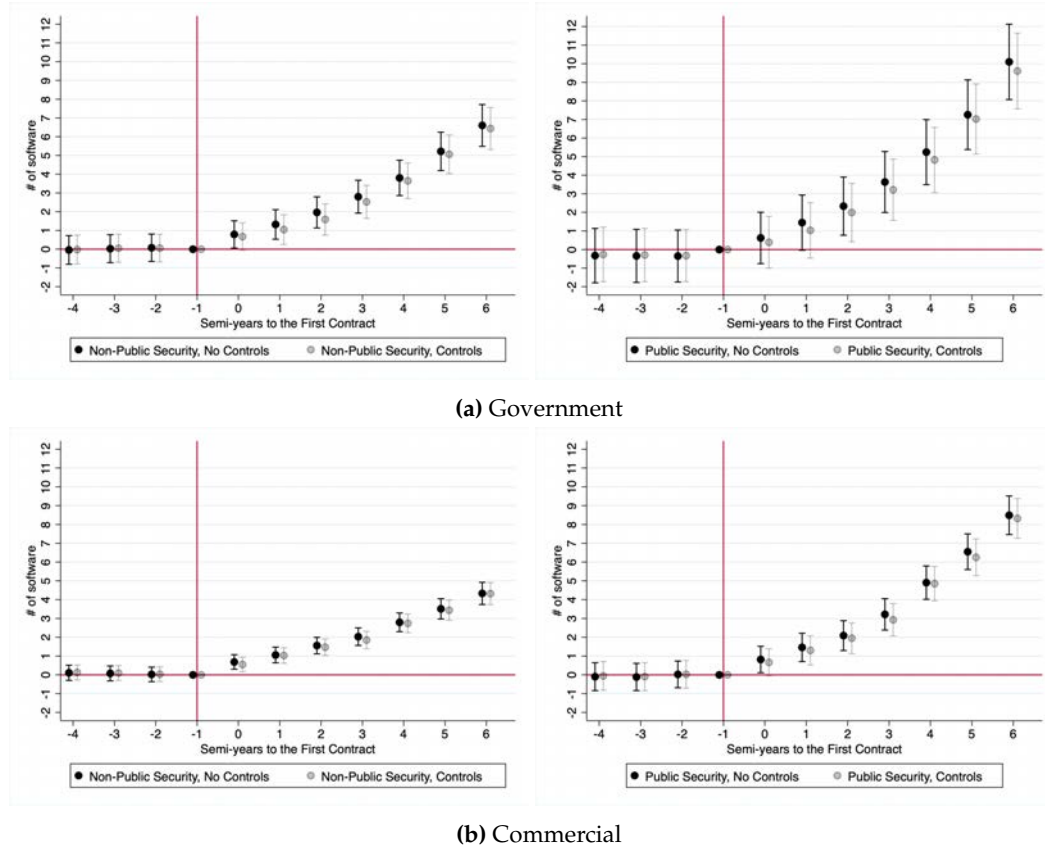
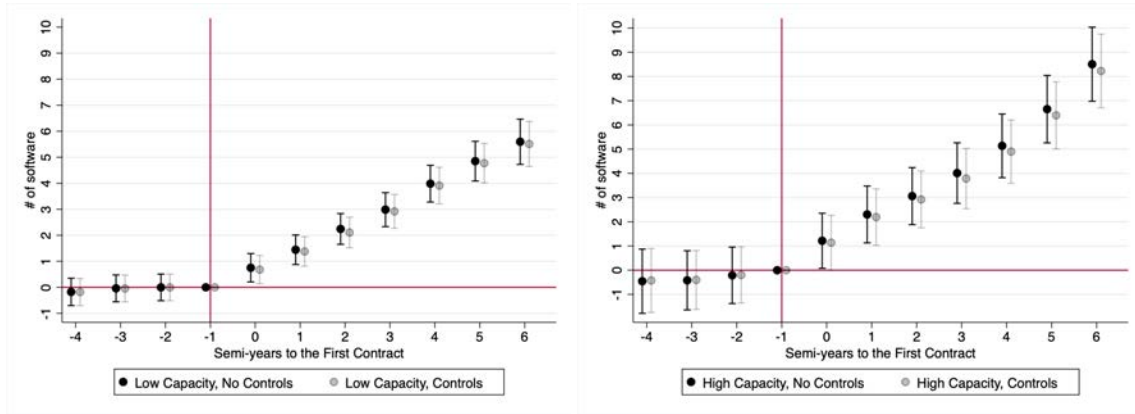
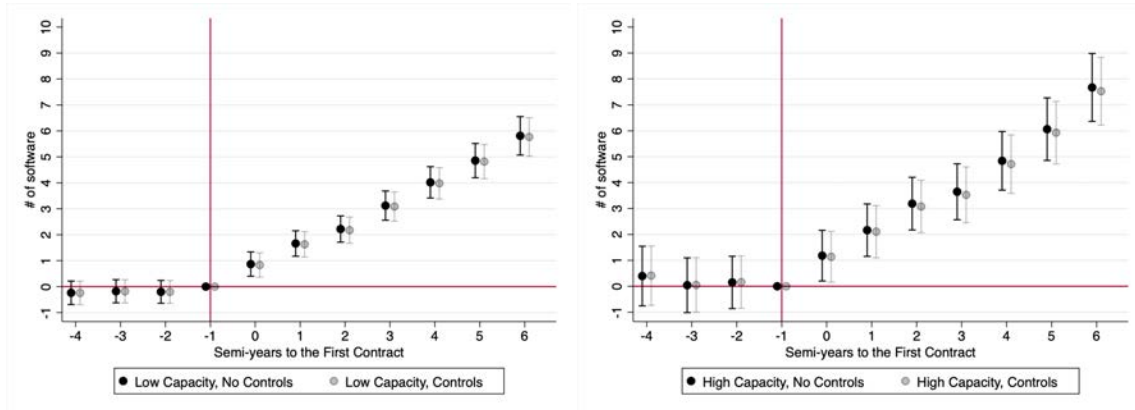


Figure A.4: Software development intended for government (Panel A) or for commercial uses (Panel B), resulting from public security contracts (right column) and non-public security contracts (left column), controlling for firm and time period fixed effects. Translucent lines/markers additionally interact pre-contract firm characteristics with a full set of time-period fixed effects.

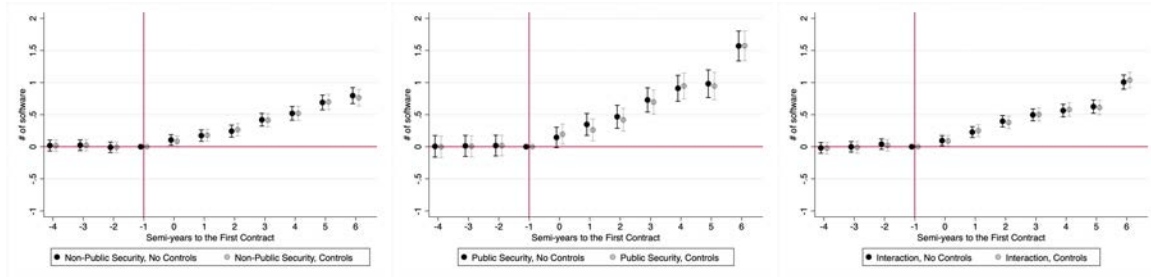


(a) Government

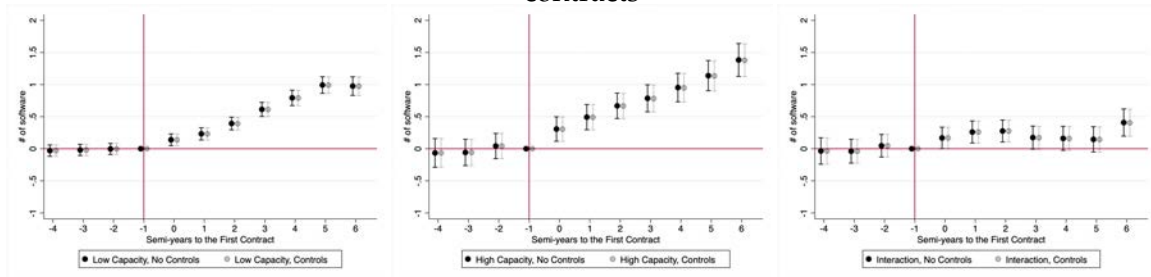


(b) Commercial

Figure A.5: Software development intended for government (Panel A) or for commercial uses (Panel B), resulting from data-rich public security contracts (right column) and data-scarce public security contracts (left column), controlling for firm and time period fixed effects. Translucent lines/markers additionally interact pre-contract firm characteristics with a full set of time-period fixed effects.



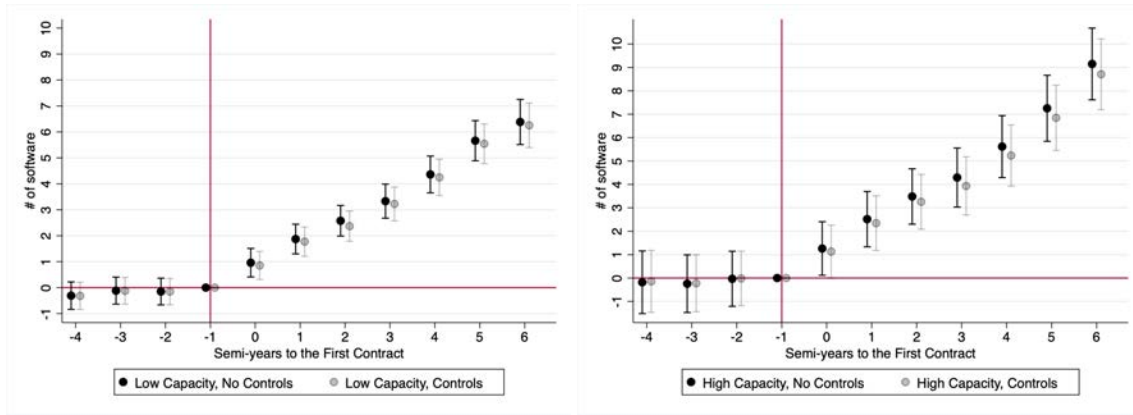
Panel A: Facial recognition AI involving video, public security vs. non-public security contracts



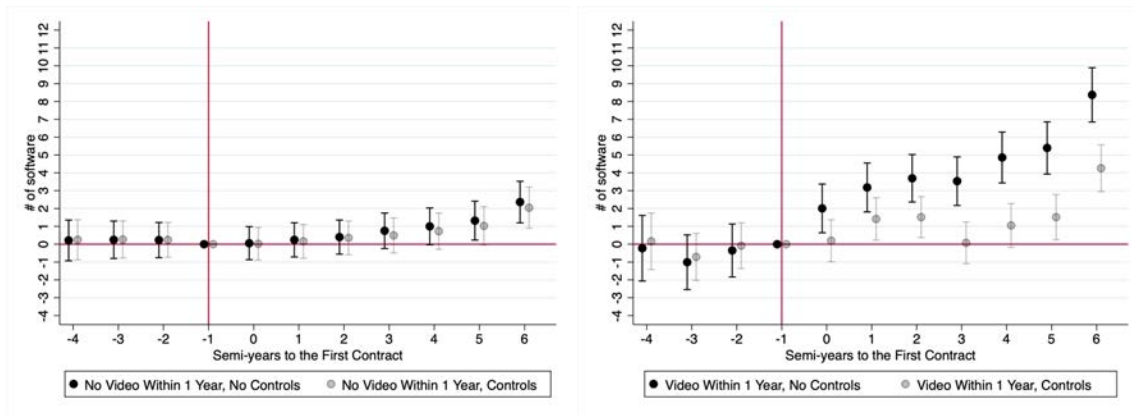
Panel B: Facial recognition AI involving video, high capacity vs. low capacity public security contracts

Figure A.6: Facial recognition software development that involves video (N-to-N matching).

Panel A: Results from non-public security contracts (left column), public security contracts (middle column), and the difference (right column). Panel B: Results for public security contracts that are data-scarce (left column), data-rich (middle column), and the difference (right column). All figures control for firm and time period fixed effects. Translucent lines/markers additionally interact pre-contract firm characteristics with a full set of time-period fixed effects.



Panel A: Data-complementary, split by surveillance capacity



Panel B: Data-complementary, split by AI video production in year 1

Figure A.7: Panel A: Data-complementary software production resulting from data-rich contracts (right column) and data-scarce contracts (left column), controlling for firm and time period fixed effects. Translucent lines/markers additionally interact pre-contract firm characteristics with a full set of time-period fixed effects. Panel B: Data-complementary software production resulting from public security contracts that led to government video facial recognition AI software within 1 year (right column), and public security contracts that did not (left column), controlling for firm and time period fixed effects. Translucent lines/markers additionally interact pre-contract firm characteristics with a full set of time-period fixed effects.

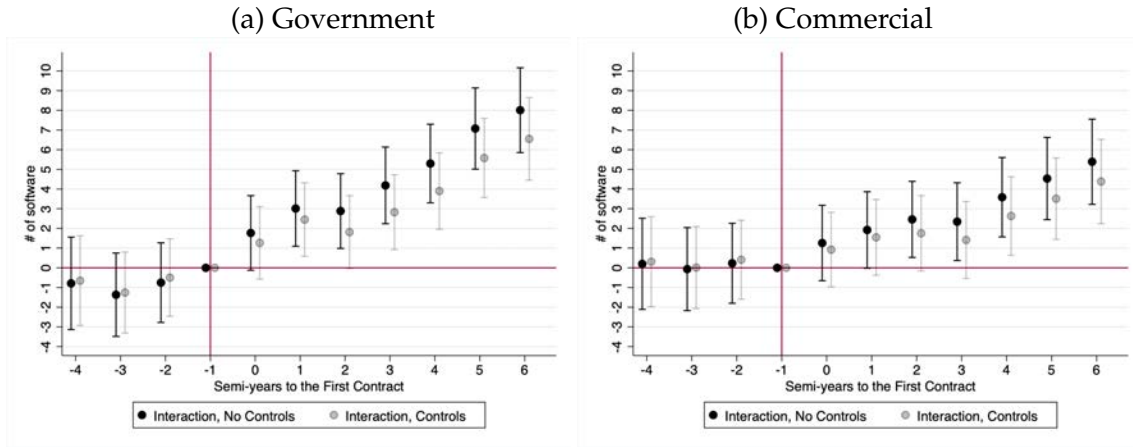


Figure A.8: Differential software development intended for government (left column) or for commercial uses (right column), resulting from public security contracts that led to data-complementary software production within 1 year, relative to public security contracts that did not, controlling for firm and time period fixed effects. Translucent lines/markers additionally interact pre-contract firm characteristics with a full set of time-period fixed effects.

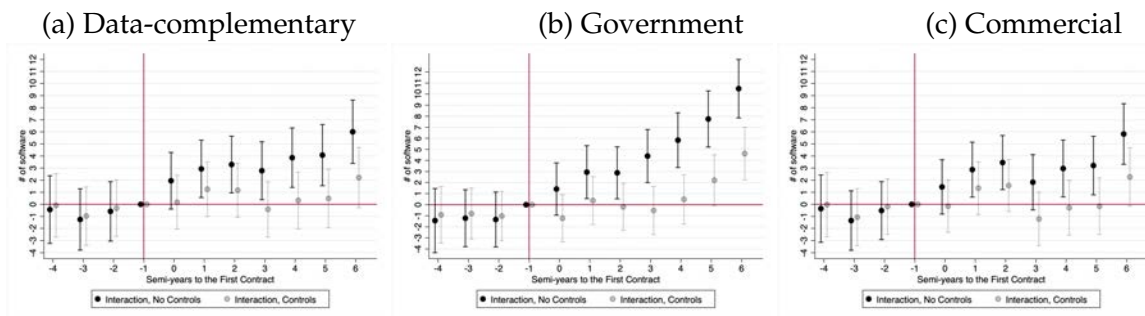


Figure A.9: Differential data-complementary software (left column) and differential AI software development intended for government (middle column) or for commercial uses (right column), resulting from public security contracts that led to video facial recognition AI software within 1 year, relative to public security contracts that did not, controlling for firm and time period fixed effects. Translucent lines/markers additionally interact pre-contract firm characteristics with a full set of time-period fixed effects.

Table A.1: List of core variables

English name	Chinese name	Source
Panel A: Raw data		
Software	软件	Chinese Ministry of Industry and Information Technology Tianyancha, Pitchbook
AI firms	人工智能公司	
Prefecture GDP	县GDP	Global Economic Data, Indicators, Charts & Forecasts (CEIC)
Prefecture population	县人口	Global Economic Data, Indicators, Charts & Forecasts (CEIC)
Fim capitalization	公司资本	Tianyancha
Firm rounds of investment funding	公司几轮投资资金	Tianyancha
Monetary size of contracts	合约金额	Chinese Government Procurement Database
Mother firm	母公司	
Panel B: Constructed data		
Software customer and function	软件客户和功能	Software text
Public security contracts	公安合约	Contract text
Camera capacity	摄像机容量	Contract text
Contract runner-up bidders	合约亚军	Contract text

Table A.2: Summary statistics — firms and their production

	Any contract		Public security contract		Public security contract by surveillance capacity	
	Yes	No	Yes	No	High	Low
	(1)	(2)	(3)	(4)	(5)	(6)
Panel A: Firm characteristics						
Year firm established	2,009.335 (6.389)	2,013.781 (4.244)	2,008.832 (6.523)	2,010.586 (5.445)	2,008.143 (6.581)	2,009.129 (6.458)
Capitalization (millions USD)	22.964 (210.840)	5.091 (43.007)	39.732 (333.095)	12.682 (149.926)	12.934 (35.929)	61.445 (464.613)
Rounds of investment funding	2.517 (1.961)	2.046 (3.258)	2.431 (1.668)	2.333 (1.803)	2.500 (1.627)	2.370 (1.708)
Observations	1,093	6,041	310	497	140	155
Panel B: Software production before contract						
Total amount of software	22.653 (37.860)	14.572 (24.473)	33.368 (54.760)	21.142 (26.759)	33.204 (52.535)	35.579 (59.246)
Business	27.492 (100.363)	28.415 (198.404)	33.709 (75.537)	30.745 (132.801)	32.648 (53.000)	37.333 (94.961)
Government	20.132 (60.669)	13.810 (76.379)	33.359 (66.071)	18.023 (71.590)	28.963 (42.447)	40.439 (84.481)
AI-common	12.673 (34.360)	11.541 (65.480)	14.222 (30.832)	14.302 (40.768)	12.519 (19.219)	17.018 (39.816)
AI-video	7.669 (19.175)	6.071 (32.115)	13.889 (31.492)	6.271 (12.481)	13.000 (29.702)	16.070 (34.445)
AI-complementary	26.666 (80.688)	21.788 (125.330)	39.385 (82.107)	25.454 (95.536)	35.815 (54.058)	45.719 (104.841)
Observations	956	6,042	234	443	108	114
Panel C: Software production after contract						
Total amount of software	24.393 (59.812)	-	35.569 (83.577)	19.903 (37.582)	33.157 (59.391)	40.568 (103.702)
Commercial	47.475 (304.587)	-	66.000 (504.701)	34.360 (125.475)	32.071 (70.675)	47.097 (162.583)
Government	29.459 (120.235)	-	43.518 (166.724)	19.762 (65.190)	25.771 (44.282)	61.045 (229.378)
AI-common	22.384 (107.543)	-	25.363 (116.453)	17.484 (81.909)	14.843 (34.371)	26.168 (87.470)
AI-video	14.422 (66.104)	-	20.958 (88.789)	8.015 (23.440)	12.043 (23.298)	29.794 (122.355)
Data-complementary	45.489 (212.602)	-	63.402 (283.432)	28.618 (106.427)	40.086 (100.173)	66.568 (257.713)
Observations	1,095	0	311	411	140	155

Note: Observations at the firm level. Standard deviations are reported below the means.

Table A.3: Summary statistics — procurement contracts

	Non-public security contracts	Public security contracts		
	All	All	Low capacity	High capacity
	(1)	(2)	(3)	(4)
Panel A: All contracts				
Admin level: provincial or above	0.340 (0.474)	0.277 (0.448)	0.138 (0.345)	0.306 (0.461)
Year contract signed	2,016.350 (1.612)	2,016.199 (1.604)	2,016.274 (1.516)	2,016.360 (1.530)
Area GDP	4,248.551 (4,979.406)	3,931.975 (4,567.528)	2,629.278 (3,364.656)	5,379.756 (5,272.500)
Area population	479.825 (264.595)	480.804 (263.863)	404.782 (221.149)	569.690 (284.979)
Cameras per million residents	4.311 (8.914)	3.392 (7.493)	0.138 (0.321)	6.920 (9.644)
Observations	15,523	10,677	4,880	4,500
Panel B: First contracts				
Admin level: provincial or above	0.462 (0.499)	0.383 (0.487)	0.272 (0.447)	0.423 (0.496)
Year contract signed	2,015.935 (1.840)	2,015.594 (1.976)	2,015.893 (1.883)	2,015.920 (1.875)
Area GDP	5,620.639 (5,493.355)	4,360.677 (4,372.221)	2,987.963 (3,021.635)	4,972.767 (4,780.787)
Area population	562.518 (269.504)	511.312 (266.436)	470.745 (254.547)	553.778 (270.646)
Cameras per million residents	4.951 (10.247)	6.097 (11.624)	0.141 (0.332)	10.575 (13.796)
Observations	796	308	103	137

Note: Observations at the procurement contract level. Standard deviations are reported below the mean. Administrative level of the contract is recorded as central government, provincial level, prefecture level and county level; the mean of an indicator of provincial or above level (provincial and central government) is shown. Local GDP is measured in millions of RMB, population in ten-thousand persons.

Table A.4: Summary statistics — localities with low vs. high surveillance capacities

	Low capacity localities (1)	High capacity localities (2)	Difference (3)
Panel A: Demographics			
Population (10,000 persons)	387.613 (263.367)	461.803 (250.099)	74.189 (32.603)**
Urban population (1,000 persons)	1,434.740 (1,302.286)	1,806.922 (1,416.332)	372.183 (171.981)**
College students (1,000 persons)	96.034 (186.146)	106.309 (193.176)	10.276 (23.506)
College teachers (1,000 persons)	5.256 (10.285)	5.573 (10.570)	0.318 (1.296)
Broadband household (1000s)	1,164.550 (1,119.982)	1,680.905 (1,306.269)	516.354 (152.231)***
Mobile phone households (1000s)	4,366.004 (4,510.161)	6,113.576 (5,812.991)	1,747.572 (617.955)***
Observations	203	102	305
Panel B: Economics			
Number of contracts	57.369 (117.253)	105.225 (178.565)	47.856 (17.075)***
# of 1st contracts	1.719 (4.615)	3.010 (8.179)	1.291 (0.733)*
Monetary size (10,000 RMB)	2,671.686 (9,762.651)	2,352.398 (9,929.068)	-319.288 (1,202.745)
GDP (100 Million RMB)	1,858.525 (2,107.872)	2,991.609 (3,249.163)	1,133.085 (320.642)***
GDP per capita (RMB)	49,138.492 (37,714.531)	68,544.117 (67,582.133)	19,405.621 (6,261.676)***
Fiscal expenditure (million RMB)	44,718.504 (46,643.832)	56,296.723 (58,102.457)	11,578.219 (6,295.382)*
Fiscal revenue (million RMB)	21,227.164 (39,860.871)	33,746.250 (50,784.539)	12,519.088 (5,433.332)**
Observations	203	102	305

Notes: Localities (at city level) are divided into below (Column 1) and above (Column 2) median in terms of their province-level surveillance-related spending prior to 2015. Broadband households are households with broadband internet connections, mobile phone households are households with a mobile phone, number of 1st contracts refers to the number of firms which had their first contract in the city, while monetary size refers to the average monetary size of all contracts. Fiscal expenditure and revenue refer to spending or revenue received by the city's government.

Table A.5: Public security contracts vs. non-public security contracts

	Government	Commercial	Data-complementary	Government	Commercial	Data-complementary
	(1)	(2)	(3)	(4)	(5)	(6)
4 Semiyears Before	-0.113 (0.195)	0.007 (0.132)	-0.115 (0.158)	-0.013 (0.218)	0.016 (0.149)	-0.009 (0.174)
3 Semiyears Before	-0.114 (0.191)	-0.000 (0.129)	-0.074 (0.155)	-0.048 (0.214)	0.006 (0.146)	-0.002 (0.171)
2 Semiyears Before	-0.103 (0.187)	-0.030 (0.126)	-0.077 (0.151)	-0.075 (0.209)	-0.011 (0.143)	-0.036 (0.167)
Receiving 1st Contract	0.412** (0.186)	0.394*** (0.126)	0.450*** (0.151)	0.227 (0.208)	0.346** (0.142)	0.343** (0.166)
1 Semiyear After	0.871*** (0.201)	0.871*** (0.135)	0.971*** (0.162)	0.687*** (0.224)	0.793*** (0.152)	0.837*** (0.178)
2 Semiyears After	1.465*** (0.211)	1.357*** (0.142)	1.483*** (0.170)	1.286*** (0.234)	1.340*** (0.159)	1.353*** (0.187)
3 Semiyears After	2.191*** (0.223)	1.983*** (0.150)	2.254*** (0.180)	2.089*** (0.248)	1.915*** (0.169)	2.137*** (0.198)
4 Semiyears After	2.992*** (0.238)	2.628*** (0.160)	3.195*** (0.193)	3.000*** (0.264)	2.619*** (0.180)	3.107*** (0.212)
5 Semiyears After	3.881*** (0.256)	3.073*** (0.173)	3.941*** (0.207)	3.937*** (0.285)	3.036*** (0.194)	3.898*** (0.228)
6 Semiyears After	4.971*** (0.278)	3.761*** (0.187)	4.724*** (0.225)	5.231*** (0.309)	3.832*** (0.210)	4.797*** (0.247)
4 Semiyears Before × Public Security	-0.149 (0.316)	-0.130 (0.214)	-0.076 (0.256)	-0.158 (0.354)	-0.121 (0.242)	-0.108 (0.283)
3 Semiyears Before × Public Security	-0.049 (0.311)	-0.133 (0.209)	-0.067 (0.251)	-0.075 (0.348)	-0.128 (0.237)	-0.094 (0.278)
2 Semiyears Before × Public Security	0.017 (0.306)	0.058 (0.206)	0.012 (0.247)	0.032 (0.342)	0.046 (0.234)	-0.004 (0.273)
Receiving 1st Contract × Public Security	0.442 (0.301)	0.437** (0.203)	0.383 (0.244)	0.167 (0.336)	0.254 (0.230)	0.150 (0.269)
1 Semiyear After × Public Security	0.907*** (0.321)	0.662*** (0.217)	0.728*** (0.260)	0.676* (0.358)	0.769*** (0.245)	0.505* (0.286)
2 Semiyears After × Public Security	1.395*** (0.337)	1.134*** (0.228)	1.261*** (0.272)	1.245*** (0.376)	1.162*** (0.257)	1.045*** (0.300)
3 Semiyears After × Public Security	1.787*** (0.351)	1.555*** (0.237)	1.760*** (0.284)	1.409*** (0.391)	1.585*** (0.268)	1.484*** (0.313)
4 Semiyears After × Public Security	2.424*** (0.370)	2.340*** (0.250)	2.511*** (0.300)	2.063*** (0.413)	2.614*** (0.282)	2.335*** (0.330)
5 Semiyears Before × Public Security	3.012*** (0.391)	3.328*** (0.264)	3.410*** (0.316)	2.524*** (0.437)	3.570*** (0.298)	3.141*** (0.349)
6 Semiyears After × Public Security	4.068*** (0.420)	4.199*** (0.282)	4.812*** (0.339)	3.568*** (0.469)	4.324*** (0.319)	4.620*** (0.374)
Observations	1.19e+05	1.20e+05	1.20e+05	1.19e+05	1.20e+05	1.20e+05

Notes: Baseline specification (Columns 1–3) controls for time period fixed effects and firm fixed effects. Columns 4–6 include controls for firms' pre-contract characteristics interacted with all semi-year indicators. Standard errors clustered at mother firm level are reported in parentheses. * significant at 10% ** significant at 5% *** significant at 1%.

Table A.6: Public security contracts — high vs. low surveillance capacity

	Government	Commercial	Data-complementary	Government	Commercial	Data-complementary
	(1)	(2)	(3)	(4)	(5)	(6)
4 Semiyears Before	-0.177 (0.268)	-0.239 (0.231)	-0.310 (0.270)	-0.182 (0.267)	-0.243 (0.231)	-0.317 (0.267)
3 Semiyears Before	-0.040 (0.264)	-0.180 (0.228)	-0.118 (0.266)	-0.044 (0.262)	-0.183 (0.227)	-0.123 (0.262)
2 Semiyears Before	-0.002 (0.261)	-0.202 (0.225)	-0.151 (0.262)	-0.004 (0.260)	-0.203 (0.224)	-0.153 (0.259)
Receiving 1st Contract	0.750*** (0.279)	0.868*** (0.239)	0.959*** (0.280)	0.680** (0.277)	0.833*** (0.239)	0.853*** (0.277)
1 Semiyear After	1.443*** (0.289)	1.663*** (0.250)	1.871*** (0.291)	1.378*** (0.288)	1.630*** (0.250)	1.772*** (0.288)
2 Semiyears After	2.243*** (0.301)	2.219*** (0.258)	2.576*** (0.301)	2.106*** (0.300)	2.174*** (0.258)	2.367*** (0.297)
3 Semiyears After	2.986*** (0.334)	3.122*** (0.287)	3.331*** (0.336)	2.917*** (0.332)	3.087*** (0.287)	3.223*** (0.331)
4 Semiyears After	3.984*** (0.360)	4.017*** (0.309)	4.362*** (0.362)	3.910*** (0.358)	3.980*** (0.308)	4.248*** (0.357)
5 Semiyears After	4.849*** (0.389)	4.857*** (0.337)	5.662*** (0.395)	4.771*** (0.387)	4.817*** (0.336)	5.543*** (0.390)
6 Semiyears After	5.595*** (0.444)	5.811*** (0.378)	6.383*** (0.443)	5.511*** (0.441)	5.769*** (0.378)	6.255*** (0.438)
4 Semiyears Before × High Capacity	-0.279 (0.620)	0.633 (0.539)	0.130 (0.627)	-0.243 (0.617)	0.653 (0.538)	0.176 (0.620)
3 Semiyears Before × High Capacity	-0.379 (0.565)	0.222 (0.488)	-0.124 (0.570)	-0.356 (0.562)	0.235 (0.487)	-0.099 (0.563)
2 Semiyears Before × High Capacity	-0.209 (0.535)	0.351 (0.463)	0.118 (0.540)	-0.192 (0.532)	0.362 (0.462)	0.136 (0.534)
Receiving 1st Contract × High Capacity	0.465 (0.508)	0.314 (0.438)	0.303 (0.512)	0.457 (0.505)	0.307 (0.437)	0.277 (0.506)
1 Semiyear After × High Capacity	0.858 (0.524)	0.502 (0.451)	0.645 (0.528)	0.817 (0.521)	0.478 (0.450)	0.574 (0.521)
2 Semiyears After × High Capacity	0.817 (0.520)	0.969** (0.449)	0.909* (0.524)	0.814 (0.518)	0.904** (0.449)	0.890* (0.518)
3 Semiyears After × High Capacity	1.023* (0.544)	0.526 (0.470)	0.963* (0.549)	0.868 (0.541)	0.442 (0.469)	0.711 (0.542)
4 Semiyears After × High Capacity	1.151** (0.565)	0.823* (0.487)	1.256** (0.570)	0.987* (0.562)	0.735 (0.486)	0.988* (0.563)
5 Semiyears Before × High Capacity	1.800*** (0.594)	1.205** (0.515)	1.592*** (0.602)	1.623*** (0.591)	1.110** (0.514)	1.303** (0.595)
6 Semiyears After × High Capacity	2.911*** (0.642)	1.861*** (0.550)	2.766*** (0.644)	2.715*** (0.638)	1.759*** (0.549)	2.452*** (0.636)

Notes: All regressions estimated on the sample of firms with first contracts with a public security agency. Baseline specification (Columns 1–3) controls for time period fixed effects and firm fixed effects. Columns 4–6 include controls for firms' pre-contract characteristics interacted with all semi-year indicators. Standard errors clustered at mother firm level are reported in parentheses. * significant at 10% ** significant at 5% *** significant at 1%.

Table A.7: Robustness — LSTM categorization model configuration

	Government	Commercial	Data-complementary
	(1)	(2)	(3)
Panel A: Baseline (timestep 20, embeddings 32, nodes 32)			
4 semiyears before	-0.177 (0.268)	-0.239 (0.231)	-0.310 (0.270)
6 semiyears after	5.595*** (0.444)	5.811*** (0.378)	6.383*** (0.443)
4 semiyears before × high capacity	-0.279 (0.620)	0.633 (0.539)	0.130 (0.627)
6 semiyears after × high capacity	2.911*** (0.642)	1.861*** (0.550)	2.766*** (0.644)
Panel B: Vary timestep 10, embeddings 32, nodes 32			
4 semiyears before	-0.113 (0.275)	-0.310 (0.324)	-0.371 (0.242)
6 semiyears after	4.637*** (0.452)	4.948*** (0.532)	3.847*** (0.397)
4 semiyears before × high capacity	-0.328 (0.638)	0.521 (0.760)	0.456 (0.563)
6 semiyears after × high capacity	2.516*** (0.658)	3.349*** (0.775)	3.579*** (0.575)
Panel C: Timestep 20, vary embeddings 16, nodes 32			
4 semiyears before	-0.268 (0.288)	-0.269 (0.270)	-0.424* (0.245)
6 semiyears after	6.102*** (0.474)	4.743*** (0.444)	5.505*** (0.406)
4 semiyears before × high capacity	-0.181 (0.669)	0.418 (0.634)	0.463 (0.570)
6 semiyears after × high capacity	2.532*** (0.689)	2.530*** (0.647)	2.513*** (0.586)
Panel D: Timestep 20, embeddings 32, vary nodes 16			
4 semiyears before	-0.206 (0.295)	-0.353 (0.310)	-0.216 (0.227)
6 semiyears after	6.017*** (0.485)	4.485*** (0.509)	5.667*** (0.374)
4 semiyears before × high capacity	-0.172 (0.685)	0.526 (0.721)	0.149 (0.526)
6 semiyears after × high capacity	3.190*** (0.706)	2.652*** (0.741)	2.378*** (0.541)

Notes: Specifications include full set of time indicators and interactions with public security contracts; only selected coefficient estimates are presented. Standard errors clustered at mother firm level are reported in parentheses. Panel A replicates baseline specification in Table A.6, Columns 1-3 using the default LSTM specification with a timestep (phrase length) of 20, embedding size (number of dimensions in a vector to represent a phrase) of 32, and 32 nodes in the model. Panel B presents results for the same model in Panel A trained with a timestep of 10 instead; Panel C presents results for the same model in Panel A trained with an embedding size of 16 instead; Panel D presents results for the same model in Panel A trained with 16 nodes instead. The full set of combinations of results with varied model parameters do not look qualitatively different. * significant at 10% ** significant at 5% *** significant at 1%.

Table A.8: Robustness — LSTM categorization model threshold

	Government	Commercial	Data-complementary
	(1)	(2)	(3)
Panel A: Baseline (threshold 50%)			
4 semiyears before	-0.177 (0.268)	-0.239 (0.231)	-0.310 (0.270)
6 semiyears after	5.595*** (0.444)	5.811*** (0.378)	6.383*** (0.443)
4 semiyears before × high capacity	-0.279 (0.620)	0.633 (0.539)	0.130 (0.627)
6 semiyears after × high capacity	2.911*** (0.642)	1.861*** (0.550)	2.766*** (0.644)
Panel B: Threshold 60%			
4 semiyears before	-0.139 (0.234)	-0.272 (0.309)	-0.309 (0.255)
6 semiyears after	3.465*** (0.389)	6.452*** (0.508)	5.826*** (0.421)
4 semiyears before × high capacity	-0.237 (0.543)	0.525 (0.721)	0.553 (0.595)
6 semiyears aafter × high capacity	2.811*** (0.562)	2.349*** (0.740)	2.765*** (0.609)
Panel C: Threshold 70%			
4 semiyears before	-0.133 (0.233)	-0.280 (0.309)	-0.304 (0.254)
6 semiyears after	3.403*** (0.387)	6.411*** (0.507)	5.789*** (0.419)
4 semiyears before × high capacity	-0.243 (0.541)	0.542 (0.720)	0.545 (0.593)
6 semiyears after × high capacity	2.765*** (0.560)	2.324*** (0.739)	2.730*** (0.607)

Notes: Specifications include full set of time indicators and interactions with public security contracts; only selected coefficient estimates are presented. Standard errors clustered at mother firm level are reported in parentheses. Panel A replicates baseline specification in Table A.6, Columns 1-3 using the default LSTM specification with a confidence threshold for the classification of software set at 50% (e.g. the model must be at least 50% confident that a given software is government software to be classified as "government"). Panels B and C replicate the exercise setting the threshold to be higher, at 60% and 70% respectively. * significant at 10% ** significant at 5% *** significant at 1%.

Table A.9: Robustness — time frame

	Government	Commercial	Data-complementary
	(1)	(2)	(3)
Panel A: Baseline			
4 semiyears before	-0.177 (0.268)	-0.239 (0.231)	-0.310 (0.270)
6 semiyears after	5.595*** (0.444)	5.811*** (0.378)	6.383*** (0.443)
4 semiyears before × high capacity	-0.279 (0.620)	0.633 (0.539)	0.130 (0.627)
6 semiyears after × high capacity	2.911*** (0.642)	1.861*** (0.550)	2.766*** (0.644)
Panel B: Full balanced panel			
4 semiyears before	0.184 (0.576)	0.035 (0.477)	-0.005 (0.563)
6 semiyears after	5.634*** (0.728)	6.165*** (0.597)	6.614*** (0.706)
4 semiyears before × high capacity	-3.218 (2.661)	0.743 (2.093)	-0.912 (2.472)
6 semiyears after × high capacity	3.404*** (1.237)	2.048** (1.024)	3.071** (1.217)
Panel C: Extended time frame			
5 semiyears before	-0.124 (0.274)	-0.204 (0.236)	-0.245 (0.275)
8 semiyears after	8.469*** (0.572)	6.986*** (0.488)	7.835*** (0.562)
5 semiyears before × high capacity	-0.342 (0.686)	0.269 (0.597)	-0.248 (0.695)
8 semiyears after × high capacity	3.793*** (0.756)	4.150*** (0.648)	5.573*** (0.750)
Panel D: Quarter as unit of analysis			
8 quarters before	-0.044 (0.256)	-0.130 (0.214)	-0.062 (0.250)
12 quarters after	5.585*** (0.416)	5.436*** (0.347)	5.762*** (0.403)
8 quarters before × high capacity	-0.515 (0.570)	0.280 (0.485)	-0.323 (0.560)
12 quarters after × high capacity	2.100*** (0.585)	1.516*** (0.492)	2.331*** (0.571)
Subsidiary Firm FE	Y	Y	Y

Notes: Specifications include full set of time indicators and interactions with public security contracts; only selected coefficient estimates are presented. Standard errors clustered at mother firm level are reported in parentheses. Panel A replicates baseline specification in Table A.6, Columns 1-3; Panel B restricts the sample to firms that have non-missing observations during the entire time frame of 4 semi-years before and 6 semi-years after the initial contracts; Panel C extends the time frame to 5 semi-years before and 8 semi-years after the initial contracts; Panel D uses quarters of a year as the unit of analysis, instead of semi-years. * significant at 10% ** significant at 5% *** significant at 1%.

Table A.10: Robustness — ambiguous public security agencies

	Government	Commercial	Data-complementary
	(1)	(2)	(3)
Panel A: Baseline			
4 semiyears before	-0.177 (0.268)	-0.239 (0.231)	-0.310 (0.270)
6 semiyears after	5.595*** (0.444)	5.811*** (0.378)	6.383*** (0.443)
4 semiyears before × high capacity	-0.279 (0.620)	0.633 (0.539)	0.130 (0.627)
6 semiyears after × high capacity	2.911*** (0.642)	1.861*** (0.550)	2.766*** (0.644)
Panel B: Drop ambiguous companies			
4 semiyears before	-0.184 (0.270)	-0.260 (0.230)	-0.319 (0.270)
6 semiyears after	5.335*** (0.448)	5.916*** (0.377)	6.094*** (0.444)
4 semiyears before × high capacity	-0.375 (0.649)	0.625 (0.557)	-0.026 (0.653)
6 semiyears after × high capacity	3.222*** (0.659)	1.371** (0.558)	2.897*** (0.657)

Notes: Panel A replicates baseline specification in Table A.6, Columns 1-3; specification includes full set of time indicators and interactions with public security contracts; only selected coefficient estimates are presented. Ambiguous public security contracts are ones that contain the keywords 'local government' ('人民政府') or 'government offices' ('政府办公室') which may be used for either public security or non-public security depending on interpretation. Panel B drops companies whose first contract is an ambiguous contract. Standard errors clustered at mother firm level are reported below the coefficients. * significant at 10% ** significant at 5% *** significant at 1%.

Table A.11: Firm, contract, and locality characteristics interacted with time period fixed effects

	Government	Commercial	Data-complementary
	(1)	(2)	(3)
Panel A: Baseline			
4 semiyears before	-0.177 (0.268)	-0.239 (0.231)	-0.310 (0.270)
6 semiyears after	5.595*** (0.444)	5.811*** (0.378)	6.383*** (0.443)
4 semiyears before \times high capacity	-0.279 (0.620)	0.633 (0.539)	0.130 (0.627)
6 semiyears after \times high capacity	2.911*** (0.642)	1.861*** (0.550)	2.766*** (0.644)
Panel B: Contract similarity with opposite capacity contracts			
4 semiyears before	-0.185 (0.268)	-0.219 (0.231)	-0.341 (0.270)
6 semiyears after	5.667*** (0.445)	5.630*** (0.380)	6.662*** (0.445)
4 semiyears before \times high capacity	-0.267 (0.620)	0.603 (0.539)	0.178 (0.627)
6 semiyears after \times high capacity	3.213*** (0.664)	1.091* (0.569)	3.940*** (0.666)
Panel C: Contract size			
4 semiyears before	-0.182 (0.267)	-0.243 (0.231)	-0.317 (0.267)
6 semiyears after	5.511*** (0.441)	5.769*** (0.378)	6.255*** (0.438)
4 semiyears before \times high capacity	-0.243 (0.617)	0.653 (0.538)	0.176 (0.620)
6 semiyears after \times high capacity	2.715*** (0.638)	1.759*** (0.549)	2.452*** (0.636)
Panel D: Firm pre-contract size			
4 semiyears before	-0.175 (0.268)	-0.240 (0.231)	-0.310 (0.270)
6 semiyears after	5.579*** (0.444)	5.824*** (0.378)	6.381*** (0.443)
4 semiyears before \times high capacity	-0.277 (0.620)	0.632 (0.539)	0.131 (0.627)
6 semiyears after \times high capacity	2.898*** (0.642)	1.871*** (0.550)	2.764*** (0.644)
Panel E: First contract location GDP			
4 semiyears before	-0.167 (0.268)	-0.249 (0.231)	-0.311 (0.270)
6 semiyears after	5.439*** (0.443)	5.957*** (0.378)	6.404*** (0.443)
4 semiyears before \times high capacity	-0.177 (0.619)	0.526 (0.538)	0.115 (0.628)
6 semiyears after \times high capacity	2.138*** (0.645)	2.605*** (0.553)	2.866*** (0.648)
Panel F: Firm age			
4 semiyears before	-0.130 (0.263)	-0.237 (0.231)	-0.282 (0.269)
6 semiyears after	53.636*** (1.226)	7.926*** (1.078)	28.782*** (1.261)
4 semiyears before \times high capacity	-0.440 (0.608)	0.626 (0.539)	0.050 (0.625)
6 semiyears after \times high capacity	3.279*** (0.630)	1.876*** (0.550)	2.924*** (0.642)

Panel G: All pre-controls interacted			
4 semiyears before	-0.133 (0.262)	-0.233 (0.230)	-0.326 (0.265)
6 semiyears after	52.516*** (1.224)	9.002*** (1.078)	28.815*** (1.250)
4 semiyears before × high capacity	-0.314 (0.605)	0.508 (0.537)	0.126 (0.617)
6 semiyears after × high capacity	2.688*** (0.651)	1.786*** (0.571)	4.031*** (0.660)

Notes: Specifications include full set of time indicators and interactions with public security contracts; only selected coefficient estimates are presented. Standard errors clustered at mother firm level are reported in parentheses. Panel A replicates baseline specification in Table A.6. Panels B - G interact controls with time dummies, where Panel B interacts contract similarity, Panel C interacts the size of the contract, Panel D interacts the monetary size of the firm, Panel E interacts the GDP of the first contract's location, Panel F interacts firm age, and Panel G interacts with all the above controls. * significant at 10% ** significant at 5% *** significant at 1%.

Table A.12: Learning by doing

	Government	Commercial	Data-complementary
	(1)	(2)	(3)
Panel A: Baseline			
4 semiyears before	-0.177 (0.268)	-0.239 (0.231)	-0.310 (0.270)
6 semiyears after	5.595*** (0.444)	5.811*** (0.378)	6.383*** (0.443)
4 semiyears before × high capacity	-0.279 (0.620)	0.633 (0.539)	0.130 (0.627)
6 semiyears after × high capacity	2.911*** (0.642)	1.861*** (0.550)	2.766*** (0.644)
Panel B: Control for government pre-contract software production			
4 semiyears before	0.138 (0.233)	-0.076 (0.220)	-0.081 (0.252)
6 semiyears after	1.769*** (0.386)	3.846*** (0.362)	3.652*** (0.415)
4 semiyears before × high capacity	0.170 (0.538)	0.869* (0.514)	0.489 (0.586)
6 semiyears after × high capacity	1.477*** (0.556)	1.116** (0.525)	1.722*** (0.602)
Panel C: Control for same category pre-contract software production			
4 semiyears before	0.138 (0.233)	0.034 (0.209)	-0.047 (0.253)
6 semiyears after	1.769*** (0.386)	2.577*** (0.344)	3.173*** (0.418)
4 semiyears before × high capacity	0.170 (0.538)	0.841* (0.487)	0.361 (0.589)
6 semiyears after × high capacity	1.477*** (0.556)	1.132** (0.498)	2.013*** (0.605)
Panel D: Control for opposite category pre-contract software production			
4 semiyears before	0.080 (0.250)	-0.076 (0.220)	-0.061 (0.256)
6 semiyears after	2.399*** (0.416)	3.846*** (0.362)	3.474*** (0.423)
4 semiyears before × high capacity	-0.078 (0.579)	0.869* (0.514)	0.302 (0.596)
6 semiyears after × high capacity	2.231*** (0.599)	1.116** (0.525)	2.111*** (0.612)

Notes: Specifications include full set of time indicators and interactions with public security contracts; only selected coefficient estimates are presented. Standard errors clustered at mother firm level are reported in parentheses. Panel A replicates baseline specification in Table A.6, Columns 1-3. Panel B controls for the total amount of government software produced by the firm at 1 semiyear before the contract. Panel C controls for the total amount of software indicated in the column by the firm at 1 semiyear before the contract. Panel D controls for total amount of opposite category software produced by the firm at 1 semiyear before the contract, where opposite category references the other category in the pairings between government and commercial intended software, and between AI and non-AI related software. * significant at 10% ** significant at 5% *** significant at 1%.

Table A.13: Effects of 2nd public security contracts

	Government	Commercial	Data-complementary
	(1)	(2)	(3)
Panel A: Baseline			
4 semiyears before	-0.177 (0.268)	-0.239 (0.231)	-0.310 (0.270)
6 semiyears after	5.595*** (0.444)	5.811*** (0.378)	6.383*** (0.443)
4 semiyears before × high capacity	-0.279 (0.620)	0.633 (0.539)	0.130 (0.627)
6 semiyears after × high capacity	2.911*** (0.642)	1.861*** (0.550)	2.766*** (0.644)
Panel B: Sample — not first contract within mother firm			
4 semiyears before	-0.078 (0.213)	-0.431 (0.362)	-0.184 (0.283)
6 semiyears after	4.606*** (0.332)	6.730*** (0.557)	6.370*** (0.438)
4 semiyears before × high capacity	1.035 (0.786)	1.047 (1.384)	0.820 (1.081)
6 semiyears after × high capacity	2.753*** (0.710)	1.975* (1.200)	1.024 (0.947)
Panel C: Sample — second contract within firm			
4 semiyears before	-1.577* (0.916)	2.214*** (0.656)	2.015*** (0.697)
6 semiyears after	8.533*** (1.430)	7.856*** (1.025)	13.538*** (1.088)
4 semiyears before × high capacity	1.090 (1.287)	-1.943** (0.923)	-1.819* (0.980)
6 semiyears after × high capacity	29.042*** (1.881)	2.876** (1.349)	17.833*** (1.432)

Notes: Specification include full set of time indicators and interactions with public security contracts; only selected coefficient estimates are presented. Standard errors clustered at mother firm level are reported in parentheses. Panel B restricts the sample to only subsidiary firms that did not earn the first contract within the mother firm—note that the number of observations falls to 9,300 observations in Panel B from 17,400 in Panel A. Panel C (number of observations = 17,400) replicates Panel A, except uses second contracts instead of first contracts earned by the firm. * significant at 10% ** significant at 5% *** significant at 1%.

Table A.14: Access to commercial opportunities

	Government	Commercial	Data-complementary
	(1)	(2)	(3)
Panel A: Baseline			
4 semiyears before	-0.177 (0.268)	-0.239 (0.231)	-0.310 (0.270)
6 semiyears after	5.595*** (0.444)	5.811*** (0.378)	6.383*** (0.443)
4 semiyears before × high capacity	-0.279 (0.620)	0.633 (0.539)	0.130 (0.627)
6 semiyears after × high capacity	2.911*** (0.642)	1.861*** (0.550)	2.766*** (0.644)
Panel B: Drop Beijing, Shanghai			
4 semiyears before	-0.179 (0.264)	-0.242 (0.166)	-0.277 (0.249)
6 semiyears after	5.511*** (0.423)	5.873*** (0.264)	6.286*** (0.397)
4 semiyears before × high capacity	-0.114 (0.634)	0.763* (0.404)	0.235 (0.603)
6 semiyears after × high capacity	2.983*** (0.641)	1.118*** (0.403)	2.863*** (0.605)
Panel C: Firm based outside contract province			
4 semiyears before	-0.195 (0.209)	-0.165 (0.245)	-0.293 (0.218)
6 semiyears after	5.254*** (0.333)	5.862*** (0.387)	6.153*** (0.346)
4 semiyears before × high capacity	-0.053 (0.555)	0.721 (0.658)	0.177 (0.586)
6 semiyears after × high capacity	2.365*** (0.542)	2.747*** (0.636)	2.815*** (0.567)

Notes: Specifications include full set of time indicators and interactions with public security contracts; only selected coefficient estimates are presented. Standard errors clustered at mother firm level are reported in parentheses. Panel A replicates baseline specification in Table A.6, Columns 1-3. Panel B excludes contracts from Beijing and Shanghai (the two highest capacity prefectures/provinces), and Panel C restricts the analysis to firms that have their first contract outside of their home province. * significant at 10% ** significant at 5% *** significant at 1%.

Appendix A Proofs

Appendix A.1 Existence and uniqueness of a BGP equilibrium with entry of all types of firms

Proposition 1 (Existence and Uniqueness) *Let $p_z(p_c)$ be the implicit function defined by the pricing equation (4) and $p_d(p_c)$ be the implicit function defined by*

$$\Pi_c(0, p_c, p_d) = \mu_z \Pi_z(p_z(p_c)). \quad (23)$$

Let $p_g(\bar{d}_g)$ be the unique solution to

$$\kappa_g \frac{\Pi_g(p_g, \bar{d}_g)}{p_g} \frac{\chi}{1 + \beta(\chi - 1)} = \bar{d}_g. \quad (24)$$

Given price p_c , a necessary condition for a BGP with $\tilde{N}_c/N_z > 0$ and $N_g/N_z > 0$ to exist is

$$\frac{q_c(0, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(0, p_c, p_d(p_c))} < \frac{Y_c}{D_p} = \frac{\left(\frac{p_c}{1-a}\right)^{-\epsilon}}{\kappa_p} < \frac{q_c(\bar{d}_g, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(\bar{d}_g, p_c, p_d(p_c))}. \quad (25)$$

If the condition above holds, sufficient conditions for a unique equilibrium to exist are

$$\gamma > 1 + \beta(\chi - 1) \quad (26)$$

$$\Pi_g(p_g(\bar{d}_g), \bar{d}_g) + \Pi_c(\bar{d}_g, \underline{p}_c, p_d(\underline{p}_c)) - \left(2 + \frac{F}{\lambda}\right) \Pi_c(0, \underline{p}_c, p_d(\underline{p}_c)) < 0 \quad (27)$$

$$\Pi_g(p_g(\bar{d}_g), \bar{d}_g) + \Pi_c(\bar{d}_g, \bar{p}_c, p_d(\bar{p}_c)) - \left(2 + \frac{F}{\lambda}\right) \Pi_c(0, \bar{p}_c, p_d(\bar{p}_c)) > 0, \quad (28)$$

where \underline{p}_c and \bar{p}_c are the smallest and largest p_c such that $p_z(p_c), p_d(p_c)$ are strictly positive.

We now proceed to prove this proposition. From the representative household's Euler equation, we obtain that in a BGP:

$$r = \theta\eta + \rho \quad (29)$$

Moreover, market clearing in the goods and data markets requires:¹

$$\tilde{N}_c q_c(0, p_c, p_d)^{1-\frac{1}{\chi}} + N_g q_c(\bar{d}_g, p_c, p_d)^{1-\frac{1}{\chi}} = Y_c = \left(\frac{p_c}{1-a}\right)^{-\epsilon} Y \quad (30)$$

$$N_z q_z(p_z)^{1-\frac{1}{\chi}} = Y_z = \left(\frac{p_z}{a}\right)^{-\epsilon} Y \quad (31)$$

$$N_g q_g(\bar{d}_g, p_g)^{1-\frac{1}{\chi}} = Y_g = G \quad (32)$$

$$\tilde{N}_c d_p(0, p_c, p_d) + N_g d_p(\bar{d}_g, p_c, p_d) = D_p = \kappa_p Y \quad (33)$$

¹Note that, as for the case of government data, we assume that private data is not sharable across firms. This can be seen from (33). Again, we abstract from the sharability of data across firms to transparently focus on the implications of the sharability of data across uses *within* a firm.

$$N_g \bar{d}_g = D_g = \kappa_g G, \quad (34)$$

From (4), it is straightforward to see that $p_z(p_c)$ exist and has a negative derivative. Equations (23) follows directly from the free-entry conditions of private innovators. Then, $p_d(p_c)$ exists and has a positive derivative since profit functions are increasing in their output price and decreasing in the data input price.

Equation (24) follows from the fact that $\Pi_g(p_g, \bar{d}_g) = p_g q_g(p_g, \bar{d}_g)^{1-\frac{1}{\chi}} \frac{1+\beta(\chi-1)}{\chi}$ together with market clearing in the government data and goods markets.

Then, combining the market clearing conditions in the private data and goods markets, we obtain \tilde{N}_c/N_z and N_g/N_z as functions of p_c :

$$\begin{bmatrix} \frac{\tilde{N}_c}{N_z} \\ \frac{N_g}{N_z} \end{bmatrix} = \begin{bmatrix} q_c(0, p_c, p_d(p_c))^{1-\frac{1}{\chi}} & q_c(\bar{d}_g, p_c, p_d(p_c))^{1-\frac{1}{\chi}} \\ d_p(0, p_c, p_d(p_c)) & d_p(\bar{d}_g, p_c, p_d(p_c)) \end{bmatrix}^{-1} \begin{bmatrix} \frac{Y_c}{N_z} \\ \frac{D_p}{N_z} \end{bmatrix}$$

$$\begin{bmatrix} \frac{Y_c}{N_z} \\ \frac{D_p}{N_z} \end{bmatrix} = \begin{bmatrix} \left(\frac{p_c}{1-a}\right)^{-\epsilon} \\ \kappa_p \end{bmatrix} \left(\frac{p_z(p_c)}{a}\right)^\epsilon q_z(p_z(p_c))^{1-\frac{1}{\chi}}.$$

When the determinant of the square matrix is negative, then $\tilde{N}_c/N_z > 0$ and $N_g/N_z > 0$ if and only if the inequalities in (25) hold. We now show that the determinant is indeed negative. This requires showing that

$$\frac{q_c(\bar{d}_g, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(\bar{d}_g, p_c, p_d(p_c))} > \frac{q_c(0, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(0, p_c, p_d(p_c))},$$

which is also necessary for (25) to hold.

The optimality condition for private data demand is,

$$d_p^{\frac{1}{\gamma}} \left(\alpha (\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha) (d_p)^{\frac{\gamma-1}{\gamma}} \right)^{\frac{1}{\gamma-1} \left(\frac{\gamma}{1+\beta(\chi-1)} - 1 \right)} = \frac{(1-\alpha)}{p_d} (p_c)^{\frac{\chi}{1+\beta(\chi-1)}} \beta \left(\frac{(1-\beta)}{\phi} \right)^{\frac{(1-\beta)(\chi-1)}{1+\beta(\chi-1)}}. \quad (35)$$

Then, using the definition of $q_c(\cdot)$, we obtain

$$\frac{q_c(\bar{d}_g, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(\bar{d}_g, p_c, p_d(p_c))} = \frac{\chi}{\chi-1} \frac{p_d(p_c)}{\beta p_c} \left(\frac{\alpha}{(1-\alpha)} \left(\frac{\bar{d}_g}{d_p(\bar{d}_g, p_c, p_d(p_c))} \right)^{\frac{\gamma-1}{\gamma}} + 1 \right) \quad (36)$$

$$= \frac{q_c(0, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(0, p_c, p_d(p_c))} \left(\frac{\alpha}{(1-\alpha)} \left(\frac{\bar{d}_g}{d_p(\bar{d}_g, p_c, p_d(p_c))} \right)^{\frac{\gamma-1}{\gamma}} + 1 \right) \quad (37)$$

$$> \frac{q_c(0, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(0, p_c, p_d(p_c))}. \quad (38)$$

To conclude the proof, we need to show conditions under which p_c exists and is unique. From the free-entry conditions for software producing firms, we obtain one equation that

implicitly defines p_c :

$$\Pi_g(p_g(\bar{d}_g), \bar{d}_g) + \Pi_c(\bar{d}_g, p_c, p_d(p_c)) - \left(2 + \frac{F}{\lambda}\right) \Pi_c(0, p_c, p_d(p_c)) = 0.$$

We first show that $\gamma > 1 + \beta(\chi - 1)$ is a sufficient condition for the left-hand-side (LHS) of this equation to be strictly increasing in p_c . Totally differentiating

$$\begin{aligned} \frac{\partial LHS}{\partial p_c} &= \frac{\partial \Pi_c(\bar{d}_g, p_c, p_d)}{\partial p_c} - \left(2 + \frac{F}{\lambda}\right) \frac{\partial \Pi_c(0, p_c, p_d)}{\partial p_c} + \left(\frac{\partial \Pi_c(\bar{d}_g, p_c, p_d)}{\partial p_d} - \left(2 + \frac{F}{\lambda}\right) \frac{\partial \Pi_c(0, p_c, p_d)}{\partial p_d} \right) \frac{\partial p_d}{\partial p_c} \\ &= \frac{\partial \Pi_c(\bar{d}_g, p_c, p_d)}{\partial p_c} - \left(2 + \frac{F}{\lambda}\right) \frac{\partial \Pi_c(0, p_c, p_d)}{\partial p_c} \\ &\quad + \left(\frac{\frac{\partial \Pi_c(\bar{d}_g, p_c, p_d)}{\partial p_d}}{\frac{\partial \Pi_c(0, p_c, p_d)}{\partial p_d}} - \left(2 + \frac{F}{\lambda}\right) \right) \left(\mu_z \frac{\partial \Pi_z(p_z)}{\partial p_z} \frac{\partial p_z}{\partial p_c} - \frac{\partial \Pi_c(0, p_c, p_d)}{\partial p_c} \right) \\ &= q_c(\bar{d}_g, p_c, p_d)^{1-\frac{1}{\chi}} - \left(2 + \frac{F}{\lambda}\right) q_c(0, p_c, p_d)^{1-\frac{1}{\chi}} \\ &\quad + \left(\left(2 + \frac{F}{\lambda}\right) - \frac{d_p(\bar{d}_g, p_c, p_d)}{d_p(0, p_c, p_d)} \right) \left(q_c(0, p_c, p_d)^{1-\frac{1}{\chi}} - \mu_z \frac{\partial \Pi_z(p_z)}{\partial p_z} \frac{\partial p_z}{\partial p_c} \right) \\ &= \left(\frac{q_c(\bar{d}_g, p_c, p_d)^{1-\frac{1}{\chi}}}{d_p(\bar{d}_g, p_c, p_d)} - \frac{q_c(0, p_c, p_d)^{1-\frac{1}{\chi}}}{d_p(0, p_c, p_d)} \right) d_p(\bar{d}_g, p_c, p_d) \\ &\quad - \left(\left(2 + \frac{F}{\lambda}\right) - \frac{d_p(\bar{d}_g, p_c, p_d)}{d_p(0, p_c, p_d)} \right) \mu_z \frac{\partial \Pi_z(p_z)}{\partial p_z} \frac{\partial p_z}{\partial p_c} \\ &> - \left(\left(2 + \frac{F}{\lambda}\right) - \frac{d_p(\bar{d}_g, p_c, p_d)}{d_p(0, p_c, p_d)} \right) \mu_z \frac{\partial \Pi_z(p_z)}{\partial p_z} \frac{\partial p_z}{\partial p_c} \\ &> 0. \end{aligned}$$

The second equality follows from the implicit function $p_d(p_c)$, the third equality from the envelope theorem, and the fourth equality simply rearranges terms. The first inequality follows from the fact that we have shown above that $\frac{q_c(\bar{d}_g, p_c, p_d)^{1-\frac{1}{\chi}}}{d_p(\bar{d}_g, p_c, p_d)} > \frac{q_c(0, p_c, p_d)^{1-\frac{1}{\chi}}}{d_p(0, p_c, p_d)}$. The last inequality follows from the fact that $\frac{\partial \Pi_z(p_z)}{\partial p_z} \frac{\partial p_z}{\partial p_c} < 0$ and that, from (35), we have that when $\gamma > 1 + \beta(\chi - 1)$, the function $d_p(\bar{d}_g, p_c, p_d)$ is weakly decreasing in \bar{d}_g . As such, $\frac{d_p(\bar{d}_g, p_c, p_d)}{d_p(0, p_c, p_d)} \leq 1$ and the inequality holds.

Finally, since when $\gamma > 1 + \beta(\chi - 1)$ the LHS is increasing in p_c , Bolzano's theorem implies that a necessary and sufficient condition for p_c to exist and be unique is that the LHS evaluated at the smallest (largest) p_c is negative (positive). The last two equations in the theorem state these conditions.

Appendix A.2 Proof of Theorem 1

We first show the comparative statics of η and n_c with respect to changes in \bar{d}_g . We then provide intuition for the result.

Part 1. Rate of Innovation Totally differentiating the free-entry conditions, we obtain

$$\begin{aligned}\frac{\partial p_c}{\partial \bar{d}_g} &= - \frac{\frac{\partial \Pi_g(\bar{d}_g, p_g)}{\partial \bar{d}_g} + \frac{\partial \Pi_g(\bar{d}_g, p_g)}{\partial p_g} \frac{\partial p_g}{\partial \bar{d}_g} + \frac{\partial \Pi_c(\bar{d}_g, p_c, p_d)}{\partial \bar{d}_g}}{- \left(\left(2 + \frac{F}{\lambda} \right) - \frac{d_p(\bar{d}_g, p_c, p_d)}{d_p(0, p_c, p_d)} \right) \mu_z \frac{\partial \Pi_z(p_z)}{\partial p_z} \frac{\partial p_z}{\partial p_c} + d_p(\bar{d}_g, p_c, p_d) \left(\frac{q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}}}{d_p(\bar{d}_g, p_c, p_d)} - \frac{q_c(0, p_c, p_d)^{\frac{\chi-1}{\chi}}}{d_p(0, p_c, p_d)} \right)} \\ \frac{\partial p_d}{\partial \bar{d}_g} &= - \left(\mu_z \frac{\partial \Pi_z(p_z)}{\partial p_z} \frac{\partial p_z}{\partial p_c} - q_c(0, p_c, p_d)^{\frac{\chi-1}{\chi}} \right) \frac{1}{d_p(0, p_c, p_d)} \frac{\partial p_c}{\partial \bar{d}_g}.\end{aligned}$$

We have shown in the proof of Proposition 1 that the denominator in $\frac{\partial p_c}{\partial \bar{d}_g}$ is positive. The numerator is positive as well since $p_g(\bar{d}_g)$ is increasing in \bar{d}_g . Taken together, they imply that

$$\frac{\partial p_z}{\partial \bar{d}_g} > 0, \frac{\partial p_d}{\partial \bar{d}_g} < 0, \frac{\partial p_c}{\partial \bar{d}_g} < 0.$$

And, finally, using the expressions for $\eta = (r - \rho)/\theta = (\mu_z \Pi_z(p_z(p_c)) - \rho)/\theta$, we get that

$$\frac{\partial \eta}{\partial \bar{d}_g} > 0.$$

Part 2. Direction of Innovation From the market clearing conditions in the commercial goods market we have

$$\begin{aligned}\left(\frac{1-a}{a} \frac{p_z}{p_c} \right)^\epsilon &= \frac{Y_c}{Y_z} = \frac{\tilde{N}_c}{N_z} \frac{1}{q_z(p_z)^{\frac{\chi-1}{\chi}}} q_c(0, p_c, p_d)^{\frac{\chi-1}{\chi}} + \frac{N_g}{N_z} \frac{1}{q_z(p_z)^{\frac{\chi-1}{\chi}}} q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}} \\ &= \frac{N_c}{N_z} \frac{q_c(0, p_c, p_d)^{\frac{\chi-1}{\chi}} + q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}}}{q_z(p_z)^{\frac{\chi-1}{\chi}}}.\end{aligned}$$

Thus,

$$\begin{aligned}n_c &= \left(\frac{1-a}{a} \frac{p_z}{p_c} \right)^\epsilon \frac{q_z(p_z)^{\frac{\chi-1}{\chi}}}{q_c(0, p_c, p_d)^{\frac{\chi-1}{\chi}} + q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}}} \\ &= \frac{1-a}{a} \left(\frac{1-a}{a} \frac{p_z}{p_c} \right)^{\epsilon-1} \frac{p_z q_z(p_z)^{\frac{\chi-1}{\chi}}}{p_c q_c(0, p_c, p_d)^{\frac{\chi-1}{\chi}}} \frac{1}{1 + \frac{p_c q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}}}{p_c q_c(0, p_c, p_d)^{\frac{\chi-1}{\chi}}}}\end{aligned}$$

$$\begin{aligned}
&= \frac{1-a}{a} \left(\frac{1-a}{a} \frac{p_z}{p_c} \right)^{\epsilon-1} \frac{\pi_z(p_z)^{\frac{\chi}{1+\beta(\chi-1)}}}{\pi_c(0, p_c, p_d) \chi} \frac{1}{\pi_c(\bar{d}_g, p_c, p_d) \frac{\chi}{1+\beta(\chi-1) \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(\bar{d}_p)^{\frac{\gamma-1}{\gamma}}}} \\
&= \frac{1-a}{a} \left(\frac{1-a}{a} \frac{p_z}{p_c} \right)^{\epsilon-1} \frac{1}{\mu_z} \frac{1}{1+\beta(\chi-1)} \frac{1}{1 + (2 + \frac{F}{\lambda}) \frac{\pi_c(\bar{d}_g, p_c, p_d)}{\pi_g(\bar{d}_g, p_g) + \pi_c(\bar{d}_g, p_c, p_d)} \frac{1}{1+\beta(\chi-1) \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(\bar{d}_p)^{\frac{\gamma-1}{\gamma}}}},
\end{aligned}$$

where the third line follows from the fact $\pi_z(p_z) = p_z q_z(p_z)^{\frac{\chi-1}{\chi} \frac{1+\beta(\chi-1)}{\chi}}$, $\pi_c(0, p_c, p_d) = p_c q_c(0, p_c, p_d)^{\frac{\chi-1}{\chi} \frac{1}{\chi}}$, and $\pi_c(\bar{d}_g, p_c, p_d) = p_c q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi} \frac{1+\beta(\chi-1) \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(\bar{d}_p)^{\frac{\gamma-1}{\gamma}}}{\chi}}$. The last line follows from the free-entry conditions.

Then, differentiating

$$\frac{d \log(n_c)}{d \log(\bar{d}_g)} > (\epsilon - 1) \frac{d \log\left(\frac{p_z}{p_c}\right)}{d \log(\bar{d}_g)} - \frac{\frac{\Pi_c(\bar{d}_g, p_c, p_d)}{\Pi_g(\bar{d}_g, p_g) + \Pi_c(\bar{d}_g, p_c, p_d)} \frac{(2 + \frac{F}{\lambda})}{1+\beta(\chi-1) \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(\bar{d}_p)^{\frac{\gamma-1}{\gamma}}}}{1 + \frac{\Pi_c(\bar{d}_g, p_c, p_d)}{\Pi_g(\bar{d}_g, p_g) + \Pi_c(\bar{d}_g, p_c, p_d)} \frac{(2 + \frac{F}{\lambda})}{1+\beta(\chi-1) \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(\bar{d}_p)^{\frac{\gamma-1}{\gamma}}}} \frac{d \log\left(\frac{\Pi_c(\bar{d}_g, p_c, p_d)}{\Pi_g(\bar{d}_g, p_g) + \Pi_c(\bar{d}_g, p_c, p_d)}\right)}{d \log(\bar{d}_g)},$$

where the inequality follows from the fact that we have shown before that $\frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(\bar{d}_p)^{\frac{\gamma-1}{\gamma}}}$ increases with \bar{d}_g when $\gamma > (1 + \beta(\chi - 1))$, which is one of the conditions we imposed for the BGP to exist and be unique.

We have also shown before that $\frac{d \log(p_z)}{d \log(\bar{d}_g)} > 0$, $\frac{d \log(p_c)}{d \log(\bar{d}_g)} < 0$. We thus have two cases.

First, if $\frac{d \log\left(\frac{\Pi_c(\bar{d}_g, p_c, p_d)}{\Pi_g(\bar{d}_g, p_g) + \Pi_c(\bar{d}_g, p_c, p_d)}\right)}{d \log(\bar{d}_g)} > 0$, then we can directly see from the expression above that $\epsilon \geq 1$ is a sufficient condition for $\frac{d \log(n_c)}{d \log(\bar{d}_g)} > 0$.

Second, if $\frac{d \log\left(\frac{\Pi_c(\bar{d}_g, p_c, p_d)}{\Pi_g(\bar{d}_g, p_g) + \Pi_c(\bar{d}_g, p_c, p_d)}\right)}{d \log(\bar{d}_g)} < 0$, we next show that $\epsilon \geq \frac{\chi + \beta(\chi - 1)}{1 + \beta(\chi - 1)}$ is a sufficient condition for $\frac{d \log(n_c)}{d \log(\bar{d}_g)} > 0$. Since, $\frac{\chi + \beta(\chi - 1)}{1 + \beta(\chi - 1)} > 1$, this condition is sufficient in the first case as well.

Since the term multiplying $\frac{d \log(p_z)}{d \log(\bar{d}_g)} > 0$, $\frac{d \log(p_c)}{d \log(\bar{d}_g)}$ is less than 1, we have that

$$\frac{d \log(n_c)}{d \log(\bar{d}_g)} > (\epsilon - 1) \frac{d \log\left(\frac{p_z}{p_c}\right)}{d \log(\bar{d}_g)} - \frac{d \log\left(\frac{\Pi_c(\bar{d}_g, p_c, p_d)}{\Pi_g(\bar{d}_g, p_g) + \Pi_c(\bar{d}_g, p_c, p_d)}\right)}{d \log(\bar{d}_g)}$$

$$\begin{aligned}
&= (\epsilon - 1) \frac{d\log\left(\frac{p_z}{p_c}\right)}{d\log(\bar{d}_g)} - \frac{\Pi_g(\bar{d}_g, p_g)}{\Pi_g(\bar{d}_g, p_g) + \Pi_c(\bar{d}_g, p_c, p_d)} \left(\frac{d\log(\Pi_c(\bar{d}_g, p_c, p_d))}{d\log(\bar{d}_g)} - \frac{d\log\Pi_g(\bar{d}_g, p_g)}{d\log(\bar{d}_g)} \right) \\
&> (\epsilon - 1) \frac{d\log\left(\frac{p_z}{p_c}\right)}{d\log(\bar{d}_g)} + \left(\frac{d\log\Pi_g(\bar{d}_g, p_g)}{d\log(\bar{d}_g)} - \frac{d\log(\Pi_c(\bar{d}_g, p_c, p_d))}{d\log(\bar{d}_g)} \right),
\end{aligned}$$

where the last inequality follows from the fact that $\frac{\Pi_g(\bar{d}_g, p_g)}{\Pi_g(\bar{d}_g, p_g) + \Pi_c(\bar{d}_g, p_c, p_d)} < 1$.

Moreover, combining the market clearing conditions in the markets for government goods (32) and data (34), we obtain $p_g(\bar{d}_g)$ and then

$$\frac{d\log(\Pi_g(\bar{d}_g, p_g(\bar{d}_g)))}{d\log(\bar{d}_g)} = \frac{\frac{\chi}{(1-\beta)(\chi-1)} + \beta(\chi-1)}{1 + \beta(\chi-1)}.$$

Furthermore, we have that

$$\begin{aligned}
\frac{d\log(\Pi_c(\bar{d}_g, p_c, p_d))}{d\log(\bar{d}_g)} &= \frac{\gamma}{\gamma-1} \beta \frac{\chi-1}{\chi} \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}} \\
&\quad + \frac{p_c q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}}}{\Pi_c(\bar{d}_g, p_c, p_d)} \frac{d\log p_c}{d\log \bar{d}_g} - \frac{p_d d_p(\bar{d}_g, p_c, p_d)}{\Pi_c(\bar{d}_g, p_c, p_d)} \frac{d\log p_d}{d\log \bar{d}_g} \\
&= \frac{\gamma}{\gamma-1} \beta \frac{\chi-1}{\chi} \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}} + \frac{d\log p_d}{d\log \bar{d}_g} \\
&\quad + \frac{p_c q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}}}{\Pi_c(\bar{d}_g, p_c, p_d)} \left(\frac{d\log p_c}{d\log \bar{d}_g} - \left(1 - (1-\beta) \frac{\chi-1}{\chi} \right) \frac{d\log p_d}{d\log \bar{d}_g} \right) \\
&= \frac{\gamma}{\gamma-1} \beta \frac{\chi-1}{\chi} \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}} + \frac{d\log p_d}{d\log \bar{d}_g} \\
&\quad + \frac{\chi}{1 + \beta(\chi-1) \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}}} \left(\frac{d\log p_c}{d\log \bar{d}_g} - \left(1 - (1-\beta) \frac{\chi-1}{\chi} \right) \frac{d\log p_d}{d\log \bar{d}_g} \right),
\end{aligned}$$

where the first line uses the envelope theorem, the second line uses that $\Pi_c(\bar{d}_g, p_c, p_d) = p_c q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}} - p_d d_p(\bar{d}_g, p_c, p_d) - \phi x(\bar{d}_g, p_c, p_d)$ and that $\phi x(\bar{d}_g, p_c, p_d) = (1-\beta) \frac{\chi-1}{\chi} p_c q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}}$,

and the last line uses that $\Pi_c(\bar{d}_g, p_c, p_d) = p_c q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}} \frac{1 + \beta(\chi-1) \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}}}{\chi}$.

Also, from the free entry condition $\Pi_c(0, p_c, p_d) = \mu_z \Pi_z(p_z)$, we have that

$$\frac{d\log(p_d)}{d\log(\bar{d}_g)} = \frac{1}{\beta} \frac{d\log(p_c)}{d\log(\bar{d}_g)} - \frac{1}{\beta} \frac{1}{1 + \beta(\chi-1)} \frac{d\log(p_z)}{d\log(\bar{d}_g)}. \quad (39)$$

Replacing, we obtain

$$\begin{aligned}
\frac{d\log(\Pi_c(\bar{d}_g, p_c, p_d))}{d\log(\bar{d}_g)} &= \frac{\frac{\gamma}{\gamma-1}\beta\frac{\chi-1}{\chi}\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}} + \frac{\frac{d\log(p_c)}{d\log(\bar{d}_g)} + \frac{1}{\beta}\frac{d\log(p_z/p_c)}{d\log(\bar{d}_g)}}{1 + \beta(\chi-1)\frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}}} \\
&+ \frac{d\log(p_c)}{d\log(\bar{d}_g)}\frac{(\chi-1)}{1 + \beta(\chi-1)} - \frac{1}{1 + \beta(\chi-1)}\frac{1}{\beta}\frac{d\log(p_z/p_c)}{d\log(\bar{d}_g)} \\
&< \frac{\gamma}{\gamma-1}\beta\frac{\chi-1}{\chi} + \frac{\beta(\chi-1)}{1 + \beta(\chi-1)}\frac{1}{\beta}\frac{d\log(p_z/p_c)}{d\log(\bar{d}_g)},
\end{aligned}$$

where the inequality follows from $\frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}} < 1$ and $\frac{d\log(p_c)}{d\log(\bar{d}_g)} < 0$.

Finally, using the inequality on $\frac{d\log(\Pi_c(\bar{d}_g, p_c, p_d))}{d\log(\bar{d}_g)}$ and the expression for $\frac{d\log(\Pi_g(\bar{d}_g, p_g, \bar{d}_g))}{d\log(\bar{d}_g)}$, we obtain

$$\begin{aligned}
\frac{d\log(n_c)}{d\log(\bar{d}_g)} &> (\epsilon - 1)\frac{d\log\left(\frac{p_z}{p_c}\right)}{d\log(\bar{d}_g)} + \left(\frac{d\log\Pi_g(\bar{d}_g, p_g)}{d\log(\bar{d}_g)} - \frac{d\log(\Pi_c(\bar{d}_g, p_c, p_d))}{d\log(\bar{d}_g)}\right) \\
&> (\epsilon - 1)\frac{d\log\left(\frac{p_z}{p_c}\right)}{d\log(\bar{d}_g)} + \left(\frac{\frac{\chi}{(1-\beta)(\chi-1)} + \beta(\chi-1)}{1 + \beta(\chi-1)} - \frac{\gamma}{\gamma-1}\beta\frac{\chi-1}{\chi} - \frac{(\chi-1)}{1 + \beta(\chi-1)}\frac{d\log(p_z/p_c)}{d\log(\bar{d}_g)}\right) \\
&= \left(\epsilon - \frac{\chi + \beta(\chi-1)}{1 + \beta(\chi-1)}\right)\frac{d\log\left(\frac{p_z}{p_c}\right)}{d\log(\bar{d}_g)} + \frac{\frac{\chi}{(1-\beta)(\chi-1)} + \beta(\chi-1)}{1 + \beta(\chi-1)} - \frac{\gamma}{\gamma-1}\beta\frac{\chi-1}{\chi} \\
&> \left(\epsilon - \frac{\chi + \beta(\chi-1)}{1 + \beta(\chi-1)}\right)\frac{d\log\left(\frac{p_z}{p_c}\right)}{d\log(\bar{d}_g)} + \frac{\frac{\chi}{(1-\beta)(\chi-1)} + \beta(\chi-1)}{1 + \beta(\chi-1)} - \frac{1 + \beta(\chi-1)}{\beta(\chi-1)}\beta\frac{\chi-1}{\chi} \\
&= \left(\epsilon - \frac{\chi + \beta(\chi-1)}{1 + \beta(\chi-1)}\right)\frac{d\log\left(\frac{p_z}{p_c}\right)}{d\log(\bar{d}_g)} + \frac{1}{(1-\beta)(\chi-1)} + \frac{(1-\beta)(\chi-1)}{\chi},
\end{aligned}$$

where the last inequality follows from the fact that $\gamma > 1 + \beta(\chi-1)$ is a condition for the BGP to exist and be unique. Then, to conclude, since $\frac{d\log\left(\frac{p_z}{p_c}\right)}{d\log(\bar{d}_g)} > 0$, a sufficient condition for $\frac{d\log(n_c)}{d\log(\bar{d}_g)} > 0$ is that $\epsilon \geq \frac{\chi + \beta(\chi-1)}{1 + \beta(\chi-1)}$.

Intuition To understand the theorem, it helps to consider the construction of a BGP equilibrium given an exogenous increase in \bar{d}_g and p_g (instead of just \bar{d}_g). The exogenous increase directly results in higher profits for those software firms obtaining government contracts through two channels. First, through higher revenues from government software production, because of both the higher p_g and productivity due the increase in \bar{d}_g . Second, through higher revenues from private software production, due to higher productivity

when government data is shared across uses.

The higher profitability results in more R&D spending in innovation. In a BGP with free entry of innovators, the opportunity cost of investment (r) has to increase until innovators are again ex-ante indifferent between introducing a new variety or not. Furthermore, the increase in r is necessary to give the signal to households to invest more of their resources, which is ultimately consistent with the BGP increase in R&D spending and, as such, in the rate of innovation η .

However, note that the above logic holds for given prices p_z, p_c, p_d . Yet, at the new higher opportunity cost r , private software only and non-software innovators would not want to introduce new varieties at the old prices. Thus, in a BGP where all three types of firms are present, it has to be that prices change such that profits increase for these other firms not directly affected by the increase in \bar{d}_g and p_g . For non-software innovators, this requires that p_z increases — which then implies that p_c has to fall so that the final goods representative firm makes zero profits (equation (4)). For private software only innovators, this requires that p_d falls to compensate for both the fall in p_c and the increase in r . Finally, under the sufficient conditions for existence and uniqueness of a BGP equilibrium, the direct effect of the increase in \bar{d}_g dominates the second round, general equilibrium effects of the changes in prices so that the overall change in η goes in the same direction as the one determined by the direct effect.

Note that the above construction determines p_c, p_z, p_d, r and η as implicit functions of \bar{d}_g, p_g purely from the free-entry conditions of firms and the Euler equation for households. Next, we turn to the market clearing conditions to understand the change in the direction of private innovation n_c . From the definition of n_c together with equations (30) and (31), we obtained before:

$$n_c = \underbrace{\left(\frac{1-a}{a} \frac{p_z}{p_c} \right)^\epsilon}_{=\frac{Y_c}{Y_z}} \frac{q_z(p_z)^{\frac{\chi-1}{\chi}}}{q_c(0, p_c, p_d)^{\frac{\chi-1}{\chi}} + q_c(\bar{d}_g, p_c, p_d)^{\frac{\chi-1}{\chi}}}. \quad (40)$$

Thus, there are two countervailing effects on the direction of private innovation from the increase in \bar{d}_g, p_g . First, the increase in p_z and decrease in p_c result in an increase in the relative demand for private software $\frac{Y_c}{Y_z}$. This demand effect biases the direction of innovation more towards private software (increases n_c). Second, the combined increase in \bar{d}_g and changes in p_c, p_d may potentially result in an increase in the relative output of private software per firm (the second term decreases). This decreases n_c . The theorem shows that, if demand is sufficiently elastic ($\epsilon \geq \frac{\chi+\beta(\chi-1)}{1+\beta(\chi-1)}$) and the conditions for a BGP to exist and be unique are satisfied, then the demand effect dominates and n_c increases.

To conclude the intuition for the theorem, consider the market clearing condition for government data (34). When \bar{d}_g is higher, more government data needs to be supplied to those firms obtaining government contracts. Yet, at the old p_g , the increase in government software production and thus government data as a by-product $\kappa_g q_g(\bar{d}_g, p_g)^{1-\frac{1}{\chi}}$ is insufficient to match the required demand. This is because there are decreasing returns to \bar{d}_g and thus the supply increases less than proportionally. Thus, it has to be that p_g increases as well so that $q_g(\bar{d}_g, p_g)^{1-\frac{1}{\chi}}$ further increases to match the required increased in \bar{d}_g .

SUPPLEMENTARY MATERIAL (NOT FOR PUBLICATION)



Figure S.1: Example of AI firm record from *Tianyancha* (excerpt).

Highlights

Employees

1,000

As of 24-Oct-2018



Last Deal Details

Undisclosed

Later Stage VC 06-May-2019

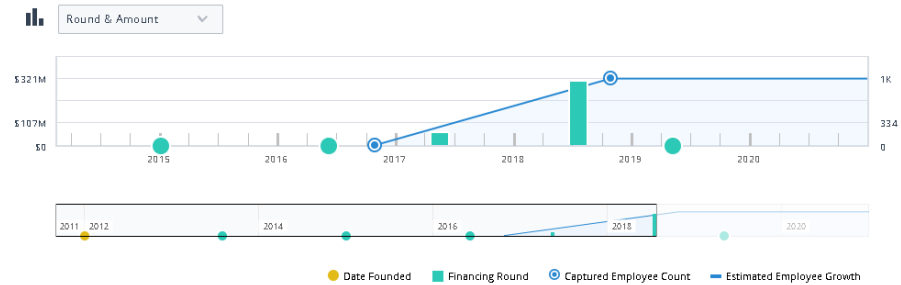
Total Raised to Date

\$355.16M

As of 06-May-2019

[Edit Highlights](#)

Timeline



General Information

Description

Provider and developer of artificial intelligence technology used in the fields of smart cities, smart medical, and smart commerce. The company is engaged in the research of computer vision, image and video intelligent understanding, distributed system and big data application, it offers traffic management software, medical diagnostic technology and intelligent hardware, enabling companies to apply AI technology in their products.

Most Recent Financing Status (as of 13-Feb-2020)

The company raised an undisclosed amount of venture funding from [REDACTED]

Previously, the company raised \$300 million of Series C+ venture funding from [REDACTED]

Website

Entity Types

Private Company

Acquirer

Financing Status

Venture Capital-Backed

Year Founded

2012

Legal Name

[REDACTED]

Universe

Venture Capital

Business Status

Generating Revenue

Employees

1,000

Ownership Status

Privately Held (backing)

[View Employee History](#)

Industries & Verticals

Primary Industry

Business/Productivity Software

Verticals

Artificial Intelligence & Machi...

Big Data

Digital Health

TMT

What PitchBook Analysts Say

[View More Analyst Insights](#)

"Both incumbents and startups are developing new hardware. While Google is putting their custom tensor processing units (TPUs) to use for many recent breakthroughs, independent leaders such as Cerebras and Graphcore have raised significant capital and developed other novel designs to cater to AI & ML applications."

| 10-Dec-2019 | Cameron Stanfill | Artificial Intelligence & Machine Learning +3

Contact Information

Primary Contact

[REDACTED]

Co-Founder & Chief Executive Officer

Phone: [REDACTED]

[Add](#)

Primary Office

[REDACTED]

[REDACTED]

[REDACTED]

[REDACTED]

China

Phone: [REDACTED]

Alternate Offices (4)

Beijing

[REDACTED]

[REDACTED]

[REDACTED]

China

Phone: [REDACTED]

Figure S.2: Example of AI firm record from *Pitchbook* (excerpt).

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道路交通安全综合管理平台维护升级项目中标(成交)公告

2016年12月30日 16:26 来源: 中国政府采购网 【打印】 [【显示公告概要】](#)

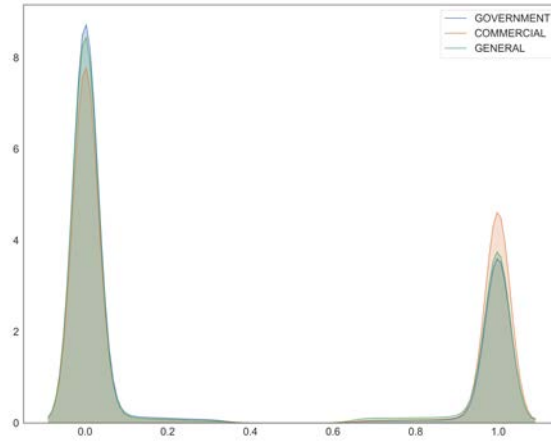
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- 项目编号: [REDACTED]
- 项目序列号: [REDACTED]
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- 项目用途、简要技术要求及合同履行日期: 嵌入式“人脸识别”系统软件开发
- 采购方式: 公开招标
- 采购日期: 2016-12-07
- 公告媒体: [REDACTED]
- 评审时间: 2016-12-29
- 评审地点: [REDACTED]
- 评审委员会成员名单: [REDACTED]
- 定标日期: 2016-12-29
- 中标(成交)信息:

序号	中标供应商	中标供应商地址	主要中标内容	中标金额 (元)
1	网络科技有限公司	[REDACTED]	嵌入式“人脸识别”系统软件开发	639000.00

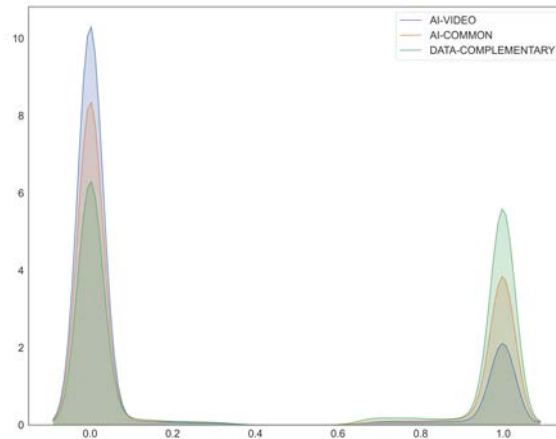
- PPP项目: 否
- 采购人名称: [REDACTED]
 联系地址: [REDACTED]
 项目联系人: [REDACTED]
 联系电话: [REDACTED]
- 采购代理机构全称: [REDACTED]
 联系地址: [REDACTED]
 项目联系人: [REDACTED]
 联系电话: [REDACTED]
- 采购文件上传(PDF格式):
 附件: [REDACTED]
- 书面推荐供应商参加采购活动的采购人和评审专家推荐意见(如有):
 无

贵州贵财招标有限责任公司

Figure S.3: Example of a procurement contract record; source: Chinese Government Procurement Database.



(a) Customers



(b) Function

Figure S.4: Probability density plots of software categorizations based on Recurrent Neural Network with Long Short-Term Memory algorithm. Top panel shows categorization by customers; bottom panel shows categorization by function.

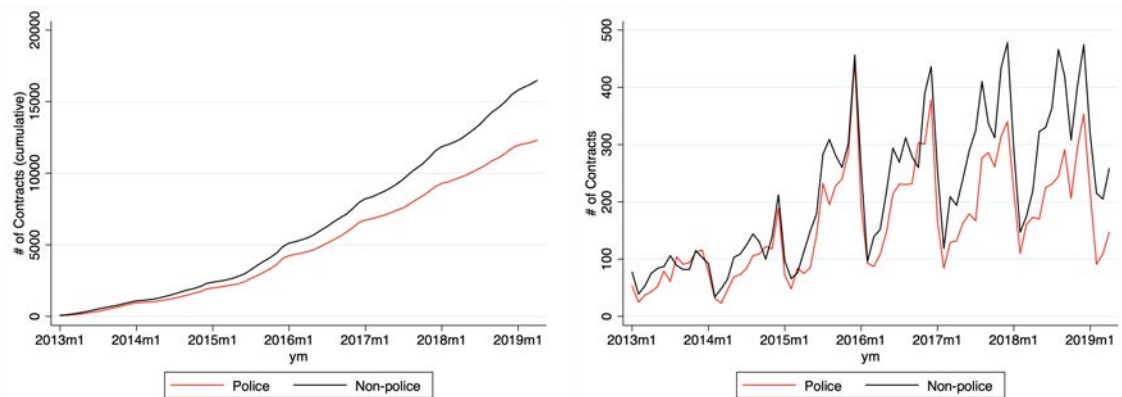


Figure S.5: Cumulative number of public security and non-public security contracts (left panel), and the flow of new contracts signed in each month (right panel).

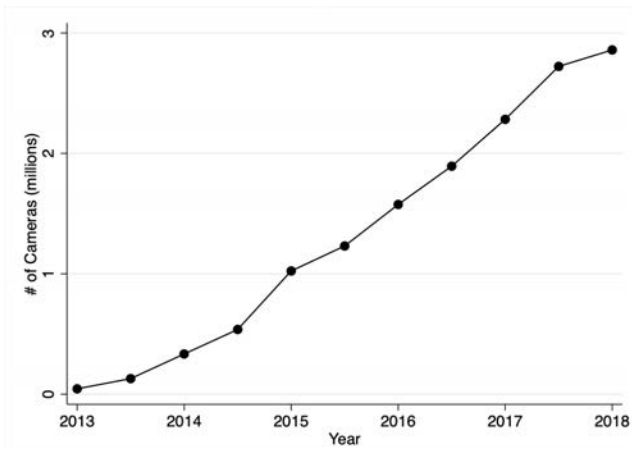


Figure S.6: Number of new public surveillance cameras in China since 2013, as measured by government procurement contracts for cameras. Source: Chinese Government Procurement Database.







	#	Developer	VISA Photos FNMR@ FMR ≤ 0.000001	VISA Photos FNMR@ FMR ≤ 0.0001	MUGSHOT Photos FNMR@ FMR ≤ 0.0001	WILD Photos FNMR@ FMR ≤ 0.00001	CHILD EXP Photos FNMR@ FMR ≤ 0.01	Submission Date
	1	yitu-002	0.004 ¹	0.001 ¹	0.013 ⁷	0.052 ¹³		2018_10_19
	2	yitu-001	0.007 ²	0.003 ⁷	0.013 ⁸	0.058 ²⁶	0.579 ¹³	2018_06_12
	3	sensetime-001	0.009 ³	0.003 ⁶	0.013 ¹¹	1.000 ⁷⁶		2018_10_19
	4	sensetime-002	0.010 ⁴	0.003 ¹⁰	0.015 ²⁹	1.000 ⁷⁷		2018_10_19
	5	siat-002	0.013 ⁵	0.004 ¹⁵	0.014 ¹⁵	0.055 ²⁰	0.428 ⁵	2018_06_13
	6	ntechlab-004	0.013 ⁶	0.003 ⁴	0.013 ¹²	0.046 ⁶	0.420 ²	2018_06_14
	7	ntechlab-005	0.014 ⁷	0.002 ²	0.013 ¹⁰	0.050 ¹⁰		2018_10_19
	8	megvii-002	0.014 ⁸	0.004 ¹²	0.030 ⁶³	0.071 ³⁵		2018_10_19
	9	vocord-005	0.016 ⁹	0.003 ³	0.015 ³²	0.048 ⁹		2018_10_18
	10	everai-001	0.016 ¹⁰	0.004 ¹⁴	0.013 ²	0.031 ²		2018_10_30

Figure S.7: Face Recognition Vendor Test (FRVT) ranking of top facial recognition algorithms, 2018. Source: *National Institute of Standards and Technology (NIST)*.

Table S.1: Top predicted words from LSTM model — non-binary categorization of software

Panel A: Customer type								
Government			Commercial			General		
Chinese	English	Freq. (%)	Chinese	English	Freq. (%)	Chinese	English	Freq. (%)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
交通	Traffic	.603	手机	Mobile Phone	.821	视觉	Vision	.474
威视	Prestige	.382	APP	App	.645	学习	Learning	.378
海康	Haikang	.369	IOS	IOS	.438	腾讯	Tencent	.340
平安	Safety	.351	iOS	iOS	.430	三维	3D	.312
海信	Hisense	.318	企业	Enterprise	.331	识别系统	Recognition System	.301
城市	City	.311	金蝶	Kingdee	.327	算法	Algorithm	.270
金融	Finance	.296	电子	Electronics	.307	计算	Computing	.252
安防	Safety	.281	健康	Health	.212	深度	Depth	.225
数字	Numbers	.272	自助	Self-Help	.209	无人机	Drone	.212
中心	Center	.269	手机游戏	Mobile Game	.201	实时	Real-time	.209
公交	Public Transport	.216	助手	Assistance	.196	认证	Certification	.207
社区	Community	.207	支付	Pay	.191	处理	Processing	.196
调度	Scheduling	.200	后台	Backstage	.189	引擎	Engine	.194
中控	Central Control	.191	门禁	Access Control	.176	技术	Technique	.187
人像	Portrait	.163	人工智能	AI	.174	分布式	Distributed	.183
指挥	Command	.161	车载	Vehicle	.174	仿真	Simulation	.179
辅助	Auxiliary	.159	智能家居	Smart Appliance	.169	网易	Netease	.173
摄像机	Camera	.158	工业	Industry	.169	工具软件	Tool Software	.172
万达	Wanda	.148	DHC	DHC	.168	程序	Program	.170
高速公路	Highway	.148	营销	Marketing	.161	互动	Interactive	.166

Panel B: Function type								
AI-Common			Data-Complementary			AI-Video		
Chinese	English	Freq. (%)	Chinese	English	Freq. (%)	Chinese	English	Freq. (%)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
指纹	Fingerprint	.342	存储	Storage	.206	人脸	Face	1.104
训练	Training	.203	可视化	Visualization	.167	深度	Depth	.321
管家	Housekeeper	.201	一体化	Integration	.164	抓拍	Snapshot	.310
文本	Text	.151	分布式	Distributed	.162	商汤	SenseTime	.287
高速公路	Highway	.150	仿真	Simulation	.157	考勤	Attendance	.258
虹膜	Iris	.147	医学影像	Medical Imaging	.148	科达	Kedacom	.258
汽车	Car	.143	通用	General	.144	跟踪	Track	.249
海尔	Haier	.137	集成	Integrated	.141	全景	Panoramic	.224
WPS	WPS	.134	数据管理	Data Management	.136	广电	Broadcast	.209
翻译	Translate	.126	宇视	UTV	.136	目标	Target/Objective	.189
推荐	Recommend	.124	管控	Manage	.126	车牌	License Plate	.189
图片	Image	.119	高速	High Speed	.126	特征	Feature	.184
测量	Test	.116	媒体	Media/Medium	.125	铂亚	Platinum	.175
征信	Credit	.111	手机软件	Phone Software	.125	预警	Warning	.166
指纹识别	Fingerprint Recognition	.106	设计	Design	.117	运通	American Express	.163
作业	Operation	.106	接口	Interface	.117	指挥	Command	.158
微信	WeChat	.105	开发	Development	.116	统计	Statistics	.149
评估	Assessment	.105	服务器	Server	.116	安居	Safety	.146
灵云	Alcloud	.102	处理软件	Processing Software	.113	SDK	SDK	.141
活体	Living Body	.098	传输	Transmission	.111	布控	Deployment	.141

Supplementary Material B Quantitative analysis

Supplementary Material B.1 $p_g G/Y$ and D_g/Y as a function of \bar{d}_g

We now show that both government spending $p_g G/Y$ and data D_g/Y increase in a BGP whenever \bar{d}_g increases.

We have that

$$\begin{aligned}
 \frac{G}{Y} &= \frac{1}{\kappa_g} \frac{N_G}{N_Z} \frac{\bar{d}_g}{q_z(p_z)^{1-\frac{1}{\chi}} \left(\frac{p_z}{a}\right)^\epsilon} \\
 &= \frac{1}{\kappa_g} \frac{\left(\frac{p_c}{1-a}\right)^{-\epsilon} - \kappa_p \frac{q_c(0, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(0, p_c, p_d(p_c))}}{\frac{q_c(\bar{d}_g, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(\bar{d}_g, p_c, p_d(p_c))} - \frac{q_c(0, p_c, p_d(p_c))^{1-\frac{1}{\chi}}}{d_p(0, p_c, p_d(p_c))}} \frac{\bar{d}_g}{d_p(\bar{d}_g, p_c, p_d(p_c))} \\
 &= \frac{1}{\kappa_g} \frac{1-\alpha}{\alpha} \left(\frac{\chi-1}{\chi} \beta(1-a)^\epsilon \frac{1}{p_d(p_c)} (p_c)^{1-\epsilon} - \kappa_p \right) \left(\frac{\bar{d}_g}{d_p(\bar{d}_g, p_c, p_d(p_c))} \right)^{\frac{1}{\gamma}},
 \end{aligned}$$

where the second equality follows from the solution to N_g/N_z in Theorem 1 and the last equality uses the expressions in (36).

Differentiating,

$$\begin{aligned}
 \frac{d \log(G/Y)}{d \log(\bar{d}_g)} &= - \frac{\frac{\chi-1}{\chi} \beta(1-a)^\epsilon \frac{1}{p_d(p_c)} (p_c)^{1-\epsilon}}{\frac{\chi-1}{\chi} \beta(1-a)^\epsilon \frac{1}{p_d(p_c)} (p_c)^{1-\epsilon} - \kappa_p} \left((\epsilon-1) \frac{d \log(p_c)}{d \log(\bar{d}_g)} + \frac{d \log(p_d)}{d \log(\bar{d}_g)} \right) \\
 &\quad + \frac{1}{\gamma} \left(1 - \frac{d \log d_p(\bar{d}_g, p_c, p_d(p_c))}{d \log(\bar{d}_g)} \right) \\
 &> - \left((\epsilon-1) \frac{d \log(p_c)}{d \log(\bar{d}_g)} + \frac{d \log(p_d)}{d \log(\bar{d}_g)} \right) - \frac{1}{\gamma} \frac{d \log d_p(\bar{d}_g, p_c, p_d(p_c))}{d \log(\bar{d}_g)},
 \end{aligned}$$

where the inequality follows from follows from $\frac{\frac{\chi-1}{\chi} \beta(1-a)^\epsilon \frac{1}{p_d(p_c)} (p_c)^{1-\epsilon}}{\frac{\chi-1}{\chi} \beta(1-a)^\epsilon \frac{1}{p_d(p_c)} (p_c)^{1-\epsilon} - \kappa_p} > 1$.

Moreover, differentiating equation (35), we obtain

$$\begin{aligned}
 \frac{1}{\gamma} \frac{d \log(d_p(\bar{d}_g, p_c, p_d))}{d \log(\bar{d}_g)} &= \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + \frac{\gamma}{1+\beta(\chi-1)}(1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}} \left(\frac{\chi}{1+\beta(\chi-1)} \frac{d \log(p_c)}{d \log(\bar{d}_g)} - \frac{d \log(p_d)}{d \log(\bar{d}_g)} \right) \\
 &\quad - \frac{1}{\gamma} \left(\frac{\gamma}{1+\beta(\chi-1)} - 1 \right) \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + \frac{\gamma}{1+\beta(\chi-1)}(1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}}.
 \end{aligned}$$

Replacing above and using the expression for $\frac{d\log(p_d)}{d\log(\bar{d}_g)}$ in (39), we obtain

$$\begin{aligned}
\frac{d\log(G/Y)}{d\log(\bar{d}_g)} &> - \left(\left(\epsilon + \frac{1-\beta}{\beta} \right) \frac{d\log(p_c)}{d\log(\bar{d}_g)} - \frac{1}{\beta} \frac{1}{1+\beta(\chi-1)} \frac{d\log(p_z)}{d\log(\bar{d}_g)} \right) \\
&\quad - \frac{1}{\gamma} \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + \frac{\gamma}{1+\beta(\chi-1)}(1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}} \frac{1}{\beta} \frac{\frac{d\log(p_z)}{d\log(\bar{d}_g)} - (1-\beta)\frac{d\log(p_c)}{d\log(\bar{d}_g)}}{1+\beta(\chi-1)} \\
&> - \left(\left(\epsilon + \frac{1-\beta}{\beta} \right) \frac{d\log(p_c)}{d\log(\bar{d}_g)} - \frac{1}{\beta} \frac{1}{1+\beta(\chi-1)} \frac{d\log(p_z)}{d\log(\bar{d}_g)} \right) \\
&\quad - \frac{1}{1+\beta(\chi-1)} \frac{1}{\beta} \frac{\frac{d\log(p_z)}{d\log(\bar{d}_g)} - (1-\beta)\frac{d\log(p_c)}{d\log(\bar{d}_g)}}{1+\beta(\chi-1)} \\
&= - \left(\epsilon + \frac{1-\beta}{\beta} \left(1 - \frac{1}{(1+\beta(\chi-1))^2} \right) \right) \frac{d\log(p_c)}{d\log(\bar{d}_g)} + \frac{1}{\beta} \frac{1}{1+\beta(\chi-1)} \frac{\beta(\chi-1)}{1+\beta(\chi-1)} \frac{d\log(p_z)}{d\log(\bar{d}_g)} \\
&> 0,
\end{aligned}$$

where the second line follows from $\gamma > 1 + \beta(\chi - 1)$, and the last line collects terms and comes from the fact that $\frac{d\log(p_c)}{d\log(\bar{d}_g)} < 0$, $\frac{d\log(p_z)}{d\log(\bar{d}_g)} > 0$.

Finally, since $D_g/Y = \kappa_g G/Y$ and we have shown before that p_g increases with \bar{d}_g , the above then implies that D_g/Y and $p_g G/Y$ increase with \bar{d}_g .

Supplementary Material B.2 Equilibrium conditions

Letting $i = c, g, z$, $\alpha = 1$ if $i = g$ or $i = z$, and $\bar{d}_g = 1$ if $i = z$, the profit maximization problem can be generically written as

$$\pi_i = \max_{d_p, x} \frac{\chi}{\chi-1} p_i \left(\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \beta \frac{\chi-1}{\chi}} (x)^{(1-\beta) \frac{\chi-1}{\chi}} - \phi x - p_d d_p.$$

First order conditions are:

$$\begin{aligned}
p_i \left(\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \beta \frac{\chi-1}{\chi}} (x)^{(1-\beta) \frac{\chi-1}{\chi}} (1-\beta) &= \phi x \\
p_i \left(\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \beta \frac{\chi-1}{\chi}} (x)^{(1-\beta) \frac{\chi-1}{\chi}} \beta \frac{(1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}}}{\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}}} &= p_d d_p.
\end{aligned}$$

This implies

$$\begin{aligned}
\pi_i &= p_i \left(\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \beta \frac{\chi-1}{\chi}} (x)^{(1-\beta) \frac{\chi-1}{\chi}} \frac{1}{\chi-1} \times \dots \\
&\quad \left(1 + \beta(\chi-1) \frac{\alpha(d_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}}} \right)
\end{aligned}$$

$$x = \left(\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \frac{\beta \frac{\chi-1}{\chi}}{1-(1-\beta) \frac{\chi-1}{\chi}}} \left(p_i \frac{1-\beta}{\phi} \right)^{\frac{1}{1-(1-\beta) \frac{\chi-1}{\chi}}}$$

$$(d_p)^{\frac{1}{\gamma}} = \frac{(1-\alpha)}{p_d} (p_i)^{\frac{1}{1-(1-\beta) \frac{\chi-1}{\chi}}} \left(\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \frac{\beta \frac{\chi-1}{\chi}}{1-(1-\beta) \frac{\chi-1}{\chi}} - 1} \left(\frac{1-\beta}{\phi} \right)^{\frac{(1-\beta) \frac{\chi-1}{\chi}}{1-(1-\beta) \frac{\chi-1}{\chi}}} \beta,$$

which then gives

$$\pi_i = (p_i)^{\frac{1}{1-(1-\beta) \frac{\chi-1}{\chi}}} \left(\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \frac{\beta \frac{\chi-1}{\chi}}{1-(1-\beta) \frac{\chi-1}{\chi}}} \left(\frac{1-\beta}{\phi} \right)^{\frac{(1-\beta) \frac{\chi-1}{\chi}}{1-(1-\beta) \frac{\chi-1}{\chi}}} \frac{1}{\chi-1} \times \dots$$

$$\left(1 + \beta(\chi-1) \frac{\alpha(d_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}}} \right)$$

$$(q_i)^{\frac{\chi-1}{\chi}} = \frac{\chi}{\chi-1} \left(\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \frac{\beta \frac{\chi-1}{\chi}}{1-(1-\beta) \frac{\chi-1}{\chi}}} \left(p_i \frac{1-\beta}{\phi} \right)^{\frac{(1-\beta) \frac{\chi-1}{\chi}}{1-(1-\beta) \frac{\chi-1}{\chi}}}$$

$$d_p = \beta \frac{\chi-1}{\chi} \frac{(1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}}}{\alpha(d_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p)^{\frac{\gamma-1}{\gamma}}} \frac{p_i}{p_d} (q_i)^{\frac{\chi-1}{\chi}}.$$

So, normalizing $\phi = (1-\beta)$, we obtain:

$$\Pi_g(\bar{d}_g, p_g) = (p_g)^{\frac{\chi}{1+\beta(\chi-1)}} (\bar{d}_g)^{\frac{\beta(\chi-1)}{1+\beta(\chi-1)}} \frac{1+\beta(\chi-1)}{\chi-1}$$

$$Y_g = N_g \frac{\Pi_g(\bar{d}_g, p_g)}{p_g} \frac{\chi}{1+\beta(\chi-1)}$$

$$D_g = N_g \bar{d}_g$$

$$\Pi_c(\bar{d}_g, p_c, p_d) = (p_c)^{\frac{\chi}{1+\beta(\chi-1)}} \left(\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \frac{\beta(\chi-1)}{1+\beta(\chi-1)}} \frac{1}{\chi-1} \times \dots$$

$$\left(1 + \beta(\chi-1) \frac{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}}}{\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}}} \right)$$

$$(d_p(\bar{d}_g, p_c, p_d))^{\frac{1}{\gamma}} = \frac{(1-\alpha)}{p_d} (p_c)^{\frac{\chi}{1+\beta(\chi-1)}} \left(\alpha(\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha)(d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \frac{\beta(\chi-1)}{1+\beta(\chi-1)} - 1} \beta$$

$$\Pi_c(0, p_c, p_d) = (p_c)^{\frac{\chi}{1+\beta(\chi-1)}} \left((1-\alpha)^{\frac{\gamma}{\gamma-1}} d_p(0, p_c, p_d) \right)^{\frac{\beta(\chi-1)}{1+\beta(\chi-1)}} \frac{1}{\chi-1}$$

$$d_p(0, p_c, p_d) = \frac{1}{(p_d)^{1+\beta(\chi-1)}} (p_c)^{\chi} (1-\alpha)^{\frac{\gamma}{\gamma-1} \beta(\chi-1)} \beta^{1+\beta(\chi-1)}$$

$$Y_c = \left(N_c + \frac{1-\lambda}{\lambda} N_g \right) \frac{\chi}{\chi-1} \left((1-\alpha)(d_p(0, p_c, p_d))^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \frac{\beta(\chi-1)}{1+\beta(\chi-1)}} (p_c)^{\frac{(1-\beta)(\chi-1)}{1+\beta(\chi-1)}}$$

$$\begin{aligned}
& + N_g \frac{\chi}{\chi-1} \left(\alpha (\bar{d}_g)^{\frac{\gamma-1}{\gamma}} + (1-\alpha) (d_p(\bar{d}_g, p_c, p_d))^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1} \frac{\beta(\chi-1)}{1+\beta(\chi-1)}} (p_c)^{\frac{(1-\beta)(\chi-1)}{1+\beta(\chi-1)}} \\
D_p &= \left(N_c + \frac{1-\lambda}{\lambda} N_g \right) d_p(0, p_c, p_d) + N_g d_p(\bar{d}_g, p_c, p_d) \\
\Pi_z(p_z) &= (p_z)^{\frac{\chi}{1+\beta(\chi-1)}} \frac{1+\beta(\chi-1)}{\chi-1} \\
Y_z &= N_z \frac{\Pi_z(p_z)}{p_z} \frac{\chi}{1+\beta(\chi-1)}.
\end{aligned}$$

Furthermore, from the profit maximization of the final goods seller together with goods market clearing, we obtain:

$$\begin{aligned}
Y_z &= \left(\frac{p_z}{a} \right)^{-\epsilon} Y \\
\frac{1-a}{a} \left(\frac{Y_c}{Y_z} \right)^{-\frac{1}{\epsilon}} &= \frac{p_c}{p_z} \\
\left[(1-a)^\epsilon (p_c)^{1-\epsilon} + a^\epsilon (p_z)^{1-\epsilon} \right]^{\frac{1}{1-\epsilon}} &= 1.
\end{aligned}$$

And the remaining market clearing conditions are

$$\begin{aligned}
G &= Y_g \\
D_g &= \kappa_g G \\
D_p &= \kappa_p Y.
\end{aligned}$$

And the free entry conditions are

$$\begin{aligned}
0 &= \Pi_g(\bar{d}_g, p_g) + \Pi_c(\bar{d}_g, p_c, p_d) - \left(2 + \frac{F}{\lambda} \right) \mu_z \Pi_z(p_z) \\
\Pi_c(0, p_c, p_d) &= \mu_z \Pi_z(p_z) \\
\mu_z \Pi_z(p_z) &= \theta \eta + \rho = r,
\end{aligned}$$

where the last equality follows from the Euler equation of the representative household in a BGP.

Supplementary Material B.3 Calibration

We externally calibrate $\theta = 2$, $\rho = 0.03$, $\chi = 6$, which are standard parameters in the literature. As for the elasticity of substitution between software and non-software intermediates, we set $\epsilon = 1$ so that the aggregate production function is Cobb-Douglas. We set $a, \mu_z, F, \kappa_g, \kappa_p$ such that the initial BGP equilibrium is symmetric: the direction of innovation is unbiased ($\frac{\tilde{N}_c}{N_z} = \frac{N_g}{N_z} = 1$) and all sectors have an identical output share ($\frac{p_c Y_c}{p_z Y_z} = \frac{p_g G}{p_z Y_z} = 1$). We assume a growth rate of 6%, which matches the annual per-capita GDP growth rate in China in recent years.

The parameters left to set are those associated with data as an input in innovation: the share of data in production β , the elasticity of substitution between government and private data γ , and the productivity of government data in private software innovation α . Admittedly, we have a large degree of uncertainty about β and γ . Our empirical evidence on the responses of government and commercial software following the receipt of data-rich government contracts at most show that $\beta > 0$ and $\gamma < \infty$. So, for our baseline calibration, we will simply set them to $\beta = 0.8$ and $\gamma = 1 + \beta(\chi - 1) + 0.1$ which ensure that a symmetric BGP equilibrium exist.

However, given β, γ , we next show how to pin down the parameter governing economies of scope α from our empirical evidence. Fixing prices and differentiating the optimal levels of software production for those firms obtaining contracts with respect to \bar{d}_g , we obtain the partial equilibrium responses:

$$\begin{aligned}\Delta \log(q_g) &= \frac{\chi\beta}{1 + (\chi - 1)\beta} \Delta \log(\bar{d}_g) \\ \Delta \log(q_c) &= \frac{\chi\beta\sigma}{1 + (\chi - 1)\beta + \gamma(1 - \sigma)} \Delta \log(\bar{d}_g),\end{aligned}$$

where

$$\sigma \equiv \frac{\alpha}{\alpha + (1 - \alpha) \frac{d_p(\bar{d}_g, p_c, p_d)}{\bar{d}_g}^{\frac{\gamma-1}{\gamma}}}.$$

These responses are the model equivalent to those that we have estimated for high capacity contracts in Appendix Table A.6, columns (1) and (2). Then, when setting the government and private data in software production in the symmetric BGP to be identical ($\bar{d}_g = d_p(\bar{d}_g, p_c, p_d)$), we obtain that $\alpha = \sigma$ and therefore:

$$\alpha = \frac{\frac{\Delta \log(q_c)}{\Delta \log(q_g)}}{1 - \frac{\gamma}{1 + \beta(\chi - 1) + \gamma} \left(1 - \frac{\Delta \log(q_c)}{\Delta \log(q_g)}\right)}.$$

We use the coefficients in Appendix Table A.6, 6 Semiyears after \times High-capacity, columns (1) and (2). They imply an elasticity of private to government software ($\frac{\Delta \log(q_c)}{\Delta \log(q_g)}$) of about 2/3. Given our parameterization, this results in $\alpha = 0.82$.