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OPTIMAL TAX TREATMENT OF THE FAMILY:
MARRIED COUPLES

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ABSTRACT

Optimal Tax Treatment of the Family: Married Couples

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This paper examines the appropriate tax treatment of the family in a series of analytical models and numerical examples. For a population of taxpaying couples which differ in earning capacity, we derive the optimal tax rates for each potential earner. These rates depend crucially upon own and cross labor supply elasticities and the joint distribution of wage rates. Our results suggest that the current system of income splitting in the United States, under which husbands and wives face equal marginal tax rates, is nonoptimal. Using results from recent econometric studies, and allowing for a sensitivity analysis, the optimal tax rates on secondary workers in the family are much lower than those on primary earners. Indeed, our best estimate is that the secondary earner would face tax rates only one-half as high as primary earners.

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1. Introduction

The appropriate tax treatment of the family has been a basic issue in the design and implementation of federal taxation in every country employing direct taxation. Many countries use personal exemptions, deductions and/or credits varying with family size. Several countries, the United States among them, allow some type of income splitting among family members.¹ These provisions generally are defended by an appeal to differing economic circumstances across families of different size and economic characteristics.

Many countries rely on the individual rather than the family as the primary unit of account for personal taxation. Important examples include Canada, Australia, Japan and The Netherlands. Among OECD countries, only France requires families to file a joint return. Further, several countries, such as Austria, Denmark, Italy and Sweden, recently have switched to the individual as the unit of account.

While the question of the appropriate unit of account for personal taxation has always been important, it is assuming increasing importance. Dramatic changes have occurred in family size and composition in most countries.² The combined effects in the United States of the post-World War II baby boom and the 1970's baby bust, the recent rapid increase in the labor force participation of married women, the postponement of marriage and child-bearing, the increased life expectancy and the soaring of the divorce rate render the traditional one worker, one child raiser, continuously married several child family representative of a dwindling proportion of the population.

While the time thus seems ripe for a reexamination of the role of the unit of account in personal taxation, such studies not only are few and far between,³ but do not focus on what we consider the most important economic issues. For example, virtually no attention is paid to the efficient allocation of the time of family members between the market and the household. Nor is the assortive mating in society and the valuation of full income examined in an attempt to design an efficient and equitable tax system.

The purpose of the present paper is to begin to provide a theory of the optimal tax treatment of the family. Our procedure is to examine a series of models, each of which focuses on a particular aspect of the problem of the tax treatment of the family. Thus Section 2 presents a model of identical families and discusses the issue of the most efficient tax system to raise the government's required revenue. Various approaches to the taxation of the family are analyzed from this efficiency point of view.

Section 3 extends the analysis to the case of differences across households in the ability to produce market income. Introducing the joint density of the wage rates of husbands and wives and a representation of social welfare enables us to discuss the tradeoff between efficiency losses and redistribution inherent in designing a tax system.

Section 4 develops an instructive and illustrative special case of the analysis by confining attention to the Stone-Geary class of utility functions. Since the analyses of Sections 2 and 3 reveal that certain empirical parameters--own and cross substitution effects on the labor supply of husbands and wives plus the parameters of the joint distribution of abilities--play a central role in the design of the optimal tax treatment

of the family, we discuss econometric estimates of these parameters and employ them to estimate the optimal tax system.

Section 5 concludes with a discussion of issues in the taxation of families of different size and composition which we address in the sequel to this paper.

2. Optimal Tax Treatment of Identical Families

We first examine the structure of the optimal tax treatment of the family in a world of identical families. This is the simplest case to begin the analysis and will prove particularly useful in generating insights in the subsequent analysis of the optimal tax treatment of non-identical families.

Assuming identical preferences and endowments and income effects are taken care of elsewhere, we may treat social welfare as the welfare of a representative consumer. The simplest case which begins to yield some insight into the problem under consideration contains three goods: the labor (available time less leisure) of the husband, L_1 , the labor of the wife, L_2 , and other consumption, C . Without loss of generality, non-leisure consumption is taken as the untaxed numeraire.

Thus the welfare of each family (and social welfare) may be represented by the usual well behaved utility function

$$(1) \quad U(L_1, L_2, C)$$

Note that for analytical convenience we put labor supply rather than the more usual leisure (the remaining fraction of time) into the utility function; hence

$$\frac{\partial U}{\partial L_i} < 0 \quad i = 1, 2,$$

the marginal utility of labor supply is assumed to be negative.

Within the context of such a model, we inquire under what conditions it is desirable to tax the earnings of husbands and wives (or primary and secondary earners) at the same rate, at different rates, or even to subsidize the earnings of one of the workers. In general, we derive the optimal tax rates for the two taxed commodities, L_1 and L_2 .

In the United States, husbands and wives are allowed to pool their income and file a joint return which taxes them as if they had each earned one-half of the income. This income splitting provision 1) reduces the rate of progression for married couples, and 2) equates the marginal rate of income taxation on the earnings of husbands and wives. The provision thus has important consequences for the horizontal and vertical equity of the income tax. It is commonly argued that the concern over the effects of income splitting stems from the progressive rate structure imbedded in the current income tax. For example, Groves [1963] argues that "The issue is associated with progressive taxation and would be of little or no importance under a proportional tax." Under a flat rate tax, there would be no rate of progression to reduce; hence, the first effect noted above would be absent. The second effect of income splitting, equating the marginal tax rate for husbands and wives, would not disappear under proportional taxation. We may then inquire as to whether it is desirable tax policy for husbands and wives (or primary and secondary workers in the family) to face the same marginal rate of tax.

The usual view on this matter is summed up by Pechman [1971],

The classic argument in favor of income splitting is that husbands and wives usually share their combined income equally. . . . Two conclusions follow from this view. First, married couples with the same combined income should pay the same tax irrespective of the legal division of income between them; second, the tax liabilities of married couples should be computed as if they were two single persons with their total income divided equally between them.

We shall demonstrate below that taxing the earnings of husbands and wives at the same rate is inefficient, in the sense that it produces a dead weight loss to society substantially in excess of that obtainable under a differentiated rate structure. The reason for this is straightforward: a tax on earnings distorts the work-leisure (or market vs. non-market work) choice; equal marginal tax rates (since the [income-compensated] supply of wives is much more elastic than that of husbands) induce a larger decline in the market work of wives relative to husbands than is socially optimal.⁴

Choosing scales of measurement so that initial net prices, which are the unit resource costs, equal unity for all goods, and that costs are constant in the relevant range, we seek the tax rates that minimize the dead weight loss from the tax system, subject to raising the required revenues per family, R . Under these assumptions, the government's problem is to⁵

$$(2) \quad \begin{aligned} \text{Min}_{\beta_1, \beta_2} W = & -1/2 \left[\left(\frac{1-\beta_1}{\beta_1} \right)^2 S_{11} + \left(\frac{1-\beta_2}{\beta_2} \right)^2 S_{22} + 2S_{12} \left(\frac{1-\beta_1}{\beta_1} \right) \left(\frac{1-\beta_2}{\beta_2} \right) \right] \\ & - \lambda \left[\left(\frac{1-\beta_1}{\beta_1} \right) L_1 + \left(\frac{1-\beta_2}{\beta_2} \right) L_2 - R \right] \end{aligned}$$

where S_{ij} is the ij^{th} Hicksian income-compensated cross-effect of a change in the net wage of i with respect to the leisure (negative of labor supply) of j , and $1-\beta_i$ is the tax rate on the earnings of i .

Differentiating with respect to $(1-\beta_1)/\beta_1$ and $(1-\beta_2)/\beta_2$ and setting the derivatives equal to zero yields

$$\begin{aligned}
 - \frac{\partial W}{\partial \left(\frac{1-\beta_1}{\beta_1} \right)} &= S_{11} \left(\frac{1-\beta_1}{\beta_1} \right) + S_{12} \left(\frac{1-\beta_2}{\beta_2} \right) + \lambda L_1 = 0 \\
 (3) \quad - \frac{\partial W}{\partial \left(\frac{1-\beta_2}{\beta_2} \right)} &= S_{12} \left(\frac{1-\beta_1}{\beta_1} \right) + S_{22} \left(\frac{1-\beta_2}{\beta_2} \right) + \lambda L_2 = 0 \\
 - \frac{\partial W}{\partial \lambda} &= \left(\frac{1-\beta_1}{\beta_1} \right) L_1 + \left(\frac{1-\beta_2}{\beta_2} \right) L_2 - R = 0
 \end{aligned}$$

Solving by Cramer's rule we have

$$\begin{aligned}
 \left(\frac{1-\beta_1}{\beta_1} \right) &= \frac{\begin{vmatrix} \lambda L_1 & S_{12} \\ \lambda L_2 & S_{22} \end{vmatrix}}{\begin{vmatrix} S_{11} & S_{12} \\ S_{12} & S_{22} \end{vmatrix}} \\
 (4) \quad \left(\frac{1-\beta_2}{\beta_2} \right) &= \frac{\begin{vmatrix} S_{11} & \lambda L_1 \\ S_{12} & \lambda L_2 \end{vmatrix}}{\begin{vmatrix} S_{11} & S_{12} \\ S_{12} & S_{22} \end{vmatrix}} .
 \end{aligned}$$

Clearly, equal tax rates on the earnings of the husband and wife are optimal when the numerators in (4) are equal or when

$$(5) \quad \lambda L_1 S_{22} - \lambda L_2 S_{12} = \lambda L_2 S_{11} - \lambda L_1 S_{12}$$

The homogeneity of demand curves may be used to reduce (5), via the row sum conditions on the Slutsky matrix, to

$$L_1 S_{23} = L_2 S_{13} \quad \text{or}$$

$$\frac{S_{23}}{L_2} = \frac{S_{13}}{L_1}$$

Given initial prices of unity, this tells us that the earnings of husbands and wives should be taxed at the same rates as under the income-splitting provision, when the labor supplies of husbands and wives have identical compensated cross elasticities of demand with respect to the consumption of goods, or

$$\eta_{23} = \eta_{13}$$

Further, the tax rate on the husband should exceed the tax rate on the wife if

$$L_1 S_{23} > L_2 S_{13} \quad (\text{and}$$

conversely if $L_1 S_{23} < L_2 S_{13}$). This is equivalent to

$$L_1 (S_{22} + S_{12}) > L_2 (S_{11} + S_{12}).$$

Thus if the cross-substitution effects are small relative to the own substitution effects, the higher tax rate should be levied according to whether

$$\frac{S_{22}}{L_2} > \frac{S_{11}}{L_1}, \quad \text{i.e.,}$$

we should tax more heavily the earnings of the factor with the smaller own-compensated wage elasticity.

The optimal tax rates need not both be positive.⁶ The denominators in (4) are necessarily non-negative, being equivalent to a second-order

principal minor of the negative semi-definite Slutsky matrix. Examining, for example, the optimal tax rate on the wife's earnings, we note that it will be negative if

$$L_2 S_{11} < L_1 S_{12}.$$

Since $S_{11} < 0$ and $L_2 \geq 0$, complementarity of husbands' and wives' labor is sufficient for a wage subsidy for wives to be optimal.⁷

While we shall return to econometric estimates of the S_{ij} in Section 4 below, we note here that numerous econometric studies of labor supply have concluded that the own-substitution effect on labor supply for wives is much larger than that for husbands as well as the cross-substitution effect;⁸ since the typical hours of work of husbands exceeds that for wives, a higher tax rate for husbands than wives would appear desirable.

3. Ability Differences and the Optimal Tax Treatment of the Family

Household behavior. Households are assumed to have identical utility functions, $U(C, L_1, L_2)$, where again, C denotes total consumption, L_1 labor supply by the husband, and L_2 labor supplied by the wife, each measured as a fraction of total hours available.⁹ Households differ in their wage rate per hour, w_1 the husband's wage-rate, and w_2 the wife's wage rate. Consumption is taken as numeraire with a unit price. There is no income apart from labor income, so $Y_1 = w_1 L_1$ and $Y_2 = w_2 L_2$. The household's before-tax total income, Y , is therefore $Y = Y_1 + Y_2 = w_1 L_1 + w_2 L_2$.

Tax instruments. The policy instrument examined in this paper is an income tax schedule which may be written in general form $t(Y_1, Y_2)$, implying that the government can distinguish, for tax purposes, between husband's and wife's incomes. We examine these possibilities by considering a general linear tax schedule of the form

$$(6) \quad t(Y_1, Y_2) = -\alpha + (1-\beta_1)Y_1 + (1-\beta_2)Y_2$$

where α is an income guarantee, $1-\beta_1$ and $1-\beta_2$ are the marginal tax rates on Y_1 and Y_2 , respectively. A requirement for joint returns without distinction between incomes would imply equal tax rates, i.e., $\beta_1 = \beta_2$. A favorable tax treatment of, say, the wife's income implies $\beta_2 > \beta_1$, etc.

If the joint distribution of w_1 and w_2 is given by $f(w_1, w_2)$, the government's budget constraint is given by

$$\int_0^{\infty} \int_0^{\infty} t(w_1 L_1, w_2 L_2) f(w_1, w_2) dw_1 dw_2 = R$$

or, by (6),

$$(7) \quad \alpha = \int_0^{\infty} \int_0^{\infty} [(1-\beta_1)w_1 L_1 + (1-\beta_2)w_2 L_2] f(w_1, w_2) dw_1 dw_2 - R,$$

where R is the net required revenue.

Policy objectives. If it is assumed that the government's policy objectives are represented by a social welfare function, W , of the form

$$(8) \quad W = \int_0^{\infty} \int_0^{\infty} G[U(C, L_1, L_2)] f(w_1, w_2) dw_1 dw_2$$

where G is a concave function. This formulation allows for a range of concern for equality from the strict utilitarian case $G(U) = U$ to the

Rawlsian case ($G = \min U$). The government maximizes (8) with regard to α , β_1 and β_2 subject to (7).

Obviously, the government is also constrained by the fact that C , L_1 and L_2 are functions of w_1 , w_2 and the tax parameters. Thus, the household's budget constraint is given by

$$(9) \quad \begin{aligned} C &= Y_1 + Y_2 - t(Y_1, Y_2) \\ &= \alpha + \beta_1 w_1 L_1 + \beta_2 w_2 L_2. \end{aligned}$$

Maximization of U subject to (9) yields the first order conditions

$$(10) \quad U_2 + \beta_1 w_1 U_1 = 0 \quad \text{and} \quad U_3 + \beta_2 w_2 U_1 = 0,$$

which, together with (9), determine the individual's equilibrium.

We may form the Lagrangian

$$(11) \quad \mathcal{L} = W - \lambda \left[\alpha - \int_0^\infty \int_0^\infty [(1-\beta_1)w_1 L_1 + (1-\beta_2)w_2 L_2] f(w_1, w_2) dw_1 dw_2 + R \right]$$

and obtain, using (9) and (10), the first order condition for maximization of (8),

$$(12) \quad \frac{\partial \mathcal{L}}{\partial \alpha} = \int_0^\infty \int_0^\infty \left[G' U_1 - \lambda + \lambda \left((1-\beta_1) w_1 \frac{\partial L_1}{\partial \alpha} + (1-\beta_2) w_2 \frac{\partial L_2}{\partial \alpha} \right) \right] f(w_1, w_2) dw_1 dw_2 = 0$$

$$(13) \quad \frac{\partial \mathcal{L}}{\partial \beta_1} = \int_0^\infty \int_0^\infty \left[G' U_1 w_1 L_1 - \lambda w_1 L_1 + \lambda \left((1-\beta_1) w_1 \frac{\partial L_1}{\partial \beta_1} + (1-\beta_2) w_2 \frac{\partial L_2}{\partial \beta_2} \right) \right] f(w_1, w_2) dw_1 dw_2 = 0$$

$$(14) \quad \frac{\partial \mathcal{L}}{\partial \beta_2} = \int_0^\infty \int_0^\infty \left[G' U_1 w_2 L_2 - \lambda w_2 L_2 + \lambda \left((1-\beta_1) w_1 \frac{\partial L_1}{\partial \beta_2} + (1-\beta_2) w_2 \frac{\partial L_2}{\partial \beta_2} \right) \right] f(w_1, w_2) dw_1 dw_2 = 0$$

Define a function h ,

$$(15) \quad h = h(w_1, w_2) \equiv G' \frac{U_1}{\lambda} + \left[(1-\beta_1) w_1 \frac{\partial L_1}{\partial \alpha} + (1-\beta_2) w_2 \frac{\partial L_2}{\partial \alpha} - 1 \right].$$

Then equations (12)-(13) may be rewritten

$$(16) \quad \frac{1}{\lambda} \frac{\partial \mathcal{L}}{\partial \alpha} = \int_0^{\infty} \int_0^{\infty} h(w_1, w_2) f(w_1, w_2) dw_1 dw_2 = 0,$$

$$(17) \quad \frac{1}{\lambda} \frac{\partial \mathcal{L}}{\partial \beta_1} = \int_0^{\infty} \int_0^{\infty} h(w_1, w_2) (-w_1 L_1) f(w_1, w_2) dw_1 dw_2 \\ + \int_0^{\infty} \int_0^{\infty} w_1 [(1-\beta_1)w_1 S_{11} + (1-\beta_2)w_2 S_{21}] f(w_1, w_2) dw_1 dw_2 = 0$$

$$(18) \quad \frac{1}{\lambda} \frac{\partial \mathcal{L}}{\partial \beta_2} = \int_0^{\infty} \int_0^{\infty} h(w_1, w_2) (-w_2 L_2) dw_1 dw_2 \\ + \int_0^{\infty} \int_0^{\infty} w_2 [w_1 (1-\beta_1) S_{12} + (1-\beta_2)w_2 S_{22}] f(w_1, w_2) dw_1 dw_2 = 0$$

where

$$(19) \quad S_{ij} = - \frac{\partial L_i}{\partial (\beta_j w_j)} - L_j \frac{\partial L_i}{\partial \alpha} \quad i, j = 1, 2$$

are the Slutsky terms for husbands' and wives' leisure.

In order to simplify the interpretation of the optimum solution (16)-(18), let us assume that w_2 is a nonrandom, strictly monotone function of w_1 . This, in effect, reduces the problem to one dimension, so we omit henceforth the subscript for w in the density functions.

We may now provide an interpretation for $h(w_1, w_2) = H(w)$. The first term in (15) is the social marginal utility (expressed in money terms by division by λ) of a lump-sum transfer to a household with wage w . This is clearly a decreasing function of w . The second term is the change in tax revenue due to such a transfer. Thus, if $T(w) = -\alpha + (1-\beta_1)w_1 L_1 + (1-\beta_2)w_2 L_2$, then this term is equal to $\frac{\partial T(w)}{\partial \alpha}$. We assume that this expression is non-

increasing with w . This is a sufficient assumption to ensure that $H(w)$ is a decreasing function of w .

The interpretation of $H(w)$ is now straightforward. It is the net social marginal utility of an increase in α (the income guarantee). Condition (16) states that

$$(20) \quad \int_0^{\infty} H(w)F(w)dw = 0,$$

where $F(w)$ is the marginal density of w_1 , i.e., the optimum level of α is such that the social marginal utility of an increase in its value averages to zero over the population.

Equations (17) and (18) can now be rewritten

$$(21) \quad \int_0^{\infty} H(w)(-w_1L_1)F(w)dw + \int_0^{\infty} w_1[(1-\beta_1)w_1S_{11} + (1-\beta_2)w_2S_{21}]F(w)dw = 0,$$

$$(22) \quad \int_0^{\infty} H(w)(-w_2L_2)F(w)dw + \int_0^{\infty} w_2[(1-\beta_1)w_1S_{12} + (1-\beta_2)w_2S_{22}]F(w)dw = 0.$$

Let us assume further that the wage income of the husband, w_1L_1 , and of the wife, w_2L_2 , are non-decreasing with the wage rate, w .¹⁰ Under these assumptions it can be shown that the first terms in (21) and (22) are non-negative.

Proposition 1. If $H(w)$ is non-increasing in w and incomes are non-decreasing with the wage rate,

(a) when $S_{12} = 0$ then $1-\beta_1 > 0$ and $1-\beta_2 > 0$;

(b) when $S_{12} < 0$ (two types of labor are complements), then
either $1-\beta_1 > 0$ or $1-\beta_2 > 0$.

The proof is obvious.

Further simplification towards empirical application is obtained by assuming that the S_{ij} are constant. In this case (21)-(22) simplify to

$$(23) \quad (1-\beta_1)\delta_{11}S_{11} + (1-\beta_2)\delta_{12}S_{12} = A$$

$$(24) \quad (1-\beta_1)\delta_{21}S_{21} + (1-\beta_2)\delta_{22}S_{22} = B$$

where

$$A = \int_0^{\infty} H(w)w_1L_1F(w)dw \leq 0, \quad B = \int_0^{\infty} H(w)w_2L_2F(w)dw \leq 0$$

and

$$\delta_{ij} = \int_0^{\infty} w_iw_jF(w)dw > 0, \quad i, j = 1, 2.$$

The solution of (23)-(24) is given by

$$(25) \quad 1-\beta_1^* = \frac{A\delta_{22}S_{22} - B\delta_{12}S_{12}}{\delta_{11}\delta_{22}S_{11}S_{22} - \delta_{12}^2S_{12}^2},$$

$$(26) \quad 1-\beta_2^* = \frac{B\delta_{11}S_{11} - A\delta_{21}S_{21}}{\delta_{11}\delta_{22}S_{11}S_{22} - \delta_{12}^2S_{12}^2},$$

where * denotes the optimum.

Notice that the covariance between husband's and wife's wage rate, expressed by δ_{12} , affects the optimum tax rates only through S_{12} . In particular, if $S_{12} = 0$, then β_1^* and β_2^* are independent of δ_{12} .

Now, the sign of the denominator in (25)-(26) is positive by the second-order conditions of the individual $S_{11}S_{22} - S_{12}^2 > 0$, and by Schwartz's inequality $\delta_{11}\delta_{22} - \delta_{12}^2 > 0$.

Proposition 2. If S_{ij} are constant, and the two types of labor are Hicksian substitutes, $S_{12} > 0$, then $1-\beta_1^* > 0$ and $1-\beta_2^* > 0$.

It is seen that when $S_{12} < 0$, i.e., when the husband's and the wife's labor are Hicksian complements, it is possible that one tax rate will be negative, that is, a wage subsidy is desirable.¹¹

Note that $\beta_1^* = \beta_2^*$ when

$$(27) \quad A\delta_{22}S_{22} - B\delta_{12}S_{12} = B\delta_{11}S_{11} - A\delta_{21}S_{21}.$$

There is no a priori reason why this condition should be satisfied.

Furthermore, when $A = B$ (equal social marginal utility for a lump-sum transfer to husband and wife) then (27) implies $\delta_{11}S_{11} = \delta_{22}S_{22}$, i.e., the product of the variance of earnings and the own-substitution effect on labor supply should be the same for husbands and wives. More generally, when $A = B$ the ratio $\frac{1-\beta_1^*}{1-\beta_2^*}$ depends positively on the ratio $\frac{\delta_{22}S_{22}}{\delta_{11}S_{11}}$, i.e., the larger the elasticity of wives' relative to husbands' labor supply the larger should be the tax on husbands' relative to wives' income. Further, given the elasticities of labor supply, the higher tax rate should be levied on the earnings with the smaller variance, ceteris paribus.

4. An Example

Suppose that the utility function is of the Stone-Geary family, often used in empirical studies

$$(28) \quad U = b_c \log(C - C_0) + b_1 \log(1 - L_1) + b_2 \log(1 - L_2),$$

where b_c, b_1, b_2 ($b_c + b_1 + b_2 = 1$) and C_0 are positive constants. The regular demand functions derived from (9) and (10) for the case are given by

$$(29) \quad C - C_0 = b_c \cdot I,$$

$$\beta_1 w_1 (1-L_1) = b_1 \cdot I,$$

$$\beta_2 w_2 (1-L_2) = b_2 \cdot I$$

where $I = \alpha - C_0 + \beta_1 w_1 + \beta_2 w_2$ is "full income."

The compensated labor supply functions are given by:

$$(30) \quad L_1 = 1 - b_1 A (\beta_1 w_1)^{b_1 - 1} (\beta_2 w_2)^{b_2} e^U$$

$$L_2 = 1 - b_2 A (\beta_1 w_1)^{b_1} (\beta_2 w_2)^{b_2 - 1} e^U.$$

Accordingly, the compensated derivatives are

$$(31) \quad S_{11} = (b_1 - 1) \left(\frac{1-L_1}{\beta_1 w_1} \right), \quad S_{12} = b_2 \left(\frac{1-L_1}{\beta_1 w_2} \right) = b_1 \left(\frac{1-L_2}{\beta_1 w_1} \right),$$

$$S_{22} = (b_2 - 1) \left(\frac{1-L_2}{\beta_2 w_2} \right).$$

Substituting (31) into equations (17)-(18), we obtain:

$$(32) \quad \int_0^\infty \int_0^\infty h(w_1, w_2) (-\beta_1 w_1 L_1) f(w_1, w_2) dw_1 dw_2 +$$

$$\int_0^\infty \int_0^\infty b_1 \left[\left(\frac{1-\beta_1}{\beta_1} \right) (b_1 - 1) + \left(\frac{1-\beta_2}{\beta_2} \right) b_2 \right] I(w_1, w_2) f(w_1, w_2) dw_1 dw_2 = 0$$

and

$$(33) \quad \int_0^\infty \int_0^\infty h(w_1, w_2) (-\beta_2 w_2 L_2) f(w_1, w_2) dw_1 dw_2 +$$

$$\int_0^\infty \int_0^\infty b_2 \left[\left(\frac{1-\beta_1}{\beta_1} \right) b_1 + \left(\frac{1-\beta_2}{\beta_2} \right) (b_2 - 1) \right] I(w_1, w_2) f(w_1, w_2) dw_1 dw_2 = 0.$$

Equations (32)-(33) can be viewed as two linear equations in the optimum $\left(\frac{1-\beta_1^*}{\beta_1^*} \right)$ and $\left(\frac{1-\beta_2^*}{\beta_2^*} \right)$. Solving these equations, using the definition of I ,

the assumption that $b_c + b_1 + b_2 = 1$ and condition (16), yields

$$(34) \quad \frac{1-\beta_1^*}{\beta_1^*} = \frac{1}{b_1} \frac{\int_0^\infty \int_0^\infty h(w_1, w_2) \beta_1^* w_1 f(w_1, w_2) dw_1 dw_2}{\int_0^\infty \int_0^\infty (\beta_1^* w_1 + \beta_2^* w_2) f(w_1, w_2) dw_1 dw_2}$$

$$(35) \quad \frac{1-\beta_2^*}{\beta_2^*} = \frac{1}{b_2} \frac{\int_0^\infty \int_0^\infty h(w_1, w_2) \beta_2^* w_2 f(w_1, w_2) dw_1 dw_2}{\int_0^\infty \int_0^\infty (\beta_1^* w_1 + \beta_2^* w_2) f(w_1, w_2) dw_1 dw_2}$$

Since the right-hand side of (34)-(35) depends on β_1^* and β_2^* , these are implicit functions for the optimum tax levels.

Consider again the simple case in which there is an exact proportional relation between w_1 and w_2 , say, $w_2 = \delta w_1$. In this case (34)-(35) simplify to

$$(36) \quad \frac{1-\beta_1^*}{\beta_1^*} = \frac{\beta_1^* a}{b_1(\beta_1^* + \delta\beta_2^*)}$$

$$(37) \quad \frac{1-\beta_2^*}{\beta_2^*} = \frac{\beta_2^* a}{b_2(\beta_1^* + \delta\beta_2^*)}$$

where

$$a = \frac{\int_0^\infty h(w) w f_1(w) dw}{\int_0^\infty w f_1(w) dw} \geq 0,$$

the wage-weighted net social marginal utility of income transfers, and f is the marginal distribution of $w_1 = w$. Clearly, a will increase with the degree of inequality aversion as reflected by $h(w)$.

When there is no correlation between w_2 and w_1 , this further reduces to

$$\beta_1^* = \frac{b_1}{a + b_1} \quad \text{and} \quad \beta_2^* = \frac{b_2}{a + b_2}.$$

As expected, the optimum tax rates are decreasing in the respective coefficients b_1 and b_2 which express the relative weight of husband and wife's

leisure in the family's utility. Furthermore, β_1^* and β_2^* decrease (i.e., tax rates increase) as a , "inequality aversion", decreases.

A variety of studies have estimated family labor supply functions. As noted in Section 2, these studies invariably conclude that the labor supply of wives is much more elastic than that of husbands.¹² For example, Pencavel and Johnson [1978] estimate a linear expenditure system with the S_{ij} 's at mean values as follows: $S_{11} = 73.9$; $S_{12} = -6.2$; $S_{22} = 249.3$. Since L_1 exceeds L_2 by a substantial amount, the compensated wage elasticity of wives is five or six times as large as that for husbands. Further, Pencavel and Johnson [1978] estimate a b_1 slightly larger than zero and a modest b_2 .

Studies of the correlation in wage rates between husbands and wives, like the labor supply studies, must account for the fact that a large percentage of wives do not work in the market at any point in time. A recent careful study by Smith [1978] suggests a substantial positive correlation in wage rates of husbands and wives.

As an instructive example, we present a sample calculation of the optimal tax rates derived from the Stone-Geary function with reasonable ranges of values of δ ; we assume $b_1 = .05$; $b_2 = .2$ and $a = .05$ ¹³ (the S_{ij} 's are simple functions of the b 's, L 's, and β 's).¹⁴

	OPTIMAL TAX RATES	
	<u>Husbands</u>	<u>Wives</u>
.05	0.48	0.25
.25	0.43	0.21
δ .50	0.38	0.17
.75	0.34	0.14

While alternative estimates would change these rates somewhat, our major qualitative feature--the higher rate of tax on husbands than wives--

results from all reasonable parameter values. We take this to be a strong indictment of the case for income splitting quoted in Section 2. In a world of married couples, the primary earner should face higher tax rates than the secondary worker.

5. Conclusion

We have examined the appropriate unit of account for personal income taxes in a world of married couples which differ in earning capacity. The typical second-best problem yielded both analytical results and empirical insights which suggest that equal marginal tax rates on husbands and wives, as under the U.S. income splitting provision, is nonoptimal. The primary earner in the family would face higher optimal tax rates than the secondary earner due to the relatively less elastic labor supply of primary workers. A numerical example based on recent parameter estimates derived from the Stone-Geary utility function suggests that the rate on husbands would be roughly twice that on wives.

Families differ in more than their ability to produce market income. They differ in the number of children, whether or not two adults are present, etc. The increase in divorce rates and other changes in family patterns suggest that the relative tax treatment of families of different size and composition is also becoming more important. Indeed, we hear more and more about incentives to marry or to divorce embedded in the tax codes of different countries. We shall deal with questions of family size and composition in a sequel to this paper. We hope that by focusing on the optimal tax treatment of the family in a world of married couples only, we have brought to attention the neglected, but crucial, issues of relative labor supply elasticities and wage rate variances and covariances of husbands and wives.¹⁵

FOOTNOTES

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1. Other countries allowing or requiring income splitting include Spain, Switzerland, France, Germany, Norway and the United Kingdom.
2. See the excellent summary by Michael, Fuchs and Scott [1978].
3. Important recent exceptions include Munnell [1978], Brazer [1978], Rosen [1978].
4. The allocative inefficiency induced by various tax devices has been a central issue in tax theory and policy for many decades. In its modern form, it dates back to Ramsey [1927] and Pigou [1947], and includes important contributions by Rolf and Break [1949], Friedman [1959], Little [1951] and Corlett and Hague [1951]. The most empirically relevant analyses are those of Harberger [1964, 1966]. While earlier contributions tended to focus on how to achieve optimal taxation, Harberger extended the analysis to include the measurement of the dead weight loss associated with any set of non-neutral taxes. Renewed interest has been stimulated by the work by Diamond and Mirrlees [1971] and Atkinson and Stiglitz [1972].
5. Here the tax rates are expressed as percentages of the net price of leisure; the more usual quotation in terms of gross earnings may be derived once we note that a subsidy to leisure at the rate $\frac{1-\beta_i}{\beta_i}$ is equivalent to a subsidy at the rate $1-\beta_i$ on the gross price. Thus,

$$P_{i \text{ net}} \left(1 + \frac{1-\beta_i}{\beta_i}\right) = P_{i \text{ gross}} = \frac{P_{i \text{ net}}}{\beta_i}.$$

6. Obviously, one tax rate must be positive with a positive revenue requirement.
7. For husbands, $L_1 S_{22} < L_2 S_{12}$.
8. For example, see Boskin [1973], Hall [1973], Rosen [1976], Heckman [1974], Hurd [1977], Ashenfelter and Heckman [1973], and Pencavel and Johnson [1978].
9. Note we here normalize total time available to unity.
10. Thus, we assume the wage elasticity of labor supply exceeds minus one. The empirical studies discussed below render this a safe supposition.
11. Note the similar conclusion arrived at in Section 2.
12. For example, see Boskin [1973], Bowen and Finegan [1969], Cain [1966], Hurd [1977], Mincer [1962], and Pencavel and Johnson [1978].
13. Since a is wage-weighted, and $\int h(w)f(w)dw$, presumably a will be close to zero unless there is extreme social inequality aversion. The level of a would affect the level of tax rates and transfers; since our focus is on the differential in these tax rates, we do not present results for other values of a . However, our calculations reveal that even with much larger values of a , the same pattern of much lower tax rates on wives occurs.
14. Obviously, the S_{ij} and δ_{ij} depend upon the tax rates; the current estimated values will change if we change tax rates. However, the qualitative conclusions reported here are quite robust to modest changes in the S_{ij} and δ_{ij} .
15. Robert Hall points out to us that as formulated, our problem can be thought of as applying to any two-dimensional labor supply decision, e.g., optimal taxation of a worker early and late in life.

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