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Volume Title: The Smoothing of Time Series

Volume Author/Editor: Frederick R. Macaulay

Volume Publisher: NBER

Volume ISBN: 0-87014-018-3

Volume URL: http://www.nber.org/books/maca31-1

Publication Date: 1931

Chapter Title: Front matter, acknowledgment, tables of content

Chapter Author: Frederick R. Macaulay

Chapter URL: http://www.nber.org/chapters/c9359

Chapter pages in book: (p. 4 - 16)

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First printing, February, 1931

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ACKNOWLEDGMENTS

The manuscript of this book has been read by Members of the Research Staff of the National Burcau and by the Bureau's Directors. I wish to acknowledge with thanks the helpful comments made by these gentlemen—Colonel M. C. Rorty in particular. I also desire to thank Dr. Henry Schultz, of the University of Chicago, who kindly read the manuscript. My obligations to Mr. Robert Henderson for specific suggestions are acknowledged in the text.

My sincere thanks are due to Miss Celeste Nason, who aided me in the earlier stages of the study, and to Miss Dorothy Achilles, my assistant in the later work. Miss Achilles not only made all the calculations and drew all the charts, but also read the manuscript with critical care.

F. R. M.

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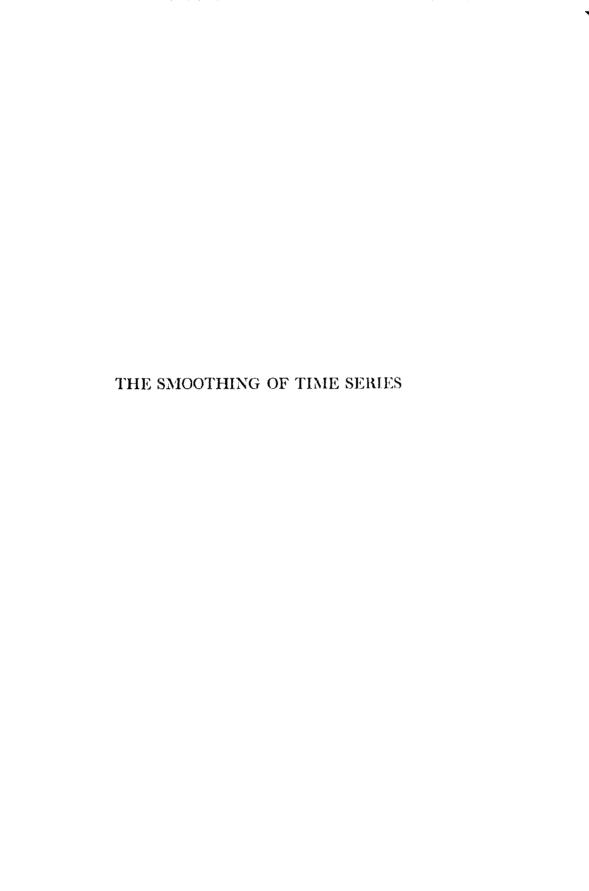
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