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THE TRANSITION TO A NEW ECONOMY  
AFTER THE SECOND INDUSTRIAL REVOLUTION

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### ABSTRACT

During the Second Industrial Revolution, 1860-1900, many new technologies, including electricity, were invented. These inventions launched a transition to a new economy, a period of about 70 years of ongoing, rapid technical change. After this revolution began, however, several decades passed before measured productivity growth increased. This delay is paradoxical from the point of view of the standard growth model. Historians hypothesize that this delay was due to the slow diffusion of new technologies among manufacturing plants together with the ongoing learning in plants after the new technologies had been adopted. The slow diffusion is thought to be due to manufacturers' reluctance to abandon their accumulated expertise with old technologies, which were embodied in the design of existing plants. Motivated by these hypotheses, we build a quantitative model of technology diffusion which we use to study this transition to a new economy. We show that it implies both slow diffusion and a delay in growth similar to that in the data.

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The period 1860–1900 is often called the *Second Industrial Revolution* because a large number of new technologies were invented at that time. These inventions heralded a period of about 70 years of ongoing, rapid technical change. Several decades passed, however, before this revolution led to a *new economy* characterized by faster growth in productivity, measured by output per hour.

In the standard growth model no such delay occur. Because technology is disembodied, faster technical change results immediately in faster growth of measured productivity. Indeed, David (1990) refers to this delay as a productivity paradox. He and other historians have offered several hypotheses for this delay. Here we build a quantitative model of technology diffusion that captures the main elements of these historians hypotheses. We show that this model can generate a delay of several decades before a sustained increase in the pace of technical change produces a new economy and we use the model to isolate the elements of the historians hypotheses that are essential to generate such a delay.

Historians such as Schurr et al. (1960), Rosenberg (1976), Devine (1983), and David (1990, 1991) focus on the development of electricity in the Second Industrial Revolution as the driving force of the prolonged period of rapid technical change after this revolution. These historians hypothesize that the development of electricity did not have an immediate payoff in terms of higher productivity growth for two reasons. One is that new technologies based on electricity diffused only slowly among U.S. manufacturing plants. The other is that, even after a new plant embodying a new technology was built, learning how best to take advantage of the technology took time.

At least two factors help account for the slow diffusion of electricity. As Devine (1983) and David (1990, 1991) explain, manufacturing plants needed to be completely redesigned in

order to make good use of electric power. Indeed, David and Wright (1999, p. 4) argue that “the slow pace of adoption prior to the 1920s was largely attributable to the unprofitability of replacing still serviceable manufacturing plants embodying production technologies adapted to the old regime of mechanical power derived from water and steam.” Rosenberg (1976) argues that ongoing technical change itself helps account for the slow diffusion: people anticipated ongoing improvements in technology and thus chose to wait for further improvements before adopting the current frontier technology.

Several historians emphasize that learning how best to use the new technologies resulting from the Second Industrial Revolution took quite some time. Schurr et al. (1960, 1990) discuss the process of learning following new applications of electricity to plant and machine design. They argue that the benefits of adopting electricity went far beyond the direct cost savings from reduced energy consumption. The electrification of plants opened opportunities for continual innovation in processes and procedures within an existing plant to improve overall productive efficiency. In practice, managers needed time to learn how best to take advantage of these opportunities. Chandler (1992) emphasizes that the knowledge gained in using new technologies was mostly organization-specific and, hence, difficult to transfer across organizations.

Our model of technology diffusion attempts to capture the main elements of these historians’ hypotheses. The idea of Devine (1983) and David (1991) that manufacturers needed to build new plants in order to adopt the new technologies based on electricity is built into the model by having new technologies embodied in the design of new manufacturing plants.

The ongoing technical change discussed by Rosenberg (1976) is modeled as ongoing

improvements in the technology embedded in these plant designs. The process of learning within an existing plant, discussed by Schurr et al. (1990) and Chandler (1992), is modeled as a stochastic process for the productivity with which that plant is able to implement the technology embodied in its design. Thus, in the model, the decision to adopt new technology amounts to a decision to close existing manufacturing plants based on old technologies and replace them with new plants based on the current frontier technology and then to undergo the process of learning to use that technology.

We quantify our model to capture the main patterns of industry evolution at the plant level in the U.S. economy. In the model, as in the data, the process of starting a new plant is turbulent and time-consuming. New plants tend to start small in terms of both employment and output and to fail often. Surviving plants tend to grow for as long as 20 years. We model this evolution as resulting from a stochastic process for plant-specific productivity (as in Hopenhayn and Rogerson 1993). We quantify this process by observing that the size of plants is determined by their specific productivities. We choose the parameters of this stochastic process to replicate the patterns of birth, growth, and death of plants in the U.S. economy as documented by Davis, Haltiwanger, and Schuh (1996).

We then ask what our model predicts about the transition from an old economy with a relatively slow pace of technical change to a new one with a relatively fast pace. In order to capture the notion that this transition began with the Second Industrial Revolution, we model the transition as arising from a once-and-for-all increase, starting in 1869, in the rate of improvement in the frontier technology embodied in the design of new plants. During the transition, new technologies diffuse only slowly, plants learn to use them efficiently over time, and there is a several-decade-long delay before the growth in output per hour climbs to its

new steady-state level. In this transition, the path of diffusion of new technology in the model is similar to the path of diffusion of electric power in U.S. manufacturing plants in the data during 1869–1939. The trends in the growth of output per hour generated by the model are also similar to those in the data for the period 1869–1969.

Two features of our model are critical in generating the slow transition. One is that, in the old economy, manufacturers build up a larger stock of knowledge using their embodied technologies than they do in the new economy. In the old economy, the pace of technical change and the diffusion of new technologies is relatively slow, and thus manufacturers spend a relatively long time building up knowledge and expertise with a given technology. At the beginning of the transition, manufacturers are reluctant to abandon this large stock of knowledge to adopt what, initially, is only a marginally superior technology. We demonstrate the importance of this feature by showing that if the stock of knowledge is not larger in the old economy than in the new one, the transition is almost immediate. The other model feature critical for the slow transition is our assumption that new technologies are embodied in the design of plants rather than disembodied. We show that if new technologies are disembodied, as they are in the standard growth model, the transition is almost immediate.

One implication of our model is that the speed of diffusion of new technologies should follow this pattern: slow in the old economy, medium during the transition, and fast in the new economy. We argue that this implication is consistent with the data on the diffusion of steam power in the old economy, electricity in the transition, and a variety of technologies in the new economy.

Our study is related to several strands of literature. The process of diffusion in our model is closely related to that in the model of Chari and Hopenhayn (1991). In the Chari-

Hopenhayn model, workers build up knowledge capital that is specific to a certain technology. and they lose this capital if they adopt a different technology. Chari and Hopenhayn (1991) argue that their model has two important implications that most other models of diffusion do not generate. First, when a new technology is introduced, workers do not simply abandon built-up knowledge in old technologies and adopt the new one. Rather they adopt the new technology only slowly. Second, investment in the old technologies continues even after a new technology is introduced. Our model shares these implications, and they are critical for generating our results.

Jovanovic and MacDonald (1994) develop a competitive model of diffusion of a single innovation in an industry. Their model is more detailed than ours in that theirs considers separate learning and production decisions and incorporates spillovers of knowledge from one plant to another. However, their study is concerned with questions appropriate for a partial equilibrium framework, while we are concerned with questions relevant for a general equilibrium framework.

Many other studies are more generally related to ours. The process of industry evolution and learning at the plant level in our model is related to that in the models of Jovanovic (1982), Hopenhayn and Rogerson (1993), and Campbell (1998). The role of learning in the transition to a new economy is related to the role of learning in the theoretical models of general purpose technologies of Aghion and Howitt (1998) and Helpman and Trajtenberg (1998) and in the applied work on the post-1974 productivity slowdown by Hornstein and Krusell (1996) and Greenwood and Yorukoglu (1997). The impact of an economy-wide transition on growth is related to that in some theories of the transition in Eastern European countries after the collapse of communism (Atkeson and Kehoe 1993, Aghion and Blanchard

1994, Brixiova and Kiyotaki 1997, and Castanheira and Roland 2000).

## 1. Productivity and diffusion after the Second Industrial Revolution

Many of the new technologies that had a profound impact on living standards in the 20th century were invented between 1860 and 1900. These technologies include electricity, the internal combustion engine, petroleum and other chemicals, telephones and radios, and indoor plumbing. (See Gordon 2000a for a description.) While all of these inventions undoubtedly had a substantial economic impact, we follow Schurr et al. (1960, 1990), Rosenberg (1976), Devine (1983), and David (1990, 1991) and focus on the new technologies based on electricity.

In this section, we document the gradual increase in the growth of productivity—output per hour—in U.S. manufacturing over the period 1869–1969 and the gradual diffusion of electric power in U.S. manufacturing over the period 1869–1939. (We choose these dates because, early in the sample period, the data are derived from the U.S. Census Bureau’s censuses of manufacturing establishments taken every decade starting in 1869.) We also review the chronology of the development of the modern technology of electric power in manufacturing.

In Figure 1, we plot output per hour in the U.S. manufacturing industry over the period 1869–1969 using annual data from the U.S Department of Commerce (1973). We also show linear trends for the three periods 1869–99, 1899–1929, and 1949–69. (These periods are chosen to omit the Great Depression and World War II.) The trend growth rates of output per hour in these three periods increased gradually, from 1.6% to 2.6% to 3.3%, respectively. (Gordon 2000b documents a similar gradual acceleration for the growth of output per hour for the economy as a whole.)



To document the slow diffusion of electricity, in Figure 2 we plot the fraction of mechanical power in U.S. manufacturing establishments that is derived from water, steam, and electricity during 1869–1939. (See Devine 1983.) Before 1899, more than 95% of mechanical power was derived from water and steam. Between 1899 and 1929, electricity use gradually replaced water and steam, so that by 1929, over 75% of mechanical power was electric. If we measure the diffusion of electricity starting in 1869, then we see that it took 50 years for electricity to provide 50% of mechanical power. This measure of the speed of diffusion is sensitive to the choice of starting date. An alternative measure of the speed of diffusion commonly used in the literature is the time required for a technology to diffuse from 5% to 50% of its potential users. For electricity in U.S. manufacturing, this occurred over the 20 years from 1899 to 1919.

Our chronology of the development of electricity after the Second Industrial Revolution follows that of Devine (1983) and David (1990, 1991). In the period 1869–99, the modern technology of electricity generation and distribution and motors driven by electricity was developed. Figure 3, taken from the work of Devine (1983), displays the gradual development of the modern technology of electric power in manufacturing. Briefly, the two major developments documented in this figure were the shift in the architecture of factories to take advantage of electric motors (outlined in panel A) and the development of the technology of producing electricity in large, centralized power plants and then shipping it over a distance to factories (outlined in panel B). In the period 1899–1929, this modern technology gradually diffused throughout the manufacturing sector. In the period 1929–69, this modern technology was the dominant one in manufacturing.

## 2. Links Between Historical Analyses and the Model

Here we report on three features of the data discussed by historians that motivate corresponding features in our model: (1) the change to electric power from steam and water power led to major changes in factory design and machine organization that went hand in hand with electrification; (2) the process of improving efficiency through changes in factory design continued for decades, through at least the 1980s; and (3) for each new factory design, the process of learning how best to use the new design took an extended period of time.

Our assumption that technology is embodied in plant design is motivated by the analysis of diffusion of Devine (1983) and David (1990, 1991). They argue that the adoption of the modern technology of electricity required a complete redesign of the manufacturing plant. In steam- and water-driven plants, power was distributed mechanically throughout the factory by a series of shafts and belts called a *direct-drive system*. In modern electric plants, power is distributed as electricity through wires to individual motors in what is called a *unit-drive system*.

Devine (1983, pp. 350, 352) describes the direct-drive system used in steam- and water-driven plants this way:

Until late in the nineteenth century, production machines were connected by a direct mechanical link to the power sources that drove them. In most factories, a single centrally located prime mover, such as a water wheel or steam engine, turned iron or steel “line shafts” via pulleys and leather belts. These line shafts—usually 3 inches in diameter—were suspended from the ceiling and extended the entire length of each floor of a factory, sometimes even continuing outside to

deliver power to another building. Power was distributed between floors of large plants by belts running through holes in the ceiling . . . . The line shafts turned, via pulleys and belts, “countershafts”—shorter ceiling-mounted shafts parallel to the line shafts. Production machinery was belted to the countershafts and was arranged, of necessity, in rows parallel to the line shafts . . . . The entire network of line shafts and countershafts rotated continuously—from the time the steam engine was started up in the morning until it was shut down at night—no matter how many machines were actually being used. If a line shaft or the steam engine broke down, production ceased in a whole room of machines or even in the entire factory until repairs were made.

Panel A of Figure 4 (from Devine 1983) illustrates this direct-drive system of power.

The system of power gradually evolved to the unit-drive system used in modern electricity-driven plants illustrated in panel D of Figure 4. In this system, each machine is driven by its own electric motor, and power for that motor is delivered through power lines from some potentially far-off electric utility plant. Panels B and C of Figure 4 show two short-lived intermediate stages in this evolution, referred to as *electric line shaft drive* and *electric group drive*.

As Devine (1983) describes, the unit-drive system has some advantages over the direct-drive system. One important advantage is that with the unit-drive system, plants could be designed and machinery in the plant could be arranged so as to handle materials according to the natural sequence of manufacturing operation, rather than according to physical placement of shafts, as required by the direct-drive system. Moreover, once the shafts in the direct-drive

system became unnecessary, plants could also be designed with improved ventilation, illumination, and cleanliness and to accommodate overhead electric cranes, which were thought to revolutionize materials-handling.

Our assumptions that technical change is ongoing and that the process of learning how best to use each new factory design takes an extended period of time are motivated by the work of many historians.

Devine (1990) and Sonenblum (1990) document that the adoption of the unit-drive system was only the first of a series of ongoing advances in the production process and modes of organization of factories that depend on the use of electricity. Moreover, these historians argue that each advance in factory design required an extended period of learning how to best use the new design.

Sonenblum (1990) documents three stages of factory design evolution. In the first stage (which he says occurred in 1899–1920), new factory design evolved from the traditional line drive through the intermediate stages of the electric line shaft drive and the electric group drive to the electric unit drive. In the second stage (1920–48), the attention in new factory design shifted to modifying the factory layout in order to accelerate the throughput of materials. Machines were arranged so that materials moved smoothly from one operation to the next, and assembly lines became more common. In the third stage (1948–85), new factories were designed to optimally use new servomechanisms that automatically controlled machine actions and numerically controlled machines.

While these factory systems were developed in the 1940s and 1950s, they began to spread into many manufacturing plants only in the 1960s. These systems allowed factories to rely less on large, inflexible assembly lines and to produce nonstandard products in small

batches. Moos (1957) and Slesinger (1958) also discuss the changes in plant design driven by the development of automatically controlled machines and the learning required to take advantage of such plants. As Devine (1990) discusses, in the 1980s the evolution of factory design evolved to accommodate new methods of computer materials-handling and computer-integrated manufacturing in which a computer controls whole groups of machines. Figure 5 (from Devine 1990) gives a brief chronology.

Chandler (1992, p. 84) discusses the type of built-up organizational capabilities that resulted from firms learning to efficiently use the technologies developed in the Second Industrial Revolution. He argues that the learned capabilities that resulted from solving problems of scaling up the processes of production manifest themselves in firms' production and distribution facilities. These learned capabilities were developed through trial and error, feedback, and evaluation and were organization-specific.

### **3. A Model of Technology Diffusion**

In this section, we develop our quantitative model of technology diffusion. We build into the model the three key elements detailed in the last section: (1) new technologies are embodied in plants; (2) improvements in the technology for new plants are ongoing; and (3) new plants must undergo an extended period of learning to use their technology most efficiently.

Our model economy is as follows. Time is discrete and is denoted by periods  $t = 0, 1, 2, \dots$ . The economy has two types of agents: workers and managers. There exist a continuum of size 1 of workers and a continuum of size 1 of managers.

Workers are each endowed with one unit of labor per period, which they supply in-

elastically. Workers are also endowed with the initial stock of physical capital and ownership of the plants that exist in period 0. Workers have preferences over consumption given by  $\sum_{t=0}^{\infty} \beta^t \log(c_{wt})$ , where  $\beta$  is the discount factor. Given sequences of wages and intertemporal prices  $\{w_t, p_t\}_{t=0}^{\infty}$ , initial capital holdings  $k_0$ , and an initial value  $a_0$  of the plants that exist in period 0, workers choose sequences of consumption  $\{c_{wt}\}_{t=0}^{\infty}$  to maximize utility subject to the budget constraint

$$(1) \quad \sum_{t=0}^{\infty} p_t c_{wt} \leq \sum_{t=0}^{\infty} p_t w_t + k_0 + a_0.$$

Managers are endowed with one unit of managerial time in each period. Managers have preferences over consumption given by  $\sum_{t=0}^{\infty} \beta^t \log(c_{mt})$ . Given sequences of managerial wages and intertemporal prices  $\{w_{mt}, p_t\}_{t=0}^{\infty}$ , managers choose consumption  $\{c_{mt}\}_{t=0}^{\infty}$  to maximize utility subject to the budget constraint  $\sum_{t=0}^{\infty} p_t c_{mt} \leq \sum_{t=0}^{\infty} p_t w_{mt}$ . Notice that we have given all the initial assets to the workers. Since worker and manager utilities are identical and homothetic, aggregate variables do not depend on the initial allocation of assets.

Production in this economy is carried out in plants. In any period, a plant is characterized by its *specific productivity*  $A$  and its *age*  $s$ . To operate, a plant uses one unit of a manager's time, physical capital, and (workers') labor as variable inputs. If a plant with specific productivity  $A$  operates with one manager, capital  $k$ , and labor  $l$ , the plant produces output

$$(2) \quad y = zA^{1-\nu}F(k, l)^\nu,$$

where the function  $F$  is linearly homogeneous of degree 1 and the parameter  $\nu \in (0, 1)$ .

The technology parameter  $z$  is common to all plants and grows at an exogenous rate. We

call  $z$  *economy-wide productivity*. Following Lucas (1978, p. 511), we call  $\nu$  the *span of control* parameter of the plant's manager. The parameter  $\nu$  may be interpreted more broadly as determining the degree of diminishing returns at the plant level. We refer to the pair  $(A, s)$  as the plant's *organization-specific capital*, or simply its *organization capital*. This pair summarizes the built-up knowledge that distinguishes one organization from another.

The timing of events in period  $t$  is as follows. The decision whether to operate or not is made at the beginning of the period. Plants that do not operate produce nothing; the organization capital in these plants is lost permanently. Plants with organization capital  $(A, s)$  that do operate, in contrast, hire a manager, capital  $k_t$ , and labor  $l_t$  and produce output according to (2). At the end of the period, operating plants draw independent innovations  $\epsilon$  to their specific productivity, with probabilities given by age-dependent distributions  $\{\pi_s\}$ . Thus, a plant with organization capital  $(A, s)$  that operates in period  $t$  has stochastic organization capital  $(A\epsilon, s + 1)$  at the beginning of period  $t + 1$ .

Consider the process by which a new plant enters the economy. Before a new plant can enter in period  $t$ , a manager must spend period  $t - 1$  preparing and adopting a *blueprint* for constructing the plant that determines the plant's initial specific productivity  $\tau_t$ . Blueprints adopted in period  $t - 1$  embody the frontier technology regarding the design of plants at that point in time. These *frontier blueprints* evolve exogenously, according to the sequence  $\{\tau_t\}_{t=0}^{\infty}$ . Thus, a plant built in  $t - 1$  starts period  $t$  with initial specific productivity  $\tau_t$  and organization capital  $(A, s) = (\tau_t, 0)$ .

We assume that capital and labor are freely mobile across plants in each period. Thus, for any plant that operates in period  $t$ , the decision of how much capital and labor to hire is static. Given a rental rate for capital  $r_t$ , a wage rate for labor  $w_t$ , and a managerial wage

$w_{mt}$ , the operating plant chooses employment of capital and labor to maximize static returns:

$$(3) \quad \max_{k,l} z_t A^{1-\nu} F(k, l)^\nu - r_t k - w_t l - w_{mt}.$$

The static returns to the owner of a plant with organization capital  $(A, s)$  in  $t$  are given by  $d_t(A) - w_{mt}$ , where  $d_t(A) = z_t A^{1-\nu} F(k_t(A), l_t(A))^\nu - r_t k_t(A) - w_t l_t(A)$  and  $k_t(A)$  and  $l_t(A)$  are the solutions to this problem.

The decision whether or not to operate a plant is dynamic. This decision problem is described by the Bellman equation

$$(4) \quad V_t(A, s) = \max [0, V_t^c(A, s)]$$

$$V_t^c(A, s) = d_t(A) - w_{mt} + \frac{p_{t+1}}{p_t} \int_{\epsilon} V_{t+1}(A\epsilon, s+1) \pi_{s+1}(d\epsilon),$$

where the sequences  $\{\tau_t, w_t, r_t, w_{mt}, p_t\}_{t=0}^{\infty}$  are given. The value  $V_t(A, s)$  is the expected discounted stream of returns to the owner of a plant with organization capital  $(A, s)$ . This value is the maximum of the returns from closing the plant and those from operating it. The term  $V_t^c(A, s)$ , the expected discounted value of operating a plant of type  $(A, s)$ , consists of current returns  $d_t(A) - w_{mt}$  and the discounted value of expected future returns  $V_{t+1}(A, s)$ . The plant operates only if the expected returns  $V_t^c(A, s)$  from operating it are nonnegative.

The decision whether or not to hire a manager to prepare a blueprint for a new plant is also dynamic. In period  $t$ , this decision is determined by the equation

$$(5) \quad V_t^0 = -w_{mt} + \frac{p_{t+1}}{p_t} V_{t+1}(\tau_{t+1}, 0).$$

The value  $V_t^0$  is the expected stream of returns to the owner of a new plant, net of the cost  $w_{mt}$  of paying a manager to prepare the blueprint for the plant. Such blueprints are prepared only if the expected returns from these plans,  $V_t^0$ , are nonnegative.



Let  $\mu_t$  denote the distribution in period  $t$  of organization capital across plants that might operate in that period, where  $\mu_t(A, s)$  is the measure of plants of age  $s$  with productivity less than or equal to  $A$ . Let  $\phi_t \geq 0$  denote the measure of managers preparing blueprints for new plants in  $t$ . Denote the measure of plants that operate in  $t$  by  $\lambda_t(A, s)$ . This measure is determined by  $\mu_t$  and the sign of the function  $V_t^c(A, s)$  according to

$$\lambda_t(A, s) = \int_0^A 1_{V^c}(a, s) \mu_t(da, s),$$

where  $1_{V^c}(a, s) = 1$  if  $V_t^c(a, s) \geq 0$  and 0 otherwise. For each plant that operates, an innovation to its specific productivity is drawn, and the distribution  $\mu_{t+1}$  is determined from  $\lambda_t, \phi_t, \{\pi_s\}$ , and  $\{\tau_t\}$  as follows:

$$(6) \quad \mu_{t+1}(A', s+1) = \int_A \pi_{s+1}(A'/A) \lambda_t(dA, s)$$

for  $s \geq 0$  and  $\mu_{t+1}(\tau_{t+1}, 0) = \phi_t$ .

Let  $k_t$  denote the aggregate physical capital stock. Then the resource constraints for physical capital and labor are  $\sum_s \int_A k_t(A) \lambda_t(dA, s) = k_t$  and  $\sum_s \int_A l_t(A) \lambda_t(dA, s) = 1$ . The resource constraint for aggregate output is  $c_{wt} + c_{mt} + k_{t+1} = y_t + (1 - \delta)k_t$ , where  $y_t$  is defined by  $y_t = z_t \sum_s \int_A A^{1-\nu} F(k_t(A), l_t(A))^\nu \lambda_t(dA, s)$ . The resource constraint for managers is

$$(7) \quad \phi_t + \sum_s \int_A \lambda_t(dA, s) = 1.$$

Managers are hired to prepare blueprints for new plants only if  $V_t^0 \geq 0$ . Since there is free entry into the business of starting new plants, in equilibrium we require  $V_t^0 \leq 0$ . We summarize this condition as  $V_t^0 \phi_t = 0$ . Also, in equilibrium,  $a_0 = \sum_s \int_A V_0(A, s) \mu_0(dA, s)$  is the value of the workers' initial assets.

Given a sequence of frontier blueprints and economy-wide productivities  $\{\tau_t, z_t\}$ , initial endowments  $k_0$  and  $a_0$ , and an initial measure  $\mu_0$ , an *equilibrium* in this economy is a collection of sequences of consumption; aggregate capital  $\{c_{mt}, c_{wt}, k_t\}$ ; allocations of capital and labor across plants  $\{k_t(A), l_t(A)\}$ ; measures of operating plants, potentially operating plants, and managers preparing plans for plants  $\{\lambda_t, \mu_{t+1}, \phi_t\}$ ; value functions and operating decisions  $\{d_t, V_t, V_t^c, V_t^0\}$ ; and prices  $\{w_t, r_t, w_{mt}, p_t, \}$ , all of which satisfy the above conditions.

To get a sense of the process for the birth, growth, and death of plants which our model generates, consider Figure 6. In this figure we show the evolution of the specific productivity of two plants that both enter in 1860. Both of these plants start with productivity equal to that of the frontier blueprint in 1860, namely,  $\tau_{1860}$ . This frontier blueprint grows exogenously over time at a constant rate as shown by the straight line labeled  $\log \tau_t$ . These plants each experience random shocks to their plant-specific productivity drawn from distributions  $\pi_s$  with age-dependent means denoted by  $\bar{\pi}_s$ . Plant 1 is relatively lucky in that it draws especially favorable shocks to its specific productivity, while plant 2 is relatively unlucky.

In every period, each plant makes a decision whether to continue or to exit. This decision is based on a comparison of the plant's current specific productivity and its future prospects for learning determined by  $\pi_s$  relative to the alternative of exiting and starting a new plant with the current frontier blueprint. Plant 1 has relatively high specific productivity; hence, it exits only after 30 years. In contrast, plant 2 has relatively low specific productivity; hence, it exits much sooner. After each of these plants exits, the manager in the plant starts a new plant with the current frontier blueprint and begins the process of building up specific productivity in the new plant.

In our model, new technologies diffuse as new plants embodying these technologies

are born and grow. Figure 6 also illustrates the mechanics of this diffusion. In 1863, the manager of plant 2 decides to exit and start a new plant that embodies the frontier blueprint of 1864 and then begins to learn with that new technology. Likewise, in 1890 the manager of plant 1 decides to exit and start a new plant that embodies the frontier blueprint of 1891 and then begins to learn with that new technology. In this manner, new technologies gradually replace old ones. Since our model has many such plants, each with different shocks to specific productivity, this diffusion of new technologies occurs smoothly over time.

#### **4. Linking Specific Productivity and Size**

Now we link the level of specific productivity of a plant or a cohort of plants to the size of these units. We use this link to argue that the data imply that the aggregate specific productivity of a cohort of plants of a given age grows substantially as the cohort ages. We then show that the model can be rewritten with size instead of specific productivity as a state variable. This alternative representation is convenient when we quantify the model.

We start with the data on employment by plants of different ages. Figure 7 presents the share of manufacturing employment in plants of various age groups stated as the share of workers employed by a one-year cohort within each age group as of 1988.<sup>1</sup> In the figure, we see that as a cohort of plants ages from newborn to 20 years old, it employs a growing share of the labor force; after that, its share declines. In our model, these data imply that the aggregate of specific productivities across a cohort of plants is also growing faster than the aggregate of all plants for the plants' first 20 years.

We develop the relationship between the employment share and the aggregate specific productivity of a cohort of plants by first deriving the relationship between the size and the

specific productivity of a single plant and then aggregating across plants in the cohort. To that end, consider the allocation of capital and labor across plants at any point in time. Since capital and labor are freely mobile across plants, the problem of allocating these factors across plants in period  $t$  is static. For a given distribution  $\lambda_t$  of organization capital, it is convenient to define

$$(8) \quad n_t(A) = \frac{A}{\bar{A}_t}$$

as the *size* of a plant of type  $(A, s)$  in period  $t$ , where

$$(9) \quad \bar{A}_t = \sum_s \int_A A \lambda_t(dA, s)$$

is the aggregate of the specific productivities across all plants. The variable  $n_t(A)$  measures the size of the plant in terms of its capital or labor or output, in that the equilibrium allocations are

$$(10) \quad k_t(A) = n_t(A)k_t, \quad l_t(A) = n_t(A)l_t, \quad \text{and} \quad y_t(A) = n_t(A)y_t,$$

where  $y_t = z_t \bar{A}_t^{1-\nu} F(k_t, l_t)^\nu$  is aggregate output. To see this, note that since the production function  $F$  is linear-homogeneous of degree 1 and there is only one fixed factor, all operating plants in this economy use physical capital and labor in the same proportions. The proportions are those that satisfy the resource constraints for capital and labor.

Now define the aggregate of the specific productivities of a cohort of plants of age  $s$  as  $\bar{A}_{t,s} = \int_A A \lambda_t(dA, s) / \bar{A}_t$ . Note from (8) that  $\bar{A}_{t,s} = \int_A n_t(A) \lambda_t(dA, s)$ . Using (10), we then have this

PROPOSITION 1. *The aggregate of specific productivities in plants of age  $s$  relative to that in*

all plants is the share of total employment in those plants, that is,  $\bar{A}_{t,s} = l_{t,s}$ , where

$$(11) \quad l_{t,s} = \int_A \frac{l_t(A)}{l_t} \lambda_t(dA, s).$$

Note for later that we use this proposition in our data analysis when we identify  $l_{t,s}$  with the employment shares in Figure 7 and use those shares to back out the relative productivities of cohorts of plants of different ages.

We now show that on a balanced growth path, for each plant we can replace the state variable specific productivity  $A$  with the state variable size  $n$ . To ensure that our model has a balanced growth path, we assume that  $F(k, l)$  has the Cobb-Douglas form  $k^\theta l^{1-\theta}$ . We define a *balanced growth path* in this economy as an equilibrium in which the following conditions hold: The quality of the frontier blueprint  $\tau_t$  and the productivity  $\bar{A}_t$  grow at a constant rate  $1 + g_\tau$ , the economy-wide level of technology  $z_t$  grows at a constant rate  $1 + g_z$ , aggregate variables  $y_t, c_t, k_t, w_t$ , and  $w_{mt}$  grow at a rate  $1 + g$ , where  $1 + g = [(1 + g_z)(1 + g_\tau)^{1-\nu}]^{1/(1-\nu\theta)}$ ; variables  $\phi_t, V_t^0$ , and  $r_t$  are constant; the distributions of organization capital across plants satisfy  $\mu_{t+1}(A, s) = \mu_t(A/(1 + g_\tau), s)$  and  $\lambda_{t+1}(A, s) = \lambda_t(A/(1 + g_\tau), s)$  for all  $t, A, s$ ; and  $V_{t+1}(A, s) = (1 + g)V_t(A/(1 + g_\tau), s)$ ,  $d_{t+1}(A, s) = (1 + g)d_t(A/(1 + g_\tau), s)$ , and  $V_{t+1}^c(A, s) = (1 + g)V_t^c(A/(1 + g_\tau), s)$  for all  $t, A, s$ .

Along the balanced growth path, we can recast our state variables as  $(n, s)$  instead of  $(A, s)$  as follows. Define the function  $W(n, s) = V_0(A, s)/y_0(1 - \nu)$ , where  $n = A/\bar{A}_0$ . Define the function  $W^c(n, s)$  from  $V_0^c(A, s)$  in a similar way. Let  $\omega_m = w_{m0}/y_0(1 - \nu)$  and  $\{\rho_s\}$  be the cumulative distribution functions of  $\eta = \epsilon/(1 + g_\tau)(1 + g_z)$  induced by  $\{\pi_s\}$ . We refer to  $\{\rho_s\}$  as the steady-state distributions of shocks to plant size. Consider the another Bellman

equation

$$(12) \quad W(n, s) = \max [0, W^c(n, s)]$$

$$W^c(n, s) = n - \omega_m + \beta \int_{\eta} W(n\eta, s + 1) \rho_{s+1}(d\eta),$$

where  $\omega_m = \beta W(\tau_0/\bar{A}_0, 0)$ . Since the value functions  $V_t$  and  $V_t^c$  solve the original Bellman equation (4) along the steady-state path, the functions  $W$  and  $W^c$  defined above satisfy this second Bellman equation. The terms in (12) have the same interpretation as those in (4) as descriptions of the returns to operating or closing a plant of size  $n$  and age  $s$ . The function  $W^c(n, s)$  defines an operating rule: plants with  $W^c(n, s) \geq 0$  operate, and those with  $W^c(n, s) < 0$  do not.

We use microeconomic data to quantify the shocks to plant size  $\eta$ . Note that since only the product  $(1 + g_\tau)(1 + g_z)$  enters the definition of shocks to size  $\eta$ , the data on the size-age distribution of plants do not pin down the relative contribution to growth in the Solow residual of growth in the two types of technology: frontier and economy-wide.

## 5. Two Model Implications

Now we discuss what the model implies for two key concepts: the average productivity of plants and the diffusion of new technologies among them.

### A. For Average Productivity at the Plant Level

We argue that the data support the view that plants accumulate a large amount of organization-specific capital as they age. This capital is reflected in their size and not in some measure of their average productivity. That plants grow in size with age is clear from the data on the employment shares of plants of different ages presented by Davis, Haltiwanger, and

Schuh (1996) (at least for plants' first 20 years of production) as well as from the panel data of Jensen, McGuckin, and Stiroh (2001). That these differences in organization-specific capital are not reflected in average productivity of capital or labor is documented by Bartelsman and Dhrymes (1998) and Jensen, McGuckin, and Stiroh (2001).

Bartelsman and Dhrymes (1998) study a sample of manufacturing plants drawn from the U.S. Census Bureau's Longitudinal Research Database (LRD). For this sample, they report a geometric weighted-average of capital and labor productivity

$$\left(\frac{y_{it}}{k_{it}}\right)^{\alpha} \left(\frac{y_{it}}{l_{it}}\right)^{1-\alpha}$$

by age category and size decile as measured by the average size of employment over the period 1972–86, where the weights are obtained from a regression of outputs on inputs. We report their values for this measure by age categories and size deciles in Figures 8A and 8B. While Bartelsman and Dhrymes (1998) find variations in this measure across individual plants, Figures 8A and 8B show that there is no systematic relationship between their measure of average productivity and either age or size.

Jensen, McGuckin, and Stiroh (2001) study labor productivity measured as value added per hour worked in a more extensive sample of manufacturing plants drawn from the LRD. They note that labor productivity varies extensively across individual plants. When they average productivity across plants in a cohort, however, they find no systematic relationship between labor productivity and age. Indeed, Jensen, McGuckin, and Stiroh report that after about 5–10 years, all cohorts of surviving plants have similar productivity levels.

This feature of the data distinguishes our approach for measuring the specific productivity of plants from much of the literature on learning-by-doing. The early literature

on learning-by-doing studies individuals performing specific tasks or groups of individuals performing a given number of tasks. (See the survey in Argote and Epple 1990.) This early literature shows that for a wide variety of tasks, an individual's average productivity increases with the number of times the task is performed. Based on this literature, one might think that the extent of learning in plants might show up as changes in the average productivity of labor in plants over time. As we show below, however, in our model, even though there is differential learning across plants, in each period the average productivity of labor is constant across plants. We have argued that this implication of our model is consistent with the data.

An individual who learns shows increases in labor productivity. An organization that learns grows by adding variable factors so as to keep labor productivity constant (at least with Cobb-Douglas production). Hence, the key variable to look at to determine the amount of organization-specific capital in a plant is not some measure of either its labor productivity or its capital productivity, but rather some measure of relative size.

To see this, consider a simplified version of our model in which the output in plant number  $i$  in period  $t$  is given by

$$(13) \quad y_{it} = z_t A_{it}^{1-\nu} l_{it}^\nu,$$

where  $A_{it}$  may depend on the age of the plant. In equilibrium, each plant in each period  $t$  chooses labor  $l_{it}$  to maximize profits, which implies that

$$(14) \quad l_{it} = A_{it} \frac{l_t}{A_t},$$

where  $l_t = \sum_i l_{it}$  and  $A_t = \sum_i A_{it}$ . Hence, taking logs of (13) and substituting for  $A_{it}$  from (14) gives that, in equilibrium, labor productivity is given by

$$\frac{y_{it}}{l_{it}} = z_t (A_t/l_t)^{1-\nu}$$



and, hence, is constant across all plants regardless of their specific productivity  $A_{it}$ . If we extend the model to include capital, then (10) implies that  $y_t(A)/l_t(A) = y_t/l_t$  and  $y_t(A)/k_t(A) = y_t/k_t$ . Hence, our model predicts that both of these measures of average productivity are constant across plants.

## B. For Diffusion

We use our model to study the diffusion of technologies that are embodied in the design of manufacturing plants. In this section, we define our measure of diffusion and discuss how we compare the implications of the model to data on diffusion.

Formally, we measure the diffusion of new technologies in our model as follows. Let

$$y_{t,s} = \int_A \frac{y_t(A)}{y_t} \lambda_t(dA, s)$$

denote the fraction of total output  $y_t$  produced in plants of age  $s$ . We measure the diffusion in period  $t+k$  of technologies developed in period  $t$  or later by

$$(15) \quad D_{t,t+k} = \sum_{s=0}^k y_{t,s},$$

which is the fraction of output produced in plants using these technologies. In our model, this diffusion is also equal to the fraction of labor employed in plants using these technologies, so that  $D_{t,t+k} = \sum_{s=0}^k l_{t,s}$ . With this link between diffusion and employment shares by age, we can use our model and the data from Figure 7 to measure the implied diffusion rate of new embodied technologies in recent years.

In Figure 9 we plot the diffusion of new embodied technologies  $D_{t,t+k}$  implied by our model in the steady state as a function of the age of the technology  $k$ . Since our data on the employment shares of plants cover plants only up to age 25, we show diffusion only up to this

age. In this figure, we see that a new embodied technology takes roughly 25 years to have diffusion reach 50%.

## 6. Calibration

Now we calibrate our model using both macroeconomic aggregates and microeconomic data on the birth, growth, and death of U.S. plants.

The choice of macro parameters is standard. The growth rate of output per hour  $g$ , the physical capital share  $\nu\theta$ , and the depreciation rate  $\delta$  are chosen to reproduce data on the U.S. manufacturing sector. We set  $g = 3.3\%$  to match the growth of manufacturing output per hour for 1949–69 reported in Figure 1. We use data for 1959–99 obtained from the U.S. Department of Commerce’s national income and product accounts to set  $\nu\theta = 18.4\%$  and  $\delta = 7.7\%$ , based on methodology described by Atkeson and Kehoe (2001). We set  $\beta = .977$ , so that the steady-state interest rate  $i$  defined by  $1 + i = (1 + g)/\beta$  is 5.7%.

Consider next the growth of the Solow residual. The steady-state growth rate of output per worker,  $1 + g$ , is related to the growth of the Solow residual by  $(1 + g)^{1-\nu\theta}$ , which can be decomposed as  $(1 + g)^{1-\nu\theta} = (1 + g_z)(1 + g_\tau)^{1-\nu}$ . Given our choices of  $g = 3.3\%$  and  $\nu\theta = 18.4\%$ , using  $(1 + g)^{1-\nu\theta} = 1.027$  implies that the growth of the Solow residual is 2.7%. Since we calibrate our model to reproduce observations on plant size, the steady state is not affected by the decomposition of the Solow residual into these components.

In our experiments, we choose the growth rate of the economy before the transition to be 1.6%. This growth rate is the trend growth rate of output per hour in manufacturing for 1869–99 shown in Figure 1. We set the initial capital-output ratio and the distribution of organization capital across plants to be those from the balanced growth path with this

growth rate.

Consider the span of control parameter  $\nu$ . Hundreds of studies have estimated production functions with micro data. These analyses incorporate a wide variety of assumptions about the form of the production technology and draw on cross-sectional, panel, and time series data from virtually every industry and developed country. Douglas (1948) and Walters (1963) survey many studies. More recent work along these lines has been done by Baily, Hulten, and Campbell (1992); Bahk and Gort (1993); and Bartelsman and Dhrymes (1998). Atkeson, Khan, and Ohanian (1996) review this literature and present evidence, in the context of a model like ours, that  $\nu = .85$  is a reasonable value for this parameter.

We use observations from micro data on manufacturing plants in the United States to choose the parameters affecting the shocks to size. We parameterize the distributions of these shocks as follows. We assume that shocks to size have a lognormal distribution, so that  $\log(\eta_s) \sim N(m_s, \sigma_s^2)$ . We choose the means and standard deviations of these distributions to be smoothly declining functions of  $s$ . In particular, we set  $m_s = \gamma_1 + \gamma_2(\frac{S-s}{S})^2$  for  $s \leq S$  and  $m_s = \gamma_1$  otherwise and  $\sigma_s = \gamma_3 + \gamma_4(\frac{S-s}{S})^2$  for  $s \leq S$  and  $\sigma_s = \gamma_3$  otherwise. With this parameterization, the shocks to size for plants of age  $S$  or older are drawn from a single distribution. Thus, shocks to size are parameterized by  $\{\gamma_i\}_{i=1}^4$  and  $S$ .

We choose the parameters governing the shocks to size so that the model matches data on the fraction of the labor force employed in plants of different age groups, as well as data on job creation and job destruction in plants of different age groups, from the 1988 panel of the U.S. Census Bureau's LRD. We choose the data from this panel because it has the most extensive breakdown of plants by age.

More formally, Davis, Haltiwanger, and Schuh (1996) define the following statistics.

*Employment* in a plant in year  $t$  is  $(l_t + l_{t-1})/2$ , where  $l_t$  is the labor force in year  $t$ . *Job creation* in a plant in year  $t$  is  $l_t - l_{t-1}$  if  $l_t \geq l_{t-1}$  and zero otherwise. *Job destruction* in a plant in year  $t$  is  $l_{t-1} - l_t$  if  $l_t \leq l_{t-1}$  and zero otherwise. In Figures 10A, 10B, and 10C, we report these three statistics for U.S. manufacturing establishments in 1988, broken down by age category.

We also plot in these figures the comparable statistics generated by our model. To produce these values, we set the model's parameter  $S = 150$  and choose the  $\gamma_i$  to minimize the sum of the squared errors between the model's and the data's statistics. For completeness, note that the implied statistics for the overall job creation and destruction rates expressed as percentages of total employment are 8.3% and 8.4% for the data and 9.9% and 9.9% in the model. The differences between the overall job creation and destruction rates in the data and the model are not large compared to the fluctuation in these rates in annual data for the period 1972–93. The standard deviations of the job creation and job destruction rates over this period are 2.0 and 2.7.

In Figure 11, we plot the means and standard deviations of shocks to the log of the size of plants,  $m_s$  and  $\sigma_s$ . The parameters that generate these shocks are  $S = 150$ ,  $\gamma_1 = -.1843$ ,  $\gamma_2 = .2481$ ,  $\gamma_3 = .1888$ , and  $\gamma_4 = .0005$ .

In our model, we have assumed that there is a fixed number of plants. An alternative, pursued by Hopenhayn and Rogerson (1993), is to assume that there is a constant fixed cost in terms of consumption goods of starting a new plant. In this alternative model, the number of plants grows over time. We have chosen our specification because it seems to be a good approximation to the data. Sands (1961) reports that over the period 1904–47, the number of manufacturing plants in the United States grew only .5% per year while output

per manufacturing establishment grew nearly 3% per year. Clearly, most of the growth of output in this period came from more output from each plant and only a small part from an increase in the number of plants.

## 7. The Transition to a New Economy

In this section, we use our quantitative model to simulate the transition to a new economy with a permanently faster pace of technical change. We think of this simulation as a quantification of the hypotheses of Devine (1983), David (1990, 1991), and others for the slow transition after the Second Industrial Revolution. In the simulation, the increase in technical change is driven by faster growth in the frontier blueprints for new plants. We think of this faster growth of the frontier blueprints as capturing the possibilities for new plant design based on electric power. We find that the process of replacing old plants based on old blueprints with new plants is gradual. As a result, there is a substantial delay before the increase in technical change is observed in faster growth of output per hour.

### A. The Transition Experiment

Consider first our transition experiment. Specifically, consider an economy that is on a balanced growth path with steady growth in the frontier blueprints causing output to grow 1.6% per year. In this economy, at the beginning of the period labeled *1869*, agents learn that the growth rate of the frontier blueprints increases once and for all, so that on the new balanced growth path, output grows 3.3% per year. We refer to these two balanced growth paths as the *old* and *new* economies, respectively.

In Figure 12, we show the model's implications for output per hour during the transition from 1869 to 1969, together with the actual data for those years. In the model as in

the data, the growth in output per hour gradually accelerates. Over the period 1869–99, the trend growth rate in output per hour is 1.6% in both the model and the data. Over the period 1899–1929, the trend growth rate in output per hour is 2.4% in the model and 2.6% in the data. In the model, the growth rate in output per hour reaches its new steady state of 3.3% by 1940.

Consider now the diffusion of new technology during the transition to a new economy. In Figure 13, we show this diffusion in the model and the data during 1869–1939. For the model, we graph the percentage of output produced in plants with blueprints dated 1869 and later. For the data, we graph the percentage of total horsepower in manufacturing establishments provided by electric motors. To make this comparison, we are assuming in the model that plants built in 1869 and later are driven by electric motors while those built before that are driven by steam and water power. In the model, it takes 45 years for technologies dated 1869 and later to diffuse to 50%. In the data, if we date the technology of electricity as starting in 1869, this level of diffusion takes 50 years.

Of course, the choice of initial dates in the data is somewhat arbitrary. To make a comparison that is not so dependent on initial dates, consider a statistic that is often used in the diffusion literature, namely, the time it takes for diffusion to go from 5% to 50%. This time is roughly 20 years (1899–1919) in the data and 19 years in the model. Either way we measure it, therefore, the diffusion in the model is similar to that in the data.

## **B. Diffusion in the Old and New Economies**

Our model implies a gradual acceleration in the speed of diffusion of new technologies: slow in the old economy, medium during the transition, and fast in the new economy. Here

we argue that this implication is consistent with the data. Since we have just discussed the transition period, we only need to examine the old and new economies here.

In our model, in the old economy, a new technology takes about 68 years to diffuse to 50%, during the transition this diffusion takes about 45 years, while in the new economy it takes about 25 years.

In terms of the data, the slow diffusion of a new technology in the old economy is similar to the slow diffusion of steam power in the United States throughout the 1800s. The date in Figure 2 indicates that by 1869 steam power had diffused to a little over 50%. If we assume that the diffusion of steam power started sometime between 1800 and 1810, then these data indicate that steam power took roughly 60 to 70 years to diffuse to 50%. In choosing this starting date we follow *Atack, Bateman and Weiss (1980)*. Moreover, as shown in Figure 2, steam power took roughly another 20 years to diffuse from 50% to 80%. In our model, in the old economy, this same diffusion of a new embodied technology from 50% to 80% takes 19 years. Thus, the diffusion in our model's old economy is roughly consistent with data on the diffusion of steam power in the 1800s.

In the new economy, new technologies take about 25 years to diffuse to 50%. This speed of diffusion is determined by our calibration of the model to shares of employment for plants of different ages.

This pattern of gradual acceleration in the speed of diffusion is consistent with the evidence presented by *Lynn (1966)*. He examines the speed of diffusion of 20 major innovations in three time periods: pre-World War I (1890–1919), post-World War I (1920–44), and post-World War II (1945–64). *Lynn* concludes that the speed of diffusion in the post-World War II period was twice that in the post-World War I period and three times that in the

pre–World War I period.

### C. The role of built-up knowledge

In our model, the stock of *built-up knowledge* embodied in plants is the key factor generating the gradual acceleration of growth and diffusion over the transition. Here we discuss how to measure this stock of built-up knowledge, and we conduct three transition experiments that highlight its role.

A measure of the stock of built-up knowledge relative to the frontier blueprints is

$$\left(\frac{\bar{A}_t}{\tau_t}\right)^{1-\nu}.$$

Note that  $\bar{A}_t/\tau_t$  is the average of the specific productivity across plants relative to the frontier blueprints available to new plants. The exponent  $1 - \nu$  expresses this ratio in units of the Solow residual of a standard growth model. In the new steady state, this ratio is 1.24, and in the original steady state, it is 2.21. Thus, the portion of aggregate productivity due to built-up knowledge is 78% higher in the original steady state than in the new steady state. This measure is lower when the growth of the frontier blueprints is faster because plants have little time to build up knowledge when they are adopting new technology relatively rapidly.

The large stock of built-up knowledge in the old economy is the reason the transition is slow. As the transition begins, managers are reluctant to close existing plants and lose this knowledge for what, initially, is only a marginally superior technology.

We demonstrate the importance of this built-up knowledge for the speed of transition as follows. Suppose, counterfactually, that existing plants in 1869 had the stock of built-up knowledge corresponding to an economy with rapid growth of the frontier blueprints. Specifically, consider a transition in which the initial distribution of plant-specific productivities



is from the new steady state. Clearly, if we also set the initial capital-output ratio equal to its new steady-state value, then there is no transition: the economy immediately grows 3.3% and new technologies diffuse to 50% in 25 years. If we set the initial capital-output ratio to its original steady-state value and compute the transition, then the trend growth rate of this economy during 1869–99 is 3.2%, and technologies dated 1869 and later diffuse to 50% in only 27 years. Thus, the transition to a new economy occurs very rapidly in the absence of a large stock of built-up knowledge about old technologies.

In our model, new technologies are embodied in plants, and adopting a new technology requires discarding built-up knowledge with the old technology. This assumption is essential in generating the slow transition to a new economy. To see this, consider an alternative transition driven entirely by an increase in the growth rate of the economy-wide technology  $z$  and not by faster growth of the frontier blueprints. When the growth rate of the economy-wide technology increases, the production possibilities for all plants immediately increase with no loss of built-up knowledge. Suppose that at the beginning of 1869, agents learn that the growth rate of the economy-wide technology increases once and for all, so that on the new balanced growth path, output grows 3.3% per year. Here, the transition to a new economy is rapid: technologies dated 1869 and later diffuse to 50% in 25 years, and the trend growth rate of output during 1869–99 is 3.2%. Clearly, when the increase in the pace of technical change is not embodied in plants, the transition takes little or no time.

In the model, the stock of built-up knowledge in the old economy depends on the span of control parameter  $\nu$ . As we increase the span of control parameter, the stock of built-up knowledge in the old economy increases and the transition to the new economy slows. For example, consider our transition experiment with  $\nu = .9$  as opposed to its baseline value of

$\nu = .85$ . In this experiment, the trend growth of output per hour in the model is 1.6% for the 1869–99 period and only 1.8% for the 1899–1929 period, and technologies dated 1869 and later take 57 years to diffuse to 50%. This transition is slower because with the higher value of  $\nu$ , there is 110% more built-up knowledge in the original steady state relative to the new steady state. When  $\nu = .85$ , the comparable number is only 78%.

## 8. Conclusion

A sustained increase in the pace of technical change eventually leads to a new economy with higher growth in productivity. Devine (1983) and David (1990, 1991), among others, argue that if new technologies are embodied in organizations and if organizations must learn to use new technologies efficiently, then the transition to the new economy will take quite some time. We have formulated a quantitative model of these hypotheses and have shown that it can account for the main features of the transition to a new economy after the Second Industrial Revolution.

David (1990) argues that this transition serves a useful historical parallel for understanding the recent seeming paradox of rapid technical change in information technologies accompanied by relatively slow growth in productivity. We argue that while this parallel may be useful qualitatively, it may be less so quantitatively. Before an analysis of the Information Technology Revolution can be fleshed out in a quantitative model, three key issues must be addressed: Where are the new technologies embodied? How long is the period of learning after these technologies are adopted? And how much built-up knowledge do existing organizations have with their current technologies? With regard to information technologies, none of these questions are easy to answer.

In our model of the Second Industrial Revolution, we followed the historical literature in assuming that new technologies are embodied in the design of manufacturing plants. This assumption does not seem to be immediately applicable to the Information Technology Revolution, since where the information technologies are embodied is not clear. There is some evidence that organizations can use these technologies efficiently only after the organizations have been substantially restructured, so the new technologies might be embodied somehow in the structure of the organization. (See Brynjolfsson and Hitt 2000.) Perhaps our model could be adapted to analyze the Information Technology Revolution, but the unit of analysis would probably shift to some level of organization other than plants.

In our model, we used data on the birth, growth, and death of plants to draw inferences about the speed of learning. It is not clear what corresponding data there are for quantifying the speed of learning in the Information Technology Revolution. Clearly, such data would be critical to evaluate the impact of these technologies.

In our model, the extent of built-up knowledge in existing organizations is smaller the faster is the pace of technical change. Since the pace of technical change was relatively fast even before the Information Technology Revolution began, our model implies that the initial stock of built-up knowledge before this revolution is relatively small. Thus, the speed of transition to a new economy should be relatively fast.

To make this concrete, consider a final transition experiment. Suppose, as before, that the pace of technical change increases so that the steady-state growth rate increases 1.7 percentage points. But instead of starting with a relatively slow growth rate of 1.6%, start with a relatively high growth rate of 3.3%. Suppose that in some period, agents learn that the growth of frontier blueprints has increased once-and-for-all, so that the economy

grows 5% per year on the new balanced growth path. In this experiment, the trend growth of output per hour is 4.1% for the first 30 years and 5.0% for the next 30 years. In this transition, new technologies diffuse to 50% in only 14 years. Clearly, the transition to a new economy occurs significantly faster in this experiment than in our baseline experiment. Since technical change over the last several decades has been relatively fast, this experiment suggests that models like ours will predict a relatively fast transition to a new economy after the Information Technology Revolution.

## Notes

<sup>1</sup>Here and throughout this study, our microeconomic data are taken from the U.S. Census Bureau's Longitudinal Research Database (LRD) on U.S. manufacturing plants. These data are broken down by crude age categories. In Figures 7, 8, and 9, we use data from the 1988 panel of the LRD obtained from the computer disk that accompanies Davis, Haltiwanger, and Schuh's (1996) book; these data are also available from Haltiwanger's Web site: <http://www.bsos.umd.edu/econ/haltiwanger/>.

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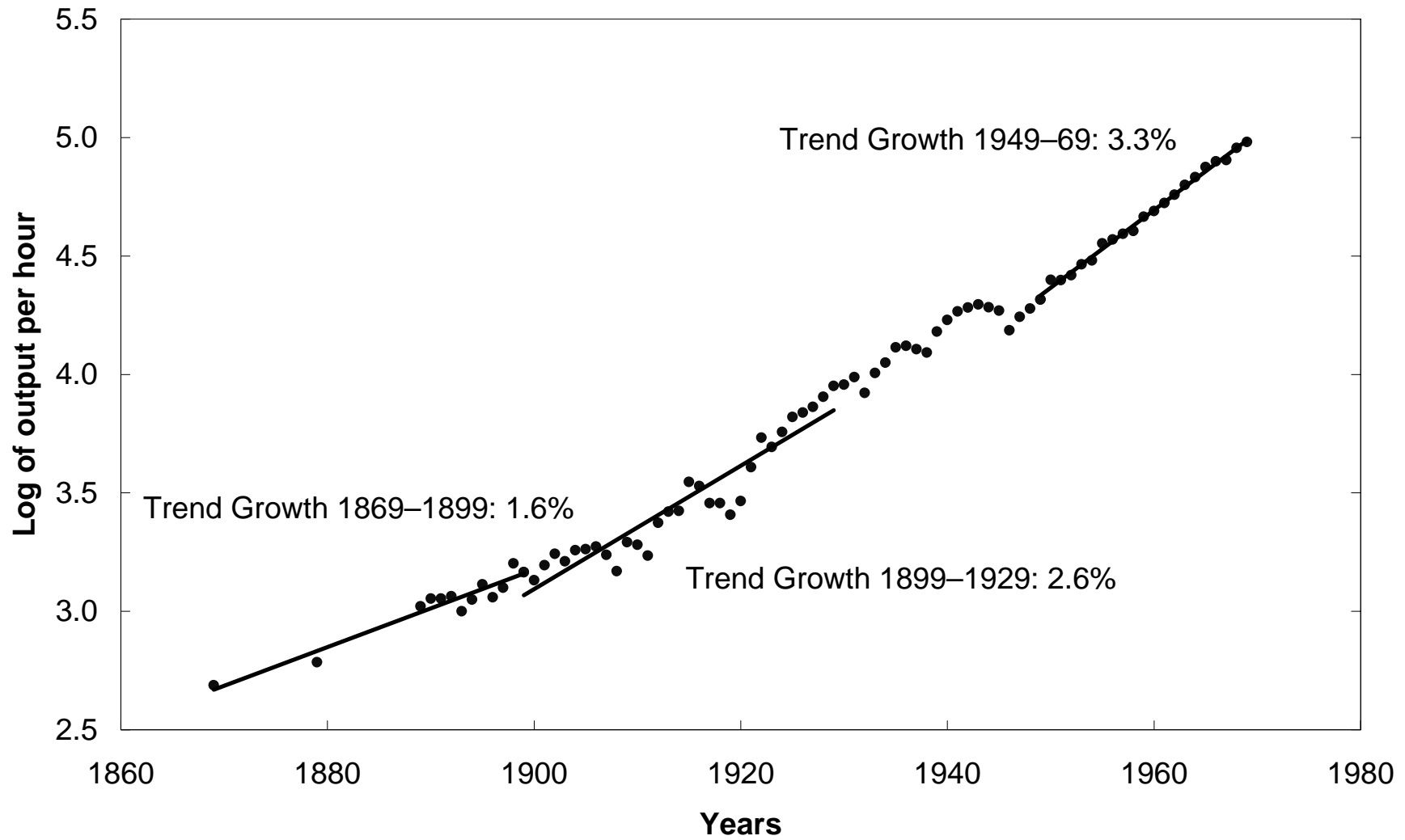
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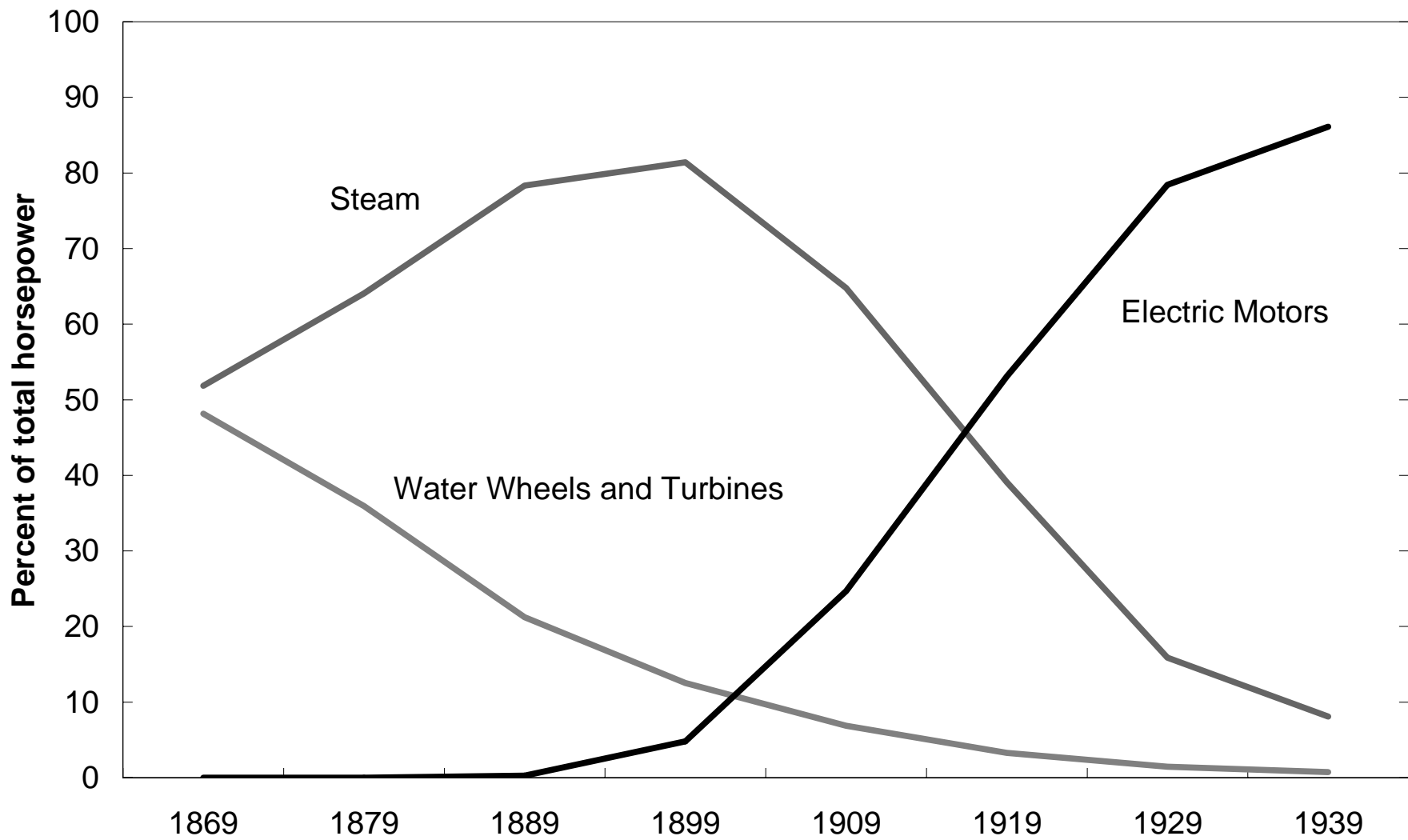
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**Figure 1:  
Output per Hour in U.S. Manufacturing**



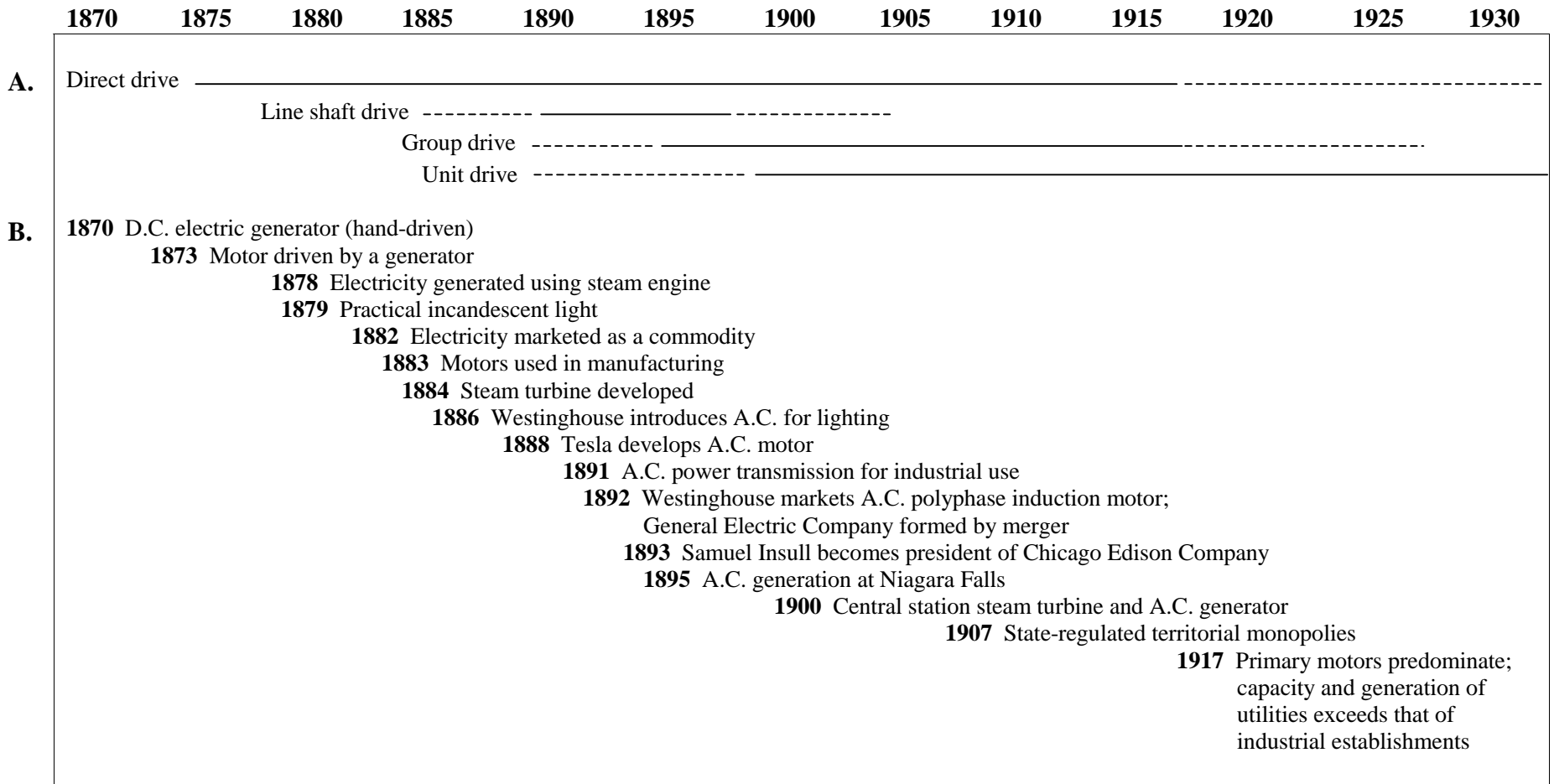
Source: U.S. Department of Commerce (1973)

**Figure 2:  
Sources of Mechanical Drive in U.S. Manufacturing Establishments  
1869–1939**



Source: Devine (1983, p. 351, Table 3)

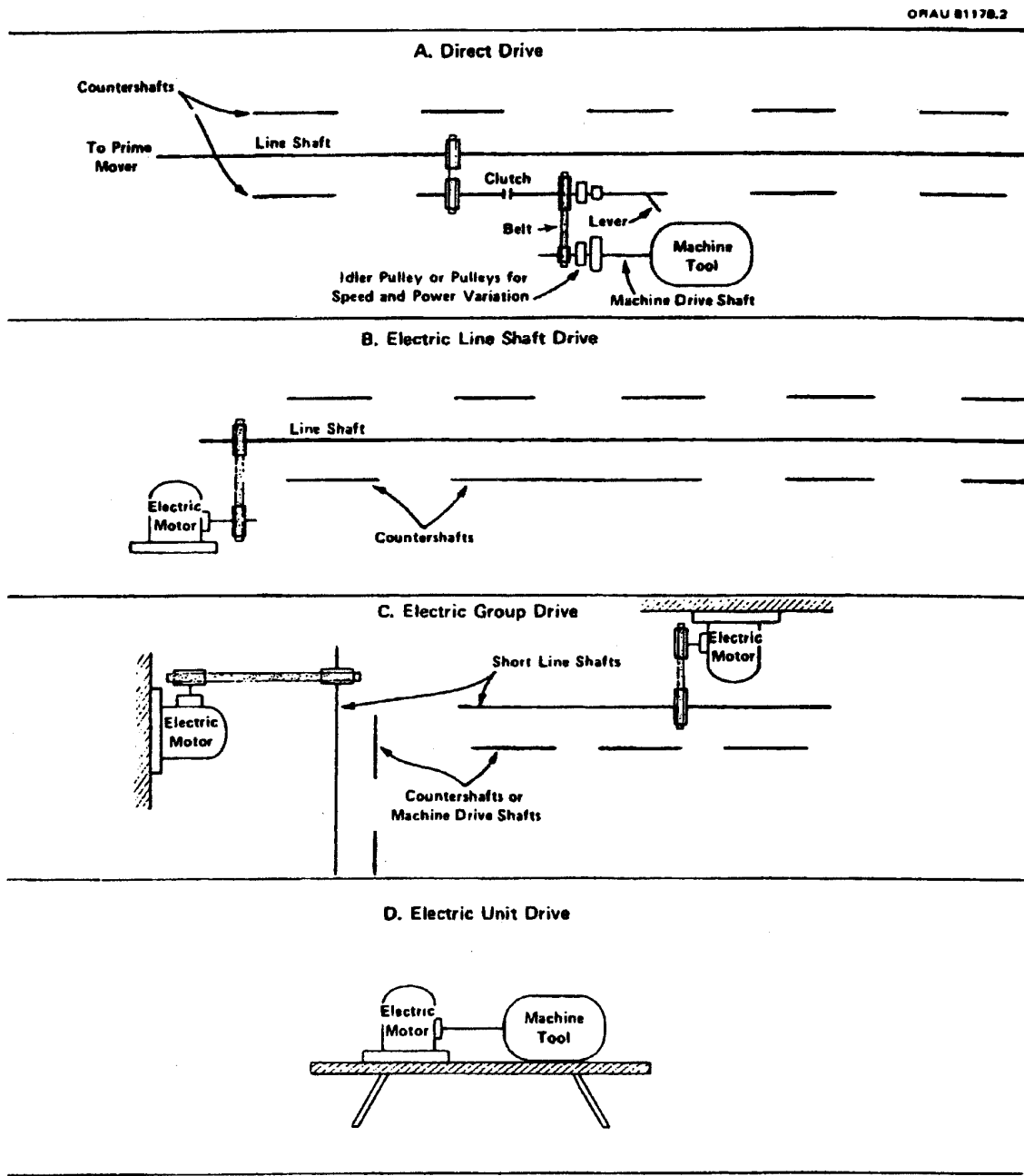
**Figure 3:** Chronology of Electrification of Mechanical Power in Industry  
 (A) Methods of Driving Machinery  
 (B) Key Technical and Entrepreneurial Developments



Source: Devine 1983, p. 354, Figure 3

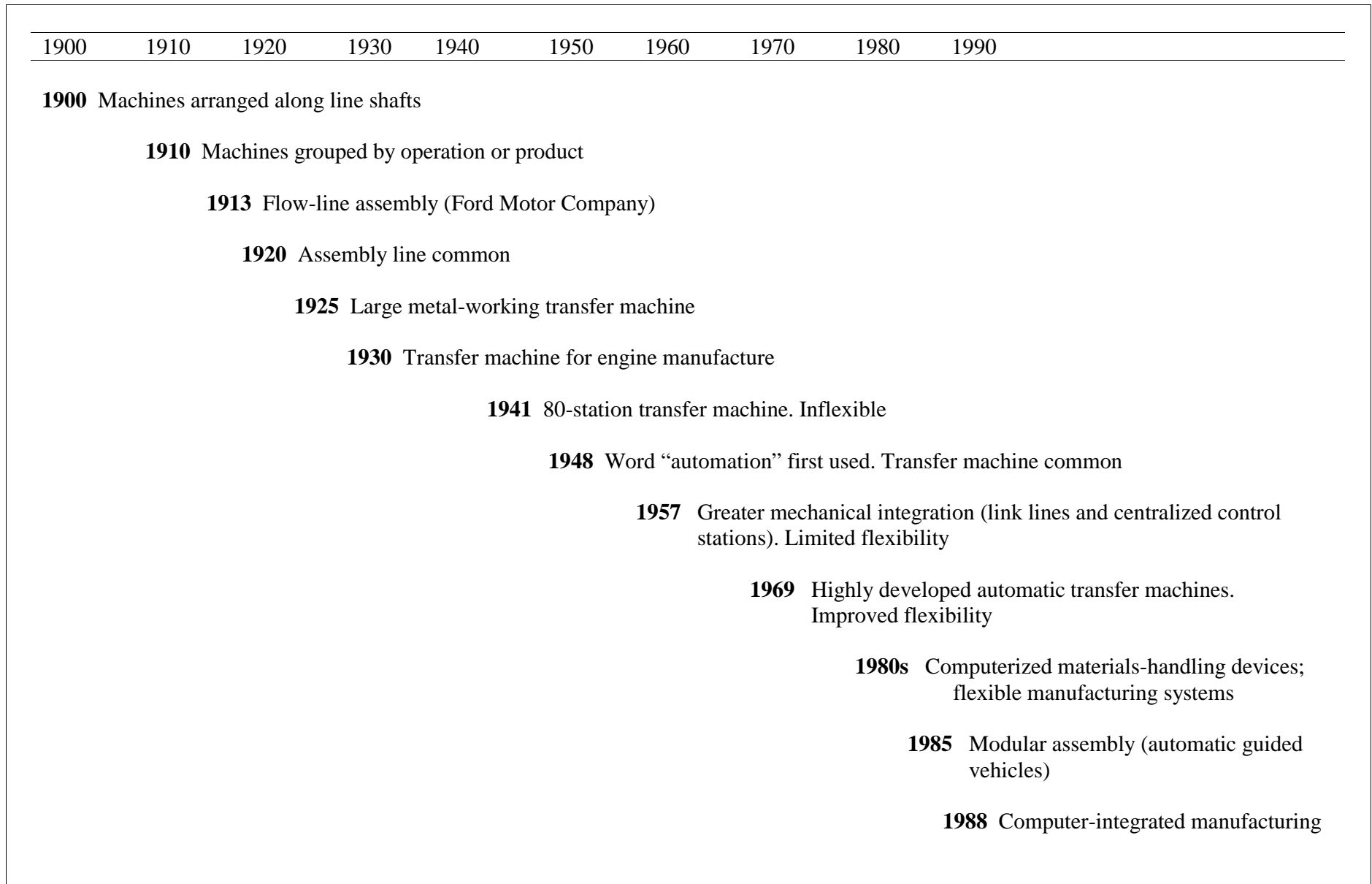
**Figure 4:** Evolution of Power Distribution in Manufacturing Establishments

## *From Shafts to Wires*



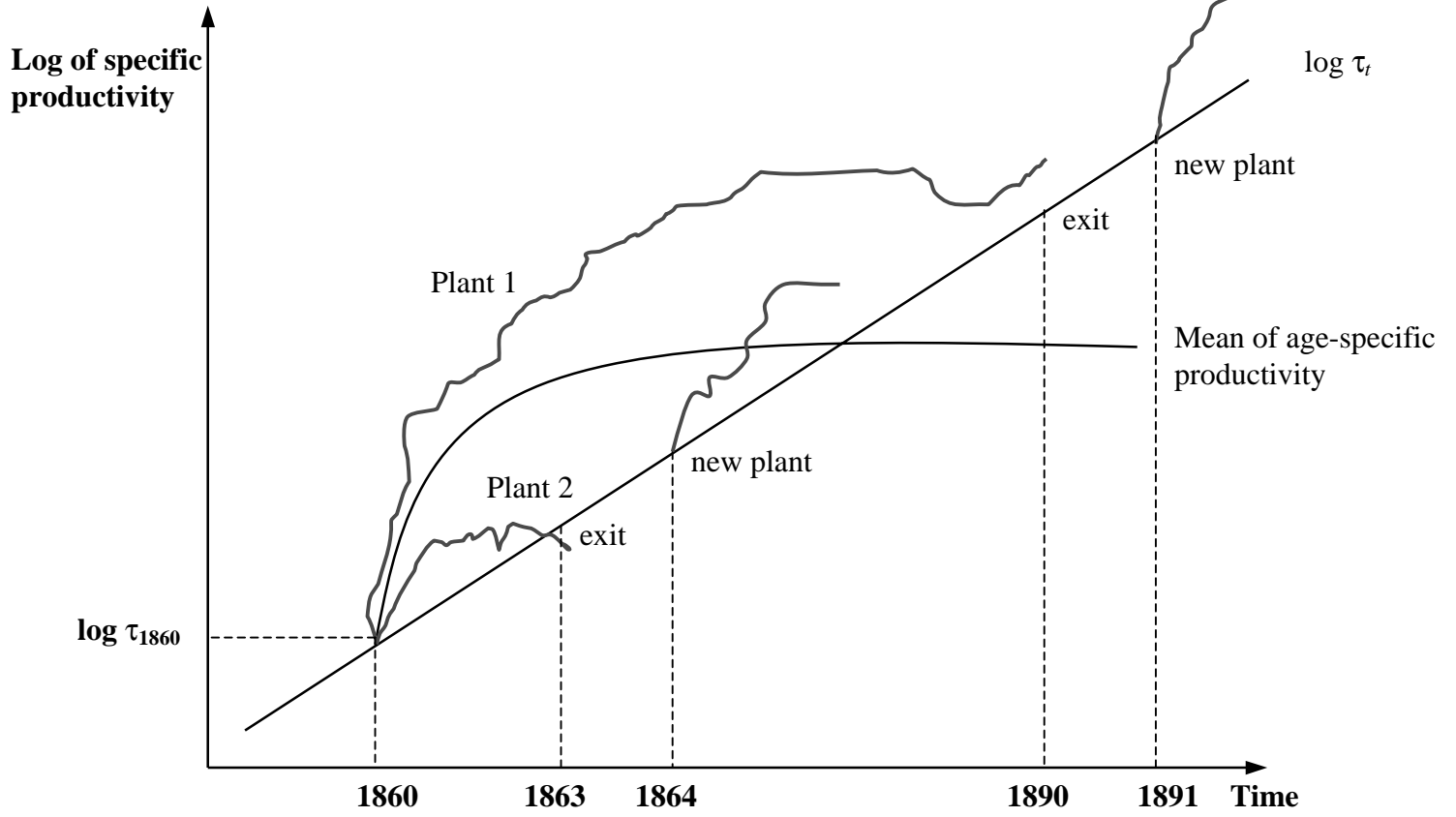
Source: Devine 1983, p. 353, Figure 2

**Figure 5:** Milestones in the Evolution of Production Organization



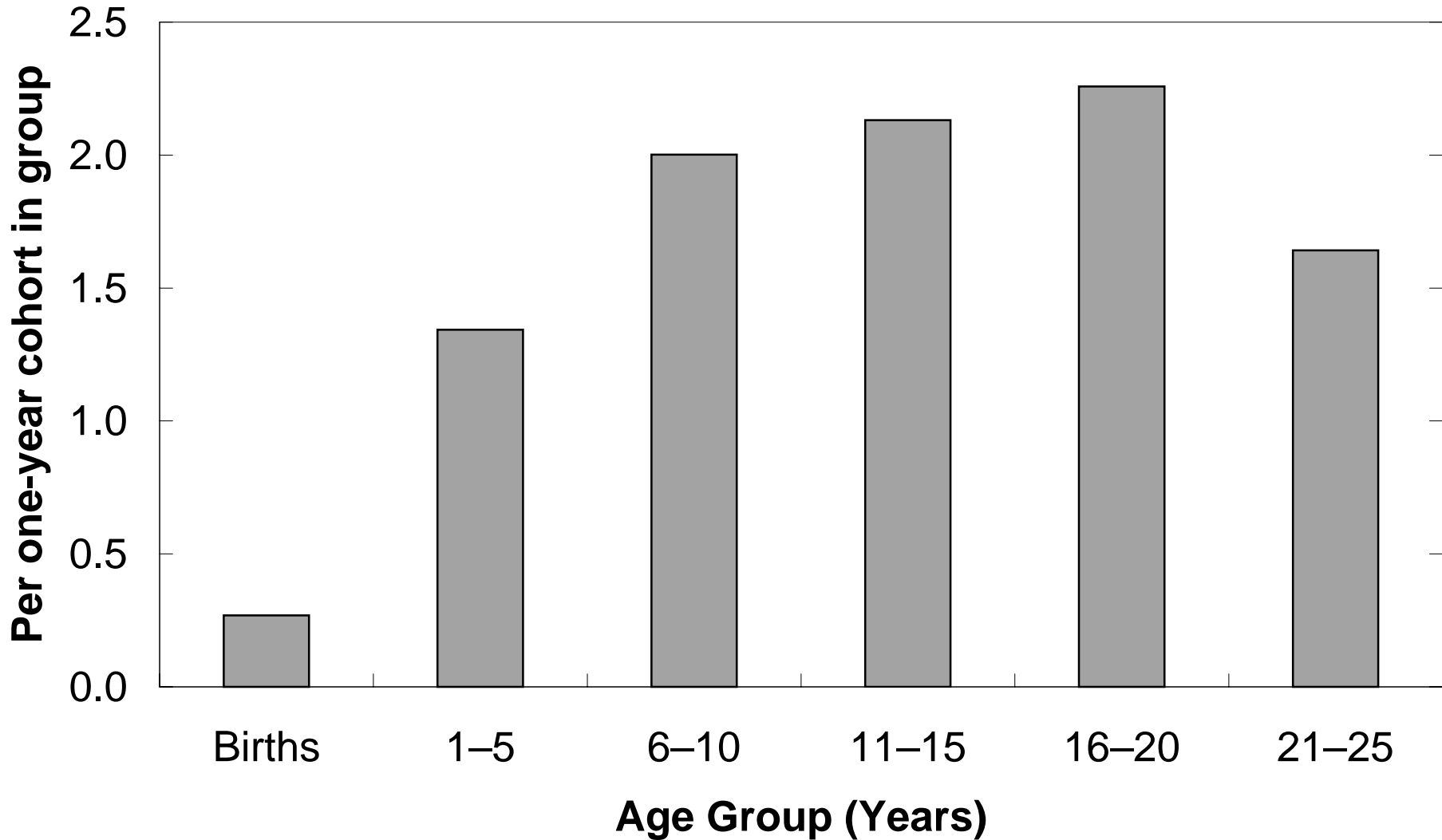
Source: Devine 1990

Figure 6: The Life Cycle of Plants in the Model



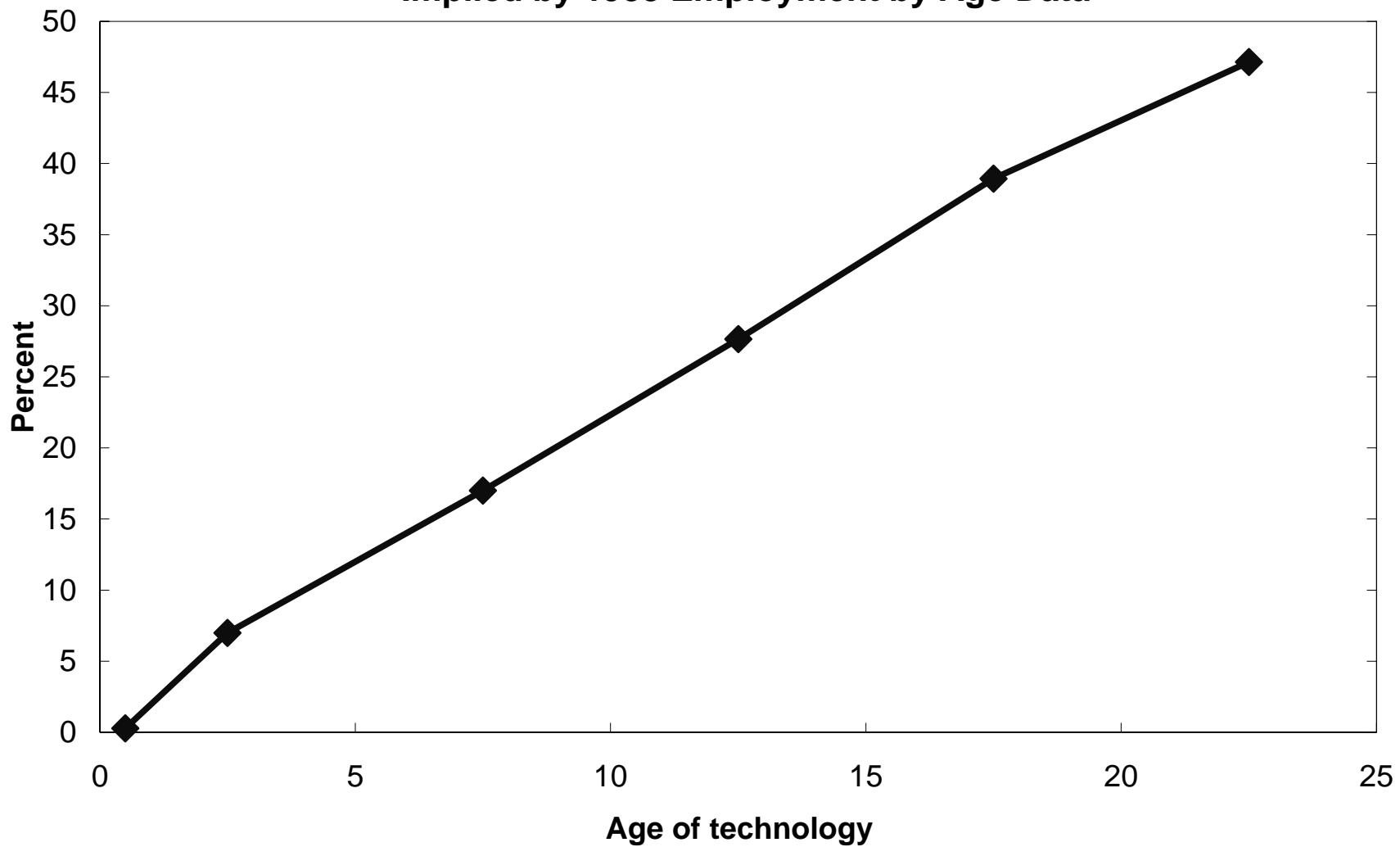


**Figure 7:  
Average Employment Share of One-Year Cohorts  
of U.S. Manufacturing Plants, 1988**



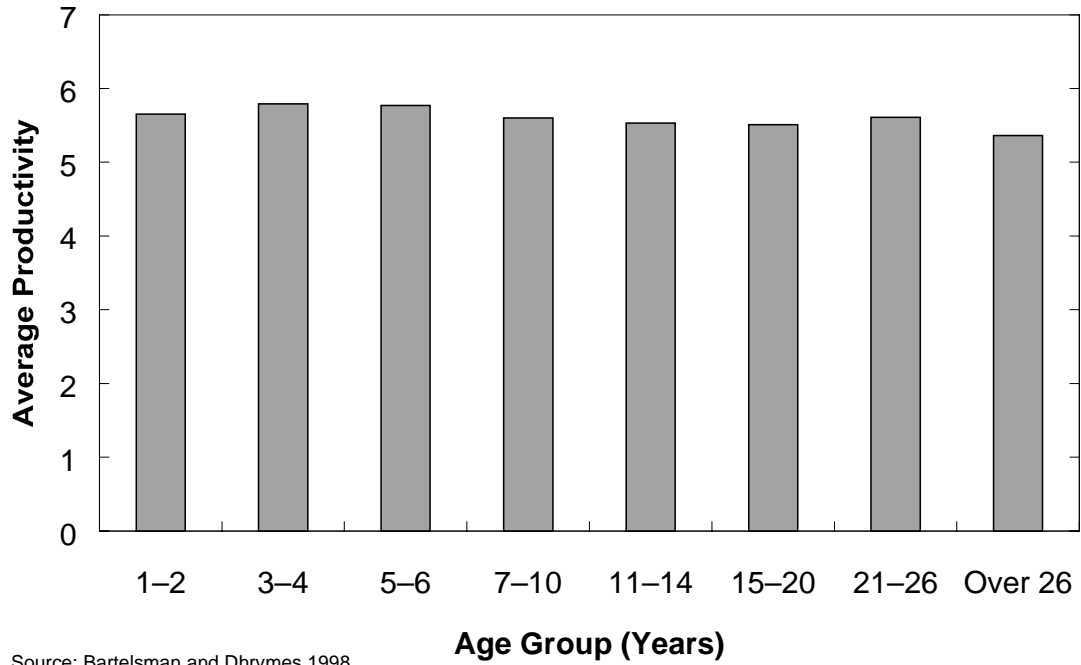
Source: See note 1.

**Figure 8:  
Diffusion of New Embodied Technologies  
Implied by 1988 Employment by Age Data**



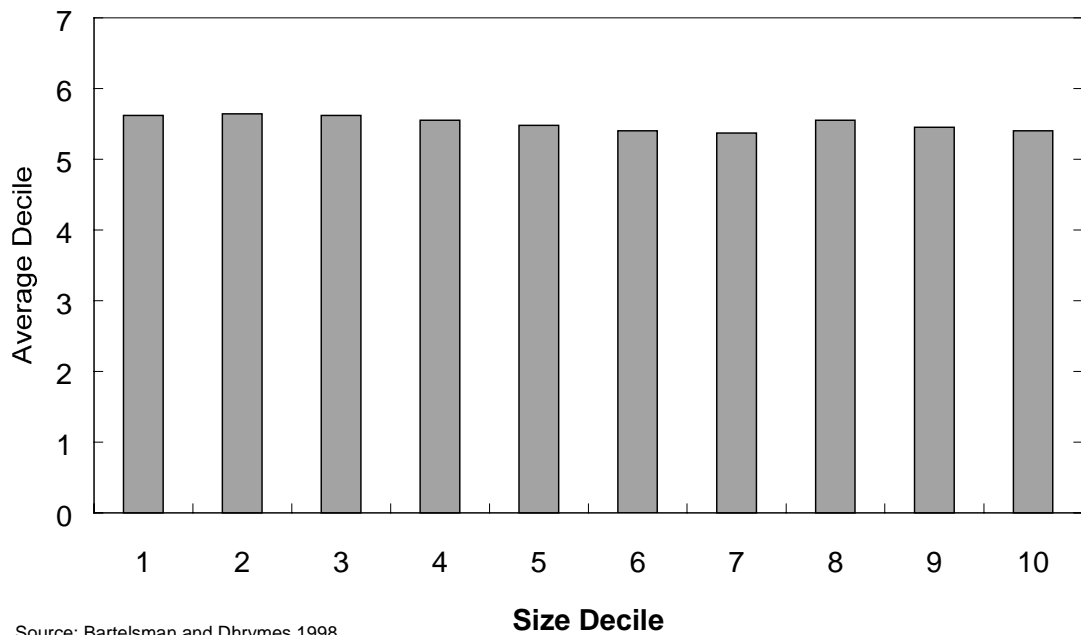
**Figure 9**

**Average Productivity of Plants by Age**



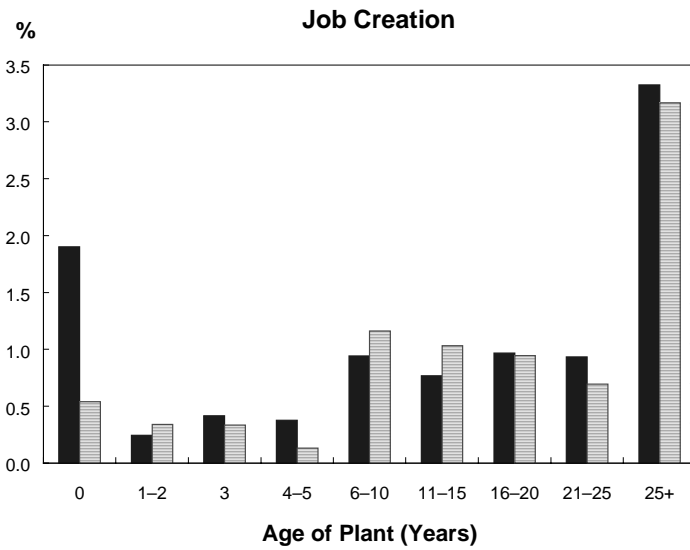
Source: Bartelsman and Dhrymes 1998

**Average Productivity of Plants by Size**

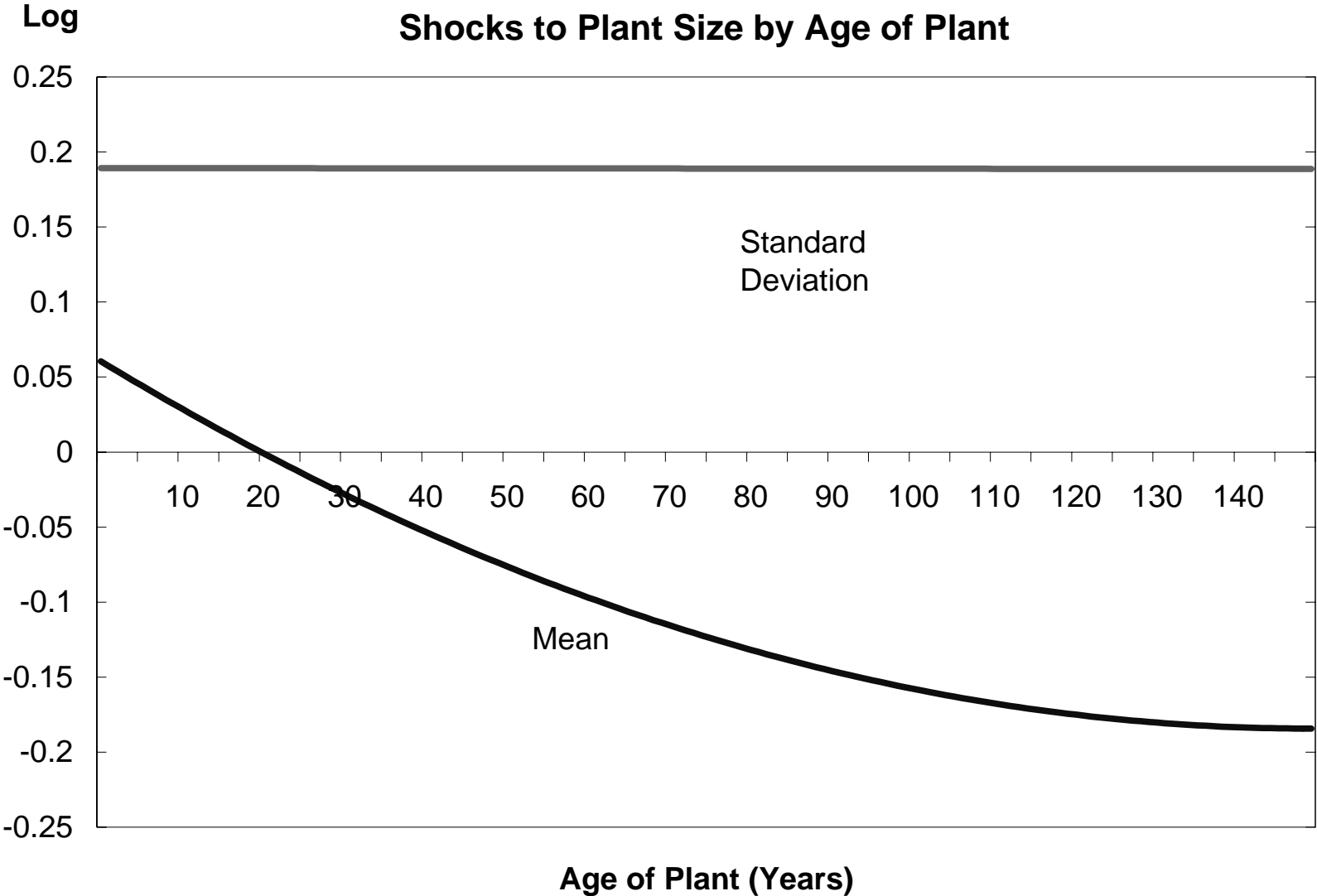


Source: Bartelsman and Dhrymes 1998

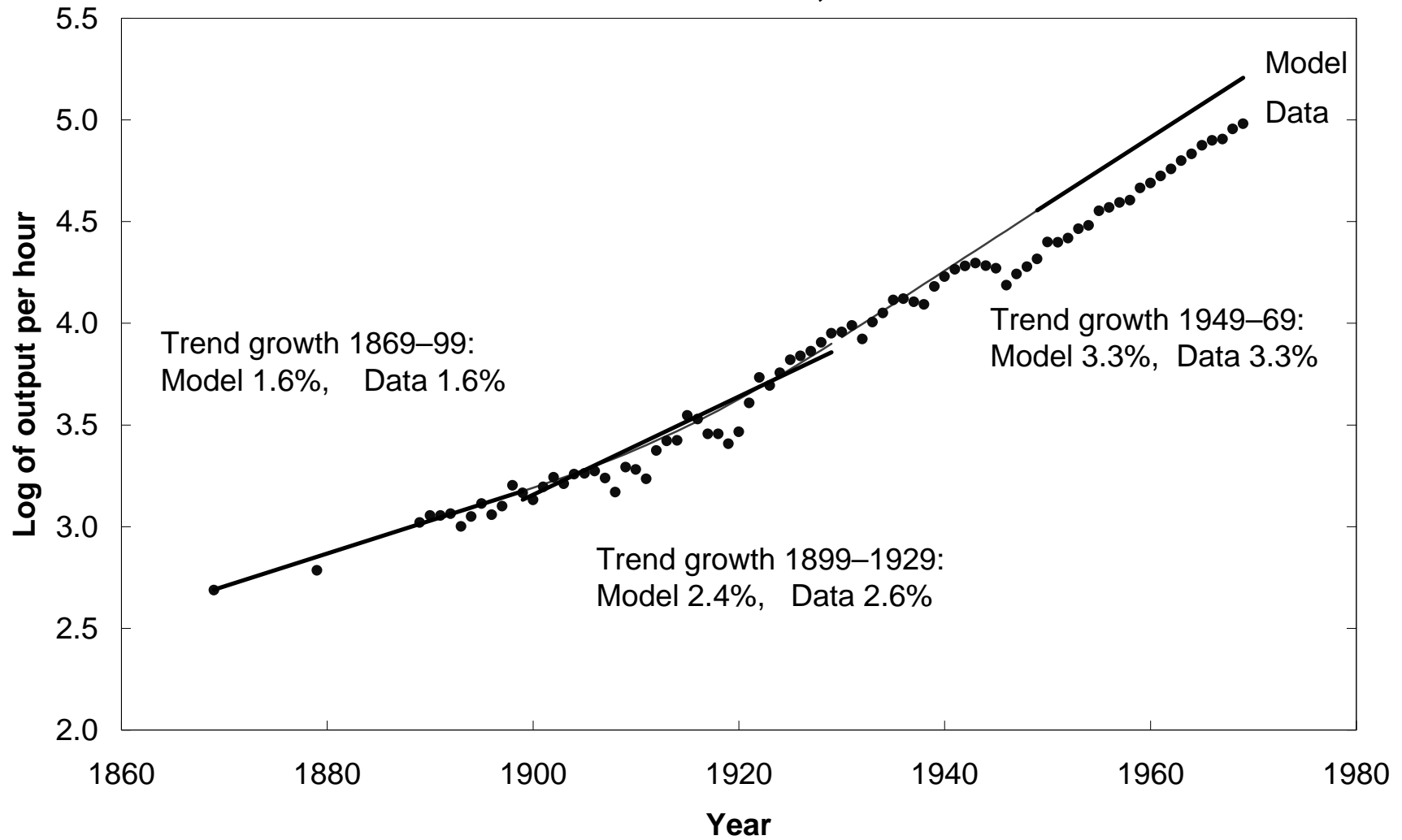
**Figure 10: Employment Statistics by Manufacturing Plant Age in the Model and in the 1988 U.S. Data (% of Total Employment)**



**Figure 11:**  
**Mean and Standard Deviation of**  
**Shocks to Plant Size by Age of Plant**



**Figure 12:  
Output per Hour in the  
Model and the U.S. Data, 1869–1969**



**Figure 13:**  
**Diffusion of New Technology, 1869–1939**  
**Model: (% of output produced in plants with new blueprints) vs.**  
**Data: (% of horsepower from electric motors in U.S. plants)**

