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ON THE INTERPRETATION OF NEAR
RANDOM WALK BEHAVIOR IN GNP

Kenneth D. West

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ABSTRACT

It is shown that GNP will have an autoregressive root very close to unity in a variant of Taylor's (1980a,b) overlapping wage contracts model, for stylized versions of simple money supply rules and plausible values for the model's parameters. In this variant, monetary policy is the only reason for serial correlation in GNP. It is premature, therefore, to conclude, as some authors have, that the presence of such a root in U.S. GNP is inconsistent with either a stationary natural rate or with nominal shocks playing a major role in the business cycle.

Kenneth D. West
Department of Economics
Princeton University
Princeton, NJ 08544

Several recent papers have studied the univariate time series process for U. S. GNP, including Campbell and Mankiw (1986), Clark (1986a,b), Cochrane (1986), Nelson and Plosser (1982), Quah (1986), Stock and Watson (1986) and Watson (1986). A major focus of these papers has been the extent to which GNP movements are well approximated by a process with a unit root with drift, as opposed to stationary movements around a time trend. The empirical evidence on this is mixed. Campbell and Mankiw (1986), Nelson and Plosser (1982), and Stock and Watson (1986) conclude that the random walk (unit root) approximation is quite good, Clark (1986a,b), Cochrane (1986) and, perhaps, Quah (1986) and Watson (1986) that it is not.

Campbell and Mankiw (1986) and Nelson and Plosser (1982) both argue that if the random walk approximation in fact is reasonable, there are important implications for business cycle theory. This is because movements in random walks are permanent: a shock today has an infinitely long lived effect. The concept of a stationary natural rate, Campbell and Mankiw note, has little utility if a GNP shock is, on average, never offset by a return to some trend rate of GNP. Nelson and Plosser suggest that monetary disturbances are unlikely to be an important source of GNP fluctuations, since monetary shocks are typically thought to have no permanent effect. Both conclude that if the random walk characterization is accurate, an implication is that fluctuations in GNP are unlikely to be driven by nominal demand shocks.¹ Similar inferences appear to be drawn by Stultz and Wasserfallen (1985), Deaton (1986) and Blanchard and Quah (1987).

Campbell and Mankiw (1986) and Nelson and Plosser (1982) of course recognize that their random walk characterization is only a convenient approximation. In any finite sample, it will not be possible to discriminate

between a unit root (random walk) and an root arbitrarily near, but below, unity (what this paper calls a "near random walk"). This is potentially a practical problem. The Monte Carlo evidence in Dickey and Fuller (1981) indicates that with Nelson and Plosser's (1982) sample size (less than 100), Nelson and Plosser's test of a unit root null is not very likely to reject even when the true process is stationary, with autoregressive coefficients whose sum is as low as .8. Coefficients of this size and larger are suggested by studies that assume the GNP process is stationary. An AR(2) of log real GNP around trend fitted to annual U.S. data 1948-1985, for example, yields coefficients whose sum is .83; since the estimate of this sum is sharply downward biased for processes with near unit roots (Fuller (1976)), the .83 point estimate is suggestive of a sum even closer to unity.²

The aims of this paper are twofold. The first is to point out that it is dangerous to use a single country's univariate GNP process to draw structural inferences concerning the stability of the natural rate, or of the importance of nominal shocks in business cycles, given that in practice one cannot discriminate between random walk and near random walk behavior. The second is to emphasize that simple natural rate models with nominal shocks are as capable as simple real business cycle models (e.g., King et al. (1987)) in generating a highly persistent process for GNP.

The paper uses a variant of Taylor's (1980a,b) overlapping wage contracts model, which maintains a stationary natural rate.³ In my variant (unlike Taylor's) the only source of instability--the only reason GNP ever deviates from the natural rate--is shocks to monetary policy. Thus, monetary policy is the only important factor in the business cycle. It is shown that near random walk behavior in GNP can result from monetary policy of the sort often

attributed to the U. S. Federal Reserve.

The basic idea is as follows. In practically any model, including Taylor's, serial correlation in movements of the money stock puts serial correlation in movements in prices. In Taylor's model, prices do not adjust instantaneously to movements in money. Additional persistence in prices is induced by the overlapping wage contracts. Movements in real interest rates and real balances therefore are serially correlated, and this induces serial correlation in aggregate demand and GNP. The degree of the serial correlation depends on the monetary authority's money supply rule and the model's basic parameters. Stylized versions of simple money supply rules, and plausible values for the model's basic parameters, suggest near random walk behavior in GNP. The implied autoregressive root is about .8 to .99.

Near random walk behavior, then, is perfectly consistent with Taylor's natural rate model. This is, of course, implicitly a message in Taylor (1980a,b), since it is argued there that, at least in the presence of supply shocks, the model is capable of tracking observed movements in GNP. The present paper generalizes Taylor's result in two ways. First, I show that near random walk behavior results even in a model with purely nominal shocks. In light of Campbell and Mankiw's (1986) and Nelson and Plosser's (1982) interpretation of their results, this seems important to establish. Second, I show that near random walk behavior results even in a version of Taylor's model extended to include standard IS and LM curves, with a monetary policy rule of targeting the interest rate. Given the widespread use of such an aggregate demand apparatus (at least in textbooks), this seems to be an useful generalization.

Before deriving my results, let me emphasize what I am not arguing. I am

not arguing that destabilizing monetary policy is the sole, or even most important, source of U. S. GNP's near random walk behavior. I am suppressing the supply and demand shocks present in Taylor (1980a,b) not because I doubt their importance, but to make my point as cleanly and emphatically as possible. I am also not arguing that the unit root approximation is a bad one. It is probably appropriate for forming simple ARIMA forecasts (McCallum (1986a)), for example. It may even be appropriate for structural estimation and inference: I am not arguing for a stationary monetary theory of the business cycle against, say, a nonstationary real theory. My point, rather, is that the stylized facts about GNP are perfectly consistent with Taylor's widely used model. Simple analysis of a given country's univariate process for GNP therefore is unlikely to be particularly helpful in distinguishing stationary from nonstationary theories, nor between models in which nominal shocks are very important from those in which they have negligible effects.

I. Near Random Walk for GNP

The aggregate supply curve (Phillips curve) is borrowed from Taylor (1980a,b). There are staggered two period wage contracts. In each period, one half of the labor force fixes its nominal wage for the next two periods.

$$(1) \quad x_t = .5x_{t-1} + .5_{t-1}x_{t+1} + .5x_{t-1}y_t + .5x_{t-1}y_{t+1},$$

$$(2) \quad p_t = .5(x_t + x_{t-1}),$$

$$(3) \quad y_t = -\delta(i_t - p_{t+1} + p_t),$$

$$(4) \quad m_t - p_t = \theta_1 y_t - \theta_2 i_t,$$

$$(5) \quad i_t = \lambda i_{t-1} + u_t.$$

The variables are: x_t = log nominal contract wage, y_t = log GNP, i_t =

nominal interest rate, $p_t = \log$ price level, $m_t = \log$ money supply, u_t a serially uncorrelated shock. A "t-1" subscript, as a prefix, denotes expectations at time t-1. All variables are zero mean deviations from trend. Trend GNP is by definition potential or natural rate GNP.

Equation (1) says that the nominal wage depends on actual and expected wages, as well as expected demand pressure. The latter is measured by expected deviations of GNP from trend. Equation (2) is a price markup equation. Equation (3) is a standard IS curve, relating GNP to the ex-ante real interest rate. Equation (4) is a standard LM curve, expressing the demand for money as a function of the nominal interest rate and GNP. As noted in the introduction, the supply and demand shocks that quite plausibly are present in equations (1) to (4) are suppressed, to emphasize the potential role for monetary policy in output fluctuations.

Equation (5) is the money supply rule, with $0 \leq \lambda < 1$ and u_t a serially uncorrelated shock. The monetary authority is thus assumed to smooth movements in interest rates. Empirical evidence that i_t followed a near random walk in the post war period (λ is near one) may be found in Fama and Gibbons (1982). A theoretical argument why the Fed might have set nominal interest rates to follow a near random walk may be found in Mankiw (1986).

It is straightforward, though tedious, to solve the model.⁴ Let

$$(6) \quad a = -(1+\gamma^{-1}\delta^{-1}) + \gamma^{-1}\delta^{-1}(4\gamma\delta+1)^{1/2},$$

$$b = 2\gamma\delta(\lambda+\lambda^2) / \{(\lambda-1)(a\gamma\delta+\lambda\gamma\delta+2+2\gamma\delta)\}.$$

The appendix shows that the contract wage x_t obeys

$$(7) \quad (1-aL)(1-\lambda L)x_t = bu_t,$$

where L is the lag operator. In conjunction with the price markup equation (2), equation (7) can be used to solve for the stochastic process for p_t . When this is plugged into the IS curve (3), one can calculate the stochastic process for y_t . Output in general follows an ARMA (2,2) process,

$$\begin{aligned}
 (8) \quad y_t &= [\eta(L)/\rho(L)]u_t, \\
 \rho(L) &\equiv (1-aL)(1-\lambda L), \\
 \eta(L) &\equiv \delta[(-1+.5b) + aL - .5bL^2] \\
 &= (-\delta+.5b\delta)[1 + (-1+.5b)^{-1}aL - (-1+.5b)^{-1}(.5b)L^2] \\
 &\equiv d_0(1+d_1L+d_2L^2).
 \end{aligned}$$

To see how the properties of (8), the univariate process y_t , depend on the monetary policy rule (depend on λ), consider two cases. The first is $\lambda=0$, $i_t=u_t$. Since $\lambda=0$ implies $b=0$ (see equation (6)), we have from (8) that

$$(9) \quad y_t = -\delta u_t.$$

So if the monetary authority takes care that the current nominal interest rate is independent of past shocks, deviations of output from the natural rate are serially uncorrelated.

Consider instead the case when λ is near unity. From (6), as $\lambda \rightarrow 1$, $b \rightarrow \infty$. It follows that for λ arbitrarily near one, d_1 (defined in (8)) will be arbitrarily near zero and d_2 arbitrarily near -1. Thus for λ very near 1, $\eta(L)$ will factor as $(-\delta+.5b\delta)(1+\eta_1L)(1-\eta_2L)$, $\eta_1 \approx 1$, $\eta_2 \approx 1-\lambda$. Since the $1-\eta_2L$ factor approximately cancels the $1-\lambda L$ autoregressive factor, y_t will behave very much like the ARMA(1,1) process that results when these factors are cancelled,⁵

$$(10) \quad y_t \approx d_0[(1+L)/(1-aL)]u_t.$$

It follows that y_t will behave much like a variable with a unit root if \underline{a} is near one.

We have $\underline{a} \rightarrow 1$ as $\gamma\delta \rightarrow 0$, i.e., as the aggregate supply and/or IS curves become horizontal. Taylor (1980b) estimated γ to be about .05 to .10. Sachs's (1980) Phillips curve regressions suggest that γ is about .01 to .07.⁶ Friedman's (1977) estimates suggest $\delta = .17$;⁷ Taylor (1985) indicates that δ is less than .125. If we take .01 to .10 as the range for γ , .1 to .2 as the range for δ , then $\gamma\delta$ is about .001 to .02. This yields a range for \underline{a} of about .96 to .998. See Table 1A. Plausible parameter values therefore suggest that the near random walk characterization will be quite good if the monetary authority attempts to stabilize interest rates by setting ${}_{t-1}(i_t - \lambda i_{t-1})$ to zero for λ near one. With \underline{a} this near unity, it will be difficult to reject the null hypothesis of a unit root, in sample sizes typically available.⁸

The intuition to the effect of λ on the univariate y_t process is as follows. With $\lambda=0$, the contract wage and price level are nonstochastic: $x_t = x_{t-1} = 0$ is the only stationary (constant mean) solution to (7) with $b=0$. So the IS curve (3) implies $y_t = -\delta i_t$, and, with $\lambda=0$, i_t is serially uncorrelated. By contrast, when $\lambda \neq 0$, the autoregressive root of $1-\lambda L$ in the monetary authority's control variable puts the same root in the wage and price processes; the long run properties of the money supply rule of course are reflected in wages and prices. But that is not all. As Taylor (1980a) has emphasized, overlapping contracts can be an endogenous source of persistence. The serial correlation in the money supply induces serial correlation in wages and prices above and beyond that directly produced by the $1-\lambda L$ root. So expected inflation, ${}_{t+1}p_t - p_t$, does not move instantaneously, and one to one,

with i_t . The real interest rate is serially correlated, and, therefore, as per the IS curve (3), so is GNP.

More generally, for any λ between 0 and 1, there will also be persistence in GNP. If λ is near zero, y_t will behave much like the serially uncorrelated variable defined in (9). The closer is λ to unity, the more will y_t behave like the serially correlated process defined in (10).

It is worth noting that a similar result obtains if, as in Taylor (1980a,b) the money supply rule involves targeting the money supply instead of the interest rate. To analyze this type of rule, it is convenient to follow Taylor and replace the IS and LM curves with a simple quantity equation,

$$(11) \quad y_t + p_t = m_t.$$

Unlike Taylor, I have set to zero shocks to velocity (deviations of velocity from trend), as explained in the introduction. Also, replace the interest rate target (5) with a money supply target,

$$(12) \quad m_t = gp_t + \lambda(m_{t-1} - gp_{t-1}) + u_t.$$

where u_t is a serially uncorrelated shock and $0 \leq \lambda \leq 1$.

To understand (12), consider first the case when $\lambda, u_t \equiv 0$. Then, as in Taylor (1980a), the parameter g measures how accommodative monetary policy is. (For my purposes one could have the monetary authority look directly at y_t as well as [or instead of] p_t ; only p_t appears in the money supply rule for consistency with Taylor (1980a,b).) The shock u_t is not present in Taylor (1980a,b). It is intended to reflect shocks to the money supply resulting from, say, random movements in the money multiplier. The $\lambda(m_{t-1} - gp_{t-1})$ term is present to capture a tendency of the monetary authority to absorb previous

control errors. If $\lambda=1$, previous u_t 's are never offset and are carried through to all future money supplies. Such random walk behavior ("base drift") has been argued to characterize Federal Reserve policy in the U.S., at least in recent years (see Walsh (1986) and the references cited therein).

The model may be solved as in Taylor (1980a,b); the details are omitted to save space. Let $\beta = 1-g$; $c = (1+.5\beta\gamma)(1-.5\beta\gamma)^{-1}$; $a = c - (c^2-1)^{1/2}$, if $c>1$; $a = c + (c^2-1)^{1/2}$, if $c<-1$; $b = .5\gamma(\lambda+\lambda^2)/[1+.5\beta\gamma-.5(1-.5\beta\gamma)(a+\lambda)]$. Then

$$(13) \quad \begin{aligned} x_t &= ax_{t-1} + b(m_{t-1} - gp_{t-1}), \\ y_t &= -.5\beta b[(1+L)/(1-aL)](m_{t-1} - gp_{t-1}) + \lambda(m_{t-1} - gp_{t-1}) + u_t. \end{aligned}$$

Consider first the case where $\lambda=0$, $m_t = gp_t + u_t$. Since $\lambda=0$ implies $b=0$ (see the formula for b above equation (13)), we have $y_t = u_t$, and y_t is serially uncorrelated. Suppose instead that $\lambda=1$, and $m_t = gp_t + (m_{t-1} - gp_{t-1}) + u_t$. Then it is straightforward but tedious to show that (13) reduces to

$$y_t = ay_{t-1} + u_t + .5(1-a)u_{t-1}.$$

So $y_t \sim \text{ARMA}(1,1)$. In any finite sample, y_t will look arbitrarily like a random walk for a arbitrarily close to unity. Now, $a \rightarrow 1$ as $\beta\gamma = (1-g)\gamma \rightarrow 0$. As was just noted, γ is about .01 to .10. Taylor (1980b) estimated β to be about .3. This indicates that $\beta\gamma$ is about .003 to .03, yielding an implied a of .78 to .93. See Table 1B.

The intuition to the effect of λ on the univariate y_t process is similar to that for the previous money supply rule. With $\lambda=0$, the contract wage and price level are nonstochastic: $x_t = x_{t-1} = 0$ is the only stationary solution to (13) with $b=0$. So the aggregate demand equation (11) implies $y_t = m_t$, and, with $\lambda=0$, m_t is serially uncorrelated. By contrast, when $\lambda=1$, the unit root in the money supply first of all puts a unit root in wages and prices; the long run

properties of wages and prices are governed by the money supply. But because of the staggered contracts, real balances, the difference between m and p , have additional persistence: prices do not move instantaneously, and one for one, with money supplies. This persistence is transmitted directly into GNP by the aggregate demand equation (11).

II. Conclusions

Neither stationarity of the natural rate, nor nominal shocks playing an important role in the business cycle, are inconsistent with a root very near to unity being present in the GNP process. In Taylor's (1980a,b) stationary natural rate model, extreme persistence in GNP movements is precisely what is predicted, given stylized versions of money supply rules often attributed to the Fed, and plausible values for the model's basic parameters. The model also predicts that different money supply rules would result in dramatically less persistent movements in GNP.

This is not to argue that, in fact, the business cycle in the U.S. is purely, or even largely, monetary in origin, nor that natural rate theory is to be preferred to non-natural rate theory. Rather, detailed study of the univariate process for a single country's GNP is unlikely to be particularly helpful in deciding some important business cycle issues. Potentially more helpful are comparative studies of GNP processes across various countries and various time periods. The evidence here is mixed. Stultz and Wasserfallen (1985) and Campbell and Mankiw (1987) conclude that during the post War period the random walk approximation is reasonable for a number of industrialized countries. This perhaps makes it less likely that GNP behavior could change dramatically with a change in policy regime. On the other hand, Stock and Watson (1986) find that for the U.S., the random walk approximation is

reasonable only in the post-1919 period. This is consistent with the present paper's model: the near random walk behavior of the nominal interest rate appears to have begun around 1915-1920 (Mankiw, Miron and Weil (1987)), and inflation appears to have been more sensitive to excess demand pre-1929 than post-War (Sachs (1980)).⁹ In any case, estimation of multivariate structural models is, of course, potentially still more helpful than is estimation of univariate time series.

Footnotes

1. Nelson and Plosser (1982, p166) conclude that "assigning a major portion of variance in output to the innovation in [a] nonstationary component gives an important role for real factors in output fluctuations and places limits on the importance of monetary theories of the business cycle." Campbell and Mankiw (1986, p24) state that their results are "inconsistent with many prominent theories in which output fluctuations are primarily caused by shocks to aggregate demand ... [including] models based on long-term nominal contracts."

2. Throughout, I assume annual rather than quarterly data, for two reasons. The first is for consistency with some of the relevant studies, including Taylor (1980b) and Nelson and Plosser (1982). The second is that the two period contract length that, for simplicity, will be assumed in section I below, is implausibly short for quarterly but not for annual data. In addition, and again for consistency, all empirical estimates are taken from studies using post World War II U. S. data.

3. I follow Taylor (1980a, 1980b) in interpreting his model as a natural rate one. McCallum (undated, 1987) argues otherwise.

4. The well known indeterminacy of rational expectations models under interest rate rules (Sargent (1979), McCallum (1986b)) applies here as well. The rule (5) is interpreted as in McCallum (1986b) as the limit of a certain non-interest rate rule that yields a unique stationary solution for y_t . The restriction $\lambda \neq 1$ is imposed because for $\lambda=1$ this solution technique breaks down (a divide by zero is implied). See the formula for \underline{h} in equation (6) below.

5. This illustrates the possibility that approximate cancellation of common autoregressive and moving average factors may help explain Rose's (1987) result that univariate time series have simpler ARMA representations than are

suggested by multiequation structural models. See Rose (1987, pp27-29).

6. Rewrite (1) as $x_t - x_{t-1} = \lambda_{t-1}(x_{t+1} - x_t) + \alpha y_t + e_t$, $\alpha \equiv 2\lambda$, $e_t \equiv -(x_t - x_{t-1}) - \lambda(y_t - y_{t-1} + y_t - y_{t-1})$. This is in the usual Phillips curve form, inflation = expected inflation + α *excess demand + shock. The .01 to .07 range reported in the text is one half of Sachs's (1980) estimates of α (i.e., one half of his post-War estimates of the coefficients that he calls β_1 and ϕ in his Tables 3 and 4).

7. This is Friedman's (1977, p322) implied estimate of the long-run elasticity of real spending with respect to the nominal interest rate, from regressions using quarterly data. (The short run [single quarter] elasticity is .09.) Friedman (1977, p323) notes that in his 1961-1976 sample period, nominal and expected real yields are likely to be very highly correlated, which suggests that his estimates are appropriate for an IS curve that depends on the expected real rate.

8. To make the argument in the preceding two paragraphs concrete, it may help to calculate y_t 's ARMA parameters for specific λ and a . Suppose that $a = .96$, $\lambda = .96$. (The value for λ is Fama and Gibbons's (1982, Table 2) point estimate of the first order serial correlation coefficient of monthly T-bill rates, 1953-1977; Fama and Gibbons do not report figures for annual interest rates.) Then one can grind through the formulas in the text to show that y_t 's moving average polynomial factors as $(1 + .32L)(1 - .98L)$. Output will therefore behave much like an ARMA(1,1) variable with a single autoregressive unit root of .96.

9. Stock and Watson (1986) suggest that the seeming stationarity of pre-1919 GNP may instead be an artifact of the way these data were constructed.

Appendix

As stated in footnote 4, the money supply rule (5) is understood to be the limit of a certain non-interest rate rule. This rule is a simple generalization of the rule in Driskell and Sheffrin (1986) and DeLong and Summers (1986):

$$(A1) \quad m_t = \alpha(i_t - z_t), \quad z_t \equiv u_t / (1 - \lambda L), \quad \alpha > 0.$$

Thus, if i_t is above (below) its target level z_t , m_t is increased (decreased). The rule (A1) yields a unique stationary solution for y_t for any finite α ; the solution for y_t under the rule (5) is understood to be the one that results when one first solves using a finite α and then takes the limit as $\alpha \rightarrow \infty$.

Use (A1) to eliminate m_t from the LM curve (4) and rearrange to get

$$i_t = (\alpha + \theta_2)^{-1} (p_t + \alpha z_t + \theta_1 y_t).$$

Substitute the above into the IS curve (3) and rearrange to get

$$(A2) \quad y_t = [1 + (\alpha + \theta_2)^{-1} \delta \theta_1]^{-1} \{-\delta \alpha (\alpha + \theta_2)^{-1} z_t + \delta_t p_{t+1} - \delta [1 + (\alpha + \theta_2)^{-1}] p_t\} \\ \equiv -\delta_0 z_t + \delta_1 p_{t+1} - \delta_2 p_t.$$

Since ${}_{t-1}z_t = \lambda z_{t-1}$, ${}_{t-1}z_{t+1} = \lambda^2 z_{t-1}$, (A2) implies

$$(A3) \quad {}_{t-1}y_t + {}_{t-1}y_{t+1} = -\delta_0 (\lambda + \lambda^2) z_{t-1} + \delta_1 ({}_{t-1}p_{t+2} + {}_{t-1}p_{t+1}) - \\ \delta_2 ({}_{t-1}p_{t+1} + {}_{t-1}p_t).$$

Use the price markup equation (2) to eliminate the price terms from (A3) and substitute the result into the supply equation (1). After some rearrangement, this becomes

$$(A4) \quad (\gamma\delta_1)_{t-1}x_{t+2} + [2+\gamma(2\delta_1-\delta_2)]_{t-1}x_{t+1} - [4+\gamma(2\delta_2-\delta_1)]_{t-1}x_t + (2-\gamma\delta_2)x_{t-1} \\ - 4(x_t - x_{t-1}) = 2\gamma(\lambda+\lambda^2)\delta_0z_{t-1}.$$

For (A4) to hold, $x_t - x_{t-1}$ must be identically zero. It follows from Driskell and Sheffrin (1986) that the polynomial

$$(A5) \quad (\gamma\delta_1)a^3 + [2+\gamma(2\delta_1-\delta_2)]a^2 - [4+\gamma(2\delta_2-\delta_1)]a + (2-\gamma\delta_2)$$

has exactly one stable and two unstable roots. Let the unique stable root be a_1 . Since $z_t \sim AR(1)$, it follows that solving the unstable roots forwards, the stable root backwards leads to a solution of the form $x_t = a_1x_{t-1} + b_1z_{t-1}$.

One can solve for b_1 by using $x_t = a_1x_{t-1} + b_1z_{t-1}$ to compute x_{t-1} , x_{t+2} , x_{t+1} and x_t and putting these into (A4). (The exact formula is not of interest.)

Let $\alpha \rightarrow \infty$. (The solution for y_t is the same whether one uses the present technique of solving for y_t using the x_t process that results for $\alpha \rightarrow \infty$, or solves for y_t for finite α and then lets $\alpha \rightarrow \infty$.) Then $\delta_0, \delta_1, \delta_2 \rightarrow \delta$ and (A5) reduces to

$$(a-1)[\gamma\delta a^2 + (2+2\gamma\delta)a - (2-\gamma\delta)].$$

Since $|a_1| < 1$ for finite α , then, by continuity, as $\alpha \rightarrow \infty$, a_1 approaches the stable root of $\gamma\delta a^2 + (2+2\gamma\delta)a - (2-\gamma\delta)$. This is $a \equiv -(1+\gamma^{-1}\delta^{-1}) + \gamma^{-1}\delta^{-1}(4\gamma\delta+1)^{1/2}$. Also $b_1 \rightarrow b$, where b is given in equation (6). Equation (7) now follows.

It is perhaps worth noting that one can derive the same result concerning near random walk behavior of y_t by letting $\lambda=1$ but (a) assuming that the α in equation (A1) is finite (but large), or (b) letting $\alpha \rightarrow \infty$ rather than $\alpha \rightarrow +\infty$.

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Table 1

Implied Autoregressive Root for GNP

A: interest rate target

Range for structural parameters:
sensitivity of wages to excess demand (χ): .01 to .10
slope of IS curve (δ): .1 to .2

Range for implied AR root: .96 to .998

B: money supply target

Range for structural parameters:
sensitivity of wages to excess demand (χ): .01 to .10
degree of monetary accommodation (g): .3

Range for implied AR root: .78 to .93

Note: The model for panel A consists of equations (1) to (5), for panel B of equations (1), (2), (11) and (12). In each case λ is assumed at or near unity.