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#### **BROKEN OR FIXED EFFECTS?**

Charles E. Gibbons
Juan Carlos Suárez Serrato
Michael B. Urbancic

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#### **ABSTRACT**

We replicate eight influential papers to provide empirical evidence that, in the presence of heterogeneous treatment effects, OLS with fixed effects (FE) is generally not a consistent estimator of the average treatment effect (ATE). We propose two alternative estimators that recover the ATE in the presence of group-specific heterogeneity. We document that heterogeneous treatment effects are common and the ATE is often statistically and economically different from the FE estimate. In all but one of our replications, there is statistically significant treatment effect heterogeneity and, in six, the ATEs are either economically or statistically different from the FE estimates.

Charles E. Gibbons
The Brattle Group
201 Mission Street Suite 2800
San Francisco, CA 94105
charlie.gibbons@brattle.com

Michael B. Urbancic Department of Economics 1285 University of Oregon Eugene, OR 97403-1285 urbancic@uoregon.edu

Juan Carlos Suárez Serrato Department of Economics Duke University 213 Social Sciences Building Box 90097 Durham, NC 27708 and NBER jc@jcsuarez.com Fixed effects are a common means to "control for" unobservable differences among observations based upon observable characteristics; examples include age, year, or location in cross-sectional studies or individual or firm effects in panel data. While fixed effects permit different mean outcomes among groups, the estimates of treatment effects are typically required to be the same; in more colloquial terms, the intercepts of the conditional expectation functions may differ, but not the slopes.

Our main contribution is considering the empirical importance of heterogeneity in these slopes (*i.e.*, treatment effects) across fixed effects groups. In particular, we compare treatment effect estimates using a fixed effects estimator (FE) to the average treatment effect (ATE) by replicating eight influential papers from the *American Economic Review* published between 2004 and 2009. Using these examples, we consider a randomized experiment in Section 1 as a case study and, in Section 3, we show generally that heterogeneous treatment effects are common and that the FE and ATE are often different in statistically and economically significant degrees. In all but one paper, there is at least one statistically significant source of treatment effect heterogeneity. In five papers, this heterogeneity induces the ATE to be statistically different from the FE estimate at the 5% level (7 of 8 are statistically different at the 10% level). Five of these differences are economically significant, which we define as an absolute difference exceeding 10%. Based upon these results, we conclude that methods that consistently estimate the ATE offer more interpretable results than standard FE models.

In Section 2, we provide a formal framework to establish the theoretical bias of the FE estimator in the presence of heterogenous treatment effects. We derive the probability limit of the FE under heterogeneous treatment effects and provide an interpretation as a weighted average of group-specific effects. We propose two alternative estimators that are able to consistently estimate the ATE under group-specific heterogeneity and derive the joint asymptotic distribution of these estimators with the FE.

One approach to incorporate heterogeneous marginal effects into a regression framework is the correlated random coefficients model (CRC). Our paper explores the empirical relevance of CRC

<sup>&</sup>lt;sup>1</sup>See Murphy and Topel (1985), Gentzkow and Shapiro (2013), and Oster (2014) for other examples of papers that replicate published studies to elucidate a methodological point. We only analyze the data that the authors openly provide on the EconLit website. Though some of these papers include both OLS and instrumental variables approaches, we consider the implications of heterogeneous treatment effects for the OLS specifications only to focus on the weighting scheme applied by this common procedure.

models by considering a simplified version: a fixed effects regression that includes group-specific marginal effects. This assumption corresponds to the following data-generating process:

$$y_i = x_i \beta_{q(i)} + \mathbf{z}_i' \gamma + \epsilon_i, \tag{1}$$

where  $y_i$  is the outcome for observation i among N,  $x_i$  is treatment or another variable of interest, and  $\mathbf{z}_i$  contains control variables, including group-specific fixed effects. The treatment effects are group-specific for each of the  $g = 1, \ldots, G$  groups, where group membership is known for each observation. Lastly,  $\epsilon_i$  is mean 0 with variance-covariance matrix  $\Omega$ . Our analysis of this model can be viewed as a special case of the results in Chernozhukov, Fernández-Val, Hahn and Newey (2013).

There is a long tradition in the econometrics literature considering average partial effects (see, e.g., Chamberlain, 1980, 1982, 1984, 1992, Wooldridge, 1997, 2005, Blundell and Powell, 2003, Graham and Powell, 2012, Chernozhukov et al., 2013).<sup>2</sup>

**Definition 1** (Average treatment effect (ATE)). The average treatment effect (ATE) for Equation 1 is defined as

$$\beta^{ATE} \equiv \sum_g \pi_g \beta_g,$$

where  $\pi_g$  is population frequency of group g.

An established result is that fixed effects regressions average the group-specific slopes proportional to both the sample frequency of the group and the conditional variance of treatment, an average that generally does not coincide with the average treatment effect.<sup>3</sup> Though this theoretical result is well established, there has been little guidance for the applied researcher regarding the empirical importance of the difference. We find that the difference can be large.

Comparison to the literature. Our approach is similar to the CRC model of Chamberlain (1982) (see also Chamberlain, 1984, 1992). The primary differences between our setting and that of the CRC is that (i) we focus on cross-sectional data, whereas the CRC is based on panel data; and (ii) we employ fixed, rather than random effects. Because of the general similarities, our approach is related to the large literature analyzing non-separable correlated heterogeneity in panel data

<sup>&</sup>lt;sup>2</sup>We assume that the sample is representative of the population of interest for the ATE; specifically,  $N_g/N \to \pi_g$ . <sup>3</sup>See, e.q., Angrist and Krueger (1999), Wooldridge (2005), Angrist and Pischke (2009).

contexts. Closest to our derivation, Wooldridge (2005) shows conditions under which the FE provides consistent estimates of the average partial effect. Our analysis builds upon this derivation for the case of fixed coefficients and offers a different interpretation of the necessary conditions for this result. Graham and Powell (2012) study the identification and estimation of average partial effects under "irregularity" conditions where the information bound may be singular and Arellano and Bonhomme (2012) study the identification and estimation of distributions of coefficients in CRC models.

Another important example is Chernozhukov et al. (2013), who study average and quantile treatment effects and derive results that nest our approach. In particular, while we focus on cross-sectional settings, our models are relevant for panel models with discrete regressors, as in Chernozhukov et al. (2013). Ghanem (2017) studies testable implications of the assumptions made in these non-separable panel data models. Finally, Imai and Kim (2016) study the linear fixed effect model from a matching perspective, reformulate our result from this perspective, and study dynamic extensions. While these papers provide a strong theoretical reason to believe that FE does not provide sample-weighted estimates, we illustrate the empirical importance of this distinction using a broad array of microeconometric questions.

In the presence of heterogeneous treatment effects, the FE gives a weighted average of these effects. The weights depend not only on the frequency of the groups, but also upon sample variances within the groups. Angrist and Krueger (1999) compare the results from regression and matching estimators to demonstrate that the effects of a dichotomous treatment are averaged using different weights under each procedure. Many empirical studies, including many of those that we replicate in this paper, run separate regressions by group out of concern for the presence of treatment effect heterogeneity. Less common are the more parsimonious interacted model or weighted regression approaches that we propose, but which assume that there is no heterogeneity in coefficients for other predictors. A related approach is the random growth model, which uses individual-specific time trends to control for differing growth rates (see, e.g., Heckman and Hotz, 1989, Papke, 1994, Friedberg, 1998). This heterogeneity is used to control for omitted variables, rather than to model the treatment effect of interest itself, however. Solon, Haider and Wooldridge (2015) declare that the FE may be biased in the presence of heterogeneous treatment effects and note that weighted least squares can be used to recover the average partial effect. We build upon their discussion by

deriving the necessary weights and providing applications to illustrate empirically the importance of the difference between weighted and FE estimates.

### 1 A Case Study: Karlan and Zinman (2008)

Even if an experiment ensures that treatment is independent of any other covariates, the FE might not be a consistent estimator of the ATE. Among our AER replications, there is one experiment that can be used to illustrate this point: Karlan and Zinman (2008). In this paper, the authors randomize the interest rate offered for a microloan across a population of South Africans and estimate the credit elasticity. One set of fixed effects that the authors use is the "pre-approved risk category" of the borrower (low, medium, or high). To offer interest rates commensurate with prevailing market rates, the authors charge higher rates to higher risk individuals. As we will show, however, that differing means in treatment do not drive the difference between the FE and ATE estimates, but rather differences in variances. To this point, the authors offer not only higher rates to riskier borrowers, but also offer a greater range of rates to this group and, as a result, the variance of treatment differs across the groups. Thus, the FE estimate will not be equal to the ATE if the responsiveness to interest rates varies across risk groups.

The FE weights are given in column 2 of Table 1. These are the relative variances of treatment by group multiplied by the sample frequency of that group (see Proposition 1). Using these weights and the group effect estimated using an interacted model (given in column 4 of Table 1), we calculate the FE estimate in the bottom row of the table in the "FE weight" column. Compare the weights from the FE model to the sample frequencies used to calculate the ATE. Note that high risk individuals are over-weighted in the FE model due to their relatively high variance in treatment and the low and medium risk individuals are under-weighted.

We find that high-risk borrowers are much less responsive to the interest rate than low-risk borrowers. Because high-risk individuals are over-weighted and have a smaller (in absolute value) treatment effect, the FE estimate underestimates the sample-weighted responsiveness of individuals to the interest rate by over 60%.

Table 1: Karlan and Zinman (2008) treatment effect weighting

|            |        | Weight  |         |  |
|------------|--------|---------|---------|--|
| Risk group | Effect | FE      | Sample  |  |
| Low        | -32.4  | 0.044   | 0.125   |  |
| Medium     | -9.9   | 0.058   | 0.092   |  |
| High       | -2.7   | 0.898   | 0.783   |  |
| Average    |        | -4.393  | -7.047  |  |
| Std. error |        | (1.129) | (1.917) |  |

Notes: The ATE estimated is the IWE estimator. The FE estimate here, -4.40, does not precisely equal the FE estimate of -4.37 reported in the paper due to slight correlation between mailer wave fixed effects, excluded from this simplified exposition, and the interest rate. Subsequent replication results in our paper do recover the actual values reported in the replicated papers, including this one, unless otherwise noted.

#### 2 Estimating the Average Treatment Effect

In this section, we first derivate the bias of the FE estimator under treatment effect heterogeneity. Based upon those results, we provide two alternative estimators that eliminate this bias. We also discuss testing procedures related to our proposed estimators.

#### 2.1 Bias of the Fixed Effects Estimator

One way to parameterize the treatment effect heterogeneity in Equation 1 is by interacting the fixed effects with treatment; call this vector  $\mathbf{a}_{i}$ . Then, the data-generating process can be rewritten as:

$$y_i = \mathbf{a}_i' \beta + \mathbf{z}_i' \gamma + \epsilon_i, \tag{2}$$

where  $\beta$  is now a vector of coefficients. Further define the  $N \times 1$  column vector forms  $\mathbf{Y}$ ,  $\mathbf{X}$ , and  $\boldsymbol{\epsilon}$  as vectors across the N observations and  $\mathbf{A}$  and  $\mathbf{Z}$  as matrices across observations. Define  $\mathbf{M} = \mathbf{I}_N - \mathbf{Z} (\mathbf{Z}'\mathbf{Z})^{-1} \mathbf{Z}'$  as the annihilator matrix for  $\mathbf{Z}$ ;  $\tilde{\mathbf{Y}}$ ,  $\tilde{\mathbf{X}}$ , and  $\tilde{\mathbf{A}}$  are annihilated versions. Notably,  $\tilde{x}_i$  is a value in the  $\tilde{\mathbf{X}}$  vector.

As a baseline case, consider an OLS model with fixed effects that does not account for treatment effect heterogeneity, which we call the *fixed effects estimator*.

<sup>&</sup>lt;sup>4</sup>Consider  $\mathbf{a}_i$  having first  $x_i$ , followed by  $x_i$  interacted with G-1 fixed effects.

**Definition 2** (Fixed effects estimator (FE)). Define the standard fixed effect estimator (FE) as:

$$\hat{b}^{FE} = \left(\tilde{\mathbf{X}}'\tilde{\mathbf{X}}\right)^{-1}\tilde{\mathbf{X}}'\tilde{\mathbf{Y}}.$$

In general, the FE is a biased and inconsistent estimator of the ATE.

**Proposition 1** (Bias and inconsistency of FE). Under the usual assumptions for Equation 1 (see Appendix A), the expected value of the FE is:

$$\mathbb{E}\left[\hat{b}^{FE} \middle| \mathbf{X}, \mathbf{Z}, \mathbf{A}\right] = \left[\sum_{i} \tilde{x}_{i}^{2}\right]^{-1} \sum_{i} \tilde{x}_{i} \tilde{\mathbf{a}}_{i}' \beta = \beta^{ATE} + \sum_{g} \frac{N_{g}}{N} \beta_{g} \left[\frac{\widehat{\operatorname{Var}}\left(\tilde{x}_{i} \mid g(i) = g\right)}{\widehat{\operatorname{Var}}\left(\tilde{x}_{i}\right)} - 1\right] + o_{p}(1),$$

where  $\widehat{\text{Var}}(\cdot)$  is the sample variance and  $N_g$  is the number of observations in group g. Further, the FE converges in probability to:

$$\hat{b}^{FE} \xrightarrow[n \to \infty]{} \beta^{ATE} + \sum_{g} \pi_{g} \beta_{g} \left[ \frac{\operatorname{Var}(\tilde{x}_{i} \mid g(i) = g)}{\operatorname{Var}(\tilde{x}_{i})} - 1 \right].$$

Hence, if the variance of  $x_i$  conditional on  $\mathbf{z}_i$  varies across groups and treatment effects also vary across groups, then the FE is a biased and inconsistent estimator for the ATE.

Proposition 1 reveals that, while the FE is an average of the group-specific effects, the weights generally do not coincide with sample frequencies. Instead, FE upweights groups with high variance in treatment conditional upon other covariates and downweights groups with low variance in treatment. This is an efficient approach if the treatment effect is the same for all groups, but leads to biased and inconsistent estimates of the ATE when the treatment effect varies across groups.

An example where FE would give unbiased results is a regression using data from a perfectly randomized experiment where treatment has the same variance across groups. Such perfection is likely unattainable in observational or experimental settings, however. Indeed, in Section 1, we replicated a randomized experiment from Karlan and Zinman (2008) as a case study. In that experiment, treatment is randomized within different fixed effects groups, but the variances of treatment are not the same across groups. There, we found that the ATE differs from the FE estimate by over 60%.

#### 2.2 Alternative Estimators

We offer two alternative estimators for the ATE that, unlike the FE, are unbiased and consistent. For the first estimator, Equation 2 hints that an interacted model could be used to estimate the treatment effect for each group; the resulting group-specific estimates are averaged to provide the ATE. This is the *interaction-weighted estimator*.

**Definition 3** (Interaction-weighted estimator (IWE)). The interaction-weighted estimator is found by estimating  $\beta$  from Equation 2 using an interacted model, then using these estimates to calculate the ATE. Thus, the IWE is given by:

$$\hat{b}^{IWE} = \hat{\mathbf{f}} \left( \tilde{\mathbf{A}}' \tilde{\mathbf{A}} \right)^{-1} \tilde{\mathbf{A}}' \tilde{\mathbf{Y}},$$

 $where^5$ 

$$\hat{\mathbf{f}} = \frac{1}{N} \left[ \begin{array}{cccc} N & N_1 & \cdots & N_{G-1} \end{array} \right].$$

Proposition 1 shows that, while FE provides a weighted average of the treatment effects, these weights do not equal sample frequencies. The regression-weighted estimator re-weights each observation to undo the FE weighting and applies the frequency weighting of the ATE. A potential advantage of this approach is that it does not require estimating each group's treatment effect.

**Definition 4** (Regression-weighted estimator (RWE)). The regression-weighted estimator re-weights each observation according to

$$\hat{w}_i = \left[\widehat{\text{Var}}\left(\tilde{x}_j \mid g(j) = g(i)\right)\right]^{-1/2}; \tag{3}$$

that is, inversely proportional to the standard deviation of the conditional treatment values within its group. Let  $\hat{\mathbf{W}}$  be a diagonal matrix of these values squared. Then, the RWE is given by:

$$\hat{b}^{RWE} = \left(\tilde{\mathbf{X}}'\hat{\mathbf{W}}\tilde{\mathbf{X}}\right)^{-1}\tilde{\mathbf{X}}'\hat{\mathbf{W}}\tilde{\mathbf{Y}}.$$

To calculate the RWE, first estimate the annihilator matrix  $\mathbf{M}$ . Then, calculate the weights according to Equation 3. Then, perform weighted least squares using the annihilated data. Note

<sup>&</sup>lt;sup>5</sup>These weights are designed to align with the definition of  $\mathbf{a}_i$ ; see footnote 4.

that the RWE can be re-written as:

$$\hat{b}^{RWE} = \left(\sum_{i} \frac{\tilde{x}_{i}^{2}}{\widehat{\operatorname{Var}}\left(\tilde{x}_{i} \mid g(j) = g(i)\right)}\right)^{-1} \sum_{i} \frac{\tilde{x}_{i}\tilde{y}_{i}}{\widehat{\operatorname{Var}}\left(\tilde{x}_{j} \mid g(j) = g(i)\right)} = \frac{1}{N} \sum_{g} N_{g} \frac{\widehat{\operatorname{Cov}}\left(\tilde{x}_{i}, \tilde{y}_{i} \mid g(i) = g\right)}{\widehat{\operatorname{Var}}\left(\tilde{x}_{i} \mid g(i) = g\right)}.$$

The IWE and RWE can be compared to the FE. First, it should be noted that, unlike the FE, both the IWE and the RWE are unbiased estimators of the ATE (see Appendix A). Furthermore, they are consistent, which we illustrate by deriving the joint asymptotic distribution of the three estimators.<sup>6</sup> To do so, we first define  $\hat{\Omega}$  to be the variance-covariance matrix of  $\epsilon$ , which may be defined following standard heteroskedastic- or cluster-robust approaches.

**Proposition 2** (Asymptotic distribution of the estimators). Under standard assumptions for the data-generating process given by Equation 1 (see Appendix A and, e.g., Wooldridge (2001)), the asymptotic distribution of the estimators is

$$\sqrt{N} \begin{bmatrix} \hat{b}^{FE} - \beta^{FE} \\ \hat{b}^{IWE} - \beta^{ATE} \\ \hat{b}^{RWE} - \beta^{ATE} \end{bmatrix} \xrightarrow{d} N \begin{pmatrix} \mathbf{0}, \begin{bmatrix} \Sigma_{FE} & \Sigma_{12} & \Sigma_{13} \\ \Sigma'_{12} & \Sigma_{IWE} & \Sigma_{23} \\ \Sigma'_{13} & \Sigma'_{23} & \Sigma_{RWE} \end{bmatrix} \end{pmatrix},$$

where

$$\begin{aligned} \mathbf{V}_{\tilde{\mathbf{X}}} &= \mathbb{E}\left[\tilde{x}_{i}^{2}\right] & \mathbf{V}_{\tilde{\mathbf{A}}} &= \mathbb{E}\left[\tilde{\mathbf{a}}_{i}'\tilde{\mathbf{a}}_{i}\right] \\ \mathbf{V}_{\tilde{\mathbf{X}}}^{W} &= \mathbb{E}\left[w_{i}^{2}\tilde{x}_{i}^{2}\right] = 1 & \mathbf{f} &= \left[1\ \pi_{1}\ \dots\ \pi_{G-1}\right] \\ \Sigma_{FE} &= \mathbf{V}_{\tilde{\mathbf{X}}}^{-1}\left[\text{plim}\ \frac{\tilde{\mathbf{X}}'\hat{\Omega}\tilde{\mathbf{X}}}{N}\right]\mathbf{V}_{\tilde{\mathbf{X}}}^{-1} & \Sigma_{12} &= \mathbf{V}_{\tilde{\mathbf{X}}}^{-1}\left[\text{plim}\ \frac{\tilde{\mathbf{X}}'\hat{\Omega}\tilde{\mathbf{A}}}{N}\right]\mathbf{V}_{\tilde{\mathbf{A}}}^{-1}\mathbf{f}' \\ \Sigma_{IWE} &= \mathbf{f}\ \mathbf{V}_{\tilde{\mathbf{A}}}^{-1}\left[\text{plim}\ \frac{\tilde{\mathbf{A}}'\hat{\Omega}\tilde{\mathbf{A}}}{N}\right]\mathbf{V}_{\tilde{\mathbf{A}}}\mathbf{f}' & \Sigma_{13} &= \mathbf{V}_{\tilde{\mathbf{X}}}^{-1}\left[\text{plim}\ \frac{\tilde{\mathbf{X}}'\hat{\Omega}\mathbf{W}\tilde{\mathbf{X}}}{N}\right]\left[\mathbf{V}_{\tilde{\mathbf{X}}}^{W}\right]^{-1} \\ \Sigma_{RWE} &= \left[\mathbf{V}_{\tilde{\mathbf{X}}}^{W}\right]^{-1}\left[\text{plim}\ \frac{\tilde{\mathbf{X}}'\mathbf{W}\hat{\Omega}\mathbf{W}\tilde{\mathbf{X}}}{N}\right]\left[\mathbf{V}_{\tilde{\mathbf{X}}}^{W}\right]^{-1} & \Sigma_{23} &= \mathbf{f}\mathbf{V}_{\tilde{\mathbf{A}}}^{-1}\left[\text{plim}\ \frac{\tilde{\mathbf{A}}'\hat{\Omega}\mathbf{W}\tilde{\mathbf{X}}}{N}\right]\left[\mathbf{V}_{\tilde{\mathbf{X}}}^{W}\right]^{-1}. \end{aligned}$$

#### Remarks.

- 1. Identification is achieved if the FE model is identified and  $Var(\tilde{x}_i \mid g(i) = g) > 0 \,\forall g$ , that is, if there is variation in treatment (either in level or assignment status) within each group.
- 2. The IWE estimates the treatment effect for each group, allowing the researcher to examine

<sup>&</sup>lt;sup>6</sup>The fixed effects that we consider denote group membership and the sizes of these groups grow with overall sample size— $i.e., N_g \to \infty \ \forall g \in 1, ..., G, G$  fixed. This is somewhat opposite of the typical configuration in panel data problems.

the various treatment effects, which themselves may be of interest. The RWE does not estimate the group-level effects, which is an advantage if the sample size is relatively small. The effective sample size is often small when clustered standard errors are employed and the RWE may be more successful in this situation. This is particularly true if the level of heterogeneity and the level of clustering are the same or colinear.<sup>7</sup>

- 3. In the presence of heterogeneous treatment effects, the IWE may reduce standard errors by modeling the effects directly. The IWE may also be more robust to model misspecification.
- 4. We only consider heterogeneity in  $\beta$  and assume constant  $\gamma$  coefficients across groups. Under this assumption, the IWE estimator is a more parsimonious version of a fully saturated model estimated separately for each group. The econometrician must decide whether this assumption is acceptable for his or her particular application.
- 5. When the IWE is estimated, a standard Wald test can be used to test for the presence of heterogeneous treatment effects. When the IWE and its associated interactions are not estimated, a score test based on the FE can be used instead.
- 6. Given the asymptotic result in Proposition 2, it is straightforward to perform a test of equality between either estimate of the ATE and the FE estimate.
- 7. These results can be confirmed using a Monte Carlo simulation; see Appendix B.

#### 2.3 Testing for Heterogeneous Treatment Effects

Armed with two estimators of the ATE, we next consider testing. First, we derive tests for the presence of heterogeneous treatment effects using both Wald and score tests. Then, we offer a specification test for equality between the ATE and the FE. These tests are implemented by Stata commands and an R package available from the authors, as discussed in Appendix C.

<sup>&</sup>lt;sup>7</sup>The RWE estimator is identified in this situation because the model form is the same as the FE model, which is identified and the clustered variance-covariance matrix is well-defined, but observations are differentially weighted based on covariates, rather than features of the error structure.

#### 2.3.1 Wald Test for Modeled Heterogeneity

If the IWE is estimated following Equation 2, then testing for the presence of heterogeneous treatment effects is straightforward. Standard or robust methods can be used to test for the joint significance of the interaction terms.

**Proposition 3** (Wald test for modeled heterogeneity). The Wald test statistic for heterogeneous treatment effects is calculated according to

$$T_W = \mathbf{p} \mathbf{V}^{INT} \mathbf{p}',$$

where

$$\mathbf{V}^{INT} = \left(\tilde{\mathbf{A}}'\tilde{\mathbf{A}}\right)^{-1}\tilde{\mathbf{A}}'\hat{\Omega}\tilde{\mathbf{A}}\left(\tilde{\mathbf{A}}'\tilde{\mathbf{A}}\right)^{-1}$$

and the  $(G-1) \times G$  matrix

$$\mathbf{p} = \begin{bmatrix} \mathbf{0} & \mathbf{1}_{G-1} \end{bmatrix}.$$

Asymptotically, this test statistic has a  $\chi^2_{G-1}$  distribution under the null hypothesis.

#### 2.3.2 Score Test for Unmodeled Heterogeneity

If the RWE is estimated, the researcher may not be interested in or able to estimate the treatment effects by group. Nonetheless, the presence of heterogeneous treatment of the form modeled by the IWE can be tested.

This procedure begins by obtaining the residual from the FE model for each observation  $e_i$ .<sup>8</sup> The score is calculated according to

$$\mathbf{s}\left(y_i; \mathbf{a}_i, \mathbf{z}_i, \hat{b}^{FE}\right) = e_i \begin{bmatrix} \mathbf{z}_i \\ \mathbf{a}_i \end{bmatrix}.$$

**Proposition 4** (Score test for unmodeled heterogeneity). A score test statistic for the presence of

 $<sup>^{8}\</sup>mathbf{e} = \mathbf{MY} - \mathbf{MX}\hat{b}^{FE}.$ 

heterogeneous treatment effects has the form<sup>9</sup>

$$T_S = N \left( \frac{1}{N} \sum_{i=1}^{N} \mathbf{s} \left( y_i; \mathbf{a}_i, \mathbf{z}_i, \hat{b}^{FE} \right) \right)' \mathbf{S}_0^{-1} \mathbf{C}' \left( \mathbf{C} \mathbf{S}_0^{-1} \mathbf{C}' \right)^{-1} \mathbf{C} \mathbf{S}_0^{-1} \left( \frac{1}{N} \sum_{i=1}^{N} \mathbf{s} \left( y_i; \mathbf{a}_i, \mathbf{z}_i, \hat{b}^{FE} \right) \right),$$

where

$$\mathbf{S}_0 = \frac{1}{N} \sum_{i=1}^{N} \mathbf{s} \left( y_i; \mathbf{a}_i, \mathbf{z}_i, \hat{b}^{FE} \right) \mathbf{s} \left( y_i; \mathbf{a}_i, \mathbf{z}_i, \hat{b}^{FE} \right)'$$

and

$$\mathbf{C} = \left[ \begin{array}{cc} \mathbf{0}_{(G-1) \times (K+1)} & \mathbf{I}_{G-1} \end{array} 
ight]$$

(see, e.g., Wooldridge, 2001). If clustering is desired, with C clusters and  $N_c$  observations in cluster c, then instead we have

$$\mathbf{S}_0 = \frac{1}{C} \sum_{c=1}^{C} \sum_{i=1}^{N_c} \sum_{i=1}^{N_c} \mathbf{s} \left( y_i; \mathbf{a}_i, \mathbf{z}_i, \hat{b}^{FE} \right) \mathbf{s} \left( y_i; \mathbf{a}_i, \mathbf{z}_i, \hat{b}^{FE} \right)'.$$

Like the Wald test above, this test statistic has an asymptotic  $\chi^2_{G-1}$  distribution under the null hypothesis.<sup>10</sup>

#### 2.3.3 Test for Equality Between the ATE and FE Estimates

Even if heterogeneous treatment effects are present, the ATE and FE may be equal or at least statistically indistinguishable. In this subsection, we derive a test that is able to distinguish between the two estimates. The same approach can be applied for either estimator of the ATE (i.e., RWE or IWE) and we refer to the chosen estimator as  $\hat{b}^{ATE}$ .

**Proposition 5** (Specification test of the differences between the FE and ATE estimates). The test of the following null hypothesis

$$H_0: \beta^{ATE} - \beta^{FE} = 0$$

$$H_a: \beta^{ATE} - \beta^{FE} \neq 0$$

<sup>&</sup>lt;sup>9</sup>This form assumes that the information matrix equality holds, which is true under standard regularity conditions and correct specification under the null (see Cameron and Trivedi, 2005).

<sup>&</sup>lt;sup>10</sup>This test may outperform the Wald test when a clustered variance-covariance matrix is used (Kline and Santos, 2012).

can be conducted using a Hausman-style test. Note that the Wald test statistic

$$T_E = rac{\left(\hat{b}^{ATE} - \hat{b}^{FE}
ight)^2}{\mathrm{Var}\left[\hat{b}^{ATE} - \hat{b}^{FE}
ight]}$$

has an asymptotic  $\chi^2(1)$  distribution under  $H_0$ . The variance term is easily computed using the joint asymptotic distribution given in Proposition 2.

### 3 Comparing FE and ATE Estimates: An AER Investigation

To consider the empirical relevance of the distinction between the FE and ATE estimators, we turn to highly-cited papers published in the American Economic Review between 2004 and 2009. The papers that we choose are well known in their respective fields and rightfully serve as prime examples of respected empirical work. We find the eight most-cited papers that use fixed effects in an OLS model as part of their primary specification and meet additional requirements that serve to limit our scope to papers in applied microeconomics with a clear effect of interest. These papers are listed in Table 2 along with the outcomes, effects of interest, fixed effects considered, and models replicated as identified by the table and column number of appearance in the original paper. A complete description of the process that we follow to identify these papers can be found in Appendix D.1.

To consider whether the difference between the FE and ATE estimators is empirically important, we test for heterogeneous treatment effects and for a difference between the FE and ATE estimates. Our results are summarized in Table 3. For each paper, we list the groups that we consider as potential dimensions of treatment effect heterogeneity along with a test for the presence of heterogeneity, a specification test comparing the ATE and FE estimates, and the percent difference in the two estimates. In the final column, we indicate whether the author considers treatment effect heterogeneity among the groups. These statistics all use the RWE and we compute standard errors following the level of clustering used by the original author. The

<sup>&</sup>lt;sup>11</sup>We develop a Stata command and R package to perform these analyses. See Appendix C. We have posted these resources online for researchers interested in implementing these tests.

<sup>&</sup>lt;sup>12</sup>In Appendix D.3, we provide both the clustered and non-clustered heteroskedasticity-robust results. If the fixed effects groups are colinear with the clustering term, we are not able to cluster the IWE estimator. This is the case for the coastal interaction in Banerjee and Iyer (2005) and in the models of Oreopoulos (2006). Because the RWE

results for the IWE are generally very similar, as we would expect, and these results are included in the detailed tables of Appendix D.3.

Column (3) shows that all but one paper has at least one set of fixed effects groups that exhibit treatment effect heterogeneity. This heterogeneity translates into significant differences between the ATE and FE estimates for five papers at the 5% level and seven papers at the 10% level, as seen in Column (4). Defining a difference to be "economically significant" if it exceeds 10%, Column (5) shows that five papers have economically significant differences between the ATE and FE estimates. The average of the largest deviation for each paper that we consider is 21%. As a comparison, Graham and Powell (2012) find a 25% difference between their CRC and FE estimates.

The weighting scheme employed by FE yields a more efficient estimator in the absence of heterogeneous treatment effects. This suggests that FE may be more efficient if heterogeneity is relatively unimportant. As we have shown, however, the FE is generally an inconsistent estimator of the ATE. This presents a bias-variance trade-off. Figure 1 shows the relationship between the largest absolute difference between the FE and RWE estimates for each paper and compares that to the percent difference in the standard errors of the two estimators. The ATE estimator exhibits standard errors that are less than ten percent larger than those for the FE in six of eight cases. Overall, the results indicate that there is not generally a strong bias-variance trade-off unless the differences between the estimates are great. But, if the difference between the estimates is great (i.e., the bias is high), then the ATE should be preferred for policy and interpretability reasons.

estimator does not require estimating the interactions, clustering is possible in these cases. We choose to present the RWE results in Table 3 for this reason.

<sup>&</sup>lt;sup>13</sup>If the difference in the standard errors is positive, the RWE has a larger standard error.

 $<sup>^{14}</sup>$ It is perhaps not surprising that the standard errors for Karlan and Zinman (2008) increase substantially given the large change in the estimate (over 60% for the RWE). But the t-statistics are similar: -4.00 using FE and -3.94 using the RWE.

Table 2: Papers from the AER used in the meta-analysis

| Citation                    | Outcome  | Effect of interest           | Fixed effects  | Table | Column    |
|-----------------------------|--|------------------------------|--|-------|-----------|
| Banerjee and Iyer (2005)    | Fertilizer use Proportion irrigated Proportion other cereals Proportion rice Proportion wheat Proportion white rice Rice yield (log) Wheat yield (log) | Proportion non-landlord land | Coastal dummy, year  | 3     | 1         |
| Bedard and Deschênes (2006) | Smoking dummy  | Veteran status               | Age, education, race, region                                 | 5     | 1         |
| Card et al. (2008)          | Saw doctor dummy<br>Was hospitalized dummy   | Age over 65 dummy            | Ethnicity, gender, region, year, education level             | 3     | 6, 8      |
| Karlan and Zinman (2008)    | Loan size  | Interest rate (log)          | Mailer wave, risk category                                   | 4     | 1         |
| Lochner and Moretti (2004)  | Imprisonment   | Education                    | Race, age, year  | 3     | 1         |
| Meghir and Palme (2005)     | Wage (log; change in)  | Education reform             | High ability dummy, high father's education dummy, sex, year | 2     | 1 (row 1) |
| Oreopoulos (2006)           | Wage (log)   | Education                    | Age, Northern Ireland dummy                                  | 2     | 3         |
| Pérez-González (2006)       | Market-book ratio Operating returns  | CEO heir inheritance         | High family ownership dummy, year                            | 9     | 1, 6      |

Notes: Additional details on our replications are found in Appendix D.

Table 3: AER replication results

| Citation                    | Fixed effect                      | Joint test | Diff. test | Percent          | In paper |
|-----------------------------|-----------------------------------|------------|------------|------------------|----------|
| (4)                         | (2)                               | (p-value)  | (p-value)  | diff.            | (a)      |
| (1)                         | (2)                               | (3)        | (4)        | (5)              | (6)      |
| Banerjee and Iyer (2005)    | Coastal                           | 0.065*     | 0.013**    | $-31.7\dagger$   |          |
| (Proportion irrigated)      | Year                              | 0.000***   | 0.896      | 0.0              |          |
| Bedard and Deschênes (2006) | Age                               | 0.942      | 0.830      | -0.2             |          |
|                             | Education                         | 0.002***   | 0.875      | -0.1             |          |
|                             | Race                              | 0.080*     | 0.084*     | 0.5              |          |
|                             | Region                            | 0.697      | 0.392      | 0.1              |          |
| Card et al. (2008)          | Ethnicity (outcome: saw doctor)   | 0.000***   | 0.211      | -0.5             | X        |
|                             | Gender                            | 0.000***   | 0.582      | -0.4             |          |
|                             | Region                            | 0.028**    | 0.258      | 0.3              |          |
|                             | Year                              | 0.229      | 0.603      | 0.8              |          |
|                             | Education (whites only)           | 0.028**    | 0.278      | -2.0             | X        |
|                             | Education (non-whites only)       | 0.967      | 0.798      | -0.4             | X        |
|                             | Ethnicity (outcome: hospitalized) | 0.001***   | 0.614      | -0.1             | X        |
|                             | Gender                            | 0.000***   | 0.068*     | -0.5             |          |
|                             | Region                            | 0.004***   | 0.301      | 0.2              |          |
|                             | Year                              | 0.383      | 0.436      | -1.3             |          |
|                             | Education (whites only)           | 0.096*     | 0.431      | 1.0              | X        |
|                             | Education (non-whites only)       | 0.743      | 0.296      | 3.3              | X        |
| Karlan and Zinman (2008)    | Mailer wave                       | 0.234      | 0.782      | 0.2              |          |
|                             | Risk category                     | 0.005***   | 0.003***   | 69.7†            |          |
| Lochner and Moretti (2004)  | Race (all)                        | 0.000***   | 0.000***   | -1.7             | X        |
|                             | Age (blacks only)                 | 0.000***   | 0.000***   | $32.6\dagger$    |          |
|                             | Year (blacks only)                | 0.000***   | 0.000***   | 1.6              |          |
|                             | Age (whites only)                 | 0.000***   | 0.000***   | $29.0^{\dagger}$ |          |
|                             | Year (whites only)                | 0.005***   | 0.095*     | -0.2             |          |
| Meghir and Palme (2005)     | High father's education           | 0.000***   | 0.000***   | 15.5†            | X        |
|                             | Gender                            | 0.344      | 0.514      | 0.3              | X        |
|                             | Year                              | 0.000***   | 0.337      | 0.1              |          |
| Oreopoulos (2006)           | N.Ireland                         | 0.000***   | 0.001***   | 0.8              | X        |
|                             | Age (Great Britain)               | 0.242      | 0.006***   | 1.8              |          |
|                             | Age (N. Ireland)                  | 0.590      | 0.275      | 0.8              |          |
|                             | Age (N. Ireland & Great Britain)  | 0.005***   | 0.053*     | 1.2              |          |
| Pérez-González (2006)       | Year (outcome: MB)                | 0.143      | 0.327      | -11.3†           |          |
| •                           | High family ownership             | 0.135      | 0.510      | 9.2              |          |
|                             | Year (outcome: OR)                | 0.111      | 0.491      | -7.5             |          |
|                             | High family ownership             | 0.423      | 0.503      | 9.4              |          |

Notes: All results are using the RWE estimator. Column 3 gives the p-value for the test of the joint significance of the interaction terms using a score test. Column 4 gives the p-value for a t test of the difference between the ATE and FE estimates. Column 5 gives the percent difference between these two estimates. The last column indicates whether the author considers heterogeneity among these groups. A single star indicates significance at the 10 percent level, two stars indicate significance at the 5 percent level, and three stars indicate significance at the 1 percent level. A dagger indicates a difference of more than 10 percent between the two estimates.

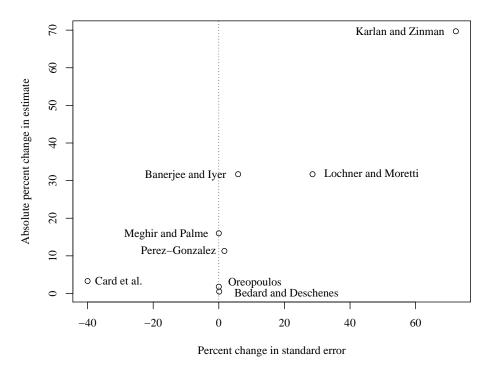


Figure 1: The relationship between the difference in the estimates and the change in variance among the AER replications

Notes: Figure is based on the full results presented in Appendix D.3. Figure plots estimates from the RWE and corresponding standard errors at the level of clustering used by the original authors, where applicable.

#### 4 Conclusion

We show that, in the presence of heterogeneous treatment effects, OLS with group fixed effects generally offers a biased estimator of the average treatment effect, a result that has relevance for a variety of fields, including labor, development, health, public finance, and corporate finance. Based on this evidence, we suggest that researchers explore the impact that heterogeneous treatment effects may have on their estimates by considering the interaction-weighted or regression-weighted estimators or by analyzing the group-specific weights implied by OLS with fixed effects. We believe that reporting average treatment effects will make estimates more interpretable for individual papers and, perhaps more importantly, across academic studies without increasing the variance of the estimates.

The methods employed in this paper, however, are subject to three notable limitations. First, when clustered standard errors are used, small-sample issues may arise when the number of groups grows close to the number of clusters. When this situation arises, researchers must choose between estimating conservative standard errors and providing a treatment effect that is representative of the whole sample. The optimal solution is inherently application specific.

Second, our discussion has been limited to the case of OLS and we have ignored issues of endogeneity. In cases where the treatment of interest can be assumed to be "as-good-as-random," as in the cases of a randomized or natural experiment, regression discontinuity, or difference-in-differences identification strategies, our methods may be applied directly. When instrumental variables are used, however, our methods will be complicated by the weights inherent in local average treatment effect estimation (Abadie, 2002, Kling, 2001); in particular, see Wooldridge (1997) for an analysis of CRC models in the context of instrumental variables estimation.

Finally, our focus in this paper has been to analyze heterogeneity in treatment effects across observable groups. Heterogeneity may also arise along unobservable margins (see, e.g., Bitler, Gelbach and Hoynes, 2014).

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#### For Online Publication

In this appendix, we first provide the asymptotic distribution of our estimators in Appendix A. Next, we give Monte Carlo simulation results as evidence for their reliability in Appendix B. Appendix C provides implementation details for our estimators in R and Stata. The final section, Appendix D provides details on our replication approach, including our selection procedure, details for the models in those papers, then detailed replication results for our estimators.

### A Asymptotic Distribution

In this appendix, we derive the asymptotic distribution of our estimators. We use standard assumptions for our data-generating process (see, e.g., Wooldridge, 2001).

**Assumptions.** Consider the following assumptions for the model defined by Equation 1:

- 1. Exogeneity:  $\mathbb{E}\left[\boldsymbol{\epsilon} \mid \mathbf{A}, \mathbf{Z}\right] = 0$
- 2. Identification:
  - (a)  $\widehat{\text{Var}}(\tilde{x}_i \mid g(i) = g) > 0 \quad \forall g \in 1, \dots, G, G \text{ fixed } (i.e., \text{ there is variation in treatment for all groups)}$
  - (b)  $\mathbf{Z}'\mathbf{Z}$  is invertible
- 3. Random sampling:
  - (a) (Heteroskedasticity-robust standard errors)  $\{(y_i, \mathbf{a}_i, \mathbf{z}_i)\}_{i=1}^N$  are i.i.d. draws from a distribution that satisfies Equation 1.
  - (b) (Cluster-robust standard errors) In the case of a clustered variance-covariance matrix  $\hat{\Omega}$ ,  $\{(\mathbf{Y}_c, \mathbf{A}_c, \mathbf{Z}_c)\}_{c=1}^C$ , where  $\mathbf{Y}_c$  is a vector of outcomes for observations in cluster c, with  $\mathbf{A}_c$  and  $\mathbf{Z}_c$  defined similarly and C fixed, are i.i.d. draws from a distribution that satisfies Equation 1.
- 4. Convergence of the variance-covariance matrix: The fourth moments of  $y_i$ ,  $\mathbf{a}_i$ , and  $\mathbf{z}_i$  exist.

We note that the IWE and RWE are both unbiased estimators of the ATE.

**Proposition 6** (Unbiasedness of IWE). Under the assumptions above, the IWE for Equation 1 is unbiased:

$$\mathbb{E}\left[\hat{b}^{IWE}\right] = \mathbf{f}\beta = \beta^{ATE}.$$

**Proposition 7** (Unbiasedness of RWE). Under the assumptions above, the RWE for Equation 1 is unbiased:

$$\mathbb{E}\left[\hat{b}^{RWE}\right] = \sum_{g} \pi_g \beta_g = \beta^{ATE}$$

Given these assumptions, standard law of large number and central limit theorem results demonstrate that the estimators converge to their respective expected values and have the asymptotic variances given in Proposition 2 and below (see, e.g., Wooldridge, 2001).

**Proposition 8** (Variances of the estimators). The variances of the estimators are:

• For the FE model:

$$Var\left(\hat{b}^{FE} \middle| \mathbf{X}, \mathbf{Z}\right) = \begin{cases} \frac{1}{N} \hat{\sigma}^2 \left[\frac{1}{N} \sum_i \tilde{x}_i^2\right]^{-1} & under \ homosked asticity \\ \frac{1}{N} \left[\frac{1}{N} \sum_i \tilde{x}_i^2\right]^{-2} \left[\frac{1}{N} \sum_i \tilde{x}_i^2 e_i^2\right] & for \ a \ robust \ estimator \\ \frac{1}{N} \left[\frac{1}{N} \sum_i \tilde{x}_i^2\right]^{-2} \left[\frac{1}{N} \sum_{c \in C} \sum_{j \in c} \sum_{i \in c} \left[\tilde{x}_j \tilde{x}_i e_j e_i\right]\right] & for \ a \ clustered \ estimator \end{cases}$$

• For the IWE:

$$Var\left(\hat{b}^{IWE}\middle|\mathbf{X},\mathbf{Z}\right) = \begin{cases} \frac{1}{N}\hat{\sigma}^{2}\hat{\mathbf{f}}\left[\frac{1}{N}\sum_{i}\tilde{a}'_{i}\tilde{a}_{i}\right]^{-1}\hat{\mathbf{f}}' & under\ homosked a sticity \\ \frac{1}{N}\hat{\mathbf{f}}\left[\frac{1}{N}\sum_{i}\tilde{a}'_{i}\tilde{a}_{i}\right]^{-1}\left[\frac{1}{N}\sum_{i}\tilde{a}'_{i}\tilde{a}_{i}e_{i}^{2}\right]\left[\frac{1}{N}\sum_{i}\tilde{a}'_{i}\tilde{a}_{i}\right]^{-1}\hat{\mathbf{f}}' & for\ a\ robust\ estimator \\ \frac{1}{N}\hat{\mathbf{f}}\left[\frac{1}{N}\sum_{i}\tilde{a}'_{i}\tilde{a}_{i}\right]^{-1}\left[\frac{1}{N}\sum_{c\in C}\sum_{j\in c}\sum_{i\in c}\tilde{a}'_{j}\tilde{a}_{i}e_{i}e_{j}\right]\left[\frac{1}{N}\sum_{i}\tilde{a}'_{i}\tilde{a}_{i}\right]^{-1}\hat{\mathbf{f}}' & for\ a\ clustered\ estimator \end{cases}$$

• For the RWE:

$$Var\left(\left.\hat{b}^{RWE}\right|\mathbf{X},\mathbf{Z}\right) = \begin{cases} \hat{\sigma}^2 \sum_{i} \hat{w}_i^4 \tilde{x}_i^2 = \hat{\sigma}^2 \sum_{g} N_g \hat{w}_{i:g(i)=g}^2 & under\ homosked a sticity \\ \sum_{i} \hat{w}_i^4 \tilde{x}_i^2 e_i^2 & for\ a\ heterosked a sticity-robust\ estimator \\ \sum_{c \in C} \sum_{j \in c} \sum_{i \in c} \left[\hat{w}_j^2 \hat{w}_i^2 \tilde{x}_j \tilde{x}_i e_j e_i\right] & for\ a\ cluster-robust\ estimator \end{cases}$$

where  $e_i$  is the residual for observation i under the corresponding estimation approach.

#### B Monte Carlo Results

This appendix explores the properties of the three estimators that we consider (*i.e.*, FE, RWE, IWE) using Monte Carlo experiments. We generate 1000 simulated datasets with 1000 observations according to the following equation:

$$y_i = \alpha_q + x_i \beta_q + z_i \gamma + \epsilon_i,$$

where  $\alpha_g$  is one of five group fixed effects with each group having an equal fraction of observations.  $x_i$  and  $z_i$  are each scalars.

We first analyze the case where the true data generating process is a model of homogenous treatment effects and show that all estimators provide consistent estimates. In particular, we set  $\beta_g = 3.5$  for all g,  $\gamma = 0.75$ , let  $\text{Cov}(x_i, z_i) = 0.3$ , and allow the variance of  $x_i$  to depend on g as follows:

$$\operatorname{Var}(x_i|g(i) = g) = \begin{cases} 58.33 & \text{if } g = 1\\ 15.03 & \text{if } g = 2\\ 7.39 & \text{if } g = 3\\ 4.57 & \text{if } g = 4\\ 2.18 & \text{if } g = 5. \end{cases}$$

Panel A of Table 4 displays the means and standard deviations of the estimates and analytic standard errors for each of the estimators. The mean estimate of  $\beta$  is very close to the true value for all three approaches when treatment effects are heterogeneous. The mean analytic standard

errors are also close to the Monte Carlo estimates of those statistics (*i.e.*, the standard deviation of the  $\beta$ s). Note that, under correct specification, the FE has smaller standard errors than the IWE and RE estimators.

We now explore the effect of allowing  $\beta_q$  to vary by group as follows:

$$\beta_g = \begin{cases} -0.5 & \text{if } g = 1\\ 1.5 & \text{if } g = 2\\ 3.5 & \text{if } g = 3\\ 5.5 & \text{if } g = 4\\ 7.5 & \text{if } g = 5. \end{cases}$$

Because each group has the same number of observations, the ATE is still 3.5. Since the variance of  $x_i$  is greater for groups with below-mean  $\beta_g$ 's, however, the FE will be biased downwards. Panel B of Table 4 displays the results from this exercise and confirms this result. Note that the standard errors of the IWE and RWE estimators are very similar, thus it does not appear that either is preferred on efficiency grounds under this data-generating process.

Table 4: Monte Carlo results

| Panel A: Homogeneous Effects               |                         |           |
|--|-------------------------|-----------|
|  | Mean                    | Std. dev. |
| Fixed Effect: $\beta$                      | 3.502                   | 0.071     |
| Fixed Effect: SE                           | 0.069                   | 0.002     |
| IWE: $\beta$                               | 3.501                   | 0.119     |
| IWE: SE                                    | 0.116                   | 0.006     |
| RWE: $\beta$                               | 3.502                   | 0.119     |
| RWE: SE                                    | 0.117                   | 0.006     |
| Panel B: Heterogeneous Effects             |                         |           |
|  | Mean                    | Std. dev. |
| Fixed Effect: $\beta$                      | 0.715                   | 0.071     |
| Fixed Effect: SE                           | 0.096                   | 0.002     |
| IWE: $\beta$                               | 3.501                   | 0.119     |
| 1 W E. P                                   | 0.001                   | 0.110     |
| IWE: SE                                    | 0.116                   | 0.006     |
| •  |                         | 0.006     |
| IWE: SE                                    | 0.116                   | 0.006     |
| $\frac{\text{IWE: SE}}{\text{RWE: }\beta}$ | 0.116<br>3.503<br>0.119 | 0.006     |

# C Implementation of the Estimators and Tests in Stata and R

As a companion to this paper, we develop Stata commands and an R package that tests for heterogeneity using both the Wald and score tests, estimates the FE, IWE, and RWE, performs the specification test for each ATE estimator, and computes the percentage difference between each

ATE estimate and the OLS estimate. These packages are available from the authors; basic syntax is discussed below.

#### C.1 Stata Commands

The ado file GSSUtest.ado contains the command GSSUtest, which estimates the IWE and performs the Wald test and the specification test of equality between the OLS estimate and the IWE. The command has the syntax:

```
GSSUtest y Tr FEg [varlist] [if] [in] [, vce(string) cluster(clustervar)] where
```

- y is the dependent variable;
- Tr is the independent variable of interest (e.g., treatment); and
- FEg is a categorical variable indexing the fixed effect group.

Other predictors can be included in varlist. For homoskedastic errors, ignore the vce() and cluster() options. For heteroskedastic-robust standard errors, use the option vce(robust) and for cluster-robust standard errors, specify cluster(clustervar).

The ado file GSSUwtest.ado contains the command GSSUwtest, which has the same syntax as above and estimates the RWE and performs the specification test of equality between the OLS estimate and the RWE. Standard errors can be computed to be robust or cluster-robust.

The intscoretest command in the ado file intscoretest.ado has the same syntax and performs the score test on the interactions between the treatment variable and the fixed effects. Standard errors can be computed to be heteroskedastic robust.

The ado file GSSUgetrdone.ado offers the command GSSUgetrdone, which has the same syntax and runs all three commands above and displays the results. GSSUgetrdone automatically uses robust standard errors in its calculations.

The results from all of the commands can be accessed through matrices stored after execution. Type ereturn list to list them.

The Stata package can be installed using the following commands:

```
* Loads website
net from http://www.jcsuarez.com/GSSU
* Describes package
net describe GSSU
* Installs commands
net install GSSU
* Downloads example data
net get GSSU
* Installs required package for GSSUgetrdone.ado
ssc install estout, replace
```

#### C.2 R Package

To estimate the IWE, use the function:

```
EstimateIWE(y, treatment, group, controls, fe.other, data, subset,
  cluster.var, is.robust, is.data.returned)
```

The RWE is estimated analogously:

```
EstimateRWE(y, treatment, group, controls, fe.other, data, subset,
  cluster.var, is.robust, is.data.returned)
```

where, for both:

- y is the name of the outcome variable;
- treatment is the name of the treatment variable;
- group is the name of the fixed effect group of interest;
- controls is a character vector of the names of other control variables;
- fe.other is a character vector of the names of other fixed effects in the model;
- data is the data frame to be used for estimation;
- subset is an optional subset declaration;
- cluster.var is the name of the variable used for clustered standard errors;
- is.robust is a logical indicating whether robust standard errors should be used; and
- is.data.returned is a logical indicating whether the data data frame should be returned with the estimation results.

For either estimation procedure, a specification test and the score test(see Appendix 2.3) are conducted by:

```
SpecTest(model, data)
ScoreTest(model, data)
```

where model is the result of one of the estimation procedures above and data is the corresponding data frame. The Wald test (see Section 2.3.1) is only conducted for the IWE estimator and has the form

```
WaldTestIWE(model)
```

The R package can be installed using the following commands:

```
install.packages('http://cgibbons.us/research/packages/GSSU.tar.gz',
   type = 'source', repos = NULL)
```

## D AER Replications

#### D.1 Paper Selection

In this paper, our goal is to determine whether the difference between an estimator of the ATE and the FE estimator is empirically important. We do this by replicating high quality papers from the AER. We examine a breadth of papers that covers several fields, several years, and several units of analysis and thus they serve as a decent representation of the use of fixed effects in the applied econometrics literature.

Our guidelines for paper selection are:

- The paper must have been published in the *American Economic Review*. We choose this qualification in order to limit our universe of analysis both in terms of quantity and quality of papers considered and to guarantee easy access to the necessary data.
- The paper must be published in the March 2004 issue or later (to March 2009, the issue predating our literature search). The *AER* policy during this period requires that, barring any acceptable restriction, the data for these papers be posted to the EconLit website. This leads to the condition that:
- The data necessary to replicate the main specification(s) of the paper must be readily available on the EconLit website.<sup>15</sup> We use these data and direct those interested to the EconLit website to obtain these files.
- The main specification(s) of the paper must have a specific effect of interest. 16
- The main specification(s) of the paper must use some type of fixed effect. We identify papers meeting this qualification by searching the PDF files of the published papers for the terms "fixed effect" (which captures the plural "effects" as well) and for "dumm" (which captures "dummy" or "dummies," common synonyms for fixed effects).
- We limit ourselves to microeconomic analyses and do not consider papers based on financial economics issues.
- We ignore papers that require special methods to handle time series issues.

We choose to replicate a total of eight papers in our analysis. To order our search, we consider papers in order of citations per year since publication. First, we use the citation counts provided by the ISI Web of Science on July 16, 2009. We limit our search to the *American Economic Review* and the years 2004–2009, as outlined above. Unfortunately, the Web of Science does not provide the volume for the papers contained therein. Instead, we create an algorithm that assigns a volume number to a paper based upon its page number; these assignments are verified as papers are considered. The total number of citations are divided by the years since publication. For example, in June 2009, a paper published in June 2004 was published 5 years before and a paper published in September 2004 was published 4.75 years before.

Citation counts are very noisy in the short time after publication that we consider here. Our citations-per-year metric might overweight later papers.<sup>17</sup> Nonetheless, the eight selected papers are drawn from a universe that includes all papers in this period with over 20 citations and 86% of all papers with 15 or more citations. It appears that we screen most of the highly-cited papers from this period and do not ignore the most recent papers, as would occur using the gross citation count.

Before estimating the ATE for the papers that we consider, we first ensure that we can replicate the results obtained by the authors as given in their respective papers. We can provide Stata DO and log files that generate and produce these results. We add our estimation procedures to these files as well.<sup>18</sup>

<sup>&</sup>lt;sup>15</sup>We determine which specifications are the "main" ones by considering the discussion of the effects in the text by the authors and ignore those specifications identified as robustness checks.

<sup>&</sup>lt;sup>16</sup>In a previous version of this paper, we included a paper by Griffith, Harrison and Van Reenen (2006). Upon reflection, this paper does not satisfy this criterion and has been removed from consideration.

<sup>&</sup>lt;sup>17</sup>In June 2009, 1 citation for a paper published in March 2009 is equal to 4 for a paper published in June 2008 and 20 for a paper published in June 2004.

<sup>&</sup>lt;sup>18</sup>See Section C.

In choosing the fixed effects groups to consider when there are several fixed effects in the regressions, we choose such that the number of groups is not unruly (U.S. states, for example, may produce too many terms to be informative). Our interacted regressions preserve all other features of the replicated specifications (e.g., clustering, robust standard errors, and inclusion of other covariates) unless otherwise noted in the text.

We do not claim that the source of heterogeneity that we consider is the most salient within the given economic situation. Additionally, we do not suggest that modeling treatment effect heterogeneity is the first-order extension of the analysis in the papers that we examine. We make no effort to search the subsequent literature to identify other areas of concern in these papers. Lastly, many of these papers employ instrumental variables to combat endogeneity. In these cases, we use the base OLS case to illustrate our point.

#### D.2 Replication Details

We replicate the specifications cited in Table 2. Some of these authors include fixed effects interactions or run regressions separately for subgroups; we list these practices in Table 5. In Banerjee and Iyer (2005), the authors have eight separate outcomes of interest. In the body of the paper, we give results only for a subset of these results.

 $\frac{2}{2}$ 

Table 5: Fixed effects interactions and regressions by subgroup conducted in the original papers

| Citation                        | Separate regressions   | Interactions  |
|---------------------------------|--|---|
| Banerjee and Iyer (2005)        | Entire country, subregion  |   |
| Bedard and Deschênes (2006)     |  |   |
| Card, Dobkin and Maestas (2008) | Race × education   | Age, age-squared  |
| Karlan and Zinman (2008)        |  |   |
| Lochner and Moretti (2004)      | Race (black, white)  |   |
| Meghir and Palme (2005)         | Sex (male, female) Father's education (low, high) Ability (low, high) Ability × father's education × sex | Sex (male, female in full sample OLS)   |
| Oreopoulos (2006)               | Country  |   |
| Pérez-González (2006)           |  | Less selective college attendance dummy<br>Graduate school attendance dummy<br>Positive R&D expenditure dummy |

Notes: Separate regressions and interaction terms only listed for specifications based upon the one given in Table 2. Pérez-González (2006) does not include the dummy variables that he subsequently interacts with treatment in his base regression; hence, we do not test their interactions here.

#### D.3 Detailed Results

In this subsection, we presented detailed results for each paper. Because the IWE and RWE results are similar, we discuss only the RWE results in the body of the paper; here, we present both sets. If clustering was used by the paper's author, we provide both the clustered and non-clustered heteroskedasticity-robust results.<sup>19</sup> The estimates are given along with standard errors in parentheses. A single star indicates significance at the 10% level, two stars significance at the 5% level, and three stars indicate significance at the 1% level.

In each table, tests for heterogeneous treatment effects are given. The Wald test is used for the IWE estimator and the score test is used for the RWE estimator.<sup>20</sup> Specification tests for the difference between the ATE and FE estimates are conduced using the Wald statistic and an asymptotic normal approximation.

Lastly, we note that we are not able to replicate the point estimate that Oreopoulos (2006) provides for his regression of Northern Ireland and Great Britain combined; we use the specification that he provides and base our results on this model.

<sup>&</sup>lt;sup>19</sup>Bedard and Deschênes (2006) and Pérez-González (2006) do not use clustered standard errors.

<sup>&</sup>lt;sup>20</sup>The Wald test is natural when the interaction coefficients are actually calculated, whereas the score test is natural when they are not, hence the pairings chosen here.

Table 6: Banerjee and Iyer (2005)

### (a) Fertilizer with coastal interaction

|                       |                      | Clustering           |                      |                      | No clustering        |                      |
|-----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|
|                       | FE                   | IWE                  | RWE                  | FE                   | IWE                  | RWE                  |
| _                     | 10.708***<br>(3.345) | 10.867***<br>(3.309) | 10.333***<br>(3.588) | 10.708***<br>(1.020) | 10.867***<br>(0.907) | 10.333***<br>(1.008) |
| Het. test stat.       |                      | 0.278                | 0.787                |                      | 3.180                | 0.787                |
| Het. test $p$ -value  |                      | 0.598                | 0.375                |                      | 0.075                | 0.375                |
| Spec. test stat.      |                      | 0.483                | 0.178                |                      | 1.726                | 2.045                |
| Spec. test $p$ -value |                      | 0.629                | 0.673                |                      | 0.084                | 0.153                |
| Percent change        |                      | 1.489                | -3.502               |                      | 1.489                | -3.502               |

#### (b) Fertilizer with year interactions

|                       | Clustering           |                      |                      | No clustering        |                      |                      |  |
|-----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|--|
|                       | FE                   | IWE                  | RWE                  | FE                   | IWE                  | RWE                  |  |
| _                     | 10.708***<br>(3.345) | 10.740***<br>(3.338) | 10.738***<br>(3.342) | 10.708***<br>(1.020) | 10.740***<br>(0.895) | 10.738***<br>(0.922) |  |
| Het. test stat.       |                      | 124.522              | 139.293              |                      | 263.139              | 139.293              |  |
| Het. test $p$ -value  |                      | 0.000                | 0.000                |                      | 0.000                | 0.000                |  |
| Spec. test stat.      |                      | 0.563                | 7.230                |                      | 0.172                | 77.485               |  |
| Spec. test $p$ -value |                      | 0.573                | 0.007                |                      | 0.863                | 0.000                |  |
| Percent change        |                      | 0.304                | 0.287                |                      | 0.304                | 0.287                |  |

### (c) Log total yield with coastal interaction

|                       |                    | Clustering         |                   |                     | No clustering       |                     |
|-----------------------|--------------------|--------------------|-------------------|---------------------|---------------------|---------------------|
|                       | FE                 | IWE                | RWE               | FE                  | IWE                 | RWE                 |
| _                     | 0.157**<br>(0.071) | 0.151**<br>(0.070) | 0.142*<br>(0.074) | 0.157***<br>(0.015) | 0.151***<br>(0.015) | 0.142***<br>(0.015) |
| Het. test stat.       |                    | 1.156              | 5.487             |                     | 26.277              | 5.487               |
| Het. test $p$ -value  |                    | 0.282              | 0.019             |                     | 0.000               | 0.019               |
| Spec. test stat.      |                    | -0.873             | 0.881             |                     | -4.386              | 21.152              |
| Spec. test $p$ -value |                    | 0.383              | 0.348             |                     | 0.000               | 0.000               |
| Percent change        |                    | -4.239             | -9.611            |                     | -4.239              | -9.611              |

(d) Log total yield with year interactions

|                       |                    | Clustering         |                    |                     | No clustering       |                     |
|-----------------------|--------------------|--------------------|--------------------|---------------------|---------------------|---------------------|
|                       | FE                 | IWE                | RWE                | FE                  | IWE                 | RWE                 |
| _                     | 0.157**<br>(0.071) | 0.157**<br>(0.071) | 0.157**<br>(0.071) | 0.157***<br>(0.015) | 0.157***<br>(0.015) | 0.157***<br>(0.015) |
| Het. test stat.       |                    | 274.215            | 126.335            |                     | 82.683              | 126.335             |
| Het. test $p$ -value  |                    | 0.000              | 0.000              |                     | 0.000               | 0.000               |
| Spec. test stat.      |                    | 0.275              | 9.096              |                     | 0.002               | 4.412               |
| Spec. test $p$ -value |                    | 0.783              | 0.003              |                     | 0.998               | 0.036               |
| Percent change        |                    | 0.003              | 0.012              |                     | 0.003               | 0.012               |

#### (e) Log rice yield with coastal interaction

|  | Clustering         |                         |                         | No clustering       |                         |                           |  |
|--|--------------------|-------------------------|-------------------------|---------------------|-------------------------|---------------------------|--|
|  | FE                 | IWE                     | RWE                     | FE                  | IWE                     | RWE                       |  |
| -  | 0.171**<br>(0.081) | 0.165**<br>(0.080)      | 0.171**<br>(0.080)      | 0.171***<br>(0.017) | 0.165***<br>(0.020)     | 0.171***<br>(0.020)       |  |
| Het. test stat. Het. test p-value                  |                    | 1.314 $0.252$           | $1.936 \\ 0.164$        |                     | 18.466<br>0.000         | $1.936 \\ 0.164$          |  |
| Spec. test stat. Spec. test p-value Percent change |                    | -0.881 $0.378$ $-3.296$ | 0.000<br>0.997<br>0.031 |                     | -3.765 $0.000$ $-3.296$ | $0.000 \\ 0.988 \\ 0.031$ |  |

### (f) Log rice yield with year interactions

|  |                    | Clustering                                |  |                     | No clustering                                   |  |
|--|--------------------|---|--|---------------------|---|--|
|  | FE                 | IWE                                       | RWE  | FE                  | IWE   | RWE  |
| nland  | 0.171**<br>(0.081) | 0.170**<br>(0.081)                        | 0.170**<br>(0.081)                             | 0.171***<br>(0.017) | 0.170***<br>(0.020)                             | 0.170***<br>(0.020)                            |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value Percent change |                    | 171.874 $0.000$ $-0.559$ $0.576$ $-0.123$ | $123.681 \\ 0.000 \\ 6.281 \\ 0.012 \\ -0.123$ |                     | $103.150 \\ 0.000 \\ -0.074 \\ 0.941 \\ -0.123$ | $123.681 \\ 0.000 \\ 6.626 \\ 0.010 \\ -0.123$ |

### (g) Percent HYV cereals with coastal interaction

|                       | Clustering |         |         | No clustering |          |          |
|-----------------------|------------|---------|---------|---------------|----------|----------|
|                       | FE         | IWE     | RWE     | FE            | IWE      | RWE      |
| _                     | 0.057*     | 0.058*  | 0.059*  | 0.057***      | 0.058*** | 0.059*** |
|                       | (0.031)    | (0.031) | (0.032) | (0.010)       | (0.009)  | (0.010)  |
| Het. test stat.       |            | 0.045   | 0.170   |               | 0.391    | 0.170    |
| Het. test $p$ -value  |            | 0.832   | 0.680   |               | 0.532    | 0.680    |
| Spec. test stat.      |            | 0.212   | 0.058   |               | 0.629    | 0.413    |
| Spec. test $p$ -value |            | 0.832   | 0.809   |               | 0.529    | 0.520    |
| Percent change        |            | 1.131   | 3.281   |               | 1.131    | 3.281    |

#### (h) Percent HYV cereals with year interactions

|   |                   | Clustering        |                   |                     | No clustering       |                     |
|---|-------------------|-------------------|-------------------|---------------------|---------------------|---------------------|
|   | FE                | IWE               | RWE               | FE                  | IWE                 | RWE                 |
| -   | 0.057*<br>(0.031) | 0.057*<br>(0.031) | 0.057*<br>(0.031) | 0.057***<br>(0.010) | 0.057***<br>(0.009) | 0.057***<br>(0.009) |
| Het. test stat.                           |                   | 78.041            | 88.748            |                     | 65.746              | 88.748              |
| Het. test $p$ -value                      |                   | 0.000             | 0.000             |                     | 0.000               | 0.000               |
| Spec. test stat.                          |                   | 0.330             | 0.313             |                     | 0.092               | 0.678               |
| Spec. test <i>p</i> -value Percent change |                   | $0.742 \\ 0.173$  | $0.576 \\ -0.191$ |                     | $0.926 \\ 0.173$    | $0.410 \\ -0.191$   |

#### (i) Percent HYV rice with coastal interaction

|                       |         | Clustering |         |          | No clustering |          |
|-----------------------|---------|------------|---------|----------|---------------|----------|
|                       | FE      | IWE        | RWE     | FE       | IWE           | RWE      |
|                       | 0.079*  | 0.080*     | 0.078*  | 0.079*** | 0.080***      | 0.078*** |
|                       | (0.044) | (0.043)    | (0.042) | (0.012)  | (0.012)       | (0.012)  |
| Het. test stat.       |         | 0.120      | 0.041   |          | 1.231         | 0.041    |
| Het. test $p$ -value  |         | 0.729      | 0.840   |          | 0.267         | 0.840    |
| Spec. test stat.      |         | 0.337      | 0.055   |          | 1.095         | 0.467    |
| Spec. test $p$ -value |         | 0.736      | 0.815   |          | 0.274         | 0.494    |
| Percent change        |         | 1.099      | -1.725  |          | 1.099         | -1.725   |

### (j) Percent HYV rice with year interactions

|                       |            | Clustering |         |  | No clustering |          |
|-----------------------|------------|------------|---------|--|---------------|----------|
|                       | FE IWE RWE |            |         | $FE \hspace{1cm} IWE \hspace{1cm} RWE$ |               |          |
| -                     | 0.079*     | 0.079*     | 0.079*  | 0.079***                               | 0.079***      | 0.079*** |
|                       | (0.044)    | (0.044)    | (0.043) | (0.012)                                | (0.012)       | (0.012)  |
| Het. test stat.       |            | 108.783    | 76.353  |  | 280.287       | 76.353   |
| Het. test $p$ -value  |            | 0.000      | 0.000   |  | 0.000         | 0.000    |
| Spec. test stat.      |            | -0.205     | 0.005   |  | -0.026        | 0.004    |
| Spec. test $p$ -value |            | 0.838      | 0.945   |  | 0.979         | 0.950    |
| Percent change        |            | -0.079     | -0.018  |  | -0.079        | -0.018   |

### (k) Percent HYV wheat with coastal interaction

|                       | Clustering |         |         |          | No clustering |          |  |  |
|-----------------------|------------|---------|---------|----------|---------------|----------|--|--|
|                       | FE         | IWE     | RWE     | FE       | IWE           | RWE      |  |  |
| -                     | 0.092**    | 0.080*  | 0.072   | 0.092*** | 0.080***      | 0.072*** |  |  |
|                       | (0.046)    | (0.046) | (0.047) | (0.012)  | (0.013)       | (0.014)  |  |  |
| Het. test stat.       |            | 7.583   | 0.526   |          | 82.283        | 0.526    |  |  |
| Het. test $p$ -value  |            | 0.006   | 0.468   |          | 0.000         | 0.468    |  |  |
| Spec. test stat.      |            | -1.285  | 3.468   |          | -5.412        | 37.519   |  |  |
| Spec. test $p$ -value |            | 0.199   | 0.063   |          | 0.000         | 0.000    |  |  |
| Percent change        |            | -13.337 | -21.610 |          | -13.337       | -21.610  |  |  |

(l) Percent HYV wheat with year interactions

|  |                    | Clustering                                      |   |                     | No clustering                                   |   |  |
|--|--------------------|---|---|---------------------|---|---|--|
|  | FE IWE RWE         |   |   | FE                  | FE IWE RWE                                      |   |  |
| _  | 0.092**<br>(0.046) | 0.091**<br>(0.045)                              | 0.091**<br>(0.046)                            | 0.092***<br>(0.012) | 0.091***<br>(0.013)                             | 0.091***<br>(0.013)                           |  |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value Percent change |                    | $179.014 \\ 0.000 \\ -0.581 \\ 0.561 \\ -0.793$ | $69.347 \\ 0.000 \\ 5.273 \\ 0.022 \\ -0.514$ |                     | $126.897 \\ 0.000 \\ -0.311 \\ 0.756 \\ -0.793$ | $69.347 \\ 0.000 \\ 2.227 \\ 0.136 \\ -0.514$ |  |

### (m) Irrigation with coastal interaction

|   |                     | Clustering   |                                  |                     | No clustering                   |                                 |
|---|---------------------|--|----------------------------------|---------------------|---------------------------------|---------------------------------|
|   | FE                  | IWE  | RWE                              | FE                  | IWE                             | RWE                             |
| -   | $0.065^*$ $(0.034)$ | 0.061*<br>(0.034)  | 0.045<br>(0.036)                 | 0.065***<br>(0.008) | 0.061***<br>(0.007)             | 0.045***<br>(0.008)             |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value |                     | $     \begin{array}{r}       1.433 \\       0.231 \\       -0.873 \\       0.383     \end{array} $ | 3.414<br>0.065<br>6.219<br>0.013 |                     | 34.449 $0.000$ $-4.402$ $0.000$ | 3.414 $0.065$ $147.436$ $0.000$ |
| Percent change  |                     | -6.785   | -31.655                          |                     | -6.785                          | -31.655                         |

### (n) Irrigation with year interactions

|                       | Clustering          |                     |                   | No clustering       |                     |                     |  |
|-----------------------|---------------------|---------------------|-------------------|---------------------|---------------------|---------------------|--|
|                       | FE                  | IWE                 | RWE               | FE                  | IWE                 | RWE                 |  |
| -                     | $0.065^*$ $(0.034)$ | $0.065^*$ $(0.034)$ | 0.065*<br>(0.034) | 0.065***<br>(0.008) | 0.065***<br>(0.007) | 0.065***<br>(0.007) |  |
| Het. test stat.       |                     | 84.841              | 80.741            |                     | 7.622               | 80.741              |  |
| Het. test $p$ -value  |                     | 0.000               | 0.000             |                     | 1.000               | 0.000               |  |
| Spec. test stat.      |                     | 0.053               | 0.017             |                     | 0.010               | 0.017               |  |
| Spec. test $p$ -value |                     | 0.958               | 0.896             |                     | 0.992               | 0.897               |  |
| Percent change        |                     | 0.006               | 0.005             |                     | 0.006               | 0.005               |  |

Table 7: Bedard and Deschenes (2006)

# (a) Age interactions

|                            | (a) Age inter    | ractions    |          |
|----------------------------|------------------|-------------|----------|
|                            | FE               | IWE         | RWE      |
|                            | 0.078***         | 0.078***    | 0.077*** |
|                            | (0.005)          | (0.006)     | (0.006)  |
| Het. test stat.            |                  | 11.090      | 11.142   |
| Het. test $p$ -value       |                  | 0.944       | 0.942    |
| Spec. test stat.           |                  | 0.108       | 0.046    |
| Spec. test $p$ -value      |                  | 0.914       | 0.830    |
| Percent change             |                  | 0.111       | -0.223   |
|                            | (b) Education is | nteractions |          |
|                            | FE               | IWE         | RWE      |
|                            | 0.078***         | 0.078***    | 0.078*** |
|                            | (0.005)          | (0.006)     | (0.006)  |
| Het. test stat.            |                  | 14.788      | 14.918   |
| Het. test $p$ -value       |                  | 0.002       | 0.002    |
| Spec. test stat.           |                  | 0.890       | 0.025    |
| Spec. test <i>p</i> -value |                  | 0.374       | 0.875    |
| Percent change             |                  | 0.712       | -0.124   |
|                            | (c) Race inte    | ractions    |          |
|                            | FE               | IWE         | RWE      |
|                            | 0.078***         | 0.078***    | 0.078*** |
|                            | (0.005)          | (0.005)     | (0.005)  |
| Het. test stat.            |                  | 3.069       | 3.073    |
| Het. test $p$ -value       |                  | 0.080       | 0.080    |
| Spec. test stat.           |                  | 1.700       | 2.978    |
| Spec. test $p$ -value      |                  | 0.089       | 0.084    |
| Percent change             |                  | 0.524       | 0.494    |
|                            | (d) Region int   | eractions   |          |
|                            | FE               | IWE         | RWE      |
|                            | 0.078***         | 0.078***    | 0.078*** |
|                            | (0.005)          | (0.005)     | (0.005)  |
| Het. test stat.            |                  | 5.514       | 5.557    |
| Het. test $p$ -value       |                  | 0.701       | 0.697    |
| C + - + - + - +            |                  | 1 001       | 0.724    |

1.231

0.218

0.245

0.734

0.392

0.075

Spec. test stat.

Percent change

Spec. test p-value

Table 8: Card et al. (2008)

(a) Hospitalized; education interactions (whites only)

|                       | Clustering |          |          | No clustering |         |         |
|-----------------------|------------|----------|----------|---------------|---------|---------|
|                       | FE         | IWE      | RWE      | FE            | IWE     | RWE     |
| _                     | 0.012**    | 0.012*** | 0.012*** | 0.012**       | 0.012** | 0.012** |
|                       | (0.005)    | (0.004)  | (0.004)  | (0.006)       | (0.006) | (0.006) |
| Het. test stat.       |            | 14.526   | 6.350    |               | 11.513  | 6.350   |
| Het. test $p$ -value  |            | 0.002    | 0.096    |               | 0.009   | 0.096   |
| Spec. test stat.      |            | 2.105    | 0.619    |               | 1.891   | 0.665   |
| Spec. test $p$ -value |            | 0.035    | 0.431    |               | 0.059   | 0.415   |
| Percent change        |            | 1.601    | 1.045    |               | 1.601   | 1.045   |

### (b) Hospitalized; education interactions (non-whites only)

|                       | Clustering       |                    |                    | No clustering    |                  |                  |  |
|-----------------------|------------------|--------------------|--------------------|------------------|------------------|------------------|--|
|                       | FE IWE RWE       |                    |                    | FE               | IWE              | RWE              |  |
| -                     | 0.013<br>(0.010) | 0.013**<br>(0.006) | 0.013**<br>(0.006) | 0.013<br>(0.010) | 0.013<br>(0.010) | 0.013<br>(0.010) |  |
| Het. test stat.       |                  | 0.609              | 1.242              |                  | 0.661            | 1.242            |  |
| Het. test $p$ -value  |                  | 0.894              | 0.743              |                  | 0.882            | 0.743            |  |
| Spec. test stat.      |                  | 0.720              | 1.090              |                  | 0.765            | 1.262            |  |
| Spec. test $p$ -value |                  | 0.472              | 0.296              |                  | 0.444            | 0.261            |  |
| Percent change        |                  | 1.462              | 3.332              |                  | 1.462            | 3.332            |  |

### (c) Hospitalized; ethnicity interactions

|                       | Clustering          |                     |                     | No clustering      |                    |                    |  |
|-----------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--|
|                       | FE                  | IWE                 | RWE                 | FE                 | IWE                | RWE                |  |
| _                     | 0.012***<br>(0.003) | 0.012***<br>(0.003) | 0.012***<br>(0.003) | 0.012**<br>(0.005) | 0.012**<br>(0.005) | 0.012**<br>(0.005) |  |
| Het. test stat.       |                     | 16.479              | 16.798              |                    | 15.917             | 16.798             |  |
| Het. test $p$ -value  |                     | 0.001               | 0.001               |                    | 0.001              | 0.001              |  |
| Spec. test stat.      |                     | 0.623               | 0.254               |                    | 0.716              | 0.132              |  |
| Spec. test $p$ -value |                     | 0.533               | 0.614               |                    | 0.474              | 0.717              |  |
| Percent change        |                     | 0.354               | -0.142              |                    | 0.354              | -0.142             |  |

(d) Hospitalized; gender interaction

|   |                    | Clustering                           |                                   |                    | No clustering                          |                                   |
|---|--------------------|--------------------------------------|-----------------------------------|--------------------|--|-----------------------------------|
|   | FE                 | IWE                                  | RWE                               | FE                 | IWE                                    | RWE                               |
| -   | 0.012**<br>(0.005) | 0.012***<br>(0.003)                  | 0.012***<br>(0.003)               | 0.012**<br>(0.005) | 0.012**<br>(0.005)                     | 0.012**<br>(0.005)                |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value |                    | $22.513 \\ 0.000 \\ -2.125 \\ 0.034$ | 22.838<br>0.000<br>3.335<br>0.068 |                    | $ 22.119 \\ 0.000 \\ -1.792 \\ 0.073 $ | 22.838<br>0.000<br>3.632<br>0.057 |
| Percent change  |                    | -0.954                               | -0.485                            |                    | -0.954                                 | -0.485                            |

#### (e) Hospitalized; region interactions

|                       | Clustering |          |          | No clustering |         |         |  |
|-----------------------|------------|----------|----------|---------------|---------|---------|--|
|                       | FE         | IWE      | RWE      | FE            | IWE     | RWE     |  |
| _                     | 0.012**    | 0.012*** | 0.012*** | 0.012**       | 0.012** | 0.012** |  |
|                       | (0.005)    | (0.003)  | (0.003)  | (0.005)       | (0.005) | (0.005) |  |
| Het. test stat.       |            | 10.712   | 13.392   |               | 10.034  | 13.392  |  |
| Het. test $p$ -value  |            | 0.013    | 0.004    |               | 0.018   | 0.004   |  |
| Spec. test stat.      |            | 0.455    | 1.068    |               | 0.427   | 1.319   |  |
| Spec. test $p$ -value |            | 0.649    | 0.301    |               | 0.670   | 0.251   |  |
| Percent change        |            | 0.145    | 0.179    |               | 0.145   | 0.179   |  |

### (f) Hospitalized; year interactions

|  | Clustering         |                     |                     | No clustering      |                    |                    |  |
|--|--------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--|
|  | FE                 | IWE                 | RWE                 | FE                 | IWE                | RWE                |  |
| -  | 0.012**<br>(0.005) | 0.012***<br>(0.003) | 0.012***<br>(0.003) | 0.012**<br>(0.005) | 0.012**<br>(0.005) | 0.012**<br>(0.005) |  |
| Het. test stat.                              |                    | 8.886               | 11.751              |                    | 12.256             | 11.751             |  |
| Het. test $p$ -value Spec. test stat.        |                    | $0.632 \\ 0.320$    | $0.383 \\ 0.606$    |                    | $0.345 \\ 0.327$   | $0.383 \\ 0.734$   |  |
| Spec. test <i>p</i> -value<br>Percent change |                    | $0.749 \\ 0.259$    | $0.436 \\ -1.250$   |                    | $0.743 \\ 0.259$   | $0.392 \\ -1.250$  |  |

### (g) Saw doctor; education interactions (whites only)

|  | Clustering       |  |  | No clustering    |  |  |
|--|------------------|--|--|------------------|--|--|
|  | FE               | IWE  | RWE  | FE               | IWE  | RWE                                    |
|  | 0.008<br>(0.007) | 0.008<br>(0.007)                               | 0.008<br>(0.007)                             | 0.008<br>(0.007) | 0.008<br>(0.007)                               | 0.008<br>(0.007)                       |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value Percent change |                  | $16.643 \\ 0.001 \\ -2.783 \\ 0.005 \\ -4.283$ | $9.133 \\ 0.028 \\ 1.179 \\ 0.278 \\ -2.008$ |                  | $19.725 \\ 0.000 \\ -2.414 \\ 0.016 \\ -4.283$ | 9.133 $0.028$ $1.752$ $0.186$ $-2.008$ |

(h) Saw doctor; education interactions (non-whites only)

|  |                     | Clustering              |                        |                     | No clustering           |                        |
|--|---------------------|-------------------------|------------------------|---------------------|-------------------------|------------------------|
|  | FE                  | IWE                     | RWE                    | FE                  | IWE                     | RWE                    |
| _  | 0.038***<br>(0.014) | 0.037***<br>(0.011)     | 0.038***<br>(0.011)    | 0.038***<br>(0.014) | 0.037***<br>(0.014)     | 0.038***<br>(0.014)    |
| Het. test stat. Het. test $p$ -value               |                     | 4.999 $0.172$           | $0.262 \\ 0.967$       |                     | $4.094 \\ 0.252$        | $0.262 \\ 0.967$       |
| Spec. test stat. Spec. test p-value Percent change |                     | -1.757 $0.079$ $-1.652$ | 0.066 $0.798$ $-0.370$ |                     | -1.722 $0.085$ $-1.652$ | 0.062 $0.804$ $-0.370$ |

#### (i) Saw doctor; ethnicity interactions

|                       |         | Clustering |         |         | No clustering |         |
|-----------------------|---------|------------|---------|---------|---------------|---------|
|                       | FE      | IWE        | RWE     | FE      | IWE           | RWE     |
| _                     | 0.016** | 0.016**    | 0.016** | 0.016** | 0.016**       | 0.016** |
|                       | (0.006) | (0.006)    | (0.006) | (0.006) | (0.006)       | (0.006) |
| Het. test stat.       |         | 27.968     | 27.804  |         | 31.706        | 27.804  |
| Het. test $p$ -value  |         | 0.000      | 0.000   |         | 0.000         | 0.000   |
| Spec. test stat.      |         | -1.103     | 1.567   |         | -1.144        | 1.416   |
| Spec. test $p$ -value |         | 0.270      | 0.211   |         | 0.253         | 0.234   |
| Percent change        |         | -0.868     | -0.501  |         | -0.868        | -0.501  |

### (j) Saw doctor; gender interaction

|  |                   | Clustering   |   |                    | No clustering                                   |   |
|--|-------------------|--|---|--------------------|---|---|
|  | FE                | IWE  | RWE                                     | FE                 | IWE   | RWE                                     |
| d65  | 0.016*<br>(0.009) | 0.015**<br>(0.006)   | 0.016**<br>(0.006)                      | 0.016**<br>(0.006) | 0.015**<br>(0.006)                              | 0.016**<br>(0.006)                      |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value Percent change |                   | $   \begin{array}{c}     103.383 \\     0.000 \\     -2.251 \\     0.024 \\     -3.221   \end{array} $ | 53.782 $0.000$ $0.302$ $0.582$ $-0.371$ |                    | $140.021 \\ 0.000 \\ -2.190 \\ 0.029 \\ -3.221$ | 53.782 $0.000$ $0.812$ $0.368$ $-0.371$ |

### (k) Saw doctor; region interactions

|                       |         | Clustering |         |         | No clustering |         |
|-----------------------|---------|------------|---------|---------|---------------|---------|
|                       | FE      | IWE        | RWE     | FE      | IWE           | RWE     |
| _                     | 0.016** | 0.016**    | 0.016** | 0.016** | 0.016**       | 0.016** |
|                       | (0.006) | (0.006)    | (0.006) | (0.006) | (0.006)       | (0.006) |
| Het. test stat.       |         | 6.137      | 9.083   |         | 6.637         | 9.083   |
| Het. test $p$ -value  |         | 0.105      | 0.028   |         | 0.084         | 0.028   |
| Spec. test stat.      |         | 0.231      | 1.279   |         | 0.165         | 1.196   |
| Spec. test $p$ -value |         | 0.817      | 0.258   |         | 0.869         | 0.274   |
| Percent change        |         | 0.053      | 0.261   |         | 0.053         | 0.261   |

(l) Saw doctor; year interactions

|   |                    | Clustering   |                                   |                    | No clustering                  |                                   |
|---|--------------------|--|-----------------------------------|--------------------|--------------------------------|-----------------------------------|
|   | FE                 | IWE  | RWE                               | FE                 | IWE                            | RWE                               |
| -   | 0.016**<br>(0.007) | 0.016**<br>(0.006)   | 0.016**<br>(0.006)                | 0.016**<br>(0.006) | 0.016**<br>(0.006)             | 0.016**<br>(0.006)                |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value |                    | $   \begin{array}{c}     10.219 \\     0.511 \\     -0.937 \\     0.349 \\     0.667   \end{array} $ | 14.077<br>0.229<br>0.271<br>0.603 |                    | 8.602 $0.659$ $-0.927$ $0.354$ | 14.077<br>0.229<br>0.424<br>0.515 |
| Percent change  |                    | -0.667   | 0.805                             |                    | -0.667                         | 0.805                             |

Table 9: Karlan and Zinman (2008)

### (a) Risk interactions

|                       |                   | Clustering             |                        |                        | No clustering          |                        |
|-----------------------|-------------------|------------------------|------------------------|------------------------|------------------------|------------------------|
|                       | FE                | IWE                    | RWE                    | FE                     | IWE                    | RWE                    |
| _                     | -4.368*** (1.093) | $-7.047^{***}$ (1.917) | $-7.410^{***}$ (1.883) | $-4.368^{***}$ (1.229) | $-7.047^{***}$ (1.880) | $-7.410^{***}$ (1.866) |
| Het. test stat.       |                   | 8.259                  | 10.518                 |                        | 6.177                  | 10.518                 |
| Het. test $p$ -value  |                   | 0.016                  | 0.005                  |                        | 0.046                  | 0.005                  |
| Spec. test stat.      |                   | -2.569                 | 8.995                  |                        | -2.407                 | 7.758                  |
| Spec. test $p$ -value |                   | 0.010                  | 0.003                  |                        | 0.016                  | 0.005                  |
| Percent change        |                   | 61.323                 | 69.652                 |                        | 61.323                 | 69.652                 |

### (b) Wave interactions

|  |                      | Clustering             |                         |                        | No clustering          |                         |
|--|----------------------|------------------------|-------------------------|------------------------|------------------------|-------------------------|
|  | FE                   | IWE                    | RWE                     | FE                     | IWE                    | RWE                     |
| _  | -4.368***<br>(1.093) | $-4.319^{***}$ (1.084) | $-4.377^{***}$ (1.091)  | $-4.368^{***}$ (1.229) | $-4.319^{***}$ (1.026) | $-4.377^{***}$ (1.025)  |
| Het. test stat. Het. test p-value                  |                      | $2.215 \\ 0.330$       | $2.905 \\ 0.234$        |                        | $1.156 \\ 0.561$       | $2.905 \\ 0.234$        |
| Spec. test stat. Spec. test p-value Percent change |                      | 0.206 $0.837$ $-1.123$ | 0.077<br>0.782<br>0.211 |                        | 0.917 $0.359$ $-1.123$ | 0.070<br>0.791<br>0.211 |

Table 10: Lochner and Moretti (2004)

# (a) Age (whites only)

|                       |                          | Clustering               |                      |                          | No clustering            |                          |
|-----------------------|--------------------------|--------------------------|----------------------|--------------------------|--------------------------|--------------------------|
|                       | FE                       | IWE                      | RWE                  | FE                       | IWE                      | RWE                      |
| -                     | $-0.001^{***}$ $(0.000)$ | $-0.001^{***}$ $(0.000)$ | -0.001***<br>(0.000) | $-0.001^{***}$ $(0.000)$ | $-0.001^{***}$ $(0.000)$ | $-0.001^{***}$ $(0.000)$ |
| Het. test stat.       |                          | 1,990.375                | 415.598              |                          | 3,382.355                | 415.598                  |
| Het. test $p$ -value  |                          | 0.000                    | 0.000                |                          | 0.000                    | 0.000                    |
| Spec. test stat.      |                          | 15.161                   | 403.287              |                          | 43.613                   | 2,070.711                |
| Spec. test $p$ -value |                          | 0.000                    | 0.000                |                          | 0.000                    | 0.000                    |
| Percent change        |                          | 33.597                   | 28.992               |                          | 33.597                   | 28.992                   |

### (b) Year (whites only)

|   | Clustering               |                        |                      | No clustering            |                          |                          |
|---|--------------------------|------------------------|----------------------|--------------------------|--------------------------|--------------------------|
|   | FE                       | IWE                    | RWE                  | FE                       | IWE                      | RWE                      |
| _   | $-0.001^{***}$ $(0.000)$ | $-0.001^{***}$ (0.000) | -0.001***<br>(0.000) | $-0.001^{***}$ $(0.000)$ | $-0.001^{***}$ $(0.000)$ | $-0.001^{***}$ $(0.000)$ |
| Het. test stat.                           |                          | 6.539                  | 10.609               |                          | 10.340                   | 10.609                   |
| Het. test $p$ -value                      |                          | 0.038                  | 0.005                |                          | 0.006                    | 0.005                    |
| Spec. test stat.                          |                          | -1.570                 | -2.782               |                          | -2.614                   | -6.955                   |
| Spec. test <i>p</i> -value Percent change |                          | $0.117 \\ -0.169$      | $0.095 \\ -0.166$    |                          | $0.009 \\ -0.169$        | $0.008 \\ -0.166$        |

# (c) Age (blacks only)

|                       | Clustering             |                          |                          | No clustering          |                          |                          |
|-----------------------|------------------------|--------------------------|--------------------------|------------------------|--------------------------|--------------------------|
|                       | FE                     | IWE                      | RWE                      | FE                     | IWE                      | RWE                      |
| _                     | $-0.004^{***}$ (0.000) | $-0.005^{***}$ $(0.000)$ | $-0.005^{***}$ $(0.000)$ | $-0.004^{***}$ (0.000) | $-0.005^{***}$ $(0.000)$ | $-0.005^{***}$ $(0.000)$ |
| Het. test stat.       |                        | 867.312                  | 38.446                   |                        | 1,424.575                | 38.446                   |
| Het. test $p$ -value  |                        | 0.000                    | 0.000                    |                        | 0.000                    | 0.000                    |
| Spec. test stat.      |                        | 13.171                   | 483.568                  |                        | 30.781                   | 1,367.197                |
| Spec. test $p$ -value |                        | 0.000                    | 0.000                    |                        | 0.000                    | 0.000                    |
| Percent change        |                        | 34.229                   | 32.562                   |                        | 34.229                   | 32.562                   |

(d) Year (blacks only)

|                       | Clustering             |                        |                   | No clustering          |                        |                        |
|-----------------------|------------------------|------------------------|-------------------|------------------------|------------------------|------------------------|
|                       | FE                     | IWE                    | RWE               | FE                     | IWE                    | RWE                    |
| _                     | $-0.004^{***}$ (0.000) | $-0.004^{***}$ (0.000) | -0.004*** (0.000) | $-0.004^{***}$ (0.000) | $-0.004^{***}$ (0.000) | $-0.004^{***}$ (0.000) |
| Het. test stat.       |                        | 36.508                 | 118.706           |                        | 72.706                 | 118.706                |
| Het. test $p$ -value  |                        | 0.000                  | 0.000             |                        | 0.000                  | 0.000                  |
| Spec. test stat.      |                        | 5.264                  | 29.450            |                        | 8.250                  | 59.070                 |
| Spec. test $p$ -value |                        | 0.000                  | 0.000             |                        | 0.000                  | 0.000                  |
| Percent change        |                        | 1.941                  | 1.675             |                        | 1.941                  | 1.675                  |

### (e) Race (all observations)

|                       | Clustering               |                          |                      | No clustering            |                          |                          |
|-----------------------|--------------------------|--------------------------|----------------------|--------------------------|--------------------------|--------------------------|
|                       | FE                       | IWE                      | RWE                  | FE                       | IWE                      | RWE                      |
| _                     | $-0.001^{***}$ $(0.000)$ | $-0.001^{***}$ $(0.000)$ | -0.001***<br>(0.000) | $-0.001^{***}$ $(0.000)$ | $-0.001^{***}$ $(0.000)$ | $-0.001^{***}$ $(0.000)$ |
| Het. test stat.       |                          | 27.187                   | 57.166               |                          | 85.278                   | 57.166                   |
| Het. test $p$ -value  |                          | 0.000                    | 0.000                |                          | 0.000                    | 0.000                    |
| Spec. test stat.      |                          | -4.592                   | -273.533             |                          | -9.098                   | -722.906                 |
| Spec. test $p$ -value |                          | 0.000                    | 0.000                |                          | 0.000                    | 0.000                    |
| Percent change        |                          | -0.701                   | -1.627               |                          | -0.701                   | -1.627                   |

Table 11: Meghir and Palme (2005)

### (a) Female interaction

|   | Clustering       |                  |                  | No clustering                          |                     |                     |
|---|------------------|------------------|------------------|--|---------------------|---------------------|
|   | FE IWE RWE       |                  |                  | $FE \hspace{1cm} IWE \hspace{1cm} RWE$ |                     |                     |
|   | 0.014<br>(0.009) | 0.014<br>(0.009) | 0.014<br>(0.009) | 0.014***<br>(0.004)                    | 0.014***<br>(0.004) | 0.014***<br>(0.004) |
| Het. test stat Het. test p-value          |                  | $0.400 \\ 0.527$ | 0.896 $0.344$    |  | 2.528 $0.112$       | 0.896 $0.344$       |
| Spec. test stat.                          |                  | 0.3232           | 0.425            |  | 1.113               | 2.663               |
| Spec. test <i>p</i> -value Percent change |                  | $0.747 \\ 0.238$ | $0.514 \\ 0.277$ |  | $0.266 \\ 0.238$    | $0.103 \\ 0.277$    |

### (b) Year interactions

|                       | Clustering       |                  |                  | No clustering       |                     |                     |
|-----------------------|------------------|------------------|------------------|---------------------|---------------------|---------------------|
|                       | FE IWE RWE       |                  |                  | FE                  | RWE                 |                     |
|                       | 0.014<br>(0.009) | 0.014<br>(0.009) | 0.014<br>(0.009) | 0.014***<br>(0.004) | 0.014***<br>(0.004) | 0.014***<br>(0.004) |
| Het. test stat        |                  | 41.964           | 60.845           |                     | 29.964              | 60.845              |
| Het. test $p$ -value  |                  | 0.000            | 0.000            |                     | 0.002               | 0.000               |
| Spec. test stat.      |                  | 2.486            | 0.922            |                     | 1.090               | 0.926               |
| Spec. test $p$ -value |                  | 0.013            | 0.337            |                     | 0.276               | 0.336               |
| Percent change        |                  | 0.523            | 0.104            |                     | 0.523               | 0.104               |

### (c) High father's education interaction

|                       | Clustering       |                    |                   | No clustering       |                     |                     |
|-----------------------|------------------|--------------------|-------------------|---------------------|---------------------|---------------------|
|                       | FE IWE RWE       |                    |                   | FE                  | IWE                 | RWE                 |
| -                     | 0.014<br>(0.009) | 0.017**<br>(0.008) | 0.016*<br>(0.009) | 0.014***<br>(0.004) | 0.017***<br>(0.004) | 0.016***<br>(0.004) |
| Het. test stat        |                  | 46.725             | 61.562            |                     | 149.110             | 61.562              |
| Het. test $p$ -value  |                  | 0.000              | 0.000             |                     | 0.000               | 0.000               |
| Spec. test stat.      |                  | 1.164              | 21.572            |                     | 9.504               | 85.655              |
| Spec. test $p$ -value |                  | 0.244              | 0.000             |                     | 0.000               | 0.000               |
| Percent change        |                  | 18.459             | 15.501            |                     | 18.459              | 15.501              |

Table 12: Oreopoulos (2006)

### (a) Age interaction (Great Britain)

|                       | Clustering          |                     |                     | No clustering       |                     |                     |
|-----------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
|                       | FE IWE RWE          |                     |                     | FE                  | IWE                 | RWE                 |
| _                     | 0.075***<br>(0.002) | 0.076***<br>(0.002) | 0.077***<br>(0.002) | 0.075***<br>(0.001) | 0.076***<br>(0.001) | 0.077***<br>(0.001) |
| Het. test stat        |                     | 879.854             | 32.831              |                     | 42.601              | 33.740              |
| Het. test $p$ -value  |                     | 0.000               | 0.242               |                     | 0.038               | 0.210               |
| Spec. test stat.      |                     | 0.959               | 7.480               |                     | 2.851               | 21.853              |
| Spec. test $p$ -value |                     | 0.338               | 0.006               |                     | 0.004               | 0.000               |
| Percent change        |                     | 1.206               | 1.794               |                     | 1.206               | 1.794               |

### (b) Age interaction (Northern Ireland)

|                       | Clustering          |                     |                     | No clustering       |                     |                     |
|-----------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
|                       | FE                  | IWE                 | RWE                 | FE                  | IWE                 | RWE                 |
| _                     | 0.106***<br>(0.004) | 0.107***<br>(0.003) | 0.107***<br>(0.004) | 0.106***<br>(0.002) | 0.107***<br>(0.003) | 0.107***<br>(0.003) |
| Het. test stat        |                     | 148, 468.588        | 25.686              |                     | 61.217              | 25.686              |
| Het. test $p$ -value  |                     | 0.000               | 0.590               |                     | 0.000               | 0.590               |
| Spec. test stat.      |                     | 0.331               | 1.192               |                     | 0.574               | 1.518               |
| Spec. test $p$ -value |                     | 0.741               | 0.275               |                     | 0.566               | 0.218               |
| Percent change        |                     | 0.500               | 0.760               |                     | 0.500               | 0.760               |

### (c) Age interaction (G.B. and N.I.)

|                       | Clustering          |                     |                     | No clustering       |                     |                     |
|-----------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
|                       | FE IWE RWE          |                     |                     | FE                  | IWE                 | RWE                 |
| _                     | 0.078***<br>(0.002) | 0.079***<br>(0.002) | 0.079***<br>(0.002) | 0.078***<br>(0.001) | 0.079***<br>(0.001) | 0.079***<br>(0.001) |
| Het. test stat        |                     | 173.473             | 50.981              |                     | 43.709              | 51.981              |
| Het. test $p$ -value  |                     | 0.000               | 0.005               |                     | 0.030               | 0.005               |
| Spec. test stat.      |                     | 0.684               | 3.753               |                     | 1.887               | 14.200              |
| Spec. test $p$ -value |                     | 0.494               | 0.053               |                     | 0.059               | 0.000               |
| Percent change        |                     | 0.668               | 1.222               |                     | 0.668               | 1.222               |

(d) N. Ireland dummy interaction (G.B. and N.I.)

|                       | Clustering          |                     |                     | No clustering       |                     |                     |
|-----------------------|---------------------|---------------------|---------------------|---------------------|---------------------|---------------------|
|                       | FE                  | IWE                 | RWE                 | FE                  | IWE                 | RWE                 |
| _                     | 0.078***<br>(0.002) | 0.079***<br>(0.001) | 0.079***<br>(0.002) | 0.078***<br>(0.001) | 0.079***<br>(0.001) | 0.079***<br>(0.001) |
| Het. test stat        |                     | 44.647              | 43.717              |                     | 91.327              | 43.717              |
| Het. test $p$ -value  |                     | 0.000               | 0.000               |                     | 0.000               | 0.000               |
| Spec. test stat.      |                     | 0.725               | 11.004              |                     | 4.831               | 109.906             |
| Spec. test $p$ -value |                     | 0.468               | 0.001               |                     | 0.000               | 0.000               |
| Percent change        |                     | 0.712               | 0.753               |                     | 0.712               | 0.753               |

Table 13: Pérez-González (2006)

#### (a) Operating returns on assets (OROA), year interactions

|  | FE                     | IWE                                     | RWE   |
|--|------------------------|---|---|
|  | $-0.027^{***}$ (0.010) | $-0.027^{***}$ $(0.009)$                | -0.025** $(0.010)$                            |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value Percent change |                        | 34.878 $0.010$ $0.217$ $0.829$ $-2.372$ | $25.540 \\ 0.111 \\ 0.474 \\ 0.491 \\ -7.464$ |

# (b) Market-to-book ratio (M-B), year interactions

|  | FE                       | IWE                                      | RWE  |
|--|--------------------------|--|--|
|  | $-0.256^{***}$ $(0.089)$ | $-0.226^{***}$ (0.083)                   | $-0.227^{***}$ $(0.087)$                       |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value Percent change |                          | 39.777 $0.002$ $0.978$ $0.329$ $-11.448$ | $24.390 \\ 0.143 \\ 0.963 \\ 0.327 \\ -11.278$ |

### (c) Operating returns on assets (OROA), high family ownership interaction

|  | FE                       | IWE                                     | RWE                                       |
|--|--------------------------|---|---|
|  | $-0.027^{***}$ $(0.010)$ | $-0.030^{***}$ $(0.009)$                | $-0.030^{***}$ $(0.008)$                  |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value Percent change |                          | 0.492 $0.483$ $-0.693$ $0.489$ $10.368$ | 0.642<br>0.423<br>0.449<br>0.503<br>9.390 |

### (d) Market-to-book ratio (M-B), High family ownership interaction

|  | FE                       | IWE   | RWE                                       |
|--|--------------------------|---|---|
|  | $-0.256^{***}$ $(0.089)$ | $-0.302^{***}$ $(0.079)$                    | $-0.279^{***}$ $(0.077)$                  |
| Het. test stat. Het. test p-value Spec. test stat. Spec. test p-value Percent change |                          | 1.482<br>0.223<br>-1.171<br>0.243<br>18.040 | 2.238<br>0.135<br>0.435<br>0.510<br>9.160 |