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COUNTRY RISKS AND INCENTIVES SCHEMES

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#### ABSTRACT

The purpose of this paper is to address the role of endogenous default penalties that are contingent upon the intensity of default on the part of the borrowing nation, and to evaluate the effects of contingency plans that make the interest rate dependent upon variables that are correlated with the default penalty. This is done by considering an economy where a default will trigger a variable cost whose magnitude is determined by the intensity of default. We design alternative incentive schemes by varying the responsiveness of the penalty to the intensity of default, without changing the total cost applied in case of a complete default. At the limit our incentive scheme converges to an exogenous default cost regime. We derive the supply of credit for the case where there is uncertainty regarding the total default cost, and we evaluate the dependency of the supply curve on the incentive scheme. A rise in the elasticity of the penalty with respect to the default intensity is shown to induce a higher default rate and to raise the country risk as reflected in the interest rate associated with a given borrowing, causing a leftward shift in the supply of credit. Using the expected welfare of a representative consumer it is shown that the introduction of partial defaults due to a variable penalty has adverse effects. Thus, our study concludes that variable default schemes that the penalty to the default rate are disadvantageous. We turn then to an assessment of the weifare effect of plans that make the interest rate contingent upon realization of shocks. In general, such a contingency plan is advantageous. For example, a plan that will index the interest rate such as to correlate it perfectly with the default penalty eliminates the adverse effects of country risk on expected income. For such an economy a contingency plan that will index the effective interest rate to the realization of the terms of trade will be beneficial in reducing the effective magnitude of country risk and the incidence of default.

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## 1. INTRODUCTION AND SUMMARY

The adverse supply shocks of the 1970's triggered substantial borrowings bu L.D.C.'s and Latin American countries. The accumulated borrowings have changed the country risk characteristics of the borrowing nations, which have found servicing their debt a challenging task. In the 1980's various countries have engaged in debt rescheduling , whereas others have found that new borrowings involve a significant risk premium $^1$ . Consequently, attention has been focussed on the design of credit policies and the role of institutions in the presence of country risk. Recently we have observed initial attempts to design payment plans that will make the effective interest rate paid by the borrowing nation contingent upon its terms of trade<sup>2</sup>. These circumstances have raised important questions regarding the design of incentive schemes for the borrowing nations. Such schemes should enhance the borrowing nations' incentives to service their debt, thereby reducing the risk premium charged for a given credit volume and allowing smoother operation of the international credit market. The purpose of this paper is to address two policy issues related to the design of incentives. We address first the role of endogenous default penalties that are contingent upon the intensity of default undertaken by the borrower nation, and then we evaluate the effects of contingency plans that make the interest rate dependent upon variables that are correlated with the default penalty.

In general, the supply of credit is determined by the nature of the expected default penalty. A default may trigger two types of penalties. The first is exogenously fixed, and its magnitude is independent of the intensity of default. The second is variable, and its magnitude is determined by the intensity of default. This paper starts by addressing a positive issue--assessing the dependency of the supply of credit on the elasticity of the penalty with respect to the default intensity. This sets the stage for the normative discussion. The first policy issue addressed is the welfare implications of contingent default penalties. We turn then to an assessment of the welfare effect of contingent interest rates in the presence of country risk.

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Section 2 starts by formulating the benchmark case, where there is only an exogenous default penalty. We consider a two-periods example. Borrowing takes place in period zero; debt repayment is scheduled for period one. In case of default, a fixed default penalty is inflicted upon the borrower. There is uncertainty in period zero regarding the magnitude of the effective default penalty, and debt issuance occurs before the resolution of uncertainty. We consider risk-neutral lenders, who charge an interest rate that results in an expected yield equal to an exogenously given risk-free interest rate. We review the derivation of the supply of credit, which may include a backward-bending portion. As was shown in Alzenman (1986), the presence of country risk introduces a distortion, calling for an optimal borrowing tax. Among other effects, the optimal tax eliminates the possibility of an equilibrium on the backward-bending portion of the supply of credit. We assume that such a tax is applied, allowing us to focus our analysis on equilibria on the upward-sloping portion of the supply of credit.

In section 3 we modify the assumptions of section 2 by allowing for a default penalty that is contingent upon the default intensity. To permit a comparison across regimes we design alternative incentive schemes by varying the responsiveness of the penalty to the intensity of default, without changing the total cost applied in case of a complete default. At the limit our incentive scheme converges to an exogenous default cost regime. The characteristics and the random nature of the full default penalty (i.e. the penalty associated with complete default) are the same as in section 2. These assumptions allow us to derive the dependency of the supply of credit on the elasticity of the penalty with respect to the default intensity. In general we will observe incidences of partial default whose magnitude rises with the level of borrowing relative to the cost of a complete default. A rise in the elasticity of the penalty with respect to the default. A rise in the associated with a given borrowing, causing a leftward shift in the supply of credit.

Section 4 conducts a welfare comparison between the regimes elaborated in sections 2 and 3. Using the expected welfare of a representative consumer it is

shown that the introduction of partial defaults due to a variable penalty has adverse effects. Thus, our study concludes that <u>variable default schemes that tie the penalty</u> to the default rate are disadvantageous. We turn then to an assessment of the welfare effect of plans that make the interest rate contingent upon realization of shocks. In general, such a contingency plan is <u>advantageous</u>. For example, it is shown that a plan that will index the interest rate such as to correlate it perfectly with the default penalty will eliminate the adverse effects of country risk on the expected income. Section 5 closes the discussion with interpretative remarks that tie the discussion in section 4 to recent attempts to make the effective interest rate paid by the borrowing nation contingent upon its terms of trade.

## 2. COUNTRY RISK WITH EXOGENOUS DEFAULT PENALTIES

The purpose of this section is to characterize country risk for the case of a fixed default penalty. This case will define the benchmark for the subsequent discussion. We start by modeling the supply of credit in the presence of country risk. Next, we discuss the demand for credit and optimal policies for the borrowing nation. The discussion in this section sketches the analysis in Alzenman (1986), whereas section 3 extends the framework for the case of endogenous default penalties<sup>3</sup>.

## 2.1 <u>The Default Decision</u>

Consider a two-periods small economy. Borrowing  $\overline{B}$  takes place in period zero at an interest rate r\*. Debt repayment  $\overline{B}(1+r^*)$  is scheduled for period one. In case of default, a stochastic penalty N is inflicted upon the borrower, given by

(1) 
$$N = N_{0} / \Psi$$

The term  $\Psi$  represents a stochastic disturbance, whose density function is g. Debt issuance occurs in period zero, before the resolution of uncertainty regarding  $\Psi$ . The information regarding  $\Psi$  is summarized by a distribution of  $\Psi$ , which is known to both the lenders and the borrowing nation. This information is applied to determine the supply of credit. We consider the case where the default decision is arrived at by a centralized decision maker, like the central bank. While consumers are assumed to be price takers in the credit market, they are fully aware of the default rule guiding the central bank. Equation (1) can reflect various economic environments. For example, let the default penalty be the result of adverse commercial policies (like banning trade in goods and services). In such a case the term  $\Psi$  may reflect a stochastic term measuring the effectiveness of the trade embargo. Alternatively, the default penalty can be the result of exclusion from future borrowing. Let N be the future cost of being excluded from the credit market (in terms of period two) due to a default in period one; and  $\Psi$  be the effective discount factor that translates the future penalty (N) into N/ $\Psi$  in terms of period one. Thus,  $\Psi$  can be viewed as a myopia measure, where a higher  $\Psi$  corresponds to a smaller weight attached to the future by the decision maker in period one. In such a case the uncertainty regarding  $\Psi$  may reflect political uncertainty regarding the horizon of the future decision maker.

Default will take place if the debt exceeds the penalty, or if

(2) 
$$\overline{B}(1+r^*) > N_{\alpha}/\Psi$$

Alternatively, the default rule can be summarized by:

(3) no default if  $\Psi > Z$ no default if  $\Psi < Z$ ;

where  $Z = N_0 / \overline{B}(1+r^*)$  denotes the marginal value of  $\Psi$  associated with default.

## 2.2 The Supply of Credit

We assume a credit market that is dominated by risk-neutral lenders, fully informed regarding the nature of the decision rule guiding the borrower, as well as regarding the borrower's indebtedness position<sup>4</sup> ( $\overline{B}$ ). A risk-neutral lender will extend credit  $\overline{B}$  at a rate r\* such that the expected yield on the risky loan equals the risk-free return:

(4)  $(1+r^*) P = 1+r_f$ 

where  $r_f$  is the exogenously given risk-free interest rate, and P is the probability of no default. From (4) we infer that

where g is the density function corresponding to  $\Psi$ , defined for  $\Psi > \varepsilon > 0$ . Thus, P is a function of  $(1+r^*)\overline{B}$ , P = P{ $(1+r^*)\overline{B}$ }, with P' < 0. Equations (4) and (5) define the credit supply curve, which is determined by the distribution g. We summarize the reduced form of the supply of credit by:

(4') 
$$\Gamma^* = \Gamma^*(\overline{B})$$

Notice that a rise in the interest  $r^*$  rate has two opposing effects on the expected income yield. The direct effect is reflected in the rise of the yield for a given probability of no default (P). But it also implies a drop in P. This second effect works to depress the expected yield, implying that under certain conditions (derived in Aizenman (1986)) the supply is backward-bending<sup>5</sup>.

# 2.3 The Demand for Credit

The demand for credit is derived from the underlying consumer preferences. We assume that consumers' utility is given by

(6) 
$$U = u(X_0) + \rho u(X_1)$$

where  $X_j$  is the consumption in period i, and p stands for the subjective rate of time preference. A representative consumer maximizes his expected utility subject to his budget constraints. He is facing an interest rate r, that may differ from the external interest rate r<sup>m</sup> due to the presence of borrowing taxes. The social role of these taxes will be examined in the sequel. The representative consumer's budget constraints are given by (7)  $X_0 = \overline{X}_0 + B$ 

(8a) 
$$X_{in} = \overline{X}_i + R_i - B(1 + r)$$

$$(8b) \qquad X_{1.d} = \overline{X}_1 - N_0/\Psi$$

where  $\overline{x}_i$  stands for the endowment in period i,  $R_1$  for lump-sum transfers in period one,  $x_{1,n}$  is the consumption in case of no default,  $x_{1,d}$  is the consumption in states of default and B is the borrowing by the consumer. Equation (7) defines the budget constraint for period zero, whereas for period one we observe two possible budget constraints, corresponding to the possibility of no default (8a) and default (8b). To simplify exposition, we abstract from production, assuming an endowment model (adding production and investment would not change the main results). Applying the budget constraints to (6) we can characterize the consumer problem as choosing B so as to maximize expected utility V:

(9) 
$$V = u(\overline{X}_0 + B) + \rho \int u(\overline{X}_1 + R_1 - B(1 + r))g(\Psi) d\Psi + \rho \int u(\overline{X}_1 - N_0/\Psi)g(\Psi) d\Psi$$
  
 $\epsilon$ 
 $Z$ 

Optimizing (9) yields the following first-order condition:

(10)  $V'(X_0)/V'(X_{1,0}) = 1 + r$ 

where  $V'(X_j)$  stands for the expected marginal utility of consuming  $X_j$ :

$$\nabla'(X_{\theta}) = u'(X_{\theta}) \quad ; \quad \nabla'(X_{1,n}) = \rho \int u'(\overline{X}_{1} + R_{1} - B(1 + r))g(\Psi) \, d\Psi.$$

$$\epsilon$$

Optimal borrowing B is chosen by the consumer so as to support a consumption path

that yields equality between the ratio of the corresponding expected marginal utilities of consumption and the interest rate. The assumption that the consumer is a price taker is reflected in the fact that each consumer treats aggregate borrowing  $\overline{B}$  (and the corresponding Z and r) as exogenously given.

## 2.4 Optimal Policu for a Borrowing Nation

To gain insight into the potential role of optimal policies let us evaluate the solution of the optimal consumption path by a centralized decision maker. Potential deviations between the planner's and the consumer's solutions will justify policies needed to support optimality. These policies will be shown to be in the form of optimal borrowing taxes. We assume that the transfer  $R_1$  is used to rebate consumers such that the net present value of the planner's revenue is zero (when the relevant interest rate from the planner's perspective is the external interest rate, r\*). Subject to this requirement the budget constraints facing the planner can be shown to be

(7) 
$$X_0 = \overline{X}_0 + \overline{B}$$

(8a') 
$$X_{1,n} = \overline{X}_1 - \overline{B}(1 + r^*)$$

(8b') 
$$X_{1,d} = \overline{X}_1 - N_0/\Psi$$

with the help of these budget constraints the planner's problem is reduced to a choice of  $\overline{B}$  that will maximize

(9') 
$$V = u(\overline{X}_0 + \overline{B}) + \rho \int u(\overline{X}_1 - \overline{B}(1 + r^*))g(\Psi) d\Psi + \rho \int u(\overline{X}_1 - N_0/\Psi)g(\Psi) d\Psi$$
  
 $\epsilon \qquad Z$ 

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A key difference between the consumer's and the planner's problems is that the centralized planner is not a price taker in the credit market, and he is aware that the choice of borrowing  $\overline{B}$  will impact on the interest rate via the supply of credit (4'). Consequently, (9') implies that the condition for optimal borrowing is

(10') 
$$V'(X_0)/V'(X_{1,n}) = (1 + r^*)(1 + \frac{d \log(1 + r^*)}{d \log \overline{B}})$$

where 
$$\vec{B}$$
  $\forall (X_0) = u'(X_0)$ ;  $\forall (X_{1,n}) = \rho \int u'(\overline{X_1} - \overline{B}(1 + r^*))g(\Psi) d\Psi$ .  
 $\epsilon$ 

Optimal borrowing  $\overline{B}$  is chosen by the planner so as to support a consumption path that yields equality between the ratio of the corresponding expected marginal utilities of consumption and the 'social' interest rate (defined by d  $log(1 + r^*)/d$ log  $\overline{B}$  ). A comparison between the planner's and the consumer's solutions reveals that the two differ in that the planner applies the 'social' interest rate, whereas the consumer applies the 'private' one. In the absence of borrowing taxes the presence of country risk implies that there is a distortion, and that from the social point of view the equilibrium is associated with "excessive" borrowing because the private falls short of the social interest rate. This situation provides the rationale for government intervention. The distortion arises from the fact that individual borrowers treat the rate of interest as given even though from the perspective of the country as a whole the rate of interest rises with the volume of borrowing. An optimal borrowing tax is needed to yield equality between the social and the private interest rates<sup>7</sup>. As is shown in Aizenman (1986), the optimal borrowing tax has an important consequence -- ruling out inefficient equilibria on the backward-bending portion of the supply of credit. Henceforth, we will assume that the optimal

borrowing tax is applied and therefore we will neglect the backward-bending portion of the supply of credit. This argument is summarized in Figure One. Curve DD is the demand for credit, KLMN plots the supply curve, and KLM' corresponds to the 'social supply' curve (the marginal to KLM). Optimality calls for a borrowing tax, defined by the vertical distance between  $\tilde{r}^{*}$  and  $\tilde{r}$  (Figure One)<sup>8</sup>.

#### 3. COUNTRY RISK WITH ENDOGENOUS DEFAULT PENALTIES

The purpose of this section is to study the role of endogenous penalties, and to assess their desirability. In section 2 we considered the case of a fixed default penalty, independent of the magnitude of the default. In that case, the borrower faced an all-or-nothing choice. In this section we allow for a penalty tied to the default rate. Let us denote by  $\tau$  the default rate ( $0 \le \tau \le 1$ ). With a default  $\tau$  only a portion  $1-\tau$  of  $\overline{B}(1+r^*)$  is paid in period one. We assume that a default  $\tau$  imposes costs of

(11)  $\tau^h N$  for  $1 \ge \tau \ge 0$ ; where  $h \ge 1$ .

Notice that h is the elasticity of the penalty with respect to the default intensity. It measures the convexity of the penalty with respect to the default rate -- a higher h implies higher responsiveness of the penalty to the default intensity. By definition, the effective penalty does not exceed N; and it approaches N as  $\tau \rightarrow 1$  (complete default). The specification in (11) is flexible enough to allow assessment of the positive and normative aspects introduced by the presence of an endogenous penalty scheme. Varying h will allow us an assessment of the role of endogenous penalties, where  $h \rightarrow 1$  will bring convergence — to the benchmark case of fixed penalties of section 2. With the exception of the specification of the variable cost in



FIGURE ONE

(11), we preserve all the other assumptions of section 2, including the distributional assumptions regarding N (see (1)).

The supply of credit in the presence of endogenous penalties is derived in several stages. First, we derive the cost minimizing default rate  $\tilde{\tau}$  from the borrower's perspective for a given  $\overline{B}(1+r^*)$ . Next, armed with the solution for  $\tilde{\tau}$  we solve for the interest r\* charged by the lenders for credit volume  $\overline{B}$ . We then study the dependency of the supply of credit on the penalty scheme, as summarized by h.

### 3.1 The Default Rate

The borrowing nation chooses in period one the default rate  $\tau$  so as to maximize the gain in net income attributed to default. The 'default income', denoted by  $\pi(\tau)$ , is:

(12) 
$$\pi(\tau) = \tau \overline{B}(1+r^*) - \tau^{\mathsf{h}} N_0 / \Psi$$
 for  $0 \leq \tau \leq 1$ 

It is composed of the benefit of partial default  $[\tau \overline{B}(1+r^*)]$  minus the cost associated with the default  $[\tau^h N_0/\Psi]$ . Let us denote by  $\tilde{\tau}$  the default rate that maximizes the default income. Direct optimization reveals that for  $h \ge 1$ 

(13) 
$$\tilde{\tau} = Min \{ 1; [\overline{B}(1 + r^*)/\{hN\} \} \}$$

To gain further insight we plot in Figure Two the marginal cost and the marginal benefit associated with default  $\tau$ . Optimal default is obtained at the intersection of the two curves. The Appendix shows that for an internal solution ( $\theta < \tilde{\tau} < 1$ ) a rise in h (the elasticity of the penalty with respect to the default intensity) will increase the default rate. In terms of Figure Two the rise in h is associated with a rightward shift of the relevant portion of the MC curve. Similarly a drop in the default penalty will shift the MC curve rightward, thus raising the default rate. Alternatively, a rise in the gross indebtedness ( $1 + r^*$ ) $\overline{B}$  will shift the MB curve



FIGURE TWO

upwards, being associated with a rise in the default rate.

Let us denote by Z the marginal value of  $\Psi$  associated with a complete default ( $\tau = 1$ ). From (13) we infer that

(14) 
$$Z = hN_0/{\overline{B}(1 + r^*)}$$
.

It is noteworthy that in the case of h = 1 the default decision degenerates to a simple rule:

$$\begin{array}{ccc} 0 & \text{if} & \Psi < N_0 / [\overline{B}(1 + r^*)] \\ (15) & \widetilde{\tau} = & \\ & 1 & \text{if} & \Psi > N_0 / [\overline{B}(1 + r^*)] \end{array}$$

Equation (15) corresponds to the case of a fixed default penalty. Applying (13) allows us to conclude that as we approach the case of exogenous penalty  $(h \rightarrow i)$  the optimal default rate for an internal solution converges to zero. Thus, as  $h \rightarrow 1$  we approach the benchmark case of section 2, where  $\tilde{\tau}$  is either zero or one. We turn now to the the derivation of the supply curve, which augments the information regarding the default rate that has been derived in this section.

# 3.2 The Supply of Credit with Endogenous Penalties

Risk neutral lenders will require interest rate r\* such that:

(16) 
$$(1+r^*)(1-E(\tilde{\tau}|1+r^*;\overline{B})) = 1+r_f$$

where  $E(\tilde{\tau}|1+r^*; \bar{B})$  stands for the expected default intensity. Debt issuance occurs before the resolution of the uncertainty regarding  $\Psi$ . Thus, the lenders will set the interest rate according to (16), by applying the expected values of  $\tilde{\tau}$  obtained from (13), yielding:

(17) 
$$E(\tilde{\tau}) = \int \{\overline{B}(1 + r^*)/\{hN\}\} g(\Psi) d\Psi + \int g(\Psi) d\Psi$$

and the implied supply of credit is given by

The Appendix evaluates the dependency of the supply schedule on the elasticity of the penalty with respect to the default intensity (h). It is shown that a rise in h shifts the supply curve leftwards, implying that a given volume of credit will require a higher interest rate. This result stems from the fact that for a given interest rate a higher convexity of the penalty scheme (d h > 0) implies a higher default rate, reducing thereby the expected yield on a given volume of indebtedness, and thus necessitating a rise in the interest rate.

To gain further insight, we now turn to a comparison between the welfare obtained subject to endogenous versus fixed penalties. This comparison will enable us to conclude with normative statements regarding the desirability of each scheme.

# 4. THE WELFARE EFFECTS OF CONTINGENT PENALTIES AND INTEREST RATES

Our discussion in section 3 implies that allowance for endogenous default penalties is associated with a rise in the country risk, as is reflected by the rise in the interest rate associated with a given indebtedness. It is noteworthy that this observation alone does not suffice to determine the welfare effects of endogenous default penalties. That is because the adverse effects of the induced rise in the interest rate will be partly offset by the rise in the incidence of partial defaults that are associated with 'default income'.

# 4.1 Endogenous Default Penalties and Welfare

We evaluate the welfare consequences of endogenous penalties by analyzing their expected utility. Formally, the expected utility associated with a given level of borrowing  $\overline{B}$  is given by

where  $\pi$  and Z are obtained from (12)-(14). Applying (19) we get that<sup>9</sup>

(20) 
$$\frac{\partial V}{\partial h} = -\int u'(X_{1,n})(\overline{B}(1-\tilde{\tau}) - \frac{\partial (1+r^*)}{\partial h})g(\Psi) d\Psi < 0$$
  
 $\partial h = \varepsilon \qquad \partial h$ 

Consequently, a greater responsiveness of the penalty scheme to the default rate results in a drop in expected welfare. This is because the added degree of freedom introduced by a variable default cost has the consequence of raising the expected

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default for a given credit volume, necessitating a higher interest rate. The rise in the interest rate dominates any indirect gains associated with the greater flexibility of the default structure.

## 4.2 The Role of Contingencies

The emerging conclusion is that welfare is reduced by making the default penalty <u>contingent</u> upon the <u>intensity of default</u>. This, however, does not imply that contingent prices are not beneficial. In fact, welfare can be enhanced if the interest rate is made contingent upon the default penalty ( $\Psi$ ). For example, consider the case of exogenous default penalties (h = 1). Suppose that the value of  $\Psi$  is public information in period one, and that we normalize N<sub>0</sub> such that the expected value of  $1/\Psi$  is one. Let us define a contingent interest rate r<sup>\*</sup>( $\Psi$ ) by

(21) 
$$1 + r^* = (1 + r_f)/\Psi$$

Recalling that the default penalty is  $N_0/\Psi$ , it is evident that  $1 + r^*$  is defined to be perfectly correlated with the default penalty. Applying the decision rule (3) it is evident that for  $\overline{B} < N_0/(1 + r_f)$  the contingent interest rate (21) <u>eliminates</u> the consequences of country risk. To verify this point, note that for  $\overline{B} < N_0/(1 + r_f)$  we observe that for all  $\Psi$ ,  $(1 + r^*)\overline{B} < N_0/\Psi$ . With such a contingency pricing no default will occur. The proposed scheme is also feasible because the expected yield is equal to the risk-free interest rate (E[(1+r\_f)/\Psi] = 1+r\_f). The expected welfare in such a system is given by

(22) 
$$\vee = u(\overline{X}_0 + \overline{B}) + \rho \int u(\overline{X}_1 - \overline{B}(1 + r^*)) g(\Psi) d\Psi$$

To gain further insight into the welfare effect of this scheme consider the case where consumers are risk neutral, i.e. where the periodic utility u(X) is linear (u(X) = X). For such an economy a welfare ranking is a comparison of expected income. A comparison of (22) and (9') reveals that the gain in expected income associated with the contingent interest-rate scheme is equal to the expected penalty in the non-contingent, exogenous penalty system (given by  $\int [N_0/\Psi]g(\Psi)d\Psi$ ). The effect of making the interest rate perfectly correlated with the Z

penalty is to eliminate the adverse effects of country risk on the expected income. With risk-averse agents the optimal contingency pricing is more complicated, because it involves also optimal reallocation of the income risk among the various parties in an attempt to reduce the volatility of income across states. But even in this case we will observe welfare gains generated by contingent interest rates.

## 5. CONCLUDING REMARKS

Rather than repeating the summary from the introduction, we conclude with interpretative remarks. Our discussion has focussed on the analysis of the potential welfare effects of contingency plans in the presence of country risk. The analysis allows us to conclude that contingency plans that make the default costs dependent upon the intensity of default undertaken by the borrower nation are not cost-minimizing schemes. At the same time, contingency plans that make the interest rate dependent upon observable variables that are correlated with the default penalty are cost-minimizing schemes. For example, a contingency plan that will make the interest rate perfectly correlated with the default penalty will fully eliminate the adverse income effects of country risk and will eliminate incidences of default for credit volumes below the ceiling. It will also have the beneficial by-product of increasing the credit ceiling. A necessary condition for the feasibility of such a system is that the realization of the default penalty should be public information. One can speculate that an example of this type of arrangement is the recent Mexican rescheduling plan, where several aspects of debt servicing were made contingent upon the future price of oil. This arrangement can enhance welfare if the default cost is low in bad states of nature, when the price of exportables is  $low^{10}$ . For such an economy a contingency plan that will index the effective interest rate to the realization of the price of exportables will be beneficial in reducing the effective magnitude of country risk and the incidence of default.

## APPENDIX

The purpose of this Appendix is to prove that for an internal solution for  $\tilde{\tau}$  a rise in h (the elasticity of the penalty with respect to the default intensity) will increase the optimal default rate and will shift the supply of credit leftward.

Direct derivation of (13) reveals that for  $0 < \tilde{\tau} < 1$ 

(A1) 
$$\frac{\partial \tilde{\tau}}{\partial h} = - [h \log [\overline{B}(1 + r^*)/\{hN\}] + h - 1] \frac{1}{(h - 1)^2}$$

thus, the sign of (A1) is determined by sign{-[h log  $[\overline{B}(1 + r^*)/{hN}] + h - 1]$ }. Note that because  $0 < \tilde{\tau} < 1$  equation (13) implies that log  $[\overline{B}(1 + r^*)/{hN}] < 0$ . Consequently, for h = 1 sign{-[h log  $[\overline{B}(1 + r^*)/{hN}] + h - 1]$ } is positive. We can prove that (A1) is positive if we can demonstrate that the expression determining the sign of (A1) rises with h (because h ≥ 1). This proof follows from the fact that

(A2) 
$$\partial - [h \log [\overline{B}(1 + r^*)/{hN}] + h - 1]/\partial h = -\log [\overline{B}(1 + r^*)/{hN}] > 0$$
.

We turn now to the derivation of the effect on the supply curve of a rise in h. We do so by evaluating the horizontal displacement of the supply schedule induced by a rise in h. From (18) we get that for a given  $(1+r^*)$ 

(A3) 
$$\Delta \overline{B} = \frac{\partial [(1+r^*)(1-E(\tilde{\tau}|1+r^*;\overline{B}))]}{\partial \overline{B}} = \Delta h (1+r^*) \int \frac{Z}{\partial h} g(\Psi) d\Psi$$
  
 $\varepsilon = \partial h$ 

The term multiplying  $\Delta \overline{B}$  corresponds to the change in expected yield induced by a rise in indebtedness. Direct inspection of (18) reveals that this change is negative, due to the induced rise in the expected default rate. The term multiplying  $\Delta h$  is positive, because we showed that  $\partial \tilde{\tau} / \partial h > 0$ . Combining that information implies that holding (1 + r\*) given

(A4)  $\partial \overline{B} / \partial h < 0$ .

-

Therefore, we conclude that a rise in h shifts the supply schedule leftward.

### FOOTNOTES

1. For a useful study on the debt problem see the World Bank Report (1986). For studies on country risk, see Harberger (1976, 1980); Eaton and Gersovitz (1981); Sachs (1984); Kletzer (1984); Edwards (1984, 1985); Dornbusch(1985); Eaton (1985); Krugman(1985); Aizenman (1986).

2. A recent example is the July 22 ,1986 agreement between Mexico and the IMF, where several aspects of debt servicing were made contingent upon the future price of oil.

3. For related studies regarding the determination of the supply of credit with exogenous default penalties see Sachs (1984) and Krugman(1985).

4. Equilibrium in a market with partial information regarding the volume of indebtedness is the topic of Kletzer (1984).

5. It can be shown that d log  $\overline{B}/d$  log  $(1+r^*) = (1-\eta)/\eta$ ; where  $\eta$  is the elasticity of P with respect to gross indebtedness  $[\eta = -d \log P/d \log \overline{B}(1+r^*)]$ . Consequently, the supply curve is backward bending if  $\eta > 1$  (for more details see Aizenman (1986)).

6. In deriving this result we use the fact that  $V_Z = 0$ .

7. The percentage optimal borrowing tax can be shown to equal  $(1 + r^*)/\{r^* d \log \overline{B}/d \log (1+r^*)\}$ .

8. It is noteworthy that as the borrowing nation approaches the inelastic segment of the supply of credit (where  $d B/d (1+r^*) \rightarrow 0$ ), optimality calls for the imposition of a dual exchange rate system. This system is equivalent to the imposition of a quota on borrowing (equal to the borrowing ceiling) and a tax on borrowing equal to the spread between the domestic interest rate and the supply price of the credit ceiling. These are the optimal policies if the equilibrium occurs at the credit ceiling level (for further details see Alzenman (1986)).

9. In deriving (20) we are using the fact that  $V_Z = 0$  and around the equilibrium  $\partial \pi/\partial (1 + r^*) = \tilde{\tau} B$  and  $\partial \pi/\partial \tau = 0$ .

10. Several factors can account for low default costs in bad states of nature. First, the cost of a trade embargo can be lower because of the drop in the value of exports. Second, bad states may be associated with higher myopia in the policy maker, whose survival may be at risk.

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