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TO COMPUTER PRICES:
THE ROLE OF DURABILITY AND CHANGING SOFTWARE

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ABSTRACT

In the second-half of the 1990s, the positive impact of information technology on productivity growth for the United States became apparent. The measurement of this productivity improvement depends on hedonic procedures adopted by the Bureau of Labor Statistics (BLS) and Bureau of Economic Analysis (BEA). In this paper we suggest a new reason why conventional hedonic methods may overstate the price decline of personal computers. We model computers as a durable good and suppose that software changes over time, which influences the efficiency of a computer. Anticipating future increases in software, purchasers may "overbuy" characteristics, in the sense that the purchased bundle of characteristics is not fully utilized in the first months or year that a computer is owned. In this case, we argue that hedonic procedures do not provide valid bounds on the true price of computer services at the time the machine is purchased with the concurrent level of software. To assess these theoretical results we estimate the model and find that before 2000 the hedonic price index constructed with BLS methods overstates the fall in computer prices. After 2000, however, the BLS hedonic index falls more slowly, reflecting the reduced marginal cost of acquiring (and therefore marginal benefit to users) of characteristics such as RAM, hard disk space or speed.

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1. Introduction

In the second-half of the 1990s, the positive impact of information technology (IT) on productivity growth for the United States became apparent (Jorgenson and Stiroh, 2000, Oliner and Sichel, 2000). The measurement of this productivity improvement depends on hedonic procedures adopted by the Bureau of Labor Statistics (BLS) and Bureau of Economic Analysis (BEA). These procedures include the hedonic adjustment of prices for mainframes and peripherals since 1985 (Cole *et al*, 1986, Cartwright and Smith, 1988), for personal computers (PC's) since 1991 (Holdway, 2001), and for semiconductors since 1996 (Grimm, 1998).¹ The rapid price declines of these products means that their production and use accounts for a sizable portion of recent U.S. productivity gains.

It is sometimes suggested that the price declines in IT products may be overstated due to the use of hedonic techniques, though this belief has not been confirmed. Triplett (1999), for example, critiques a number of suggested reasons why the hedonic techniques might overstate the price decline of IT products, but he generally finds that these reasons are not persuasive. Empirically, Landefeld and Grimm (2000) show that the hedonic adjustments used in official statistics closely match those recommended by academic studies, such as Berndt and Rappaport (2001), so there is no presumption of a downward bias in the official calculations. But concern about this potential bias will no doubt continue.²

In this paper we suggest a new reason why conventional hedonic methods may overstate the price decline of personal computers, which are treated here as a durable good. We suppose

¹ See Moulton (2001) who details the use of hedonic methods in U.S. statistical agencies.

² For semiconductors, Aizcorbe (2004) argues that falling price-cost margins by selling firms may accentuate the price decline. Gordon (2000) presents a different reason why the TFP contribution of IT capital may be overstated. He argues that the increase in TFP during the second-half of the 1990s is a cyclical rather than trend increase, and by focusing only on the trend, the contribution of IT capital to productivity is smaller. Conversely, Benkard and Bajari (2003) argue that standard hedonic index can be upward biased due to unobserved characteristics.

that software changes over time, which influences the efficiency of a computer. Anticipating the future increases in software, purchasers may “overbuy” characteristics, in the sense that the purchased bundle of characteristics is not fully utilized in the first months or year that a computer is owned. Forward looking buyers will equate the marginal benefits of characteristics over the *lifetime* of a machine to the marginal cost at the time of purchase. This means that the marginal costs are equated to marginal benefits evaluated at *future* levels of software. In this case, we argue that hedonic procedures do not provide valid bounds on the true price of computer services at the time the machine is purchased with the concurrent level of software.

There are two ways that this concern might influence calculations of total factor productivity (TFP). Following Oliner and Sichel (2000), let us make the distinction between the *use* of IT capital and the *production* of IT capital. The use of IT capital will influence TFP calculations through the measurement of the IT capital stock. This will require depreciation rates for computer equipment, and if changes in software influences the efficiency of a machine then depreciation rates should reflect this. We do not attempt to solve that problem here, though our framework could likely be adapted to address it.³ Rather, we focus on the production of IT capital, and in particular, on the hedonic price index constructed for personal computers, as in Holdway (2001). This hedonic index can be used to construct dual TFP for personal computers, *i.e.* as the difference between weighted growth in factor prices within that sector and the growth in the hedonic output price. If the hedonic output price is intended to reflect the efficiency of new machines to users at the *current* level of software, then we argue that conventional hedonic methods may well overstate this price decline.

³ Overviews of the measurement of capital and depreciation rates are provided by Diewert (1980), Harper, Berndt and Wood (1989), and Hulten (1990), though only Diewert (1980, pp. 503-506) includes a discussion of hedonics. Specific discussion of depreciation for computers is in Oliner (1993) and Harper (2001).

We begin the analysis in section 2 by describing a case where the conventional hedonic adjustment provides a valid measure for the true services price of computers, similar to Rosen (1974) or Pakes (2003), though we allow for purchases of multiple units. In that section, it is assumed that the computers being purchased are nondurable. In section 3 we analyze the case where computers are durable and software is changing over time. We find that conventional hedonic methods do not provide valid bounds to the true price of computer services (evaluated with current levels of software). The extent to which the true services price deviates from the conventional hedonic index will depend on the *interaction* between software and characteristics in the services that buyers' obtain from the machine. If software and characteristics are complements, in the sense that anticipated increases in software will lead the buyer to purchase more characteristics today, then it is more likely that the conventional hedonic methods will overstate the true price decline.

To assess these theoretical results, in sections 4 and 5 we estimate the model in a two-step procedure. First, monthly hedonic regressions are run over a sample of desktop PC's, from August 1997 to September 2001. Second, we utilize a dataset of all purchases of PC's at the University of California, Davis over similar dates. In the second step, the estimated hedonic coefficients are regressed on the characteristics actually purchased each month and a weighted average of software quality over the lifetime of the machine. The coefficients obtained in this second step reveal the users' "production functions" by which characteristics and software are transformed into computer services. Therefore, we can use these coefficients to obtain the true services price for users, and compare this with the bounds obtained from conventional hedonic methods.

It turns out that our results differ in the first and second-halves of our sample. Before 2000, we generally find that the hedonic price index constructed with BLS methods overstates the fall in computer prices, as compared to the true price index constructed using the estimated production functions for users. This accords with our theoretical results. Furthermore, we find that the true services price falls *faster* when it is evaluated with *future* rather than *current* levels of software. This corresponds to our intuition that characteristics may be overbought, so their value with current software is less than with future software, and the true price index with current software is above the price index with future software.

After 2000, however, the BLS hedonic index falls more slowly, reflecting the reduced marginal cost of acquiring (and therefore marginal benefit to users) of characteristics such as RAM, hard disk space or speed. Depending on the starting month, by the end of 2001 it turns out that the BLS index matches quite closely the true production function index constructed with *current* software. In this sense, the overstatement of the price decline by BLS methods has been ameliorated in recent years. The production function index constructed with *future* software falls faster than either of the other two indexes, however, which is explained by the forthcoming release of Windows XP and 2003, with its large hardware requirements. Additional conclusions are provided in section 6.

2. Buyer's Problem With Nondurable Capital

In his classic treatment, Rosen (1974) considers the problem of buyers and sellers who purchase and produce differentiated goods. Under his assumptions (perfect competition and many varieties) this results in an equilibrium price schedule $p_t = h_t(x_t)$, where $x_t \in \mathbb{R}^M$ is the vector of characteristics and p_t is the price in period t . We will take this price schedule as given and re-examine the buyer's problem, introducing one important difference from Rosen: we shall

allow the buyer to purchase *multiple units* of the differentiated good, *i.e.* multiple computers. The reason for allowing this will become clear shortly. Since this assumption is more realistic for firms than for consumers, we will use that language to describe our model, but much the same results would hold for a consumer purchasing multiple units.

In addition to computers, the firm uses other inputs denoted by the vector y_t . The services obtained in year $t = 1, \dots, T$ from a computer of characteristics with x_t is $f(x_t, s_t)$, where the vector s_t denotes the state of software. We will sometimes refer to $f(x_t, s_t)$ as the “production function” for the firm, and it shows how computer characteristics and software combine to create computing services. Treating the computer as a non-durable good, the firm purchases n_t identical units in year t , and new machines the next year.⁴ The computers, purchased along with other inputs y_t , yields per-period revenue $G[y_t, n_t f(x_t, s_t)]$ for the firm. Then the maximization problem is to choose n_t , x_t and y_t to:

$$\max_{n_t, x_t, y_t} G[y_t, n_t f(x_t, s_t)] - n_t h_t(x_t) - q_t y_t, \quad (1)$$

where $p_t = h_t(x_t)$ is the price of a computer and q_t is the price of the other inputs y_t .

We will let $K_t \equiv n_t f(x_t, s_t)$ denote the capital stock of computers, measured in efficiency units. To compare our results with Rosen and other authors, suppose first that the number of computers purchased n_t cannot be varied (for example, $n_t = 1$). Then the first order conditions for problem (1) are:

$$G_y[y_t, n_t f(x_t, s_t)] = q_t, \quad (2)$$

$$G_K[y_t, n_t f(x_t, s_t)] n_t f_x(x_t, s_t) = n_t h_t'(x_t), \quad (3)$$

⁴ We could generalize the problem to allow the firm to choose several type of computers, each in multiple units, by giving it several service functions $f(x_t, s_t)$, *e.g.* for desktops, laptops, etc.

where $h_t'(x_t)$ denotes the vector of derivatives $(\partial h_t/\partial x_{1t}, \dots, \partial h_t/\partial x_{Mt})$ for the M characteristics.

Canceling n_t from the left and right-hand side of (3), the first-order condition is interpreted as the marginal benefit of each characteristic ($G_K f_x$) equaling its marginal cost (h_t'). A difficulty that arises is that the marginal benefit depends on the quantity of other inputs purchased via $G_K[y_t, n_t f(x_t, s_t)]$, or implicitly, on their prices q_t . This complicates the empirical application of hedonic methods, and several approaches have been taken to simplify the problem.

First, we could suppose that the revenue function is additively separable, so that $G[y_t, n_t f(x_t, s_t)] = g(y_t) + n_t f(x_t, s_t)$. In that case, the maximization of firm profits in (1) implies the sub-problem of choosing choose characteristics x_t to:

$$\max_{x_t} f(x_t, s_t) - h_t(x_t), \quad (4)$$

for which the first-order condition is simply $f_x(x_t, s_t) = h_t'(x_t)$. This formulation of the problem is implicitly used by Pakes (2003), for example. Second, we could reformulate the buyer's problem in terms of its dual, and carry along the prices q_t of the other goods in the first-order conditions. Diewert (2003) takes this approach and shows how an aggregate of the prices q_t affects the hedonic price surface.

Third, the approach we shall take is to allow the firm to optimally choose the number of computers n_t . This implies the additional first-order condition:

$$G_K[y_t, n_t f(x_t, s_t)] f(x_t, s_t) = h_t(x_t). \quad (5)$$

Combining (3) and (5) we readily obtain:

$$\frac{h_t'(x_t)}{h_t(x_t)} = \frac{f_x(x_t, s_t)}{f(x_t, s_t)}. \quad (6)$$

This shows the equality of the marginal price of characteristics with their marginal value to the user when the number of units are also chosen. It is analogous to the first-order condition derived by Rosen (1974), and has the benefit that the price or quantity of other goods purchased do not appear.

The simplicity of the first-order condition (6) will be useful empirically, but also allows a reformulation of the theoretical problem. Again letting $K_t \equiv n_t f(x_t, s_t)$ denote the capital stock of computers, so that $n_t = K_t / f(x_t, s_t)$, problem (1) can be re-written as:

$$\max_{K_t, x_t, y_t} G(y_t, K_t) - K_t \left(\frac{h_t(x_t)}{f(x_t, s_t)} \right) - q_t y_t . \quad (1')$$

For the choice of characteristics x_t , it is evident that to maximize (1'), the buyer must solve the sub-problem:

$$\min_{x_t} \frac{h_t(x_t)}{f(x_t, s_t)} . \quad (7)$$

Notice the difference between this sub-problem and that in (4): both are correct, but are obtained under slightly different assumptions. The formulation in (1') and (7) makes it clear that the *price of computer services* is $p_t / f(x_t, s_t) = h_t(x_t) / f(x_t, s_t)$, that is, the *ratio* of the nominal price to benefits rather than their *difference* in (4). We will presume that the goal of a price index is to measure the change over time in the “true” services price $p_t / f(x_t, s_t)$.

The first-order conditions for (7) are just (6), and the simple statement of the problem also allows the second-order conditions to be easily examined. Minimizing (7) is equivalent to minimizing its natural log, and a sufficient second-order condition for a local minimum are:

$$\left[\frac{\partial^2 \ln h_t(x_t)}{\partial x_t^2} - \frac{\partial^2 \ln f(x_t, s_t)}{\partial x_t^2} \right] \text{ is positive definite around } x_t. \quad (8)$$

Consider the case where the price function for computers, $h_t(x_t)$, takes on the semi-log form, $\ln p_t = \ln h_t(x_t) = \alpha_t + \beta_t' x_t$. Then (8) is satisfied if and only if $\ln f(x_t, s_t)$ is concave in a neighborhood around x_t . We state a slightly stronger version of this second-order condition as one possible assumption:

Assumption 1

- (a) $h_t(x_t)$ is semi-log in x_t , $\ln p_t = \ln h_t(x_t) = \alpha_t + \beta_t' x_t$, $t = 1, \dots, T$;
- (b) $\ln f(x, s)$ is concave in x in an open convex region that includes (x_t, s_t) , $t = 1, \dots, T$, where the characteristics and software are non-decreasing over time, $(x_{t-1}, s_{t-1}) \leq (x_t, s_t)$.

The assumption that $(x_{t-1}, s_{t-1}) \leq (x_t, s_t)$ in part (b) is made for notational convenience, and could be weakened. Note that by letting $x_t = \ln z_t$ for underlying characteristics z_t , then Assumption 1 can also be used for the log-log hedonic price function.

Clearly, parts (a) and (b) of Assumption 1 go together: with other assumptions on the functional form of the hedonic regression $h_t(x_t)$, there would be alternative properties for $f(x_t, s_t)$ implied by the second-order conditions. For example, suppose that we treated $h_t(x_t)$ as linear in x_t rather than semi-log. By twice differentiating (1) with respect to x_t , it is easy to show that the second-order condition is satisfied if $G(y_t, K_t)$ is concave in K_t and $f(x_t, s_t)$ is concave in x_t . We state this as an alternative assumption:

Assumption 2

(a) $h_t(x_t)$ is linear in x_t , $p_t = h_t(x_t) = \alpha_t + \beta_t' x_t$, $t = 1, \dots, T$;

(b) $f(x, s)$ is concave in x in an open convex region that includes (x_t, s_t) , $t=1, \dots, T$, where the characteristics and software are non-decreasing over time, $(x_{t-1}, s_{t-1}) \leq (x_t, s_t)$.

The BLS actually uses a linear hedonic regression (Holdway, 2001), but we will derive results that hold under either Assumptions 1 or 2.

The BLS makes a hedonic adjustment to computer prices to deflate the output of the computer sector within the producer price index. This price index then becomes an input price to sectors using computers, where we expect the hedonically-adjusted price index to reflect the cost of services obtained. To describe this in terms of problem (1'), the "true" price of computer services is $p_t/f(x_t, s_t)$, or the nominal price deflated by the services obtained from a machine. Let $P^0(p_{t-1}, p_t, x_{t-1}, x_t)$ and $P^1(p_{t-1}, p_t, x_{t-1}, x_t)$ denote two alternative measures of a constant-quality price ratio for a computer model between years $t-1$ and t , *i.e.* with *constant* characteristics. We wish to use these measures to obtain bounds on the true services price $p_t/f(x_t, s_t)$, such that:

$$P^0(p_{t-1}, p_t, x_{t-1}, x_t) \geq \frac{p_t/f(x_t, s_t)}{p_{t-1}/f(x_{t-1}, s_t)} \quad (9a)$$

and,

$$P^1(p_{t-1}, p_t, x_{t-1}, x_t) \leq \frac{p_t/f(x_t, s_{t-1})}{p_{t-1}/f(x_{t-1}, s_{t-1})} \quad (9b)$$

The right side of (9) is the ratio of the price of computers services, but measured at a *constant* level of software (s_t or s_{t-1}). If the inequalities in (9) hold, then we have obtained bounds on the change in the true services price, using the constant-quality price ratios P^0 and P^1 . Provided that these bounds are similar, then we conclude that the use of either one provides a good measure of the change in the services price for that computer.

In practice, BLS constructs the producer price index for personal computers as follows (Holdway, 2001). Let $p_t = h_t(x_t) = \alpha_t + \beta_t' x_t$ denote the linear hedonic regression, $t=1, \dots, T$. Then $h_t(x_{t-1}) = p_t - \beta_t'(x_t - x_{t-1})$ measures the price in year t *minus* an adjustment for the changed characteristics between the two years. Triplett (1986) refers to this as making an “explicit hedonic adjustment” to the period t price. The ratio of prices in year t and $t-1$ with constant characteristics is:

$$P^0(p_{t-1}, p_t, x_{t-1}, x_t) \equiv \frac{h_t(x_{t-1})}{p_{t-1}} = \frac{[p_t - \beta_t'(x_t - x_{t-1})]}{p_{t-1}} . \quad (10a)$$

While (10) is the method used by BLS, it is straightforward to consider alternative ways to make the hedonic adjustment. In particular, rather than adjusting the period t price in (10a), we could instead adjust the period $t-1$ price, obtaining:

$$P^1(p_{t-1}, p_t, x_{t-1}, x_t) \equiv \frac{p_t}{h_{t-1}(x_t)} = \frac{p_t}{[p_{t-1} + \beta_{t-1}'(x_t - x_{t-1})]} . \quad (10b)$$

We would expect the indexes P^0 and P^1 to be quite close in practice, provided that the price surface $h_t(x_t)$ is not changing too rapidly over time.

The particular form for the hedonic correction used in (10) depends on the functional form of $h_t(x_t)$. If instead we suppose that $\ln p_t = \ln h_t(x_t) = \alpha_t + \beta_t' x_t$ is semi-log, $t = 1, \dots, T$, then the constant-quality price ratios are:

$$P^0(p_{t-1}, p_t, x_{t-1}, x_t) \equiv \frac{h_t(x_{t-1})}{p_{t-1}} = \frac{p_t \exp[-\beta_t'(x_t - x_{t-1})]}{p_{t-1}} , \quad (11a)$$

and,

$$P^1(p_{t-1}, p_t, x_{t-1}, x_t) \equiv \frac{p_t}{h_{t-1}(x_t)} = \frac{p_t}{p_{t-1} \exp[\beta_{t-1}'(x_t - x_{t-1})]} . \quad (11b)$$

Following Berndt and Rappaport (2001, p. 270), we define the hedonic Laspeyres and Paasche prices indexes, respectively, as (11a) and (11b) evaluated using the *mean value* of characteristics over the models available each period. The mean value of characteristics are *also* used to evaluate the expected prices, $\bar{p}_t \equiv h_t(\bar{x}_t)$, $t = 1, \dots, T$. Notice that the hedonic Laspeyres index is then $P^0 = h_t(\bar{x}_{t-1})/h_{t-1}(\bar{x}_{t-1})$, which uses last-period characteristics, while the hedonic Paasche index is $P^1 = h_t(\bar{x}_t)/h_{t-1}(\bar{x}_t)$, which uses present-period characteristics.⁵

We will use (11) as the constant-quality price ratio corresponding to Assumption 1, and those in (10) for Assumption 2. The question is whether either of these provide valid bounds to the true price of computer services. The following result shows that this is indeed the case.

Proposition 1

Suppose that characteristics are chosen optimally as in (6). Then under Assumption 1 (or 2), the constant-quality price ratios defined in (10) (or 11, respectively) provide bounds to the change in the true price of computers services, so that (9) is satisfied.

The proof of Proposition 1 is in the Appendix, and follows from exploiting the concavity of $f(x_t, s_t)$ or $\ln f(x_t, s_t)$. Proposition 1 gives us some confidence in the hedonic adjustment made by BLS, but it obtained by ignoring issues of dynamics. The durability of computers, along with changing software, is introduced in the next section.

⁵ Of course, the usual Laspeyres and Paasche price indexes use last-period and present-period *quantity weights*, respectively. We will not have the quantities available in our dataset, so our definition of these terms in the hedonic context refers to the use of last-period and present-period characteristics. Feenstra (1995) argues that the Laspeyres and Paasche hedonic indexes provides bounds on the change in consumer welfare, analogous to Proposition 1.

3. Dynamic Problem With Changing Software

We now suppose that a computer purchased lasts for a number of periods. The services received in period t for a computer purchased in $t-\tau$ with characteristics $x_{t-\tau}$, is $f(x_{t-\tau}, s_t)$. We adopt the convention that if $f(x_{t-\tau}, s_t)$ ever become negative (*i.e.* the computer is dysfunctional), then we redefine the value of this function at zero. The firm will continue to use this computer so long as $f(x_{t-\tau}, s_t) > 0$. Let \bar{T} be the longest period that any computer is held. Then the buyer solves the dynamic problem:

$$\max_{y_t, n_t, x_t} \sum_{t=\bar{T}}^{\infty} \beta^{t-\bar{T}} G[y_t, \sum_{\tau=0}^{\bar{T}} n_{t-\tau} f(x_{t-\tau}, s_t)] - n_t h_t(x_t) - q_t y_t, \quad (12)$$

where $p_t = h_t(x_t)$ is again the price of a computer, $K_t \equiv \sum_{\tau=0}^{\bar{T}} n_{t-\tau} f(x_{t-\tau}, s_t)$ is the capital stock measured in efficiency units, and the values of n_t and x_t for $t < \bar{T}$ are taken as given. Note that for simplicity we have treated the future state of software s_t as known with perfect foresight.

The first-order conditions for (12) are:

$$G_y(y_t, K_t) = q_t, \quad (13a)$$

$$\sum_{\tau=0}^{\bar{T}} \beta^\tau G_K(y_{t+\tau}, K_{t+\tau}) f(x_t, s_{t+\tau}) = h_t(x_t), \quad (13b)$$

$$\sum_{\tau=0}^{\bar{T}} \beta^\tau G_K(y_{t+\tau}, K_{t+\tau}) n_t f_x(x_t, s_{t+\tau}) = n_t h_t'(x_t), \quad (13c)$$

Dividing (13c) by (13b), we obtain:

$$\frac{\sum_{\tau=0}^{\bar{T}} \beta^\tau G_K(y_{t+\tau}, K_{t+\tau}) f_x(x_t, s_{t+\tau})}{\sum_{\tau=0}^{\bar{T}} \beta^\tau G_K(y_{t+\tau}, K_{t+\tau}) f(x_t, s_{t+\tau})} = \frac{h_t'(x_t)}{h_t(x_t)} \quad (14)$$

as the first-order condition that defines the choice of characteristics x_t for the computer(s) purchased in period t .

This first-order condition is *forward looking*, in that the firm will be evaluating the marginal productivity of characteristics over the lifetime of the machine. To make this explicit, note that (14) can be rewritten as:

$$\sum_{\tau=0}^{\bar{T}} \theta_{t,\tau} \frac{f_x(x_t, s_{t+\tau})}{f(x_t, s_{t+\tau})} = \frac{h_t'(x_t)}{h_t(x_t)} \quad (15a)$$

$$\text{with the weights, } \theta_{t,\tau} \equiv \frac{\beta^\tau G_K(y_{t+\tau}, K_{t+\tau}) f(x_t, s_{t+\tau})}{\sum_{\tau=0}^{\bar{T}} \beta^\tau G_K(y_{t+\tau}, K_{t+\tau}) f(x_t, s_{t+\tau})}, \text{ where } \sum_{\tau=0}^{\bar{T}} \theta_{\tau,t} = 1. \quad (15b)$$

To simplify this first-order condition, it is convenient to adopt a specific functional form for the production function $f(x_t, s_t)$. In particular, we shall adopt the translog form:

$$\ln f^\ell(x_t, s_t) = a_\ell' x_t + \frac{1}{2} x_t' A x_t + b' s_t + \frac{1}{2} s_t' B s_t + x_t' \Gamma s_t, \quad (16)$$

where $\ell = 1, \dots, L$ denotes different buyers. The parameters (A, b, B, Γ) are constant across buyers, while we allow the marginal benefits to vary across users by the coefficients a_ℓ . To satisfy Assumption 1(b) the matrix A must be negative semi-definite, and we shall consider some restrictions on the matrix Γ below.

Notice that the marginal value of characteristics, f_x^ℓ / f^ℓ , is linear in the software s_t . It follows that by substituting (16) into (15), we can re-write the first-order condition as:

$$\frac{f_x^\ell(x_t, \tilde{s}_t)}{f^\ell(x_t, \tilde{s}_t)} = \frac{h_t'(x_t)}{h_t(x_t)}, \quad (17a)$$

$$\text{where, } \tilde{s}_t \equiv \sum_{\tau=0}^{\bar{T}} \theta_{t,\tau} s_{t+\tau}. \quad (17b)$$

That is, the marginal value of characteristics, evaluated with the *average future state of software* \tilde{s}_t , equals the marginal cost of characteristics today. This first-order condition (17) takes the place of (9), as obtained with a nondurable computer, and shows that the characteristics x_t chosen at time t are *optimal for the future state of software* \tilde{s}_t .

Turning to the hedonic adjustment of computer prices, we continue to assume that the goal of the constant-quality price ratios $P^0(p_{t-1}, p_t, x_{t-1}, x_t)$ and $P^1(p_{t-1}, p_t, x_{t-1}, x_t)$ is to satisfy the inequalities in (9). However, now we need to ask: at what level of software are the efficiency of the new and old computers compared? In (9), we considered the software available at either s_{t-1} or s_t . In the dynamic model, however, the characteristics chosen in (17) are optimal for the future level of software \tilde{s}_t . This can be expected to impact the form of the inequalities in (9), as is confirmed by the following result:

Proposition 2

Suppose that computer services are given by the translog function (16) and characteristics are chosen optimally as in (17). Then under Assumption 1 (or 2), the constant-quality price ratios defined in (10) (or 11, respectively) provide the bounds:

$$P^0(p_{t-1}, p_t, x_{t-1}, x_t) \geq \frac{p_t/f^\ell(x_t, \tilde{s}_t)}{p_{t-1}/f^\ell(x_{t-1}, \tilde{s}_t)}, \quad (18a)$$

and,

$$P^1(p_{t-1}, p_t, x_{t-1}, x_t) \leq \frac{p_t/f^\ell(x_t, \tilde{s}_{t-1})}{p_{t-1}/f^\ell(x_{t-1}, \tilde{s}_{t-1})}. \quad (18b)$$

The constant-quality price ratios P^0 and P^1 appearing on the left of (18) are similar to current BLS practice, while the expressions on the right of (18) are the true change in the price of

computer services. So this result shows that BLS methods provides valid bound to the true change in the price of computer services when period $t-1$ and t machines *are both evaluated at the same average future level of software*. It is worth stressing that these bounds (like those in Proposition 1) are an economic property, and depend on optimizing behavior, *i.e.* on the first-order condition (17) as well as the concavity properties in Assumption 1 or 2. In our empirical work we shall evaluate these bounds by computing the quality-adjusted price ratios on the left of (18) and estimating the production function $f^\ell(x_t, \tilde{s}_t)$ that appears on the right. We will find periods in the sample where the bounds do not hold, which can arise due to non-optimizing behavior or due to mis-measurement of the production function.

Setting aside the empirical validity of the bounds in (18), however, there is another question we can ask about Proposition 2, and that concerns the level of software used to evaluated true ratio of services price on the right of (18). Suppose that instead of evaluating the firms' production functions $f^\ell(x_t, \tilde{s}_t)$ with *future* software as in (18), our goal instead is to evaluate it with *current* software (s_t or s_{t-1}), as on the right of (9). Thus, when the BLS producer price index for computers is used to deflate computer input purchases by firms, we are assuming that the price index accurately reflects cost of purchasing services at the current level of software. Therefore, we are interested in knowing whether BLS procedures—like the construction of the constant-quality price ratios P^0 and P^1 —provide bounds to the true services price ratio at current levels of software.

To answer this question, we introduce additional restrictions on the production function $f^\ell(x_t, s_t)$. In particular, suppose that characteristics and software are *complements* in the sense that $\partial^2 \ln f^\ell / \partial x_t \partial s_t = \Gamma > 0$. To interpret this condition, note that from the first-order condition

(9) we have:

$$\frac{dx_t}{ds_t} = - \left[\frac{\partial^2 \ln f}{\partial x_t^2} \right]^{-1} \left[\frac{\partial^2 \ln f}{\partial x_t \partial s_t} \right] = -A^{-1}\Gamma. \quad (19a)$$

Assuming that $\ln f^\ell(x_t, s_t)$ is strictly concave in x_t (slight stronger than Assumption 1b) so that

A^{-1} is negative definite, with $\Gamma > 0$ we obtain:

$$\Gamma' \frac{dx_t}{ds_t} = -\Gamma' A^{-1}\Gamma \text{ is positive definite.} \quad (19b)$$

Thus, with $\Gamma > 0$ increases in software will tend to increase the characteristics (in the sense that pre-multiplying dx_t/ds_t by the positive matrix Γ yields a positive definite matrix). In this sense, characteristics and software are complements.

With this assumption we have the following extension of Proposition 2:

Corollary

If $\Gamma > 0$, then the bounds in (18) become:

$$P^0(p_{t-1}, p_t, x_{t-1}, x_t) \geq \frac{p_t/f^\ell(x_t, \tilde{s}_t)}{p_{t-1}/f^\ell(x_{t-1}, \tilde{s}_t)} \leq \frac{p_t/f^\ell(x_t, s_t)}{p_{t-1}/f^\ell(x_{t-1}, s_t)}, \quad (20a)$$

and,

$$P^1(p_{t-1}, p_t, x_{t-1}, x_t) \leq \frac{p_t/f^\ell(x_t, \tilde{s}_{t-1})}{p_{t-1}/f^\ell(x_{t-1}, \tilde{s}_{t-1})} \leq \frac{p_t/f^\ell(x_t, s_{t-1})}{p_{t-1}/f^\ell(x_{t-1}, s_{t-1})}. \quad (20b)$$

Conversely, if $\Gamma < 0$ then the second inequalities appearing in (20a) and (20b) are reversed.

The first inequalities appearing in (20) are identical to those in (18), of course, so the new results in the Corollary are the second inequalities. From (20), it is evident that BLS procedures do not provide bounds to the true services price ratio evaluated at *the current (period t-1 or t) fixed level of software*. When $\Gamma > 0$, the constant-quality price ratio P^0 on the left of (20a) is no

longer an upper bound for the change in the price of services on the right. While the price ratio P^1 on the left of (20b) is a lower bound for the change in the price of services, there is nothing that guarantees that this bound will be tight: it could be significantly less than the true change in the prices of computer services. When $\Gamma < 0$ then the second inequalities in (20) are reversed, but with mixed signs within Γ we will generally have to evaluate the production functions $f^\ell(x_t, \tilde{s}_t)$ and $f^\ell(x_t, s_t)$ to know how the true ratio of services price compares at the future and current levels of software.⁶

As noted in the previous section, when we evaluate the quality-adjusted price ratios P^0 and P^1 at the *mean* level of characteristics each year (and corresponding expected price), we obtain the hedonic Laspeyres and Paasche indexes, respectively. These are the bounds on the left of (20), and the Laspeyres index is currently constructed by the BLS. Likewise, we can evaluate the production functions appearing in (20) at the mean level of characteristics each year to obtain indexes of the true price of computer services. As in (20) these indexes can be constructed with either future levels of software (\tilde{s}_{t-1} or \tilde{s}_t) or current levels of software (s_{t-1} or s_t). The precise construction of these indexes is discussed in the next section.

4. Measurement of Computer Price Indexes

Our interest is in estimating Γ and other parameters of the translog services function (16), and use these to construct the true price ratio of computer services, measured with constant software s_{t-1} or s_t as on the right of (20). These time-series of true services prices can then be compared to the constant-quality price ratios P^0 and P^1 in (11). If there is a significant difference

⁶ Note that the second inequalities appearing in (20) are numerical rather than economic properties: once the sign pattern of Γ is established by estimation, if it has mostly positive elements then the true price index with current software should exceed that with future software.

between the change in the true price ratio and these constant-quality price ratios, this will indicate the potential bias in current BLS procedures.

The estimation will rely on a two-step procedure. In the first step we estimate conventional hedonic regressions on desktop PC's from monthly data. The data are from the *PC Data Retail Hardware Monthly Report* and report quantities, average monthly prices and a number of machine characteristics for desktop computers. These data run from August 1997 to December 1999.⁷ We augment these data with desktop computer ads from *PC Magazine*; these data cover April 1999 to September 2001, but have fewer observations per month. Following Benkard and Bajari (2003), for each machine in our data, we collected processor benchmark data from *The CPU Scorecard*. The benchmark data reduce the complex interaction between a processors type and speed to a single index measuring performance. In addition to the processor benchmark, we include the amount of memory, the size of the hard drive and a number of indicator variables in the hedonic regressions. These indicator variables are: whether the computer has a CD player, sound card, Zip drive, network card, LCD monitor and whether it has SCSI hard drives. In addition, we treat the computer's factory installed operating system as a characteristic in the hedonic regressions. The summary statistics for prices and computer characteristics are reported in Table 1, while Table 2 reports the correlation matrix for the variables.

We estimate the semi-log form:

$$\ln p_{it} = \alpha_t + \beta_t' x_{it} + \varepsilon_{it}, \quad i = 1, \dots, N; t = 1, \dots, T, \quad (21)$$

where $i = 1, \dots, N$ denotes individual personal computers (not necessarily available each period), and $t = 1, \dots, T$ denotes months from August 1997 to September 2001. Using these monthly

⁷ We thank Lanier Benkard for providing these data.

hedonic regressions, we construct the change in constant-quality prices from (11) as:

$$\ln P_i^0 = \ln p_{it} - \ln p_{it-1} - \hat{\beta}_t' (x_{it} - x_{it-1}), \quad (22a)$$

$$\ln P_i^1 = \ln p_{it} - \ln p_{it-1} - \hat{\beta}_{t-1}' (x_{it} - x_{it-1}). \quad (22b)$$

As discussed in section 3, we follow Berndt and Rappaport (2001, p. 270) and construct the hedonic Laspeyres and Paasche price indexes by evaluating (22a) and (22b) using the mean value of characteristics over the models available each period, \bar{x}_{t-1} and \bar{x}_t , and the prices

$\ln \bar{p}_t \equiv \hat{\alpha}_t + \hat{\beta}_t' \bar{x}_t$, $t = 1, \dots, T$. Substituting these into (22), we obtain:

$$\text{Change in hedonic Laspeyres index} = [\hat{\alpha}_t - \hat{\alpha}_{t-1} + (\hat{\beta}_t - \hat{\beta}_{t-1})' \bar{x}_{t-1}], \quad (23a)$$

$$\text{Change in hedonic Paasche index} = [\hat{\alpha}_t - \hat{\alpha}_{t-1} + (\hat{\beta}_t - \hat{\beta}_{t-1})' \bar{x}_t]. \quad (23b)$$

The average of these is:

$$\text{Change in hedonic Fisher index} = [\hat{\alpha}_t - \hat{\alpha}_{t-1} + \frac{1}{2}(\hat{\beta}_t - \hat{\beta}_{t-1})' (\bar{x}_t + \bar{x}_{t-1})]. \quad (24)$$

These log changes can be cumulated to obtain the levels of each index.

In the second-step, we make use of actual purchases of desktop PC's by each academic or administrative department at the University of California, Davis, which we index by $\ell = 1, \dots, L$. These data cover July 1997 through September of 2001 and report the machine characteristics for all purchases by each academic and administrative department. Table 3 reports the summary statistics for these data.⁸ The UC Davis data is used to estimate the parameters of the translog production function (16), by using the first-order condition (17). Using (16) and (21), the (17)

⁸ We do not use the purchase price for the UC Davis dataset because it includes peripheral equipment, but we report this price in Table 3 for completeness.

becomes:

$$\hat{\beta}_t = a_\ell + Ax_{i\ell t} + \sum_{\tau=0}^{\bar{T}} \theta_{t,\tau} \Gamma s_{t+\tau} + u_{it}, \quad i = 1, \dots, N; \ell = 1, \dots, L; t = 1, \dots, T. \quad (25)$$

In this notation, $x_{i\ell t}$ denotes a computer of type i purchased by department ℓ in month t . Notice that (25) is a vector of equations, one for each characteristic. From (16b), the weights $\theta_{t,\tau}$ sum to unity over $\tau = 0, 1, \dots, \bar{T}$, where \bar{T} is the numbers of periods that a machine purchased at time t is used. For simplicity in the estimation we set \bar{T} at 3 years.

Having obtained the estimates of A and Γ from (25), we can use these to construct the true change in computer services price, using the software at date $t-1$:

$$\begin{aligned} & \ln \left[\frac{p_{it}/f^\ell(x_{it}, s_{t-1})}{p_{it-1}/f^\ell(x_{it-1}, s_{t-1})} \right] \\ &= \ln p_{it} - (\hat{a}_\ell' x_{it} + \frac{1}{2} x_{it}' \hat{A} x_{it} + x_{it}' \hat{\Gamma} s_{t-1}) \\ & \quad - \ln p_{it-1} + (\hat{a}_\ell' x_{it-1} + \frac{1}{2} x_{it-1}' \hat{A} x_{it-1} + x_{it-1}' \hat{\Gamma} s_{t-1}), \end{aligned} \quad (26)$$

which follows from (16). To simplify (26), we can use the Quadratic Identity of Diewert (1978, pp. 118), which states that the difference between the quadratic functions $\ln f^\ell(x_{it}, s_{it-1})$ and $\ln f^\ell(x_{it-1}, s_{it-1})$ equals:

$$\ln f^\ell(x_{it}, s_{it-1}) - \ln f^\ell(x_{it-1}, s_{it-1}) = \frac{1}{2} \left[\frac{\partial \ln f^\ell}{\partial x_{it}} + \frac{\partial \ln f^\ell}{\partial x_{it-1}} \right] (x_{it} - x_{it-1}), \quad (27)$$

where both derivatives are evaluated at s_{it-1} . Let us denote the estimates of these derivatives by:

$$\hat{\beta}_{t-1}^\ell \equiv \frac{1}{2} \left[\frac{\partial \ln f^\ell}{\partial x_{it}} + \frac{\partial \ln f^\ell}{\partial x_{it-1}} \right] = \hat{a}_\ell + \frac{1}{2} \hat{A}(x_{it} + x_{it-1}) + \hat{\Gamma} s_{it-1}, \quad (28)$$

which follows from the definition of the translog function in (16).

Then substituting (28) and (29) into (26), we can alternatively express the true change in services price, using the firms' production functions, as:

$$\ln \left[\frac{p_{it}/f^\ell(x_{it}, s_{t-1})}{p_{it-1}/f^\ell(x_{it-1}, s_{t-1})} \right] = [\ln p_{it} - \ln p_{it-1} - \hat{\beta}_{t-1}^\ell (x_{it} - x_{it-1})] . \quad (26')$$

This formula applies to a single machine. To obtain an index of the true services price we evaluate (26') at the mean value of characteristics in each period. We also use these mean characteristics to evaluate $\hat{\beta}_{t-1}^\ell$ in (28), and to evaluate the prices $\ln \bar{p}_t \equiv \hat{\alpha}_t + \hat{\beta}_t' \bar{x}_t$, also using the mean a_ℓ across departments. This gives us the index of the true change in services price:

Change in true services price with software s_{t-1}

$$= [\alpha_t + \hat{\beta}_t' \bar{x}_t - \alpha_{t-1} - \hat{\beta}_{t-1}' \bar{x}_{t-1} - \hat{\beta}_{t-1}^\ell (\bar{x}_t - \bar{x}_{t-1})] . \quad (29)$$

Similarly, we can construct the true index using software at date t . Let $\hat{\beta}_t^\ell$ denote exactly the same expression as in (28) but using s_t rather than s_{t-1} .⁹ Then taking the average of (29) evaluated with $\hat{\beta}_{t-1}^\ell$ and $\hat{\beta}_t^\ell$, we obtain a Fisher-type true index:

Change in true services price with current software $\frac{1}{2}(s_{t-1} + s_t)$

$$= [\alpha_t + \hat{\beta}_t' \bar{x}_t - \alpha_{t-1} - \hat{\beta}_{t-1}' \bar{x}_{t-1} - \frac{1}{2}(\hat{\beta}_{t-1}^\ell + \hat{\beta}_t^\ell)' (\bar{x}_t - \bar{x}_{t-1})] . \quad (30)$$

Finally, we can evaluate the firms' production functions using future software \tilde{s}_t , defined

⁹ Again, we evaluate $\hat{\beta}_t^\ell$ at the mean level of characteristics and the mean level of a_ℓ across departments.

in (17b), rather than current software s_t . Let $\tilde{\beta}_{t-1}^\ell$ denote exactly the same expression as in (28) but using \tilde{s}_{t-1} rather than s_{t-1} , while $\tilde{\beta}_t^\ell$ uses \tilde{s}_t . Then the Fisher-type true index using the future levels of software is:

$$\begin{aligned} &\text{Change in true services price with future software } \frac{1}{2}(\tilde{s}_{t-1} + \tilde{s}_t) \\ &= [\alpha_t + \hat{\beta}_{it}' \bar{x}_t - \alpha_{t-1} - \hat{\beta}_{it-1}' \bar{x}_{t-1} - \frac{1}{2}(\tilde{\beta}_{t-1}^\ell + \tilde{\beta}_t^\ell)'(\bar{x}_t - \bar{x}_{t-1})]. \end{aligned} \quad (31)$$

We can compare these true service price indexes, obtained from the firms' production functions, to the Laspeyres and Paasche bounds from (23) or the hedonic Fisher index in (24). Notice that the difference between the change in the true services price using current software in (30) and the hedonic Fisher index in (24) can be simplified as:

$$\begin{aligned} &\text{Change in true services price with current software – hedonic Fisher index} \\ &= \sum_{i=1}^N \frac{1}{2} [(\hat{\beta}_{t-1} + \hat{\beta}_t) - (\hat{\beta}_{t-1}^\ell + \hat{\beta}_t^\ell)]'(\bar{x}_t - \bar{x}_{t-1}). \end{aligned} \quad (32)$$

Likewise, the difference between (31) and (24) has the same form as (32), but using $\tilde{\beta}_{t-1}$ and $\tilde{\beta}_t$ rather than $\hat{\beta}_{t-1}$ and $\hat{\beta}_t$. With characteristics growing over time, expression (32) will be *positive* provided that $\frac{1}{2}(\hat{\beta}_{t-1} + \hat{\beta}_t) > \frac{1}{2}(\hat{\beta}_{t-1}^\ell + \hat{\beta}_t^\ell)$. This condition states that the typically estimated hedonic coefficients, $\hat{\beta}_{t-1}$ and $\hat{\beta}_t$, exceed the true value of these characteristics to the user with software at time t-1 and t, $\hat{\beta}_{t-1}^\ell$ and $\hat{\beta}_t^\ell$. This corresponds to our intuition that users may “overbuy” characteristics such as RAM and hard disk space, because they will become more valuable at future states of software.

5. Empirical Results

5.1 Hedonic Regressions

To conserve on space, we do not report each of the coefficients from the monthly hedonic equations, but Table 4 summarizes the coefficients for the included characteristics. The typical R^2 from the hedonic regression is roughly 0.60, but ranges from 0.13 to 0.90. It is important to note that the value of the characteristics captured by indicator variables may not be identified in a given month, since in some months all of the computers in the sample have or do not have the given characteristic. In general, the mean coefficient for each of the characteristics is positive. The exceptions are the indicator variables for whether the computer has a CD or a sound card; the coefficients associated with these characteristics are quite noisy.

Figures 1 through 3 track the monthly hedonic coefficients for the processor speed, RAM and hard drive size variables and provide 95 percent confidence intervals for the point estimates. We focus on these three characteristics because their coefficients are identified in every month and they are the main determinants of a computer's price.¹⁰ Each of the coefficients display a general downward trend as characteristic prices fell during our sample; a regression of the coefficient on a linear time confirms this and yields negative and significant coefficient for each of the variables. The processor speed coefficient displays a sharp increase between May 1999 and June 1999. We have verified with cpuscorecard.com that this is not due to a change in the benchmark definition. In addition, the hard drive coefficient exhibits a sharp decline between August 1997 and August 1998. Finally, the processor speed and RAM coefficients display a reduction in precision later in the sample. This is due to smaller sample sizes for the *PC*

¹⁰ These three variables alone account for, on average, over 80 percent of the *explained* variation from the hedonic regressions.

Magazine price data compared to the *PC Data Retail Hardware Monthly Report* data.¹¹

5.2 Departmental Production Functions

A key component for the decision process of the consumer or firm is the expected software quality; admittedly, this is difficult to quantify. We discussed a number of potential measures of quality with software programmers and settled on the *recommended hard drive space* for both Microsoft Windows and Microsoft Word. Increases in software require additional hard-drive capacity and will be reflected in the recommended hard drive capacities of the programs.¹² This measure displays a general upward trend as both Office and Windows have added features. As with the dependent variable in the second stage, our software quality measure exhibits time series variation and is identified from the change in the average characteristics of purchased computers over time.

Estimating (25) requires including the *expected* movements in software quality over the lifetime of the machine. Rather than modeling the primitives of these expectations, we include the actual movements of our software quality measure. To capture the uncertainty associated with these expectations, we assume an artificially high discount rate, 2% per month, in (17b). This implies that departments place more weight on the expectations of software quality during the earlier months of a computer's lifetime. The high discount rate suggests they do so because there is less uncertainty regarding quality early in the lifetime of the machine.

We focus on the first order condition (25) for three characteristics: processor speed, hard drive size and RAM. We estimate the three first order conditions simultaneously via least

¹¹ In our second stage regressions, we report heteroskedastic consistent standard errors to account for this.

¹² The required memory was also a candidate. However, the programmers that we spoke to were under the impression that software engineers now "waste" more memory than in previous periods, whereas this is not the case for hard-drive space. Including the recommended RAM levels does not qualitatively change the results.

squares and impose symmetry in the matrix A of the production function.¹³ The results from the second stage regressions are reported in Table 5. The results with respect to the quadratic portion of the production function (the A matrix) are largely consistent with our economic intuition. The diagonal elements are negative suggesting decreasing returns to speed, hard drive capacity and memory. Two of the three off-diagonals are positive, the exception being the cross-derivative of RAM and hard drive capacity.

The results with respect to the software measures are somewhat puzzling. Increases in the hard disk requirements of Microsoft Office tend to *increase* the marginal product of the computer characteristics ($\Gamma_{\text{Office}} > 0$ in two out of three columns of Table 5). This means that Office and the hardware characteristics are complements, in the sense that increases in Office requirements leads to *higher* purchases of speed, RAM, and hard disk size. In other words, departments “over purchase” the characteristics in the current period to compensate for future increases in Office software requirements; this is consistent with our priors. In contrast, the coefficients associated with Windows hard disk requirements tend to be negative ($\Gamma_{\text{Windows}} < 0$ in two out of three columns), which suggests that departments *reduce* their demand for hardware characteristics in response to an increase in Windows hard disk requirements.

One possible explanation for this finding is that departments do not increase the characteristics of a computer purchase in response to expected changes in Windows, but instead shorten the time period in which the computer is held. That is, if departments expect increases in Windows quality in the near future, they reduce the characteristics of the current purchase in expectation of buying a computer when the new version of Windows was released. This is consistent with anecdotal evidence that suggests that consumers do not upgrade Windows as

¹³ Individual tests on the symmetry of the off-diagonals fail to reject equality.

much as Office, instead implicitly “upgrading” by purchasing a new machine, and that quality changes of Windows appear to be more discrete than quality changes of Office. Behavior of this type is outside our model, however, because the time a computer is held is taken as exogenous. An alternative, statistical explanation for $\Gamma_{\text{Windows}} < 0$ is that it is capturing the overall negative trend in the hedonic coefficients, which are the dependent variable in (25).

5.3 Price Indexes

Given the estimates from the second stage, we calculate five price indexes. The first three are the hedonic Laspeyres, Paasche and Fisher, in (23)-(24); the fourth is the true services price with current software $\frac{1}{2}(s_{t-1} + s_t)$, in (28), which we refer to as the “production function, current software;” and the fifth is the true services price with future software $\frac{1}{2}(\tilde{s}_{t-1} + \tilde{s}_t)$, which we refer to as the “production function, future software.” The five price indexes are graphed in Figures 4-7 and display a number of interesting points.

First, the production function method that uses current software levels is consistently higher than the hedonic Fisher index in Figure 4, which is itself bounded quite tightly by the Laspeyres and Paasche indexes. A close examination of that figure shows that the indexes diverge immediately in the first months of our sample, however, so to control for this possibly erratic behavior, in Figure 5 we show the same five indexes but normalized at 100 in May 1998 rather than August 1997. In this case the production function index with current software is still above the hedonic Fisher index, but by the end of the sample the indexes are about equal. This means that the slower decline of the production function index in the early years (1998-1999) is offset by a faster decline of this index in later year (2000-2001), as compared to the hedonic Fisher index.

This difference in the growth rates over the two halves of our sample can also be seen from Figures 6 and 7, where we graph the five indexes from August 1997 – July 1999 and August 1999 – September 2001, respectively. In Figure 6, the faster decline of the hedonic indexes from the production function indexes are readily apparent. This is also seen from the average annual growth rates (AAGR) reported in Table 6, where the hedonic Fisher declines at a 51% AAGR during the first half of the sample, as compared to 14% and 38% for the production function with current and future software, respectively.¹⁴ If the sample for this study had stopped in 1999, the evidence in Figure 6 and Table 6 would have led to the conclusion that the hedonic method (either the Fisher, Laspeyres or Paasche) was substantially overstating the true decline in prices as measured by the production function method with current software. This is consistent with the results of the above Corollary when $\Gamma > 0$, so that software requirements and hardware are complements.¹⁵

However, this overstatement is reversed in the second half of the sample, as shown in Figure 7 and the third row of Table 6, where the hedonic Fisher index falls at a 20% AAGR, as compared to 35% and 38% for the production function with current and future software, respectively. Evidently, both of the production function indexes are being pulled down by factors that do not influence the hedonic indexes. In 2001, the AAGR of the production function index with future software is actually above that with current software, which from the above Corollary, can occur if and only if some of the Γ coefficients are negative. Recall that these coefficients are negative for Windows software in two of the three regressions shown in Table 5,

¹⁴ In comparison, Berndt and Rappaport (2001, p. 271) report an AAGR for the hedonic Laspeyres and Paasche indexes of -40% and -42%, respectively, over 1994-1999, for desktop PC's.

¹⁵ The fact that the hedonic indexes are also overstating the decline in the production function index with future software is not consistent with the inequality (18a) in Proposition 2. But notice that if we exclude the first 9 months of the sample, as in Figure 6, then the hedonic indexes closely track the production function index with future software, at least through the first half of the sample.

meaning that the Windows quality is a substitute rather than a complement with hardware characteristics. This puzzling finding seems to affect the production function indexes in the second half of our sample, possibly because of the especially large hard disk requirements of Windows XP and 2003. We have already suggested above that the negative Γ coefficients on Windows may be due to our assumption of a fixed lifetime of a machine (3 years). We conclude by suggesting two other reasons for the slower growth rate of the hedonic indexes in the second half of our sample, as compared to the production function method.

First, we mention again that our sample used to estimate the hedonic regressions is much smaller after 2000, because it is collected from advertisements in *PC Magazine* rather than the *PC Data Retail Hardware Monthly Report* data. The somewhat erratic behavior of the hedonic coefficients after 2000, and the fact that the hedonic indexes actually *increase* in 2001, suggest that a large sample of computer prices and characteristics would be desirable in the second half of our sample. This might affect our results.

Setting aside this statistical concern, there is the conceptual possibility that technological improvements in the production of RAM, hard disk space and speed of machines means that these are no longer the limiting features of a computer. Rather, some computer scientists have suggested that it is the *functionality* of software that limit users, and not the hardware. In this case the slowdown in the fall of the hedonic computer price would be a real phenomena, and the overstatement of the “true” decline in the price of computer services price would be history. Under this scenario, the benefits to users would need to be evaluated using *both* hardware and software. While we have incorporated software in this paper, it has been more as a complement (or substitute) for hardware, but not as an independent feature affecting the functionality of machines. Assessing this aspect of software is one important area for future research.

6. Conclusions

In this paper we show that conventional hedonic methods may overstate the price decline of personal computers, which are treated here as a durable good. Optimizing agents that anticipate increases in software quality will “overbuy” the characteristics of a computer, in the sense that the purchased bundle of characteristics is not fully utilized in the first months or year that a computer is owned. Forward looking buyers equate the marginal benefit of characteristics over the *lifetime* of a machine to the marginal cost at the time of purchase. In this case, hedonic procedures may not provide valid bounds on the true price of computer services at the time when the new machine is purchased, with the concurrent level of software. While we focus on personal computers, our results may also apply to any durable good in which the quality of a complementary product changes over time. For example, if there are switching costs associated with bank accounts, then a consumer will establish a deposit account based on expected changes in the size of banks’ ATM networks, ATMs being a strong complementary product to a deposit account.¹⁶

Our empirical application confirms the theoretical results in the first half of our sample. Using data from UC Davis computer purchase behavior, we find that the hedonic price index constructed with BLS methods typically overstates the fall in computer prices, as compared to the true price index constructed using the users’ estimated production function. Furthermore, we find that the true services prices falls *faster* when it is evaluated with *future* rather than *current* levels of software. However, in the second half of the sample this bias has been ameliorated and even reversed so that, depending on the starting month, the overall decline in the hedonic indexes is not that different from the true indexes that result from estimating the firms’ production

¹⁶ For example, Knittel and Stango (2003) estimate hedonic price regressions for banking services and find that ATM network sizes have a significant impact on prices, as does the compatibility between deposit accounts of one bank and the ATM’s of another.

functions over computer characteristics. This provides some empirical justification for the hedonic methods now used by BLS and BEA, despite the fact that their theoretical properties are called into question when computers are treated as a durable good and software changes.

We have suggested that one area for further research is to directly evaluate the usefulness of software in enhancing consumer benefits of personal computers. White *et al* (2004) provide evidence on the price declines of these software over 1984 to 2000, and note that price declines are generally greater in the later years of their sample. Conversely, Ellison and Fudenberg (2000) argue theoretically that the backwards connectivity of software packages, as well as network effects, can lead firms to develop *too many* upgrades resulting in a loss in social welfare. So a full evaluation of the costs and benefits of software is evidently complicated. But perhaps we have reached a point where more attention needs to be paid to software and its characteristics, and not to the declining costs of extra megahertz or gigabytes, in evaluating the productivity and welfare impact of personal computers.

Appendix

Proof of Proposition 1:

First suppose that Assumption 2 holds. The efficiency of a computer purchased in year t relative to that in year $t-1$, with both using the software in t , is:

$$\begin{aligned} f(x_t, s_t)/f(x_{t-1}, s_t) &\geq [f(x_{t-1}, s_t) + f_x(x_t, s_t)(x_t - x_{t-1})]/f(x_{t-1}, s_t) \\ &= \{f(x_{t-1}, s_t) + [f(x_t, s_t)/h_t(x_t)] \beta_t'(x_t - x_{t-1})\}/f(x_{t-1}, s_t) \end{aligned}$$

where the first line follows from concavity of $f(x_t, s_t)$ with $x_{t-1} \leq x_t$, and the second line from (6) and the definition of $\beta_t \equiv h_t'(x_t)$. Multiplying through by $[h_t(x_t)/f(x_t, s_t)]$ and rearranging terms, we obtain, $[h_t(x_t) - \beta_t'(x_t - x_{t-1})]/f(x_{t-1}, s_t) \geq h_t(x_t)/f(x_t, s_t)$. Then dividing by $[h_{t-1}(x_{t-1})/f(x_{t-1}, s_t)]$ and using the definition of P^0 in (10a), we readily obtain (9a).

The efficiency of a computer purchased in year t relative to $t-1$, using the software in $t-1$, is:

$$\begin{aligned} f(x_t, s_{t-1})/f(x_{t-1}, s_{t-1}) &\leq f(x_t, s_{t-1})/[f(x_t, s_{t-1}) - f_x(x_{t-1}, s_{t-1})(x_t - x_{t-1})] \\ &= f(x_t, s_{t-1})/\{f(x_t, s_{t-1}) - [f(x_{t-1}, s_{t-1})/h_{t-1}(x_{t-1})] \beta_{t-1}'(x_t - x_{t-1})\} \end{aligned}$$

where the first line follows from concavity of f with $x_{t-1} \leq x_t$, and the second line from (6) with $\beta_{t-1} \equiv h_{t-1}'(x_{t-1})$. Inverting this expression, multiplying by $[h_{t-1}(x_{t-1})/f(x_{t-1}, s_{t-1})]$ and rearranging terms, we obtain $[h_{t-1}(x_{t-1}) + \beta_{t-1}'(x_t - x_{t-1})]/f(x_t, s_{t-1}) \geq h_{t-1}(x_{t-1})/f(x_{t-1}, s_{t-1})$. Then dividing by $[h_t(x_{t-1})/f(x_t, s_{t-1})]$, using the definition of P^1 in (10b), and inverting again we readily obtain (9b).

Now suppose that Assumption 2 holds. The log-efficiency of a computer purchased in year t relative to that in year $t-1$, with both using the software in t , is:

$$\ln f(x_t, s_t) - \ln f(x_{t-1}, s_t) \geq \beta_t'(x_t - x_{t-1})$$

which follows from concavity of $\ln f(x_t, s_t)$ with $x_{t-1} \leq x_t$, and (6) with $\beta_t \equiv h_t'(x_t)/h_t(x_t)$. Taking exponents and inverting we obtain $f(x_{t-1}, s_t)/f(x_t, s_t) \leq \exp[-\beta_t'(x_t - x_{t-1})]$. Then it follows from the definition of P^0 in (11a) that (9a) holds.

The log-efficiency of a computer purchased in year t relative to that in year $t-1$, with both using the software in $t-1$, is:

$$\ln f(x_t, s_{t-1}) - \ln f(x_{t-1}, s_{t-1}) \leq \beta_{t-1}'(x_t - x_{t-1}) ,$$

using the concavity of $\ln f(x_t, s_{t-1})$ with $x_{t-1} \leq x_t$, and (6) with $\beta_{t-1} \equiv h_{t-1}'(x_{t-1})/h_{t-1}(x_{t-1})$. Taking exponents and inverting we obtain $f(x_{t-1}, s_{t-1})/f(x_t, s_{t-1}) \geq \exp[-\beta_{t-1}'(x_t - x_{t-1})]$. Then it follows from the definition of P^1 in (11b) that (9b) holds. QED

Proof of Proposition 2:

The proof of this result is identical to that of Proposition 1, where we just replace s_{t-1} with \tilde{s}_{t-1} and s_t with \tilde{s}_t , and make use of (17a) rather than (9).

Proof of the Corollary:

The first inequalities in (20a) and (20b) are identical to those in (18a) and (18b). Taking natural logs of the second inequality in (20a), and multiplying by -1 , we obtain:

$$\ln f(x_t, \tilde{s}_{t-1}) - \ln f(x_{t-1}, \tilde{s}_{t-1}) \geq \ln f(x_t, s_{t-1}) - \ln f(x_{t-1}, s_{t-1}) ,$$

which can be re-written as:

$$\int_{x_{t-1}}^{x_t} [\partial \ln f(z, \tilde{s}_{t-1}) / \partial z - \partial \ln f(z, s_{t-1}) / \partial z] dz \geq 0 .$$

By the mean value theorem, the integrand can be written as $[\partial^2 \ln f(z,s) / \partial z \partial s]'(\tilde{s}_{t-1} - s_{t-1})$ for some value of s between s_{t-1} and \tilde{s}_{t-1} . This expression is non-negative because (i) $\Gamma = \partial^2 \ln f / \partial x_t \partial s_t > 0$ by hypothesis, and (ii) $\tilde{s}_{t-1} \geq s_{t-1}$ from (17b) and because software is growing over time from Assumption 1(b) or 2(b). Therefore, the second inequality in (20a) holds. A similar proof applies to the second inequality in (20b), and to the converse case where $\Gamma = \partial^2 \ln f / \partial x_t \partial s_t < 0$. QED

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Processor Speed Hedonic Coefficients

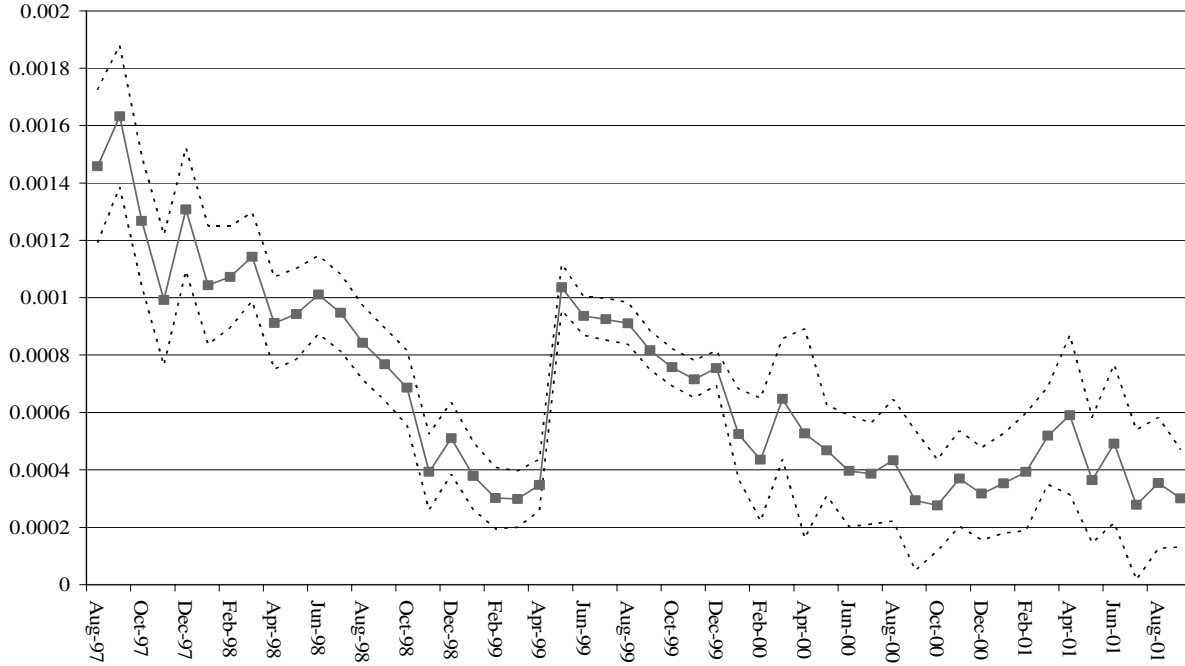
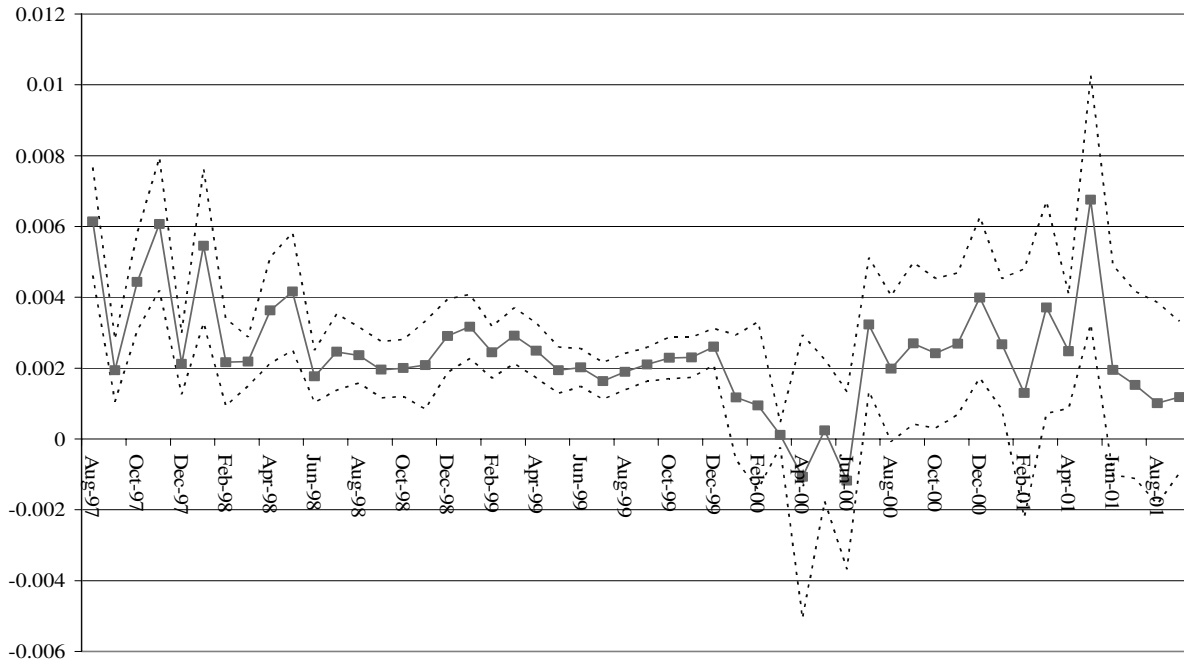


Figure 1: Plot of the Monthly Processor Speed Hedonic Coefficients for Semi-Log Model

RAM Hedonic Coefficients**Figure 2: Plot of the Monthly RAM Hedonic Coefficients for Semi-Log Model**

Hard Drive Size Hedonic Coefficients

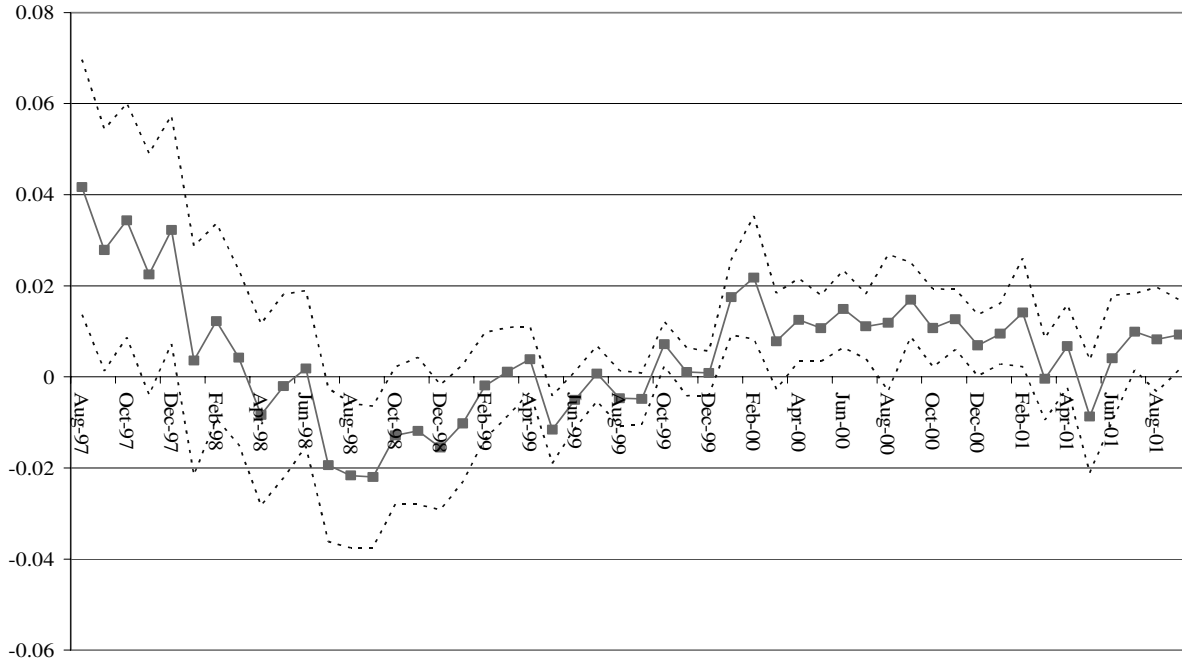


Figure 3: Plot of the Monthly Hard Drive Hedonic Coefficients for Semi-Log Model

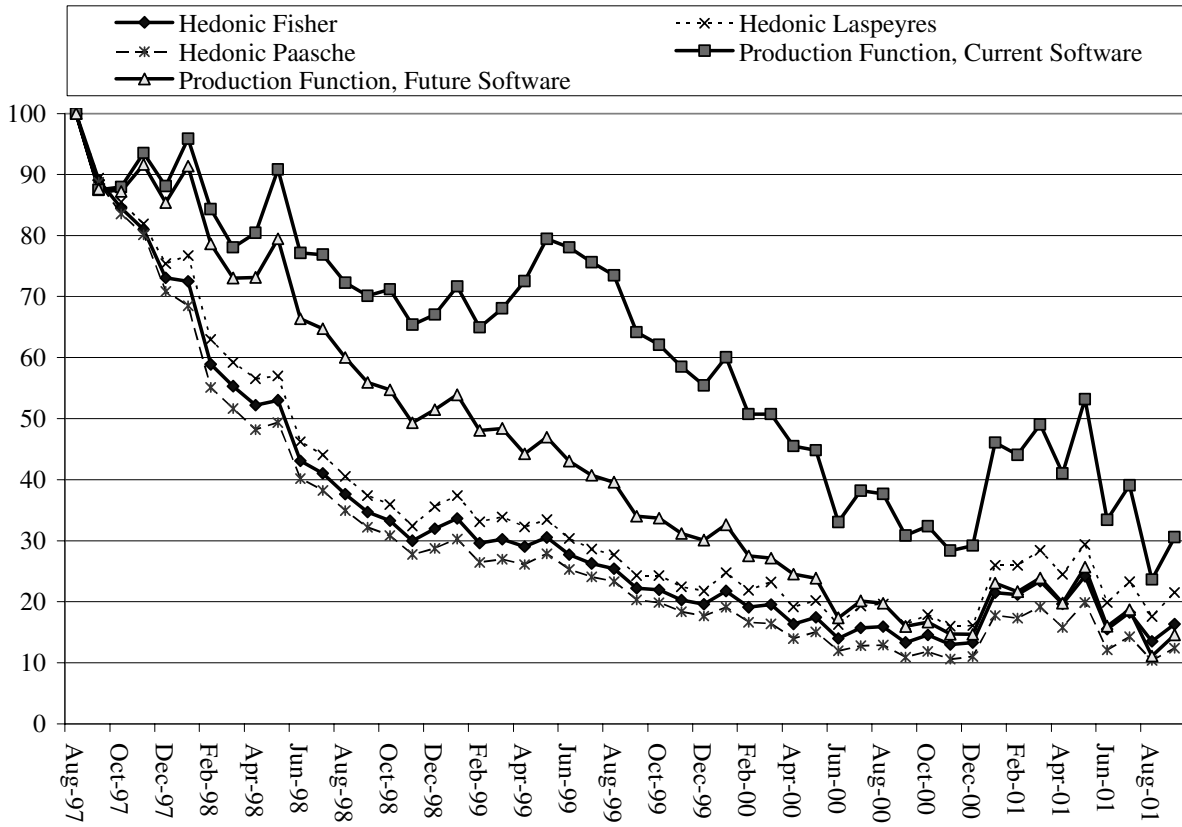


Figure 4: Price Index Calculations

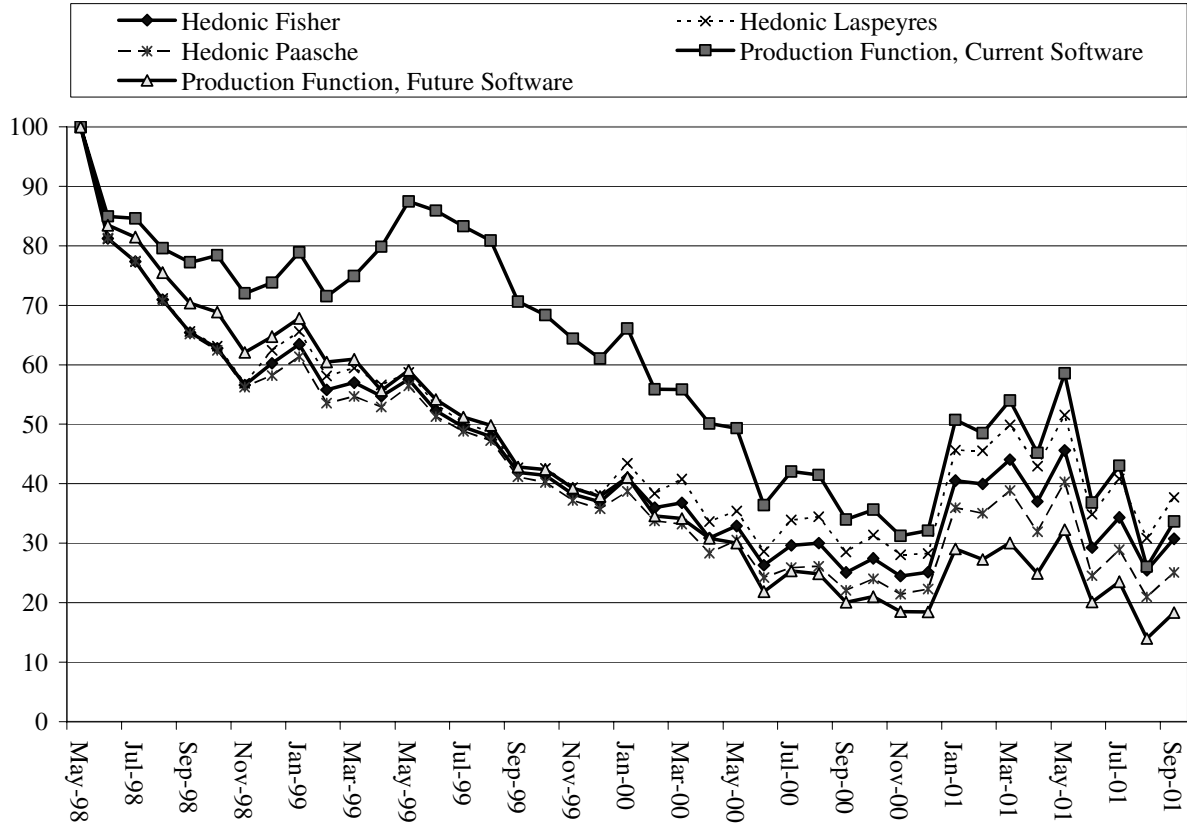


Figure 5: Price Indexes Beginning in May of 1998

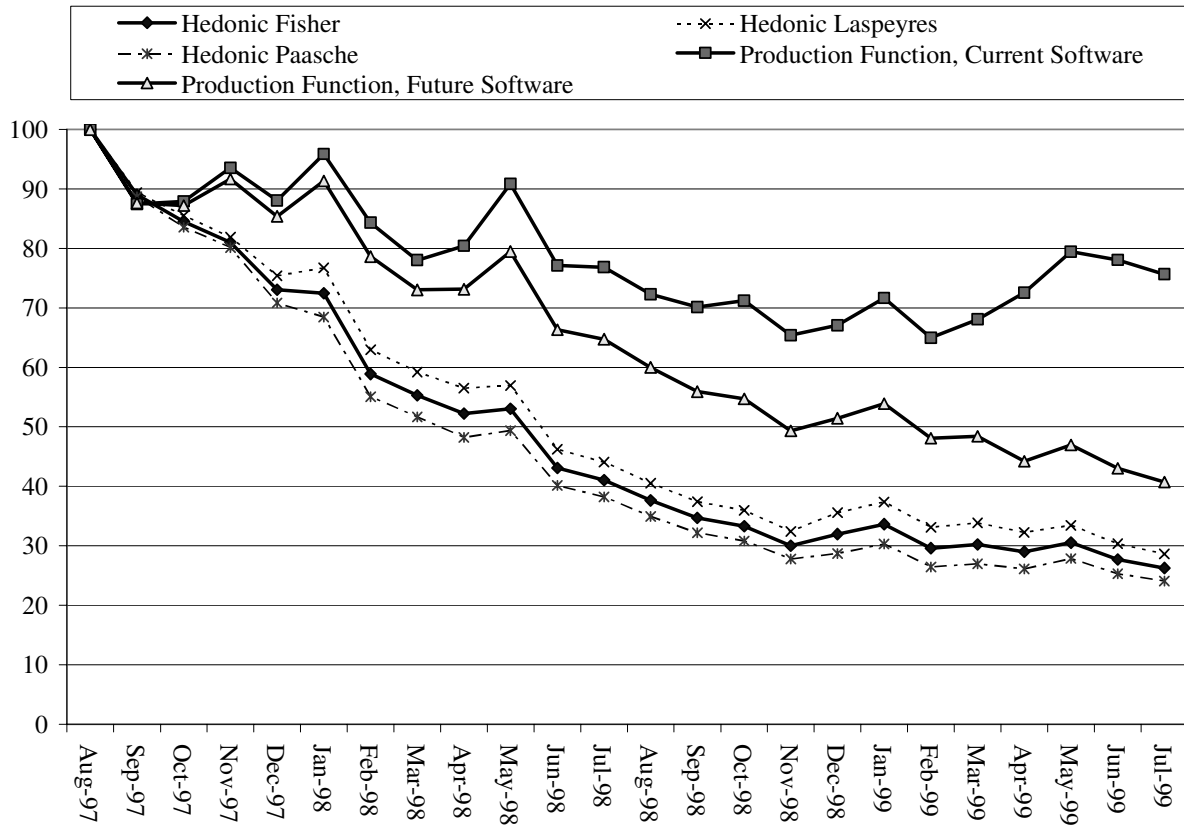


Figure 6: Price Indexes during First Half of the Sample

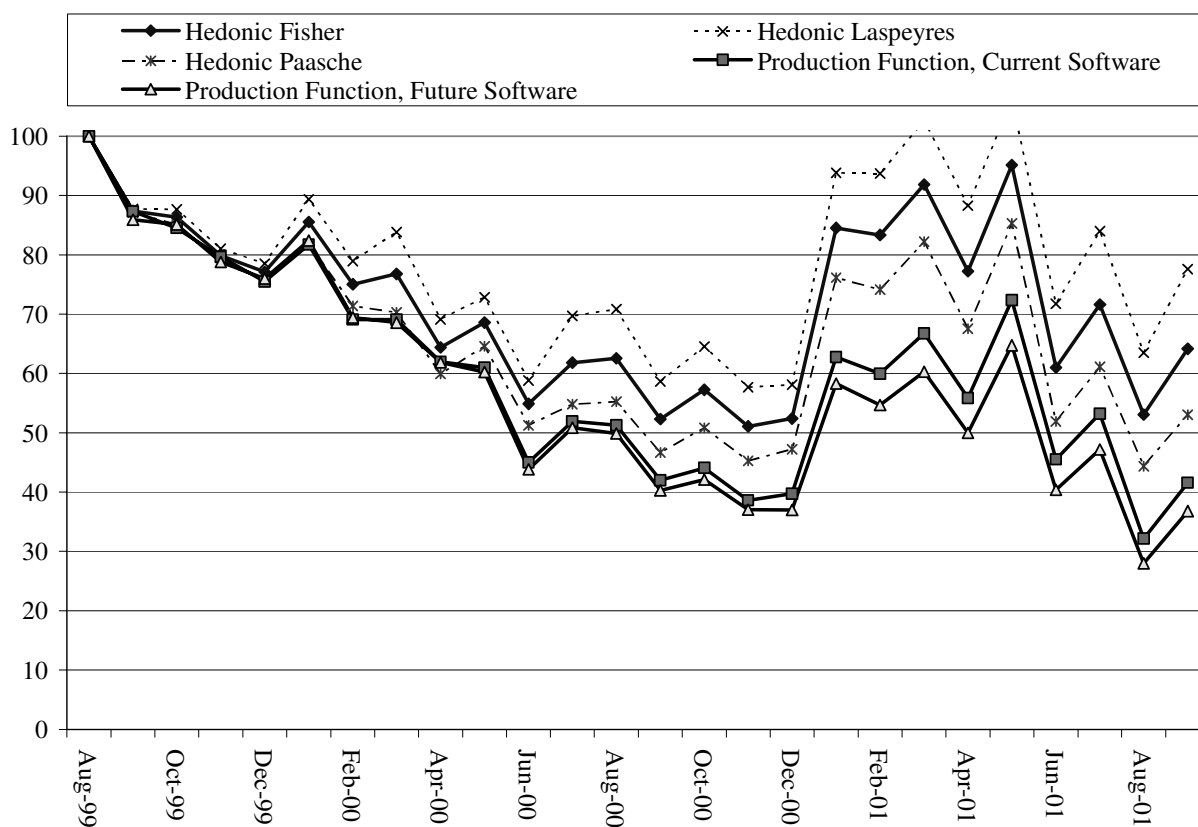


Figure 7: Price Indexes during Second Half of the Sample

Table 1: Aggregate Summary Statistics

Variable	Mean	Median	Std Dev	Min	Max
Price	1197.52	1088.91	5999.20	400	9430
Processor speed	851.971	777	622.98	55	7768
Ram (megabytes)	52.505	32	45.15	0	1128
HD Size (gigabytes)	5.731	4.30	5.88	0	200
Have CD?	0.681	1	—	0	1
SCSI?	0.004	0	—	0	1
Zip Drive?	0.034	0	—	0	1
NIC?	0.215	0	—	0	1
Sound Card?	0.397	0	—	0	1
LCD?	0.063	0	—	0	1

Sample Size: 32,406

Table 2: Correlation Matrix of Computer Characteristics

	Price	Processor speed	RAM	HD Size	Have CD?	SCSI?	Zip Drive?	NIC?	Sound Card?	LCD?
Price	1.00									
Processor speed	0.21	1.00								
Ram (megabytes)	0.31	0.66	1.00							
HD Size (gigabytes)	0.21	0.83	0.66	1.00						
Have CD?	-0.02	-0.01	-0.00	-0.00	1.00					
SCSI?	0.10	0.01	0.00	-0.01	0.03	1.00				
Zip Drive?	0.08	0.10	0.17	0.15	-0.01	-0.01	1.00			
NIC?	0.11	0.25	0.11	0.14	0.03	0.10	-0.02	1.00		
Sound Card?	0.14	0.51	0.29	0.50	-0.01	-0.01	0.05	0.07	1.00	
LCD?	0.07	0.12	0.09	0.14	0.03	0.00	-0.01	0.02	0.10	1.00

Table 3: Aggregate Summary Statistics for UC Davis Purchasing Data

Variable	Mean	Median	Std Dev	Min	Max
Price	2488.72	2344.00	991.34	824	18340
Processor speed	1809.78	1650	858.04	272	4519
Ram (megabytes)	162.874	128	131.36	0	4096
HD Size (gigabytes)	13.878	10	12.877	0	180
Have CD?	0.720	1	—	0	1
SCSI?	0.068	0	—	0	1
Zip Drive?	0.389	0	—	0	1
NIC?	0.704	1	—	0	1
Sound Card?	0.503	1	—	0	1
LCD?	0.182	0	—	0	1

Sample Size: 3,718

Table 4: Summary Statistics for Hedonic Coefficients, Semi-Log Model

Variable	Mean	Std Dev	Min	Max	N
Processor speed	0.0007	0.0003	0.0003	0.0016	50
Ram	0.0024	0.0015	-0.0012	0.0068	50
HD Size	0.0050	0.0138	-0.0219	0.0416	50
Have CD?	-0.0218	0.0746	-0.1973	0.1941	49
SCSI?	0.2239	0.1249	-0.0231	0.5398	29
Zip Drive?	0.0283	0.1047	-0.2288	0.2631	36
NIC?	0.0567	0.0899	-0.2304	0.1905	50
Sound Card?	-0.0384	0.3867	-0.9108	0.4198	29
LCD?	0.3309	0.3623	-0.7544	0.9122	31

Table 5: Second Stage Production Function Estimates

In this table, we report the results from estimating $\beta_t = a_k + Ax_{kt} + \sum \theta_{t,\tau} \Gamma S_{t+\tau} + u_{kt}$ using data from UC Davis departmental computer purchases from July 1997 to September 2001 using the first stage hedonic pricing coefficients for processor speed, RAM and hard-drive size; the parameter estimates represent the parameters of the production function. The θ 's are not separately identifiable from the Γ 's. Instead, we define the θ 's by assuming a monthly interest rate of 2% and that departmental output is constant over the three years. The measure of software quality is the recommended hard-drive space for Microsoft Office and Windows. We assume that each department has an idiosyncratic constant term, a_k , but departments have the same A , θ and Γ .

	β_{Speed}	β_{RAM}	β_{HDSize}
Speed	$-5.92 \times 10^{-8***}$ (1.01×10^{-8})	—	—
RAM	2.06×10^{-8} (2.43×10^{-8})	-1.27×10^{-7} (1.87×10^{-6})	—
HD Size	$2.47 \times 10^{-6***}$ (2.61×10^{-7})	$-2.20 \times 10^{-6*}$ (1.26×10^{-6})	$-6.96 \times 10^{-5***}$ (1.68×10^{-5})
Have CD?	1.06×10^{-6} (7.21×10^{-6})	4.20×10^{-5} (5.28×10^{-5})	$-7.33 \times 10^{-3*}$ (4.28×10^{-3})
SCSI?	-5.93×10^{-6} (1.21×10^{-5})	1.29×10^{-4} (8.90×10^{-5})	-6.78×10^{-4} (7.19×10^{-4})
Zip Drive?	$-1.63 \times 10^{-5**}$ (6.64×10^{-6})	$8.93 \times 10^{-5*}$ (4.87×10^{-6})	$-7.66 \times 10^{-5*}$ (3.95×10^{-5})
NIC?	4.76×10^{-6} (6.87×10^{-6})	9.04×10^{-6} (5.04×10^{-5})	$-1.78 \times 10^{-3***}$ (4.09×10^{-4})
Sound Card?	-6.88×10^{-6} (6.64×10^{-6})	$-1.02 \times 10^{-4**}$ (4.86×10^{-5})	-5.96×10^{-4} (3.95×10^{-4})
LCD?	$5.45 \times 10^{-5***}$ (9.51×10^{-6})	5.76×10^{-5} (6.70×10^{-5})	$1.28 \times 10^{-3**}$ (5.51×10^{-4})
Γ_{Office}	$1.62 \times 10^{-3***}$ (1.51×10^{-4})	$-5.10 \times 10^{-4***}$ (1.27×10^{-4})	8.25×10^{-4} (3.04×10^{-4})
Γ_{Windows}	$-8.35 \times 10^{-5**}$ (4.11×10^{-5})	$4.96 \times 10^{-4***}$ (4.27×10^{-5})	-8.29×10^{-6} (5.04×10^{-6})

N=3931. White's heteroskedastic consistent standard errors in parentheses. * denotes significant at the .10 level, ** significant at the .05 level, and *** significant at the .01 level.

Notes: An F-test marginally rejects symmetry between the processor speed and hard drive equations (p-value equal to 0.126). Equality between the processor speed and RAM equations and the hard drive and RAM equations cannot be rejected (p-values equal to 0.617 and 0.402, respectively). The results with respect to software quality remain qualitatively unchanged if symmetry is not imposed. Including a time trend also left the results qualitatively unchanged.

Table 6: Average Annual Growth Rates of Price Indexes

	Hedonic Fisher index	Production Function, Current Software	Production Function, Future Software
Entire Sample*	-36.4	-25.5	-38.2
First Half	-51.3	-13.6	-38.0
Second Half	-19.9	-34.7	-38.3
1997	-62.4	-32.1	-38.3
1998	-57.6	-24.1	-40.4
1999	-39.3	-17.4	-42.2
2000	-32.5	-48.3	-52.4
2001	30.6	-6.3	0.7

Notes: As in Figures 6 and 7, the first half of the sample is defined as August 1997 to July 1999, while the second half is defined as August 1999 to September 2001.

* If the average annual growth rates are instead computed from May 1998 to September 2001, which excludes the first 9 months of the sample, then we obtain -30.2 for the hedonic Fisher index, -28.2 for the production function with current software, and -40.5 for the production function with future software.