Cyclical Analysis of Time Series:
Selected Procedures
and Computer Programs

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Technical Paper 20
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(Resolution adopted October 25, 1926, and revised February 6, 1933, February 24, 1941, and April 20, 1968)
IN MEMORY OF

SOPHIE SAKOWITZ,
WHO WORKED ALL HER LIFE IN THE FIELD OF
BUSINESS CYCLE ANALYSIS
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