1. Introduction

In the last decade, the Japanese economy has gone through both its strongest expansion of the last twenty years and its most severe recession of the last forty years. During this decade, business fixed investment was unusually volatile, and in a sense documented below seemed to be a dominant factor in both the recent 1986–1991 boom and the post-1991 bust. In this paper we attempt to explain the behavior of business fixed investment in Japan, with extra attention given to the 1986–1994 cycle.

We consider two approaches, one quite briefly, the other in some detail. Both approaches assume a frictionless world in which capital is accumulated to maximize a present value. The two differ in how the present value is measured. The approach presented in brief is based on Tobin’s Q, and uses stock prices to measure the relevant present value. Japanese asset prices zoomed in the late 1980s, and then collapsed. Our efforts to link asset prices and investment with a Q-model were, however, quite unsuccessful, a result consistent with a number of studies including Hayashi (1990) and Mullins and Wadwhani (1989).

Our second approach is a neoclassical, or flexible accelerator, model. Here, we compute the relevant present value ourselves, from data on output and the tax-adjusted cost of capital. Using our model, we con-
clude that business investment in Japan has responded to output and the cost of capital in a sensible way. This holds not only on average during our entire 1961–1994 sample but also in particular during the 1986–1994 period: one does not have to give pride of place to the extraordinary asset price movements to tell a coherent story about the behavior of investment.

Our formulation of the flexible accelerator model takes account of a secular increase in the capital–output ratio that occurred during our sample. Using a one-sector stochastic growth model that includes costs of adjusting capital, we show that this increase can be rationalized as a result of exogenous change in the marginal rate of transformation between investment and consumption.1 According to the model, the secular increase in the capital–output ratio will be matched by a corresponding secular fall in the relative price of investment goods. And we do find in the data that, because of a fall in the relative price of investment goods, the tax-adjusted cost of capital has fallen at roughly the same rate as the capital–output ratio has risen.

Our empirical work estimates a decision rule for capital accumulation that can be derived either from a log-linear approximation of the growth model’s first-order condition for the capital stock, or from a dynamic logarithmic version of the well-known neoclassical model in which the capital stock adjusts partially towards its target level each period. The target level is the (log of) the capital stock that equates the marginal product of capital to the cost of capital; in our Cobb–Douglas specification this is the difference between (the log of) output and (the log of) the cost of capital. We use both our model’s decision rule and unrestricted autoregressions to model capital, in conjunction with unrestricted autoregressions used to model both output and the cost of capital. These estimates are consistent with our model in three ways.

First, the decision rule and the unrestricted autoregressions for the capital stock are quantitatively very similar. Second, because of convex costs of adjusting the capital stock, forward-looking firms will begin to adjust their capital stocks in advance of actual movements in the target level of capital. If firms make forecasts of movements in the target level using information not used by us, this adjustment will show up as Granger causality from capital to the target level. And we do indeed find such causality. Third, our logarithmic model allows capital to have different elasticities with respect to output and the cost of capital.2

1. The logic here is essentially that of Greenwood et al. (1995).
2. This property is shared by the Bischoff (1971) formulation of the neoclassical model, although Bischoff appeals to a putty–clay distinction between old and new capital rather than to the time-series properties of output and the cost of capital.
costs of adjustment, the long- and short-run responses of capital to a shock to one of these variables will be stronger the more persistent is the shock. These responses will be quite small, for example, if there is very little persistence (lots of mean reversion), so that initial movements are typically followed by reversions back to initial levels in output and the cost of capital. In our data, output shocks are persistent and cost of capital shocks are mean-reverting. Correspondingly, we find a large (and of course positive) elasticity of capital with respect to output, and a small (and of course negative) elasticity of capital with respect to the cost of capital.

We use the estimates of the decision rule to determine whether investment was anomalous during 1986–1991 or 1991–1994. In each of the two periods, we decompose unexpected movement in the capital stock into two components. One component is the reaction of the capital stock to surprises in output and the cost of capital; the second component is a residual surprise to the capital stock. In each period, we find that much of the unexpected movement in the capital stock is attributable to output shocks and cost of capital shocks. We conclude that given the 1986–1991 and 1991–1994 movement in output and the cost of capital, the movements in investment that occurred are consistent with historical experience.

The paper has many limitations. We emphasize two here. First, we do not attempt to explain systematically the behavior of any aggregate variable except investment: For the most part we leave uninterpreted what moves output and the cost of capital (productivity? monetary policy?). Similarly, we gloss over many aspects of the Japanese economy—the current crisis in the banking system, for example—that might require close attention if our aim were to provide a detailed analysis of the causes of the boom and bust. Second, because of space and time constraints we were not able to evaluate a model that focuses on credit constraints and balance-sheet effects (e.g., Kiyotaki and Moore, 1994, 1995); it is entirely possible that such a model will provide a more persuasive and more complete explanation of the behavior of aggregates than we provide here. We hope to address both limitations in future research.

The paper is organized as follows. Section 2 describes the behavior of some key variables. Much of the material in this section will be familiar to Japan experts. Section 3 digresses from the main theme of the paper, and discusses the evolution of balance-sheet variables. Section 4 describes our general equilibrium model, Sections 5 and 6 our Q and flexible accelerator models, Section 7 how we constructed the data used in our empirical work, Section 8 the results of the Q-regressions, and Section 9 the results of the flexible accelerator regressions.
2. Behavior of Aggregate Variables

In this section, we describe the recent behavior of some key variables. Our purposes are to describe broad patterns to readers who are unfamiliar with the Japanese economy, and to introduce many of the variables that will be central to our analysis. Section 2.1 considers some basic national income and product account (NIPA) data, Section 2.2 capital stock data, and Section 2.3 asset price data. Section 2.4 summarizes. Unfortunately, because of data limitations, the frequency of the data changes from quarterly (NIPA) to annual (capital stock data) to quarterly and semiannual (asset price data); it may help to note that our subsequent analysis actually uses annual data, typically using annual averages of the higher-frequency underlying data.

Data sources are described in detail in a Data Appendix available from the authors. Briefly, the basic sources are as follows. NIPA data: the Japanese Economic Planning Agency (henceforth, EPA) and the Bank for International Settlements; monetary and financial data; the Bank of Japan, and International Financial Statistics; capital stock and balance sheet data: the EPA. Except when otherwise stated, all data are real (1985 prices). All quarterly data are expressed at annual rates. All data are aggregate, not per capita.

2.1 NIPA DATA

Table 1 presents data on quarterly growth rates for GDP and its major components. As indicated in the means presented for 1961–1973 in column (3) of the first row of Table 1, GDP growth averaged a phenomenal 8.6% before the first OPEC shock. There is no agreed-upon date for the precise end of what has come to be known as the “rapid growth” era. But 1973:4 seems as good a candidate as any. Since then, growth has averaged 3.3% [column (4) in the first row of Table 1]. A comparison of columns (3) and (4) for the other rows indicates that the slowdown in growth affected all the major components of GDP. The dates in columns (5)–(7) are trough (1986:4) and peak (1991:2) dates chosen by the EPA.

To begin motivating our focus on business fixed investment, let us consider in more detail the last expansion and the ongoing contraction. Table 2 divides changes in GDP into various components, for the expansion of 1986:4–1991:2 and for the 15 quarters from 1991:2 to the end of our sample. To read the table, consider column (2). GDP in 1986:4 was 334.2 trillion 1985 yen, or about 3.3 billion dollars at 100 yen/dollar. It increased by 80.5 trillion yen from 1986:4 to 1991:2 [row (2), column (2); Table 1, column (6) indicates that the corresponding compound growth rate is 4.8% per year]. GDP further increased by a paltry 5.9 trillion yen
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<td>(4.9)</td>
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<td>(4.4)</td>
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<td>(9.2)</td>
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<td>(14.1)</td>
<td>(15.0)</td>
<td>(12.4)</td>
<td>(13.2)</td>
<td>(13.4)</td>
<td>(7.4)</td>
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</table>

The data are quarterly, real (1985 yen), seasonally adjusted and expressed at annual rates. Growth rates are computed by averaging log differences beginning with the quarter following the start date; the column (7) figure, for examples, averages log differences in the 15 quarters from 91:3 to 95:1. “Private P and E” is gross private fixed capital formation of plant and equipment; “residential” is the same for residences. The rates of growth for inventory investment are the rates of growth of the level, not the change.
## Table 2  LEVEL AND CHANGE IN NIPA AGGREGATES, MOST RECENT CYCLE

| Date | GDP  | Private Investment | | | | | | | | Net Exports |
|------|------|--------------------|-------------------------------------------------|-----------------------------------------------------------------|-----------------------------------------------------------------|-----------------------------------------------------------------|-----------------------------------------------------------------|-----------------------------------------------------------------|-----------------------------------------------------------------|
|      | (1)  | (2)                | (3) Plant and Equipment | Residential | (5) Inventories | (6) Private Consumption | (7) Government Cons. and Investment | (8) |
| (1)  | 86:4 | 334.2              | 54.7                    | 16.5        | 0.5             | 197.8                    | 57.0                           | 7.6 |
| (2)  | 90.5 | 37.0               | 4.8                     | 2.9         | 38.7            | 3.8                        | -6.7                          |     |
| (3)  | 91:2 | 414.7              | 91.7                    | 21.3        | 3.4             | 236.5                      | 60.9                          | 1.0 |
| (4)  | 95:1 | 420.7              | 72.2                    | 22.0        | -1.4            | 249.1                      | 75.4                          | 0.1 |

Rows (1), (3), and (5) present the value of the indicated national income and product account components, in trillions of real, seasonally adjusted 1985 yen. Rows (2) and (4) present the change in each component, 86:4–91:2 [row (2)] and 91:2–95:1 [row (4)]. The inventory investment figure in column (5) includes inventory investment by the government. The sum of components may not add to the total because of rounding.
between 1991:2 and 1995:1. Columns (3)–(8) give the corresponding figures for some major components of GDP.

It may be seen that the changes in GDP went hand in hand with large changes in private plant and equipment investment. While such investment has averaged about 15% of GDP in the sample, its increase was nearly half (37.0/80.5) that of the increase in GDP from 1986:4 to 1991:2, and its 19.5-trillion-yen decline from 1991:2 to 1995:1 was associated with a minuscule increase in GDP.³

Complementary evidence on this comovement of GDP and private plant and equipment investment is provided by the predictions of a VAR, which we briefly summarize here. Using a VAR in the arithmetic differences in the six variables listed in columns (3)–(8) in Table 2, we decomposed movements in GDP and in each of the six variables into expected and unexpected components, for the last cycle. Unsurprisingly, we found that GDP growth from 1986:4 to 1991:2 was substantially higher than was expected in 1986:4, and that GDP growth from 1991:2 to 1995:1 was much lower than was expected in 1991:2. We also found that when we broke the GDP forecast error into errors in forecasting each of the six components in Table 2, the dominant element was the forecast error in plant and equipment investment.

We conclude that a first step in understanding the recent behavior of the Japanese economy is to understand private plant and equipment investment, and that is the focus of our paper.

2.2 CAPITAL STOCK DATA

Our capital stock data are those for nonfinancial corporations. We focus on this sector because its investment is largely congruent with that of private investment in plant and equipment. In 1993, for example, over 80% of such investment was accounted for by corporations, and, conversely, over 80% of total investment by nonfinancial corporations consisted of investment in plant and equipment. Our capital stock data also reflect some public and corporate residential investment (about 5% of total sectoral investment in 1993) and some plant and equipment investment by public corporations such as NTT, the telephone company (about 10% in 1993).⁴

³. That the change in inventory investment is a small part of the change in GDP is consistent with previous downturns in Japan. See West (1992). That fluctuations in plant and equipment investment have been central to the last cycle is noted in, for example, Economic Planning Agency (1994, p. 44).

⁴. Many small firms are included in this sector. According to the 1991 Establishment Census of Japan, the total employment of nonfinancial corporations is 41.8 million. Of this total, 13.5 million work at corporations of a single establishment, with no branch offices, of fewer than 100 employed, and only 4.6 million work at corporations whose
This capital stock includes both structures and equipment; unfortunately, these two types of capital cannot be distinguished as is conventionally done in U.S. investment studies. The corresponding output variable used in our analysis is what the EPA calls “output of industry.” Here, “industry” includes, for example, production of services and residential construction: apart from statistical discrepancy, industry output = GDP – (output of government) – (output of nonprofit institutions serving households). The capital stock and output of industry are only available annually. Some details on conversion to 1985 prices are given in a footnote.5

Figure 1a plots the growth rate of capital stock, with shaded areas depicting contractions.6 Once again, growth rates were astounding before 1973. The effects on capital growth of the 1986–1991 boom and the 1992–1994 collapse in plant and equipment investment are apparent in the picture: capital growth was at a post-1974 high during the boom, a 1961–1994 low during the collapse. Figure 1b and c plot the levels and growth rates of output of industry and of GDP. Figure 1b indicates that industry output comprises the bulk of GDP, Figure 1c that the two move closely together but that industry output is more volatile.

Figure 1d plots the capital–output ratio. A steep upward trend is apparent. Growth in this ratio was particularly rapid in 1969–1975, but it appears that more or less steady growth has continued since then. We document below that there is a corresponding downward trend in the ratio of the deflator for private investment in plant and equipment to that of the output deflator (see Section 7 and Figure 4).7 These trends are

stocks are publicly traded. Therefore, our study may complement panel studies of investment by publicly traded corporations.

5. The EPA provides the data in 1985 yen for 1969–1993. For 1961–1968 we constructed a real capital-stock figure from the nominal figure and the deflator for private investment in plant and equipment, and we constructed a real output series from nominal and 1980-based data by assuming that inflation rates in 1985 prices were the same as those in 1980 prices. The base year for the real 1994 capital stock and output of industry was 1990; we converted to 1985 prices by assuming real growth rates were the same in 1990 and 1985 prices.

6. For quarterly data, we use turning points defined by the EPA [although EPA documents sometimes seem ambiguous, for example as to whether the most recent peak is 1991:1 (EPA, 1994, p. 418) or 1991:2 (EPA, 1994, p. 46)]. To define annual turning points, we looked at GDP growth in the years surrounding the EPA dates. For example, for the most recent cycle, the rate of GDP growth in 1985, 1986, and 1987 was 5.0, 2.6, and 4.1; for 1990, 1991, and 1992 the figures were 4.8, 4.2, and 1.0. This suggested a 1986 trough and a 1991 peak. After completing this paper, we found that the EPA (1996, p. 1) has defined 1993:4 to be a trough, a choice not obviously in accord with the annual growth rates of GDP plotted in Figure 1c.

7. Fumio Hayashi has informed us that there is some evidence that the published figure for the capital stock in 1970 is too low. When combined with reasonable measures of gross investment, this will cause overstatement of the growth of the capital stock, particularly around 1970. We have not, however, been able to construct an alternative measure.
Figure 1

(a) Growth rate of real capital stock, nonfinancial corporations

(b) Output of industry (solid) and GDP (dashed) (trillion 1985 yen)

(c) Growth rates of output of industry (solid) and GDP (dashed)

(d) Ratio of capital stock to output of industry

not due to the particular definition of output or capital. The trend in the capital–output ratio, and in the ratio of a capital to output-goods deflator, is equally evident when (for example) capital includes inventories and fixed capital of not just the nonfinancial corporate sector but that for the whole economy, and when output is GDP (not depicted in Figure 1). Approximate constancy of the capital–output ratio is one of the basic stylized facts of growth theory (Kaldor, 1963; Simon, 1990). Perhaps the Japanese growth in the ratio is a transitional phenomenon rationalizable in a familiar way by the Cass–Koopmans–Solow growth model. If so, experience from the United States perhaps suggests that a steady state has been reached, since the aggregate capital–output ratio was about 2.5 by the end of our sample.

Our empirical work does not take a stand on whether or not this
growth is transitional, although our model in Section 4 does point out that an indefinite continuance of the trend is perfectly consistent with balanced growth. Rather, we take the message of Figure 1d to be that a good model of investment must account for the growth in the ratio that has occurred.

2.3 PRICE AND ASSET PRICE DATA

As is well known, Japanese stock and land prices zoomed in the late 1980s, and then collapsed. Figure 2a plots the real (1985 prices) semian- nual (end of quarters 1 and 3) value of the Topix index along with cor- responding dividends multiplied by 10. (The closest U.S. equivalent to the Topix is probably the S and P 500. Throughout this subsection, real values are computed using the GDP deflator.) The “bubble” period is
typically considered to have begun late in 1985, or towards the left end of the next to last shaded area in the graph. A sharp peak occurred at the end of 1989, anticipating the turndown in real activity. In the four years from 1985:3 to 1989:3, the real value of the index increased by a factor of about 2.5, implying an annual rate of appreciation of 23.1%. The subsequent decline left 1995:1 stock prices barely 15% above their 1985:3 value. As may be seen, dividend–price ratios are small by U.S. standards: in 1985:3 they were 1.01%, and had fallen to 0.96% by 1995:1.

Figure 2b plots real, semiannual (end of quarters 1 and 3) land prices, measured as the average price in all urban districts. The runup began at the end of 1986, and the peak occurred in early 1991, so that land prices followed rather than preceded stock prices. From 1986:3 to 1991:1, the index increased by about half, with an implied annual rate of appreciation of about 8.4%. The 1995:1 value of the index is about 20% above the 1986:3 value. It should be noted that the comparable land-price index for the six largest cities in Japan is more volatile, increasing by a factor of more than 2 between 1986:3 and 1991:1, and declining more than 40% since then.

Figure 2c plots end-of-quarter values of a safe nominal interest rate, the call rate. (Among U.S. rates, the closest equivalent is probably the Federal funds rate.) It also plots our measure of the business borrowing rate. For 1992–1994, the latter is the end-of-quarter value of the Bank of Japan series “average contracted interest rates on new loans and discounts, long-term.” For 1961–1991, the borrowing rate was set to the quarterly holding yield of long-term bonds of NTT, the main telephone company, plus 1%. The risk premium of 1% corresponds to the average spread between the series for new loans and discounts and the NTT rate, for the period for which we had data on both series (1992:1 through 1993:1). It may be seen in Figure 2c that an inverted term structure causes the call rate to be above the borrowing rate on occasion.

Interest rates increased during the recent 1986–1991 period of expansion and fell during the ongoing contraction. The increases in the call rate after mid-1989 are commonly thought to have been part of an intentional attempt by the Bank of Japan to “pierce the bubble” in stock and land prices, and to cool down an overheated economy. Similarly, the recent declines seem to have resulted from explicit attempts by the Bank to spark the economy.

The final figure is that of the quarterly real yen-dollar exchange rate. The nominal rate at the end of quarter was deflated by the GDP deflators for Japan and the U.S. (1985 = 100). The real appreciation of the yen in the fixed rate era (1961–1971) reflects the generally higher rate of inflation in Japan.
2.4 SUMMARY

The GDP boom of 1986–1991 and collapse of 1992–1994 went hand in hand with a boom and collapse in business investment in plant and equipment. This motivates us to focus on such investment. Since, in turn, the models we use are formulated in terms of the capital stock, we turn to a capital stock that pretty much moves one to one with such investment, the capital stock of nonfinancial corporations. Because such data are available only annually, the rest of the analysis is annual.

A runup and decline in stock and land prices preceded the real cycle by a year or two, suggesting the possibility of a link running from asset price and balance-sheet movements to business investment. We consider this possibility both with formal tests of Q-theory (Sections 5 and 8) and an informal examination of data patterns that are central to credit constraint models such as Kiyotaki and Moore (1994, 1995) (Section 3).

The pattern in the cost of capital is less evident, at least for 1986–1991. But whatever the pattern, the secular growth in the capital-output ratio suggests a secular fall in the return to capital. So we are compelled to consider the trend as well as the cyclical behavior of the cost of capital. Sections 6 and 9 investigate our version of a flexible accelerator model, in which capital accumulation depends on both output and the cost of capital.


This section digresses from the analysis in the rest of the paper to summarize some basic observations on the movement of balance sheets of nonfinancial corporations during 1961–1994. The aggregate balance-sheet data we discuss are consistent with the NIPA data on saving and investment. The data are available annually, at the end of the year. Most are available only at current prices (an exception is the capital stock). In principle, assets are valued at market rather than book value. We focus on the balance sheet of the nonfinancial incorporated business sector.

We combine some underlying items into four types of assets [items (3.1) to (3.4) below], a liability [item (3.5)], and net worth [item (3.6)]:

(3.1) capital + inventories (denoted $p_{Ki}K_i$, where $p_{Ki} = 1$ in 1985): The sum of net fixed assets (capital) and inventories.

8. Four other sectoral balance sheets are maintained: financial institutions; households, including unincorporated nonfinancial enterprises; nonprofit institutions serving households; general government. Note that in contrast to the U.S. balance-sheet data from the Federal Reserve System, Japan lumps unincorporated enterprises with the household sector.
(3.2) **Land** \((p_{L_t}L_t)\): Nonreproducible tangible assets, excluding improvements in land insofar as such improvements are included in NIPA business fixed investment.

(3.3) **Equity** \((p_{E_t}E_t)\): Holdings of shares of other corporations.

(3.4) **Monetary assets** \((M_t)\): Financial assets apart from equity; this includes, for example, money, debt, and trade credit.

(3.5) **Debt** \((B_t)\): All liabilities, apart from net worth and the value of equity; this includes, for example, debt and trade credit.

(3.6) **Net worth** \((W_t)\): Net worth plus the value of own equity.

Table 3a and b summarize trends and fluctuations of these balance-sheet items. These tables present the real value and growth rate of each

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<th>Table 3</th>
<th>BALANCE SHEETS OF NONFINANCIAL CORPORATIONS, SELECTED YEARS</th>
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<td>Capital+ inventories</td>
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<td>Net worth</td>
<td>81.9</td>
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<td>Total assets</td>
<td>174.6</td>
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</table>

| Capital+ inventories                      | 10.0 | 15.3 | 1.7 | 5.5 | 2.8 | 5.8 | 3.2 | 6.7 |
| Land                                     | 13.6 | 18.5 | -4.6 | 10.7 | 3.9 | 19.3 | -7.4 | 8.4 |
| Equity                                   | 4.9 | 19.0 | -9.8 | 10.6 | 13.8 | 20.2 | -9.0 | 6.7 |
| Monetary assets                          | 14.1 | 11.1 | -1.2 | 5.7 | 5.4 | 6.6 | -1.0 | 6.7 |
| Debts                                    | 13.1 | 11.4 | 0.1 | 4.7 | 5.0 | 7.4 | 1.9 | 7.0 |
| Net worth                                | 10.3 | 18.8 | -3.4 | 9.6 | 4.5 | 14.7 | -6.7 | 7.2 |
| Total assets                             | 11.8 | 15.7 | -1.5 | 7.0 | 4.7 | 11.2 | -2.7 | 7.1 |

**Notes:**
1. Units in panel (a) are trillions of 1985 yen, computed by deflating the nominal data with the GDP deflator. Data are for end of year.
2. The annualized growth rates in panel (b) are computed from the end of the first year to the end of the second year.
balance-sheet item, computed by deflating the supplied nominal values with the GDP deflator (1985=100). Here is how we characterize the dates in the tables, which do not match the official business-cycle dates used in other parts of the paper. The period 1962–1969 is part of the rapid economic growth era of 1950s and 1960s; 1970–1973 and 1986–1990 are periods with asset price inflation; 1974–1977 and 1991–1994 are periods of slow growth, which for brevity we call recessions; 1978–1981 and 1982–1985 are periods of relatively steady growth on average.

To fix the scale of the entries in Table 3, it may help to note that the 1990 real GDP is about 399 trillion yen. So land is large relative to GDP, and is an important share—more than a quarter—of total assets. A second point worth noting is that cross-holdings of equity are an important share—about a tenth—of assets. Because land and equity are important parts of assets, net worth is sensitive to fluctuations in the prices of such assets.9

The figures in Tables 3a and b show three patterns. The most important is that all six balance-sheet items tend to expand together rapidly during booms and tend to shrink (or grow more slowly) during the recessions. This is true not only for the real assets—capital+inventories, land, and equity—but also for the real value of monetary assets and debts. Second, for the 33-year period 1961–1994, capital+inventories, equity, and monetary assets grow at a similar rate, with debt and net worth growing at a slightly higher and land at a distinctly higher rate. Third, movements in equity, land, and net worth tend to be more volatile than those in capital+inventories, monetary assets, and debt.

A natural next question would be how much of these movements is due to net acquisition of these items, and how much to the changes in asset prices relative to the GDP deflator. Net acquisitions of each balance sheet item are measured in the capital finance accounts of the sectors, as shown in Table 4. The change in the market value of an asset or liability may be written as the sum of net acquisitions and revaluation due to changing prices. This revaluation is captured in the reconciliation accounts, with the identity (year-to-year change in an entry on the balance sheet) = (entry on the capital finance account) + (entry on the reconciliation account).10 For example, for capital + inventories $K_t$ and monetary assets $M_t$,

---

9. It should be noted that the reliability of the data on land and equity is suspect. There is some evidence that land values are overstated, and in a way that is not particularly easy to correct (see Ando and Auerbach, 1990). Equity values, on the other, may be understated, since for nontraded equities face value is used. These mismeasurements of land and equity may cause serious problems in constructing Tobin’s Q.

10. While the main function of the reconciliation account is to capture capital gains and losses due to changing prices, the reconciliation account of capital appears to include as well (1) the difference between historical and replacement cost of depreciation (Hayashi (1986)), (2) some measurement error, and (3) the effects of changes in the accounting system.
Table 4

<table>
<thead>
<tr>
<th>Outflow</th>
<th>Inflow</th>
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</thead>
<tbody>
<tr>
<td><strong>Real Transactions</strong></td>
<td></td>
</tr>
<tr>
<td>Gross fixed capital formation + inventory investment</td>
<td>( (I^K_t) ) Savings (including net capital transfers) ( (S_t) )</td>
</tr>
<tr>
<td>Net purchase of land</td>
<td>( (I^T_t) ) Capital consumption ( (D_t) )</td>
</tr>
<tr>
<td>Savings—investment</td>
<td>( (DSI_t) ) (depreciation)</td>
</tr>
<tr>
<td><strong>Financial transactions</strong></td>
<td></td>
</tr>
<tr>
<td>Net acquisition of equity</td>
<td>( (IE_t) ) Net increase in liabilities ( (IB_t) )</td>
</tr>
<tr>
<td>Net acquisition of monetary assets</td>
<td>( (IM_t) ) Net issue of equity ( (IW_t) )</td>
</tr>
</tbody>
</table>

The reconciliation account is defined as

\[
    (3.7) \quad p_t K_t - p_{t-1} K_{t-1} = \frac{IK'_t}{p_t} - \frac{D_t}{p_t} + \left( \frac{RK'_t}{p_t} + \frac{1}{p_t} - \frac{1}{p_{t-1}} \right) \frac{p_{t-1} K'_{t-1}}{p_t},
\]

and

\[
    (3.8) \quad \frac{M_t}{p_t} - \frac{M_{t-1}}{p_{t-1}} = \frac{IM_t}{p_t} + \left( \frac{1}{p_{yt}} - \frac{1}{p_{yt-1}} \right) M_{t-1} + \left[ \frac{RM_t}{p_{yt}} + \left( \frac{1}{p_{yt}} - \frac{1}{p_{yt-1}} \right) M_{t-1} \right],
\]

where \( p_{yt} \) is the expectation of the price level \( p_t \) at date \( t - 1 \). [This expectation was computed from the fitted value of an AR(1) in the inflation rate.]

Equation (3.9) says that the change in the real value of capital + inventories is equal to the sum of the real values of net investment and capital gains. We regard the reconciliation account \( RK'_t \) as a measure of nominal capital gains, and construct real capital gains as \( RK'_t / p_t \) plus a term due to inflation. We apply this decomposition to land and equity. Concerning monetary assets in (3.10), we consider the effect of expected inflation in the second term on the right-hand side as a part of net acquisition of monetary assets; the underlying idea is that expected inflation affects nominal returns on monetary assets. Thus only unexpected inflation and the recon-
ciliation account figure into computation of real capital gains [the last two terms of the right-hand side of (3.10)]. We decompose similarly for debts. Then the change in the real net worth becomes

\[
\frac{W_t - W_{t-1}}{p_{yt}} = \frac{S_t + IW_t + FS_t - DSI_t}{p_{yt}} + \left( \frac{1}{p_{yt}} - \frac{1}{p_{yt-1}} \right) (M_{t-1} - B_{t-1}) \\
+ \frac{RK_t' + RL_t' + RE_t' + RM_t - RB_t}{p_{yt}} + \left( \frac{1}{p_{yt}} - \frac{1}{p_{yt-1}} \right) (p_{Kt-1}K_{t-1}' + p_{Lt-1}L_{t-1}' + p_{Et-1}E_{t-1}) \\
+ \left( \frac{1}{p_{yt}} - \frac{1}{p_{yt}} \right) (M_{t-1} - B_{t-1}).
\]

(3.11)

The first line of the right-hand side is the real value of the net saving and issues of own equity, together with the effects of expected inflation. The second and third lines are real capital gains on capital+inventories, land and equity, and monetary assets net of debts.\footnote{In theory, the difference between saving and investment in real transactions should equal the financial surplus in financial transactions. In the data, however, they do not match because of differences in sources. So we include this gap as a part of net acquisition of net worth.}

Table 5 presents the total real value of net acquisitions and capital gains during each period. (The final period is 1991–1993 rather than 1991–1994 because of some incompatibilities introduced by data revisions made with the release of the 1994 data.) The first point to note is that real capital gains are the major factor in fluctuations of net worth of nonfinancial corporations, rather than net savings and net issue of equities. These capital gains and losses are large even when compared to annual GDP (1990 real GDP=399 trillion). During the 1986–1990 asset price inflation, real net worth increased by about 528 trillion 1985 yen, of which 430 trillion were capital gains and 98 trillion were net savings and net issues of equities. During 1991–1993, net worth dropped by 274 trillion, with a capital loss of 311 trillion partially offset by 37 trillion of net saving and net issues of equity. A particularly important source of real capital gains and losses is fluctuations of land and equity prices (although, as noted above, these prices may be measured poorly). This pattern also holds for the 1970–1973 asset price inflation and the 1974–1977 recession.

A second point to note is that the issue of debt is very procyclical. Debt expansion was particularly notable during the 1970–1973 and 1986–1990 asset price inflations, and contraction (or slow growth) of debt is notable during the 1974–1977 and 1991–1993 recessions. Procyclical movement
Table 5  NET ACQUISITIONS AND REAL CAPITAL GAINS OF NONFINANCIAL CORPORATIONS, SELECTED YEARS

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<tbody>
<tr>
<td>Capital+inv.</td>
<td>na</td>
<td>108.5</td>
<td>89.1</td>
<td>75.7</td>
<td>83.4</td>
<td>85.5</td>
<td>146.5</td>
<td>94.0</td>
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<tr>
<td></td>
<td>cg</td>
<td>-36.0</td>
<td>15.8</td>
<td>-58.9</td>
<td>-22.0</td>
<td>-47.6</td>
<td>-30.6</td>
<td>-42.6</td>
</tr>
<tr>
<td>Land</td>
<td>na</td>
<td>14.5</td>
<td>27.1</td>
<td>5.9</td>
<td>1.0</td>
<td>4.4</td>
<td>36.6</td>
<td>3.5</td>
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</tr>
<tr>
<td></td>
<td>cg</td>
<td>43.9</td>
<td>62.0</td>
<td>-36.9</td>
<td>73.7</td>
<td>33.0</td>
<td>335.4</td>
<td>-161.6</td>
</tr>
<tr>
<td>Equity</td>
<td>na</td>
<td>4.7</td>
<td>3.2</td>
<td>1.9</td>
<td>2.5</td>
<td>1.2</td>
<td>12.8</td>
<td>-4.4</td>
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</tr>
<tr>
<td></td>
<td>cg</td>
<td>3.7</td>
<td>23.4</td>
<td>-19.8</td>
<td>15.0</td>
<td>34.4</td>
<td>120.7</td>
<td>-84.2</td>
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<tr>
<td>Monetary assets</td>
<td>na</td>
<td>108.9</td>
<td>107.0</td>
<td>-12.3</td>
<td>38.0</td>
<td>45.4</td>
<td>167.9</td>
<td>-57.9</td>
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</tr>
<tr>
<td></td>
<td>cg</td>
<td>4.4</td>
<td>-16.2</td>
<td>0.2</td>
<td>23.9</td>
<td>28.6</td>
<td>-20.7</td>
<td>15.4</td>
</tr>
<tr>
<td>Debts</td>
<td>na</td>
<td>161.2</td>
<td>159.4</td>
<td>7.4</td>
<td>57.0</td>
<td>77.7</td>
<td>266.2</td>
<td>-1.7</td>
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</tr>
<tr>
<td></td>
<td>cg</td>
<td>-5.0</td>
<td>-24.9</td>
<td>-5.7</td>
<td>21.4</td>
<td>21.2</td>
<td>-25.0</td>
<td>38.3</td>
</tr>
<tr>
<td>Net worth</td>
<td>na</td>
<td>75.5</td>
<td>67.0</td>
<td>63.8</td>
<td>67.8</td>
<td>58.9</td>
<td>97.6</td>
<td>37.0</td>
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<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>cg</td>
<td>21.0</td>
<td>109.9</td>
<td>-109.7</td>
<td>69.2</td>
<td>27.2</td>
<td>429.8</td>
<td>-311.3</td>
</tr>
</tbody>
</table>

Units are trillions of 1985 yen. “na” is net acquisitions, “cg” is capital gains, computed in accordance with equations (3.9), (3.10), and (3.11). See text for additional details.

of the debt and net worth of nonfinancial firms is consistent with models that emphasize the interaction between credit and investment as a possible propagation mechanism over business cycles. For example, Kiyotaki and Moore (1994) show that small temporary shocks to technology and income distributions may generate large and persistent fluctuations of aggregate output and asset prices through the interaction of collateral value, credit, and investment.

A third point is that, in terms of trend, net saving and net issues of own equity are important sources of upward movement of net worth, along with the upward trend in the relative prices of land and equity. In contrast, capital+inventories generally experiences real capital losses, because, as depicted in Figure 4, the price of capital is falling relative to the GDP deflator. A final point is that nonfinancial corporations bought land and equities net in 1986–1990 and sold equities net in 1991–1993.

4. A Simple General Equilibrium Model

In this section we present a simple general equilibrium model of investment. Our aims are twofold. Following Greenwood, Hercowitz, and Krusell (1995), the first is to link theoretically the upward trend in the capital-output ratio and the downward trend in the ratio of the investment-goods deflator to the output deflator, and to show that such trends in fact are consistent with balanced growth. To illustrate that these theoretical points do not require undue specialization of the
model, we include standard features such as elastic labor supply that do not play a role in the empirical work [and could, but do not, include still more features such as government and foreign sectors; see Greenwood, Hercowitz, and Krusell (1995) or Jones and Manuelli (1994)]. The second aim is to motivate the regressions presented and discussed in subsequent sections. We do, however, forewarn the reader that the model is rather stylized, and we do not constrain the empirical work to fit precisely in the model.

The model is in the vein of the closed-economy one-sector Cass–Koopmans model, but with (exogenous) change in the marginal rate of transformation between investment goods and consumption goods. The production function and basic resource constraints are

\[ Y_t = \tilde{A}_t F(K_t, H_t N_t A_t) = \tilde{A}_t K_t^\theta (H_t N_t A_t)^{1-\theta}, \]  
\[ K_t = (1 - \delta)K_{t-1} + I_t, \]  
\[ Y_t = \zeta_t N_t + P_{It}(I_t + \frac{\phi}{2} X_t^2 K_{t-1}), \]  
\[ X_t = \frac{K_t - G_K K_{t-1}}{K_{t-1}} \equiv \frac{I_t}{K_{t-1}} - G_K + 1 - \delta. \]

In (4.1), the aggregate output \( Y_t \) is a Cobb–Douglas function of the aggregate capital stock \( K_t \), the labor hours per worker \( H_t \), the population \( N_t \), the deterministic labor productivity level \( A_t \), and the stationary stochastic aggregate productivity level \( \tilde{A}_t \). In (4.2), capital accumulation proceeds as usual, with \( \delta \) the constant depreciation rate and \( I_t \) gross investment. In (4.3), output is used for per capita consumption \( \zeta_t \) and investment. \( P_{It} \) is the relative price of investment goods. It equals an exogenous marginal rate of transformation between investment and consumption goods. The adjustment cost \( (\phi/2)X_t^2 K_{t-1} \) is increasing in the deviation of capital growth from its steady-state rate \( G_K \). Baxter and Crucini (1993) and Cogley and Nason (1995) use similar adjustment costs. In (4.4), \( X_t \) is defined as the rate of capital accumulation over its steady-state gross growth rate \( G_K \) (which is solved for below).

Preferences of the representative household are given by the expected discounted utility

\[ E_t \sum_{j=0}^{\infty} \beta^j N_{t+j}[u(\zeta_{t+j}) - B_{t+j}v(H_{t+j})], \]
where \( u(\zeta) = (\zeta^{1-\sigma} - 1)/(1 - \sigma) \), \( v(H) = H^{1+\nu}(1 + \nu) \), and \( B \) is a measure of the disutility of labor.

Let the aggregate productivity \( \tilde{A}_t \) be strictly positive, with mean one, and follow a finite-state stationary Markov process. Let the labor productivity \( A_t \), disutility of labor \( B_t \), and population \( N_t \) grow, and let the relative price of investment goods \( P_{i+1} \) shrink, at constant rates,

\[
A_{t+1} = G_A A_t, \quad B_{t+1} = G_B B_t, \quad N_{t+1} = G_N N_t, \quad P_{i+1} = P_i / G_{PI}, \tag{4.6}
\]

\[
G_B = (G_A(G_{PI})^{\theta(1-\theta)}/(1 - \theta))^{1-\theta} < (\beta G_N)^{-1}. \tag{4.7}
\]

where all \( G_i \geq 1, i = A, B, N, PI \); (4.7) guarantees no trend in labor hours.

It may be shown that the competitive equilibrium exists. The corresponding social planner's problem maximizes the preferences of the representative household, subject to the resource constraint. The first-order conditions for labor hours and investment are given by

\[
\frac{u'(\zeta_t)(1 - \theta) Y_t}{H_t N_t} = B_t v'(H_t), \tag{4.8}
\]

\[
P_i(1 + \phi X_i) = \theta \frac{Y_t}{K_t} + E_t \left( \frac{\beta u'(\zeta_{t+1})}{u'(\zeta_t)} P_{i+1}[1 - \delta + \phi X_{i+1}(G_K + 0.5X_{i+1})] \right). \tag{4.9}
\]

Equation (4.8) equates the marginal product of labor in terms of utility to the marginal disutility of labor. Equation (4.9) equates the marginal cost of investment to the marginal value of an additional unit of capital. The marginal value has three terms: the marginal product of capital, the expected discounted resale value of remaining capital, and the expected marginal saving of adjustment costs the following period.

Let us first consider the growth implications of the model. By examining (4.1) to (4.9), we see that there is no trend in labor hours, and that one plus the growth rate of aggregate capital is given by \( G_K = G_A G_N G_{PI}^{1/\theta} \). Output grows at the rate \( G_A G_N G_{PI}^{1/\theta} \), which is lower than that of aggregate capital by a factor of \( G_{PI} \). It follows that \( K/Y \) is growing at the rate that \( P_i \) is shrinking, thus establishing the desired theoretical link between the two trends observed in the data. Further, define the cost of capital \( C_t \) as the opportunity cost of owning one unit of capital from date \( t \) to date \( t+1 \):

\[
C_t = P_i \left( 1 - \frac{P_{i+1}}{P_i} (1 - \delta) \frac{\beta u'(\zeta_{t+1})}{u'(\zeta_t)} \right), \tag{4.10}
\]
Let $K^*_t = Y_t/C_t$. $K^*_t$ is the target capital stock, which, apart from a proportionality factor $\theta$, would obtain if there were no adjustment costs to investment. Observe that the cost of capital $C_t$ is also shrinking at rate $G_{p_t}$. So the rates of growth actual ($K_t$) and target ($K^*_t$) capital are the same.

We now show that the investment first-order condition (4.9) may be approximated in a computationally convenient fashion, as a dynamic, logarithmic version of a flexible accelerator familiar from Hall and Jorgenson (1967). Let $M_{t+1} = (P_{t+1} / P_t) \left[ \beta u' (\zeta_{t+1}) / u' (\zeta_t) \right]$ be the intertemporal marginal rate of substitution in terms of investment goods. Upon manipulating (4.9), we obtain

$$X_t = \frac{\phi^{-1}C_t}{P_{it}} \left( \frac{\theta Y_t}{C_t K_t} - 1 \right) + E_t[M_{t+1} X_{t+1} (G_K + 0.5 X_{t+1})]. \quad (4.11)$$

Let $M = EM_i$ be the unconditional mean of $M_t$. Using $X_t = -G_K + 1 + \Delta K_t / K_{t-1}$, $C_t / P_{it} = 1 - (1 - \delta)E_t M_{t+1}$, and the definitions of $K^*_t$ and $M$, (4.11) becomes

$$\frac{\Delta K_t}{K_{t-1}} = (G_K - 1)(1 - G_M) + [\phi^{-1} - \phi^{-1}(1 - \delta)M] \left( \frac{\theta K^*_t}{K_t} - 1 \right)$$

$$+ MG_K E_t \frac{\Delta K_{t+1}}{K_t} - u_t, \quad (4.12)$$

where $-u_t = \phi^{-1}(1 - \delta)(M - E_t M_{t+1}) \left[ (\theta K^*_t / K_t) - 1 \right] + G_K E_t [(M_{t+1} - M)(\Delta K_{t+1} / K_t - G_K + 1)] + 0.5 E_t (M_{t+1} X_{t+1}^2)$. Equation (4.12) implies that the growth rate of the capital stock is a linearly increasing function of two variables: the percentage gap between the target and actual capital stocks, and the expected growth rate of the capital stock. Now take the following first-order approximation. [See Abel and Blanchard (1986) for some empirical evidence in an investment context supporting an approximation such as the one about to be used.] Note that all the terms in $u_t$ are the products of random variables that are zero in the nonstochastic steady state, and so will be small when the system is near the steady state. Next, use $(K_t - K_{t-1}) / K_{t-1} \approx \Delta \ln k_t = \Delta K_t / K_t \approx \ln (\theta K^*_t / K_t) - 1 \approx \ln (\theta K^*_t / K_t) \equiv \ln \theta + k^*_t - k_t$; here and throughout the paper, when upper- and lowercase are both used, the lowercase denotes a logarithm. Finally, define $\alpha = \phi/[1 - (1 - \delta)M]$ and $b = MG_K$. We end up with an equation used in the empirical work,
\[ \Delta k_i = \text{constant} + \frac{1}{\alpha} (k_i^* - k_i) + E_i b \Delta k_{t+1} - e_i, \]  
\hspace*{1cm} (4.13) 

where \( e_i \) collects approximation errors and terms assumed to be small.

5. Q-Model

Our empirical work on \( Q \) is conventional. Define \( Q_t \) as the ratio of the marginal value of capital to the price of capital. Given constant returns to scale, such as is assumed in the model in the previous section, the marginal value of capital [defined as the right-hand side of (4.9) in the model of the previous section] is equal to its average value (see Hayashi, 1982). Thus under a standard set of assumptions about stock-market behavior, \( Q_t \) can be measured as Tobin's \( Q \), the ratio of the stock-market valuation of capital to the replacement cost of capital.

Apart from deterministic terms, the regressions actually run were

\[ \frac{I_t}{K_t} = \gamma Q_{t-1} + \text{disturbance}, \]  
\hspace*{1cm} (5.1)

or \( \frac{I_t}{K_t} = \gamma Q_t + \text{disturbance} \), possibly with a correction for first-order serial correlation. Here, \( Q_{t-1} \) is \( Q \) at the end of period \( t - 1 \) (beginning of period \( t \)).

6. Flexible Accelerator Model

In this section we derive the equations used in the main part of our empirical work. The investment first-order condition that we begin with was presented in equation (4.13) of the general equilibrium model of Section 4. But since we do not wish to tie ourselves inflexibly to that model, we make a self-contained presentation here.\(^{12}\) Our dynamic, logarithmic implementation is similar in spirit though not in all detail to that of the familiar Hall–Jorgenson (1967) approach to investment as implemented by Clark (1979) and many other authors. A representative firm minimizes

\[ 0.5 E_t \sum_{j=0}^{\infty} b^j [(k_{t+j}^* - k_{t+j})^2 + \alpha (k_{t+j} - k_{t+j-1})^2 + 2k_{t+j} e_{t+j}], \]  
\hspace*{1cm} (6.1) 

\[ k_t^* = y_t - c_t. \]  
\hspace*{1cm} (6.2)

\(^{12}\) Among the features of our empirical work not suggested by the model: we obtain discount factors from observed rates of return on financial assets rather than intertemporal marginal rates of substitution; we allow multiple rather than single shocks; we have stochastic rather than deterministic trends.
In (6.1), $E_i$ is mathematical expectation, using data as of period $t$, assumed equivalent to linear projections, $0 < b < 1$ is a discount factor, $k_t = \ln K_t$ is the log of the capital stock at the end of period $t$, $k_t^* = \ln K_t^*$ is the log of the target capital stock, which would obtain in a deterministic steady state, $e_t$ is a stationary cost shock observable to the firm but not the econometrician, and $\alpha$ is a positive parameter that reflects the relative importance of costs of being away from $K_t^*$ and of adjustment. In (6.2), $y_t = \ln(\text{output})$ and $c_t = \ln(\text{cost of capital})$; the underlying technology is Cobb–Douglas. Inessential constants have been omitted from (6.1) and (6.2) for clarity.\(^{13}\)

Upon differentiating (6.1) with respect to $k_t$, we obtain equation (4.13), and familiar manipulations lead to

$$k_t = \lambda k_{t-1} + \sum_{j=0}^{\infty} \frac{\lambda}{\alpha} (b\lambda)^j E_t k_{t+j}^* - \sum_{j=0}^{\infty} \frac{\lambda}{\alpha} (b\lambda)^j E_t e_{t+j},$$

whence

$$k_t - k_t^* = \lambda (k_{t-1} - k_{t-1}^*) - \Delta k_t^* + (1 - \lambda) \sum_{j=0}^{\infty} (b\lambda)^j E_t \Delta k_{t+j}^* - \sum_{j=0}^{\infty} (b\lambda)^j E_t e_{t+j}.$$

In (6.3), $0 < \lambda < 1$ is the smaller root of the equation $b\lambda^2 + (1 + \alpha + b\alpha)\lambda + \alpha = 0$, and we derive (6.4) from (6.3) using $\lambda/\alpha = (1 - \lambda)(1 - b\lambda)$. We turn to (6.4) from (6.3) to have a decision rule in terms of a stationary variable: in our data, the percentage deviation of capital from its target value, $k_t - k_t^*$, and the growth rate of target capital, $\Delta k_t^*$, arguably might be well modeled as stationary, possibly around a one-time change in mean in 1974; rapidly growing variables like $k_t$ and $y_t$ will not.

To solve (6.4) for the implied process for $k_t - k_t^*$, let $f_t$ denote a vector of variables that are useful in forecasting future $\Delta k_t^*$'s, including at least two of $\Delta k_t^*$, $\Delta y_t$, and $\Delta c_t$—say $\Delta k_t^*$ and $\Delta c_t$ for concreteness. (Given $\Delta k_t^* = \Delta y_t - \Delta c_t$, and our use of linear models, all results are identical when we use any two of $\Delta k_t^*$, $\Delta y_t$, and $\Delta c_t$.) Let $Z_t = (k_t - k_t^*, f_t)'$. Through most of the work $f_t$ contains no variables in addition to $\Delta k_t^*$ and $\Delta c_t$, and $Z_t$ is $3 \times 1$. We have

$$k_t - k_t^* = \lambda (k_{t-1} - k_{t-1}^*) - E \left[ \sum_{j=0}^{\infty} (b\lambda)^j \Delta k_{t+j}^* | Z_{t-1}, Z_{t-2}, \ldots \right] + \epsilon_{1t}.$$

13. Nickell (1979) also suggested a log-linear flexible accelerator model.
\[
\varepsilon_{lt} = \varepsilon_{lt} - \left( \lambda / \alpha \right) \sum_{j=0}^{\infty} (b \lambda) E_{lt+j} \varepsilon_{lt+j} + \sum_{j=0}^{\infty} (b \lambda) \Delta k^*_{t+j} | Z_{t-j}, Z_{t-2}, \ldots | - E_{lt}[\Delta k^*_{t} - (1 - \lambda) \sum_{j=0}^{\infty} (b \lambda) \Delta k^*_{t+j}].
\]

We assume that lagged \( Z_t \)'s are part of the firm's information set, which means that \( \varepsilon_{lt} \) is uncorrelated with lags of \( Z_t \). We assume as well that \( \varepsilon_t \) is also uncorrelated with these lags, and that \( \varepsilon_t \) is serially uncorrelated. A process for \( Z_t \) consistent with (6.5) is a VAR, say

\[
Z_t = \Pi Z_{t-1} + \varepsilon_t. \tag{6.6}
\]

Equation (6.6) assumes a VAR (1) because that is maintained in most of our empirical work. Generalization to higher-order VARs is routine.

We obtain unrestricted estimates of (6.6) by OLS. We obtain estimates that are restricted to follow the decision rule implied by (6.5) by solving for a \( \Pi \) consistent with (6.5). Details on the procedure are given in Section 7.3 and the Appendix. Given a set of restricted or unrestricted estimates of (6.6), most of the analysis is concerned with the coefficients and residuals in the corresponding unit root VAR in the levels of \( y, c, \) and \( k \) (and, in systems in which \( f_{lt} \) includes a variable in addition to \( \Delta k^* \) and \( \Delta c \), in the level of the additional variable as well). We solve for the short- and long-run elasticities of capital with respect to output and the cost of capital (also known as dynamic multipliers, or impulse response functions). We also compute the 1986 forecast of the 1991 values of \( k_t, k^*_t, y_t, \) and \( c_t \), and similarly the 1991 forecast of the 1994 values. We then use the actual realized values to compute the surprise components, which are simply the differences between forecast and actual. We further obtain an orthogonal decomposition of the surprise components into those due to shocks to the variables in \( f_{lt} \) and a residual, uncorrelated, "\( k_t \) shock," as follows. To do so, we use the VAR in the levels of the variables, and apply a Choleski decomposition with the residual for \( k_t \) ordered last.

7. Data and Estimation Technique for Investment Regressions

The capital stock \( K_t \) (\( k_t = \ln K_t \) for the flexible accelerator) is as described in Section 2 above. Throughout this section, \( P_{lt} \) refers to the deflator for private investment in plant and equipment. Because of a possible change in regime around 1974, all specifications were estimated both on the full sample and on a sample that began in 1974. The full-sample regressions always included a constant and post-1973 dummy, the post-1973 ones a constant.
7.1 Q-REGRESSIONS

Gross investment [the numerator of the left-hand side of (5.1)] was computed by deflating the sectoral nominal gross investment figure by the deflator for private investment in plant and equipment. In most of the regressions reported below,

\[ \text{denominator of } Q = \text{nominal value of net fixed assets}, \]
\[ \text{numerator of } Q = (\text{inventories + land} + \text{cross-holding of equities} + \text{monetary assets}) - \tau_t A_t, \]

where \( \tau_t \) is the effective corporate tax rate, and \( A_t \) is the expected present value of depreciation of past investments. Construction of \( \tau_t \) is discussed in Section 7.2; of \( A_t \) at the end of this section. For 1961–1968, the equity value was constructed working backwards from the 1969 value, using the balance-sheet figures on net acquisitions and the Topix index. All the other items in (7.1) were obtained directly from nominal quantities on the balance sheet. In some regressions we lumped inventories with net fixed assets. In that case, (7.1a) was changed so that nominal inventories were added to net fixed assets, and (7.1b) was changed so that the value of inventories was not subtracted out.

Figure 3a depicts \( I/K \). Figures 3b and c depict \( Q \) when capital is defined as in most of this paper, to consist of net fixed assets, and next when the definition is broadened to include inventories. There is a suggestion of a downward movement in the early part of the sample, which is good news for \( Q \)-theory given the broadly parallel downward movement in \( I/K \). The bad news is that \( Q \) is almost always negative in the basic specification, reflecting a negative numerator in equation (7.1b). One possible problem is that throughout the sample, there is mismeasurement of equities caused by use of book value of equity for nontraded corporations (see Section 3); Hoshi and Kashyap (1990) find that this biases \( Q \) downwards in Japanese data. Another possible problem is mismeasurement of the value of land (see Section 3), overstatement of which would lower the numerator of \( Q \). In our empirical work we do not, however, attempt to correct for such mismeasurement.

Some details on construction of the present value of future depreciation:

---

14. The problem does, however, seem to run deeper than measurement of equity at book rather than market. Hoshi and Kashyap (1990) find that a substantial fraction of firms with equity valued at market have \( Q < 0 \), even after making a careful calculation of the market value of land.
tion deductions \( A_t \), which may be skipped without loss of continuity: A precise definition of \( A_t \) may be found in, e.g., Hayashi (1990). For 1961–1981, we set \( A_t = \) (denominator of \( Q_t \)) \times \[\text{Homma et al.'s (1984, Table 3-1) figure for } A_t\]/[\text{Homma et al.'s (1984, Table 3-1) figure for net fixed assets}]. (Homma et al. use Japanese manufacturing data.) For 1982–1994, we relied on Iwamoto (1989), who shows that under certain assumptions,

\[
A_{t+1} = \frac{1 - a}{a + i_{t+1}} \left[aP_{lt}I_t + (a + i_t)A_t\right], \quad (7.3)
\]

where \( a \) is the percentage depreciation per year, set to 0.09, and \( i_t \) is the safe nominal interest rate, set to the fourth-quarter holding yield of the long-term bonds of NTT, the national telephone company.

7.2 DATA FOR FLEXIBLE ACCELERATOR REGRESSIONS

For \( y_t \), we use the log of the output of industry, as described in Section 2 above. The cost of capital \( c_t \), used in the regressions is the log of a conventionally computed user cost of capital given by
In (7.4), \( \tau_t \) is the effective corporate tax rate, \( z_t \) is the present value of depreciation deductions per dollar of new investment; \( P_{yt} \) is the price of output, measured as the deflator for output of industry, 1985=100; \( E_t[P_{t+1}/P_{yt}] \) is the fitted value of an AR(1) in \( P_{t+1}/P_{yt} \); \( \delta \) is the depreciation rate, set at 0.10, which is approximately the depreciation rate implied by the balance-sheet data; and \( 1 + i_{at} \) is the nominal discount factor for the firm. Some details on \( \tau, z, \) and \( i_a \) are given at the end of this section. It may help to note that \( C_{2t} \) is usually approximated as

\[
C_{2t} \approx i_{at} - \text{expected inflation in } P_{lt} + \delta.
\]

Figure 4a plots the level \( C_t = \exp(c_t) \) of the cost of capital. As suggested by the Figure 4b plot of \( P_{lt}/P_{yt} \) (the ratio of the price of investment goods to that of output), the downward trend in the cost of capital is largely attributable to a secular fall in this ratio. As indicated in Figure 4c and d, there is no trend apparent either in the tax factors in the \( C_{yt} \) term or in the real interest-rate terms collected in \( C_{2t} \). The latter terms do, however, have sharp cyclical effects. The spikes in \( C_{2t} \) and hence in \( C_t \) during 1972–1975 are caused by violent movements in actual and thus in expected inflation: from 1972 through 1975 actual inflation in \( P_{lt} \) was (in percent) 3.0, 12.5, 23.7, 4.9, while expected inflation was 2.6, 8.1, 14.5, 3.7. The downward trend, as well as the volatility around the time of the first OPEC shock, is also found in the cost of capital series presented in Tajika, Hayashi, and Abrai (1987). Figures 4a and 5 show that the blip in \( C \) around 1974–1975 is transmitted to \( k^* \) and thus to \( k^* - k \).

Some details on taxes and the nominal discount factor, which may be skipped without loss of continuity:

7.2.1 Taxes  All tax rates are statutory maximums, and were obtained from various editions of the Ministry of Finance’s Schematic Explanation of Japanese Taxes. Let \( \tau_c \) be the corporate tax rate on retained earnings, \( \tau_g \) the

15. A number of studies since Clark (1979) have computed expected inflation from output rather than capital-goods prices. The capital-goods inflation rate is appropriate not only in the model in Section 4, but, more generally, in “putty-putty” models in which firms are viewed as renting capital period by period at the market price of capital. See Ando et al. (1974).
enterprise tax rate, \( \tau_1 \) the local tax rate. Let \( 1 + i_{st} \) be a safe nominal interest rate, computed as the annual average of monthly call rates. Then 
\[
\tau = [\tau_c(1 + \tau_1) + \tau_{g}][(1 + i_{st})/(1 + i_{st} + \tau_{g})];
\]
the second factor in brackets allows for the deductibility of the enterprise tax against next period’s income (see Hayashi, 1990). Because of the absence of data on the split between structures and machinery, the present value of depreciation deductions \((z_t)\) was fixed at 0.562 for all \( t \); 0.562 is the 1961–1981 average of the \( \{z_t\} \) series given in Hayashi (1990, p. 308), who studies manufacturing firms.

This tax measure ignores a host of what we hope are minor complications. Readers familiar with the U.S. investment literature may wonder at the absence of reference to the investment tax credits; Hayashi (1990), however, states that these are of small magnitude in Japan. We also
ignore, for example, special tax treatment of dividends received by corporations, the existence of certain tax-free reserves, special capital gains taxes on land, and periods of "special depreciation."

7.2.2 Nominal Discount Factor We set \( i_{at} = (1 - \omega)(\text{expected net nominal return on equity from } t \text{ to } t + 1) + \omega(1 - \tau_c)(\text{net nominal rate on debt}) \), where \( \omega \) is the share of debt financing. We set \( \omega = 0.6 \), which is roughly consistent with the average debt/equity and net-worth ratios for nonfinancial corporations for the whole sample (see Ando and Auerbach, 1990). The expected return on equity was assumed to be the nominal return on safe government debt plus a constant risk premium. The annual average of call rates was used for the safe nominal rate. The constant risk premium was set at 0.05, which is the average annualized excess return of Topix over the call rate, using either monthly data 1970–1995 or semiannual (March and September) data 1961–1995. The nominal rate on debt was set equal to the annual average of the business borrowing rate described in Section 2 and plotted in Figure 2c.

A small amount of experimentation at a preliminary stage of the research for this paper suggested that the results would not be sensitive to the assumed risk premium for equity, the assumed depreciation rate, and the use of annual averages rather than end-of-year values for interest rates.

7.3 ESTIMATION TECHNIQUE FOR FLEXIBLE ACCELERATOR REGRESSIONS

In unrestricted regressions, estimates were obtained by OLS, and the usual OLS standard errors are reported. For restricted regressions, estimates of the \( k_t - k_t^\ast \) equation were obtained with a numerical technique, and inference conducted using a bootstrap technique. Details on both estimation and inference are in the Appendix. With respect to estimation, we merely note here:
1. We did not estimate but instead imposed an annual discount factor, setting \( b = 0.95 \).\(^{16}\)

2. To obtain restricted estimates, we used a two-step procedure that under conventional econometric assumptions is consistent but not efficient. In a first step, we obtained consistent estimates of \( \alpha \) and \( \lambda \) from the unrestricted estimates. In a second step, we used an iterative procedure to solve for a \( k_t - k_t^* \) process compatible with these values and with the unrestricted coefficients in the equations for \( f_t \). [Recall that \( f_t \) is the vector of variables used to forecast future \( \Delta k_t^* \)'s, \( f_t = (\Delta k_t^*, \Delta c_t)' \) in our basic specification.] This iterative procedure takes proper account of the Granger causality from \( k - k^* \) to \( \Delta k^* \). (Without such causality, one could of course directly compute, without iterating, a restricted \( k - k^* \) process.) Note that since restricted and unrestricted coefficients in the \( \Delta k^* \) and \( \Delta c \) equations are the same, so, too, are the coefficients and residuals in the equations for the levels of \( y \) and \( c \).

3. We leave unrestricted all coefficients on deterministic terms.

With respect to our bootstrap inference: 95% confidence intervals for regression parameters and impulse responses were obtained by sorting 1000 sets of estimates from lowest to highest and dropping the smallest and largest 25. A bootstrap \( p \)-value of a test of the cross-equation restrictions was obtained by comparing the actual value of the test statistic with the 1000 values computed in the bootstrap. The test statistic was the difference between the logarithms of the determinants of the variance–covariance matrices of the restricted and unrestricted residuals.

8. Results for Q-Regressions

Table 6 presents the results of the regression (5.1). Columns (1) and (3) report results when beginning of period \( Q \) is used, for both the whole and the post-1973 sample. Since the diagnostics reported at the foot of the table suggested substantial serial correlation, estimates with a correction for first-order serial correlation are reported in columns 2 and 4. The results are not encouraging. In addition to substantial serial correlation, the coefficient on \( Q \) is generally wrong-signed and is far from significant at conventional levels in the one specification in which it is correctly signed [column (2)]. The regressions with end-of-period \( Q \) [columns (5) and (6)] and when capital is defined to include inventories [columns (7) and (8)] are equally unsupportive.

\(^{16}\) The growth model of Section 4 suggests computing \( b \) from the average value of \( 1 - C_t \) \([C_t \text{ is defined in (7.4)}]\) and the growth rate of the capital stock. If we do so using the data described in the Section 7, however, we get \( b = 1.03 \).
Table 6: REGRESSION RESULTS, Q-MODEL

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<tr>
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<tr>
<td>$Q_{t-1}$</td>
<td>-0.008</td>
<td>0.008</td>
<td>-0.077</td>
<td>-0.024</td>
<td>-0.019</td>
<td>-0.067</td>
<td>-0.004</td>
<td>0.016</td>
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<td></td>
<td>(0.035)</td>
<td>(0.025)</td>
<td>(0.010)</td>
<td>(0.019)</td>
<td>(0.032)</td>
<td>(0.023)</td>
<td>(0.039)</td>
<td>(0.029)</td>
</tr>
<tr>
<td>$Q_t$</td>
<td></td>
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<td>-0.19</td>
<td>-0.067</td>
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<td></td>
<td>(0.026)</td>
<td>(0.019)</td>
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<tr>
<td>$Q_{t-1}$ with</td>
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<td></td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>inventories</td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Constant</td>
<td>0.196</td>
<td>0.139</td>
<td>0.195</td>
<td>0.155</td>
<td>0.251</td>
<td>0.143</td>
<td>0.254</td>
<td>0.199</td>
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<td>(0.036)</td>
<td>(0.004)</td>
<td>(0.010)</td>
<td>(0.008)</td>
<td>(0.008)</td>
<td>(0.008)</td>
<td>(0.015)</td>
<td>(0.032)</td>
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<tr>
<td>post-1973 dummy</td>
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<td>-0.027</td>
<td>-0.090</td>
<td>-0.087</td>
<td>-0.028</td>
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<tr>
<td></td>
<td>(0.016)</td>
<td>(0.016)</td>
<td>(0.014)</td>
<td>(0.019)</td>
<td>(0.019)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\rho$</td>
<td></td>
<td></td>
<td></td>
<td>0.911</td>
<td>0.666</td>
<td>0.905</td>
<td>0.905</td>
<td>0.905</td>
</tr>
<tr>
<td></td>
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<td></td>
<td></td>
<td>(0.080)</td>
<td>(0.161)</td>
<td>(0.084)</td>
<td>(0.084)</td>
<td>(0.084)</td>
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<tr>
<td>$R^2$</td>
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<td>0.900</td>
<td>0.336</td>
<td>0.573</td>
<td>0.797</td>
<td>0.257</td>
<td>0.784</td>
<td>0.901</td>
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<tr>
<td>S.e.e.</td>
<td>0.022</td>
<td>0.015</td>
<td>0.013</td>
<td>0.010</td>
<td>0.022</td>
<td>0.013</td>
<td>0.022</td>
<td>0.015</td>
</tr>
<tr>
<td>Q-statistic</td>
<td>24.31</td>
<td>15.15</td>
<td>6.81</td>
<td>10.70</td>
<td>25.33</td>
<td>5.45</td>
<td>24.82</td>
<td>14.80</td>
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<td>[0.03]</td>
<td>[0.24]</td>
<td>[0.03]</td>
<td>[0.00]</td>
<td>[0.36]</td>
<td>[0.00]</td>
<td>[0.04]</td>
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<td>Durbin–Watson</td>
<td>0.73</td>
<td>1.19</td>
<td>1.08</td>
<td>0.74</td>
<td>0.73</td>
<td>0.89</td>
<td>0.72</td>
<td>1.19</td>
</tr>
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</table>

Notes:
1. The table presents the results of ordinary least-squares regression estimates in columns (1), (3), (5), (6), and (7), with heteroscedasticity and autocorrelation consistent standard errors computed using four lags of the estimator suggested in Newey and West (1987). Columns (2), (4), and (8) present estimates using a Cochrane–Orcutt correction for first-order serial correlation, with the row labeled $\rho$ presenting the resulting estimate of the first-order serial correlation coefficient. For description of summary statistics, see notes to Table 7 below.
2. In all columns, the dependent variable is the ratio of real (1985 yen) gross investment in a given year to the end-of-the-year capital stock, for nonfinancial corporations. $Q$ is measured at the end of the year, so $Q_{t-1}$ is beginning of period $Q$. "$Q$ with inventories" combines inventories and fixed capital. All measures of $Q$ are adjusted for taxes. See text for further details.
Given the wildly unsatisfactory nature of these results, and the more fundamental problem that \( Q \) is negative for most of our sample (see Figure 3), we decided not to attempt to refine or interpret these estimates.

### 9. Results for Flexible Accelerator Regressions

#### 9.1 MEANS OF BASIC VARIABLES

Table 7 presents means and standard deviations of the basic variables, for the annual intervals corresponding to those presented in Table 1. The pattern for the capital stock \( k \) and for output of industry is a familiar one, with robust growth before 1973 followed by more moderate growth after 1974, and with the 1986–1991 period relatively strong, the 1991–1994 period exceptionally weak. As indicated in Figure 4, the cost of capital \( c \) fell through most of the period, especially in the early part of the sample. The column (3) and (4) subperiod figures for this variable are heavily

<table>
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<tr>
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</tr>
</thead>
<tbody>
<tr>
<td>(1) ( k )</td>
<td>8.0</td>
<td>12.7</td>
<td>5.3</td>
<td>5.7</td>
<td>6.5</td>
<td>3.0</td>
</tr>
<tr>
<td></td>
<td>(4.4)</td>
<td>(3.7)</td>
<td>(1.5)</td>
<td>(1.1)</td>
<td>(0.9)</td>
<td>(1.4)</td>
</tr>
<tr>
<td>(2) ( k^* = y - c )</td>
<td>7.9</td>
<td>17.2</td>
<td>3.0</td>
<td>2.5</td>
<td>7.2</td>
<td>5.9</td>
</tr>
<tr>
<td></td>
<td>(16.8)</td>
<td>(7.9)</td>
<td>(18.2)</td>
<td>(19.7)</td>
<td>(4.1)</td>
<td>(3.2)</td>
</tr>
<tr>
<td>(3) ( y )</td>
<td>5.7</td>
<td>9.5</td>
<td>3.5</td>
<td>4.1</td>
<td>5.5</td>
<td>0.1</td>
</tr>
<tr>
<td></td>
<td>(3.8)</td>
<td>(2.5)</td>
<td>(2.4)</td>
<td>(2.0)</td>
<td>(1.1)</td>
<td>(1.0)</td>
</tr>
<tr>
<td>(4) ( c )</td>
<td>-2.3</td>
<td>-7.6</td>
<td>0.5</td>
<td>1.6</td>
<td>-1.8</td>
<td>-5.8</td>
</tr>
<tr>
<td></td>
<td>(16.1)</td>
<td>(9.3)</td>
<td>(18.3)</td>
<td>(19.7)</td>
<td>(3.5)</td>
<td>(2.5)</td>
</tr>
<tr>
<td>(5) ( p_l - p_y )</td>
<td>-1.8</td>
<td>-2.8</td>
<td>-1.2</td>
<td>-1.0</td>
<td>-1.2</td>
<td>-2.6</td>
</tr>
<tr>
<td></td>
<td>(1.9)</td>
<td>(1.6)</td>
<td>(1.8)</td>
<td>(1.9)</td>
<td>(0.9)</td>
<td>(0.4)</td>
</tr>
<tr>
<td>(6) ( c_1 )</td>
<td>0.0</td>
<td>-0.1</td>
<td>0.1</td>
<td>0.1</td>
<td>-1.5</td>
<td>-0.1</td>
</tr>
<tr>
<td></td>
<td>(1.5)</td>
<td>(0.9)</td>
<td>(1.8)</td>
<td>(1.9)</td>
<td>(1.4)</td>
<td>(0.1)</td>
</tr>
<tr>
<td>(7) ( c_2 )</td>
<td>-0.5</td>
<td>-4.7</td>
<td>1.6</td>
<td>2.4</td>
<td>0.9</td>
<td>-3.2</td>
</tr>
<tr>
<td></td>
<td>(16.5)</td>
<td>(9.5)</td>
<td>(19.1)</td>
<td>(20.5)</td>
<td>(4.5)</td>
<td>(2.7)</td>
</tr>
</tbody>
</table>

Notes:
1. The data are annual and real (1985 yen). Growth rates are computed by averaging log differences beginning with the year following the start date; the column (6) figure, for example, averages log differences in the 3 years from 1992 to 1994. \( k \) is net fixed assets of nonfinancial corporations, \( y \) is output of industry, \( c \) is the cost of capital, constructed as described in the text and note 2 below. In columns (1) and (2), the sample periods for \( k \) and \( y \) begin in 1961 rather than 1962. Because of this, and because of rounding, rows (3) and (4) may not add to row (2). See text for further details.
2. The cost of capital in row (4) is the product of the three terms in rows (5) through (7). Row (5) is the ratio of deflator for private investment in plant and equipment to that for output of industry. Row (6) reflects tax factors. Row (7) largely reflects a nominal discount factor and expected inflation. See the text for details. Rows (5) to (7) may not add to row (4) because of rounding. See text for further details.
influenced by the fact that the sample starts in 1973 (see Figure 4a); moving the starting date to 1975 would result in negative average growth rates.

It may be seen in column (1), rows (1) and (2) that the growth rates of capital and of the target level of capital $k^*$ are quite similar over the entire sample period, despite the growing capital-to-output ratio [column (1), row (1) vs. column (1), row (3)]. We note that this is consistent with the model of Section 4, and with the less structured Cobb–Douglas specification of target capital in Section 6. Our empirical work does not, however, rely on the Section 4 prediction that the capital–output ratio will increase indefinitely: The point is that simple statistics such as in Table 7, plots such as Figures 4 and 5, and conventional unit-root tests (details omitted) do suggest that the unit-root specification in the cost of capital and the capital–output ratio, as well as cointegration between actual and target capital, reasonably characterize the behavior in our sample.

Rows (5) to (7) of Table 7 further decompose the growth in the cost of capital. Column (1) indicates that over the whole sample, the fall in the cost of capital is basically attributable to the fall in the relative price of new capital goods to output [line (5)]. In the boom of 1986–1991, however, the fall is also attributable to tax factors [line (6), column (5)]; the main event here was a series of cuts in the corporate tax rate from 43.3% in 1986 to 37.5% in 1990 and 1991. In the 1991–1994 period, falls in the relative price and in the real interest-rate term [line (7)] were both important. The latter reflects the general fall in interest rates associated with the Bank of Japan’s interest-rate cuts; see Figure 2c above.

Table 7 indicates that at least the secular movement in the capital stock is consistent with the secular movement in output and the cost of capital. To analyze cyclical dynamics, we turn to regression analysis.

9.2 REGRESSION ANALYSIS

9.2.1 Unrestricted Regressions Table 8 presents VAR estimates, obtained by OLS. As a preliminary, columns (1a) and (1b) present a very simple specification, a bivariate VAR in $(k - k^*, \Delta k^*)$. The $t$-statistics implied by the column (1b) figures indicate that relative to an information set consisting of past $k - k^*$'s and past $\Delta k^*$'s, $k - k^*$ Granger-causes $\Delta k^*$ even though $\Delta k^*$ does not Granger-cause itself; on average, a 1% (say) excess of $k$ over $k^*$ is associated with $\Delta k^*$ rising by about 0.5% the next year.

Columns (2a) through (2c) add $\Delta c$ to the VAR. Column (2c) indicates that $k - k^*$ helps predict not only $\Delta k^*$ but one of its components, $\Delta c$, with a 1% (say) excess of $k$ over $k^*$ on average being followed with $\Delta c$ falling by about $-0.5\%$ in the next year. The estimates and standard errors in
column (2b) suggest that it helps to include both $\Delta k_{t-1}^*$ and $\Delta c_{t-1}$ as predictors of $\Delta k_t^*$; column (2c) suggests the same, a little more mildly.

Columns (3a) through (3c) add a second lag of each of the three variables $k - k^*$, $\Delta k^*$, and $\Delta c$. While individual $t$-statistics are small, both $F$-tests and $t$-tests on the sum of the coefficients on $k - k^*$ strongly reject the null that $k - k^*$ does not help predict $\Delta k^*$ and $\Delta c$.

Finally, columns (4a) and (4c) present results when the sample is restricted to 1974–94. Once again, rises in $k - k^*$ anticipate rises in $\Delta k^*$ and falls in $\Delta c$ [columns (4b) and (4c)].

In the three specifications (2)–(4), point estimates sometimes look different. We therefore began the analysis using all three. In this preliminary analysis, all three proved to yield quite similar answers to the questions we ask (see Table 10 below), indicating that from the perspective of the VAR in $(y, c, k)$ many of the shifts in coefficients observed in Table 8 are offsetting. So for parsimony and computational simplicity we focused on the one-lag specifications in columns (2) and (4). We repeated all estimates with both samples, although for conciseness in reporting results we generally give more detailed attention to the full-sample estimates in column (2).

### 9.2.2 Impulse Response Functions

To interpret these full-sample estimates, we solve for the restricted $k_t - k_t^*$ process using the method in the Appendix and then, using $k^* = y - c$, transform to a unit-root VAR in $(y, c, k)$. Apart from deterministic terms and the residual, the result is

\[
y_t = 0.015k_{t-1} + 1.172y_{t-1} - 0.187y_{t-2} + 0.033c_{t-1} - 0.018c_{t-2}, \quad (9.1a)
\]

\[
(-0.054, 0.092) \quad (0.730, 1.42) \quad (-0.436, 0.242) \quad (-0.027, 0.105) \quad (-0.084, 0.048)
\]

\[
c_t = -0.477k_{t-1} - 1.406y_{t-1} + 1.883y_{t-2} + 0.582c_{t-1} - 0.059c_{t-2}, \quad (9.1b)
\]

\[
(-0.884, -0.228) \quad (-3.71, 1.42) \quad (0.488, 4.06) \quad (0.206, 0.881) \quad (-0.423, 0.220)
\]

\[
k_t = 0.953k_{t-1} + 0.294y_{t-1} - 0.247y_{t-2} - 0.048c_{t-1} + 0.000c_{t-2}, \quad (9.1c)
\]

\[
(0.892, 1.012) \quad (0.040, 1.36) \quad (-1.35, -0.025) \quad (-0.146, -0.007) \quad (-0.031, 0.112)
\]

\[
\alpha = 15.17, \quad \lambda = 0.79. \quad (9.1d)
\]

\[
(1.15, 92.3) \quad (0.41, 0.92)
\]

In parentheses are 95% confidence intervals, from a bootstrap.

In the $y$ and $c$ equations, the confidence intervals on the estimates of the coefficients on $k_{t-1}$ suggest that the Granger causality found in Table 8 reflects a systematic tendency for movements in $k$ to anticipate movements in $c$ but perhaps not $y$. [Asymptotic standard errors (not reported) suggest the same.] In (9.1d), the confidence intervals around $\alpha$ and $\lambda$ are large. The point estimates of these two parameters, which suggest con-
Table 8 REGRESSION RESULTS, FLEXIBLE ACCELERATOR MODEL

<table>
<thead>
<tr>
<th>Regressor and Summary Statistic</th>
<th>Dependent Variable (1a)</th>
<th>Dependent Variable (1b)</th>
<th>Dependent Variable (2a)</th>
<th>Dependent Variable (2b)</th>
<th>Dependent Variable (2c)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_{t-1} - k_{t-1}^*$</td>
<td>0.428</td>
<td>0.523</td>
<td>0.452</td>
<td>0.492</td>
<td>-0.477</td>
</tr>
<tr>
<td></td>
<td>(0.160)</td>
<td>(0.162)</td>
<td>(0.156)</td>
<td>(0.153)</td>
<td>(0.165)</td>
</tr>
<tr>
<td>$k_{t-2} - k_{t-2}^*$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Delta k_{t-1}^*$</td>
<td>-0.093</td>
<td>0.083</td>
<td>-1.630</td>
<td>2.070</td>
<td>-1.883</td>
</tr>
<tr>
<td></td>
<td>(0.171)</td>
<td>(0.174)</td>
<td>(0.967)</td>
<td>(0.951)</td>
<td>(1.021)</td>
</tr>
<tr>
<td>$\Delta k_{t-2}^*$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Delta c_{t-1}$</td>
<td>-1.570</td>
<td>2.029</td>
<td>-1.824</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.973)</td>
<td>(0.957)</td>
<td>(1.028)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Delta c_{t-2}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Constant</td>
<td>-1.071</td>
<td>1.114</td>
<td>-0.878</td>
<td>0.865</td>
<td>-0.758</td>
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<tr>
<td></td>
<td>(0.283)</td>
<td>(0.288)</td>
<td>(0.300)</td>
<td>(0.296)</td>
<td>(0.317)</td>
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<tr>
<td>Post-1973 dummy</td>
<td>0.183</td>
<td>-0.254</td>
<td>0.087</td>
<td>-0.128</td>
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<tr>
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<td>(0.062)</td>
<td>(0.084)</td>
<td>(0.082)</td>
<td>(0.088)</td>
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<tr>
<td>$R^2$</td>
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<td>0.347</td>
<td>0.593</td>
<td>0.422</td>
<td>0.285</td>
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<tr>
<td>S.e.e.</td>
<td>0.135</td>
<td>0.139</td>
<td>0.131</td>
<td>0.129</td>
<td>0.138</td>
</tr>
<tr>
<td>Q-statistic [p-value]</td>
<td>1.92 [0.98]</td>
<td>2.88 [0.94]</td>
<td>1.22 [1.00]</td>
<td>1.16 [1.00]</td>
<td>0.80 [1.00]</td>
</tr>
<tr>
<td>Durbin-Watson</td>
<td>2.32 2.40</td>
<td>1.96 2.02</td>
<td>1.94</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Sample period</td>
<td>1964–94 (31 obs.)</td>
<td></td>
<td></td>
<td></td>
<td>1964–94 (31 obs.)</td>
</tr>
</tbody>
</table>

Notes:
1. The table presents the results of ordinary least-squares estimates of the vector autoregressions with the indicated variables. Asymptotic standard errors are in parentheses. "S.e.e." is the degrees-of-freedom-adjusted estimated of the standard deviation of the regression disturbance. The number of degrees of freedom in the Q-statistic is 8 in specifications 1–3, 5 in specification 4. The sample period that is given is for the dependent variable.
2. $k(t)$ is the log of the capital stock, $c(t)$ the log of the cost of capital, and $k^*(t)$ the target level of capital, defined as the difference between log of output and $c(t)$. See text for further discussion.
3. The capital stock $k$ is for nonfinancial corporations, the output $y$ is the output of industry, and the cost of capital $c$ was constructed as described in the text. All variables are real (1985 prices).
### Table 8 (continued)

<table>
<thead>
<tr>
<th></th>
<th>(3a) $k_i - k_i^*$</th>
<th>(3b) $\Delta k_i^*$</th>
<th>(3c) $\Delta c_i$</th>
<th>(4a) $k_i - k_i^*$</th>
<th>(4b) $\Delta k_i^*$</th>
<th>(4c) $\Delta c_i$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>-0.097</td>
<td>1.507</td>
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<td>0.462</td>
<td>-0.435</td>
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<td>(0.175)</td>
<td>(0.191)</td>
</tr>
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<tr>
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<td>(1.426)</td>
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<td>(1.480)</td>
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<td>(1.251)</td>
<td>(1.360)</td>
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<td>1.893</td>
<td>-1.732</td>
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<tr>
<td></td>
<td>(1.288)</td>
<td>(1.262)</td>
<td>(1.337)</td>
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<td>(1.021)</td>
<td>(1.082)</td>
<td>(1.305)</td>
<td>(1.284)</td>
<td>(1.395)</td>
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<td></td>
<td>1.817</td>
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<td>1.667</td>
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<tr>
<td></td>
<td>(1.303)</td>
<td>(1.277)</td>
<td>(1.353)</td>
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<tr>
<td></td>
<td>-0.894</td>
<td>0.883</td>
<td>-0.800</td>
<td>-0.677</td>
<td>0.645</td>
<td>-0.575</td>
</tr>
<tr>
<td></td>
<td>(0.338)</td>
<td>(0.332)</td>
<td>(0.351)</td>
<td>(0.298)</td>
<td>(0.293)</td>
<td>(0.318)</td>
</tr>
<tr>
<td></td>
<td>0.132</td>
<td>-0.152</td>
<td>0.080</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(0.098)</td>
<td>(0.096)</td>
<td>(0.102)</td>
<td></td>
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<tr>
<td></td>
<td>0.597</td>
<td>0.431</td>
<td>0.314</td>
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<td>0.442</td>
<td>0.349</td>
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<tr>
<td></td>
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<td>0.138</td>
<td>0.138</td>
<td>0.136</td>
<td>0.148</td>
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<tr>
<td></td>
<td>5.48</td>
<td>5.84</td>
<td>4.57</td>
<td>1.09</td>
<td>1.33</td>
<td>0.93</td>
</tr>
<tr>
<td></td>
<td>[0.71]</td>
<td>[0.67]</td>
<td>[0.80]</td>
<td>[0.96]</td>
<td>[0.93]</td>
<td>[0.97]</td>
</tr>
<tr>
<td></td>
<td>2.45</td>
<td>2.54</td>
<td>2.40</td>
<td>1.85</td>
<td>1.89</td>
<td>1.83</td>
</tr>
</tbody>
</table>

1965–94 (30 obs.) 1974–94 (21 obs.)
siderable persistence in \( k \), directly reflect the smooth evolution of \( k \) despite some sharp movements in \( c \) and \( y \). These estimates seem roughly comparable to estimates of some U.S. studies.\(^{17}\) In the \( k \)-equation (9.1c), the coefficients on the first lag of \( y \) and of \( c \) each are significantly different from zero at the 5% level. These coefficients indicate that, historically, a 1% rise in output has been associated with about a 0.3% rise in the next year’s capital stock, and that a corresponding increase in the cost of capital has been associated with a 0.05% fall. The larger short-run elasticity with respect to output was also found in Yoshikawa (1995).

To consider longer-term multipliers, we solve for the moving-average representation. In Figure 6, the solid line plots the first 10 of the moving-average weights (impulse responses), the dashed lines the 95% bootstrap confidence intervals.\(^{18}\) These are not responses to orthogonalized innovations, but to the actual disturbances in the \( (y, c, k) \) VAR. The top row presents responses of \( k \), with the responses for \( y \) and \( c \) included on the next two rows. Note that the scale of the \( c \) response is different from that for \( k \) and \( y \). Since \( k - k^* = k - (y - c) \) is stationary, the long-run response of \( k \) to a given shock is equal to the difference between the long-run \( y \) and \( c \) responses. The plots stop at 10 periods because the long run is effectively reached at this horizon.

The plot in the upper left-hand corner shows that a 1% shock to \( y \) leads dynamically to monotonic increases in \( k \) that asymptote at 0.55%. [The long run is not 1%, because this plot takes account of the reaction of all the variables in the system to the increase in \( y \). Such a shock tends to lead to not a 1% but a 1.14% long-run increase in \( y \) (leftmost plot in the second row), and a 0.58% long-run increase in \( c \) (leftmost plot in the bottom row).] A 1% shock to \( c \) leads ultimately to a \(-0.07%\) fall in \( k \).

What explains the stronger response (larger elasticity) of \( k \) to shocks to \( y \) than to \( c \)? As noted in the introduction, because our model has convex adjustment costs, it predicts a smaller response to shocks to \( c \), in both the short and the long run, if there is less persistence (more mean reversion) in \( c \); it would not make sense for a firm to rapidly cut back on \( k \) in response to a rise in \( c \) if this rise were likely to be swiftly offset with a subsequent fall. And \( c \) does appear to be less persistent than \( y \). The figure indicates that the long-run response of \( c \) itself to a 1% shock to \( c \) is only 0.11%, in contrast to the 1.14% response of \( y \) to its own shocks.

\(^{17}\) Setting \( M \) equal to the mean of \( 1 - C_{2t} \) yields \( \phi = 2.2. \) [See (4.4), (4.12), and (7.4).] Although there are differences in functional form and data frequency, this looks comparable to a value calibrated by Cogley and Nason (1995, p. 505).

\(^{18}\) Slight qualification: The lower end of the confidence interval on the one-step-ahead response of \( c \) to a shock to \( y \) is \(-3.71\); for readability, the Figure 6 graph stops at \(-2.6\). This is the only number truncated in the graphs.
While the relevant measure of mean reversion is the multivariate one depicted in the figure, this mean reversion is also evident in the univariate c-process. The first-order autocorrelations of $\Delta c$ and its components and of $\Delta y$ are

<table>
<thead>
<tr>
<th></th>
<th>$\Delta c$</th>
<th>$\Delta (p_1 - p_2)$</th>
<th>$\Delta c_1$</th>
<th>$\Delta c_2$</th>
<th>$\Delta y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1962–1994</td>
<td>-.17</td>
<td>.26</td>
<td>.14</td>
<td>-.22</td>
<td>.64</td>
</tr>
</tbody>
</table>

Thus, the mean reversion observed in Figure 6 apparently is driven by mean reversion in $c_2$, the interest-rate component of the cost of capital.

In sum, then, our model rationalizes three notable characteristics of the data: the growth of the capital–output ratio, the apparently strong ability of $k - k^*$ to predict $\Delta k^*$ and $\Delta c$, and the signs and relative magnitudes of the elasticity of capital with respect to output and the cost of capital.

9.2.3 Decomposition of Forecast Error of the Capital Stock  Table 9 presents a decomposition for the period 1986–1991, and for 1991–1994, computed from the estimates in equation (9.1). The first column in each panel repeats the Table 7 figures on realized annual growth rates. The second column presents the 1986 and 1991 forecasts from the VAR, the third column the difference between actual and forecast. These two columns do not exploit an orthogonalization. The last two columns rely on the Choleski factorization described above, in which residuals to the $y$ and $c$ equations precede that for the $k$-equation. Column (4) sums the effects of the $y$ and $c$ shocks (this sum is independent of whether $y$ or $c$ appears first in the ordering), while column (5) presents the residual $k$-shock.

Capital growth was stronger than predicted in 1986–1991, weaker in 1991–1994. But conditional on the path of output and the cost of capital, much of this behavior is easily rationalized. In both episodes, about half the surprise in capital was due to surprises in $y$ and $c$, leaving a residual surprise in $k$ to account for the other half ($\frac{1}{2} \approx 0.89/1.79, 1.05/1.94$) and for a smaller fraction of the actual movement.

In 1991–1994, it may look odd that the target capital $k^*$ was slightly above the predicted ($= 0.07$), while innovations in $k^*$ led to a negative surprise in $k$ ($= -0.89$). This seems to result from two factors. The first is that all of the good news in $k^*$ resulted from a surprise fall in the cost of capital; the output surprise was negative. As explained above, $k$ responds more strongly to shocks to $y$ than to $c$. Second, much of the good news in $k^*$ came in the last year of the three-year period; the 1991–1993 forecast error in $k^*$ in fact was negative [$-0.60\%$ (annualized)].
### Table 9 DECOMPOSITION OF FORECAST ERROR OF CAPITAL STOCK

<table>
<thead>
<tr>
<th>Due to shock to:</th>
<th>Actual</th>
<th>Forecast</th>
<th>Total</th>
<th>(3) y, c eqns.</th>
<th>(4) k eqn.</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a) 1986–1991</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(1) k</td>
<td>6.47</td>
<td>4.68</td>
<td>1.79</td>
<td>0.90</td>
<td>0.89</td>
</tr>
<tr>
<td>(2) k* = y – c</td>
<td>7.23</td>
<td>5.97</td>
<td>1.27</td>
<td>0.84</td>
<td>0.43</td>
</tr>
<tr>
<td>(3) y</td>
<td>5.47</td>
<td>3.48</td>
<td>2.00</td>
<td>1.99</td>
<td>0.01</td>
</tr>
<tr>
<td>(4) c</td>
<td>-1.76</td>
<td>-2.49</td>
<td>0.73</td>
<td>1.15</td>
<td>-0.42</td>
</tr>
<tr>
<td>(b) 1991–1994</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(1) k</td>
<td>2.97</td>
<td>4.92</td>
<td>-1.94</td>
<td>-0.89</td>
<td>-1.05</td>
</tr>
<tr>
<td>(2) k* = y – c</td>
<td>5.92</td>
<td>5.84</td>
<td>0.07</td>
<td>0.30</td>
<td>-0.22</td>
</tr>
<tr>
<td>(3) y</td>
<td>0.10</td>
<td>3.57</td>
<td>-3.47</td>
<td>-3.46</td>
<td>-0.01</td>
</tr>
<tr>
<td>(4) c</td>
<td>-5.82</td>
<td>-2.27</td>
<td>-3.55</td>
<td>-3.76</td>
<td>0.21</td>
</tr>
</tbody>
</table>

**Notes:**
1. See the note to Table 7 and the text for descriptions of the data. All growth rates are annualized. For example, actual growth of \( k \) for 1986–1991 was approximately \( 5 \times 6.47\% \). Components may not add up to a total because of rounding.
2. The trivariate VAR whose estimates are presented in equation (9.1) was used to compute the forecasts of the levels of the indicated variables. The decomposition of the shock presented in columns (4) and (5) is obtained by performing a Choleski decomposition with the residual for \( k \) ordered last.

#### 9.2.4 Results for Alternative Specifications

Table 10 summarizes impulse responses and decompositions of the 1986–1994 forecast error, for five additional specifications: unrestricted VARs with one lag and two lags, full sample and post-1973 sample (VAR estimates for all but the two-lag, post-1973 sample are in Table 8), and the restricted one-lag VAR for the post-1973 sample. For ease of comparison, it also repeats results for the one-lag, restricted, full-sample VAR already reported in Figure 6 and Table 9.

In a nutshell, the results already presented are quite robust to the variations in specification presented in the table. In panels (a) and (b), the initial response of \( k \) to a shock to \( y \) ranges from about 0.3% to 0.5%, and asymptotes at around 0.6 to 0.9. The initial and long-run response of a shock to \( c \) is negative (apart from the initial response in the full-sample, two-lag specification) and quite small algebraically. In panels (c) and (d), the decompositions attribute the lion’s share of the movement in \( k \) to the two components of \( k^* \) (again with the exception of the full-sample, two-lag VAR).

Quantitative consistency between the unrestricted and restricted estimates is also suggested by the bootstrap test of the restrictions. The \( p-\)
Table 10  RESULTS WITH ALTERNATIVE SPECIFICATIONS

(a) Response of $k$ to a 1% Shock, Full-Sample Estimates

<table>
<thead>
<tr>
<th>Horizon</th>
<th>Restricted</th>
<th></th>
<th>Unrestricted</th>
<th></th>
<th>Unrestricted, 2 lags</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$y$</td>
<td>$c$</td>
<td>$k$</td>
<td>$y$</td>
<td>$c$</td>
</tr>
<tr>
<td>2</td>
<td>.29</td>
<td>-.05</td>
<td>.95</td>
<td>.50</td>
<td>-.03</td>
</tr>
<tr>
<td>10</td>
<td>.55</td>
<td>-.07</td>
<td>.92</td>
<td>.80</td>
<td>-.08</td>
</tr>
</tbody>
</table>

(b) Response of $k$ to a 1% Shock, Post-1973-Sample Estimates

<table>
<thead>
<tr>
<th>Horizon</th>
<th>Restricted</th>
<th></th>
<th>Unrestricted</th>
<th></th>
<th>Unrestricted, 2 lags</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$y$</td>
<td>$c$</td>
<td>$k$</td>
<td>$y$</td>
<td>$c$</td>
</tr>
<tr>
<td>2</td>
<td>.40</td>
<td>-.04</td>
<td>.95</td>
<td>.51</td>
<td>-.03</td>
</tr>
<tr>
<td>10</td>
<td>.71</td>
<td>-.05</td>
<td>.94</td>
<td>.81</td>
<td>-.04</td>
</tr>
</tbody>
</table>
(c) Decomposition of Forecast Error of $k_t$, Full-Sample Estimates

<table>
<thead>
<tr>
<th></th>
<th>Restricted</th>
<th></th>
<th>Unrestricted</th>
<th></th>
<th>Unrestricted, 2 lags</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Forecast</td>
<td>Surprise</td>
<td>Forecast</td>
<td>Surprise</td>
<td>Forecast</td>
<td>Surprise</td>
</tr>
<tr>
<td></td>
<td>Total $y + c$ $k$</td>
<td></td>
<td>Total $y + c$ $k$</td>
<td></td>
<td>Total $y + c$ $k$</td>
<td></td>
</tr>
<tr>
<td>1986–91</td>
<td>4.7</td>
<td>1.8 0.9 0.9</td>
<td>4.4</td>
<td>2.0 1.3 0.7</td>
<td>4.0</td>
<td>2.5 2.7 −0.2</td>
</tr>
<tr>
<td>1991–94</td>
<td>4.9</td>
<td>−1.9 −0.9 −1.0</td>
<td>4.8</td>
<td>−1.8 −1.4 −0.4</td>
<td>4.8</td>
<td>−1.8 −2.9 1.1</td>
</tr>
</tbody>
</table>

(d) Decomposition of Forecast Error of $k_t$, Post-1973 Estimates

<table>
<thead>
<tr>
<th></th>
<th>Restricted</th>
<th></th>
<th>Unrestricted</th>
<th></th>
<th>Unrestricted, 2 lags</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Forecast</td>
<td>Surprise</td>
<td>Forecast</td>
<td>Surprise</td>
<td>Forecast</td>
<td>Surprise</td>
</tr>
<tr>
<td></td>
<td>Total $y + c$ $k$</td>
<td></td>
<td>Total $y + c$ $k$</td>
<td></td>
<td>Total $y + c$ $k$</td>
<td></td>
</tr>
<tr>
<td>1986–91</td>
<td>4.6</td>
<td>1.9 1.1 0.7</td>
<td>4.5</td>
<td>1.9 1.3 0.6</td>
<td>4.5</td>
<td>1.9 1.8 .2</td>
</tr>
<tr>
<td>1991–94</td>
<td>4.9</td>
<td>−2.0 −1.3 −0.6</td>
<td>4.9</td>
<td>−1.9 −1.7 −0.3</td>
<td>4.5</td>
<td>−1.5 −1.6 .0</td>
</tr>
</tbody>
</table>

Notes:
1. See notes to Table 7 and the text for description of the data.
2. All estimates are computed from trivariate VARs in $(y, c, k)$. The “restricted” estimates in panels (a) and (c) are computed from equation (9.1). The text does not directly present the parameters for the VARs in $(y, c, k)$ for the other specifications in the table, although the parameters in the underlying VARs in $(k - k^*, \Delta k^*, \Delta c)$ are in the following columns in Table 8: “unrestricted” in panels (a) and (c), column (2); “unrestricted” in panels b and d, column (4); “unrestricted, 2 lag” in panels (a) and (c), column (3) in Table 8. The “unrestricted, 2 lags” estimates in panels (b) and (d) are computed from an underlying set of estimates whose variables are identical to that in column (3) of Table 8 except that there is no post-1974 dummy. The “restricted” estimates in panels (b) and (d) are computed by imposing the restrictions as described in the text.
3. Panels (a) and (b) present the response of $k$ to a 1% nonorthogonalized shock to the indicated variable. See text for details. See notes to Table 9 for an explanation of panels (c) and (d).
4. The “restricted” full-sample estimates repeat results depicted in Figure 6(a) or Table 9(c).
value for this test was 0.654 for the whole sample, 0.737 for the post-1973 sample.\textsuperscript{19}

9.3 VARS WITH ADDITIONAL VARIABLES

We also estimated and applied three additional specifications, each of which added a fourth variable to the system. Our motivations were twofold. First, it is possible that sharper or more informative estimates might result, insofar as the additional variable helps predict $\Delta k^*$. Second, according to other investment models, a variable might help predict capital accumulation even if it does not help predict $\Delta k^*$.

The variable added was the yen–dollar real exchange rate, or real net worth of nonfinancial corporations, or real land prices. The exchange rate was chosen because of the prominence it plays in discussion of the Japanese economy, both generally and during the recent cycle (e.g., Economic Planning Agency, 1994). Net worth was chosen because of the role it plays in credit-constraint models such as Kiyotaki and Moore (1994, 1995). Land prices were chosen again because of their value as collateral in credit-constraint models [see Ogawa et al. (1994) for an application to Japan], and, more generally, because of the role land price fluctuations may have played in encouraging speculative behavior (e.g., Chirinko and Schaller, 1995).

Each variable was entered as a log difference. [In the notation of Section 6, then, $f = (\Delta k^*, \Delta c, \Delta z)'$ and $Z = (k - k^*, \Delta k^*, \Delta c, \Delta z)'$, where $z$ is the log of the additional variable.] We then estimated unrestricted and restricted first-order VARs for the full and the post-1973 samples. There were few differences between the two samples, so in Table 11 we report and discuss only the full-sample results, focusing on impulse responses and the 1986–1994 decomposition.

In Table 11, columns (2)–(4) of panel (a) indicate that of the three variables, only the real exchange rate has predictive power for $k - k^*$, $\Delta k^*$, or $\Delta c$ at traditional significance levels; a real exchange-rate appreciation is associated with an increase in $\Delta k^*$ and a fall in $c$ and $k - k^*$. (Although not reported in the table, in all three specifications the coeffi-

\textsuperscript{19} As suggested by the relative size of these two $p$-values, bootstrap confidence intervals are generally larger for the post-1973 sample. This no doubt partly results from a smaller sample size, but may also indicate that the full-sample intervals are a little misleading. In particular, for the first-order serial correlation coefficient of the residual to the restricted equation for $k$, the point estimates and 95% bootstrap confidence intervals are 0.56 ($-0.40$, 0.28) for the full sample and 0.46 ($-0.69$, 0.77) for the post-1973 sample. Thus for the full sample there is evidence against the implicit bootstrap assumption that the residuals are i.i.d. We take the similarity of the results for all specifications in Table 10 to indicate that this mild serial correlation has negligible economic importance.
### Table 11 RESULTS WITH ADDITIONAL INFORMATION VARIABLES

#### (a) Regression Estimates

<table>
<thead>
<tr>
<th>Variable (z)</th>
<th>Coefficients on Add'l Variable</th>
<th>Response of k to a 1% shock</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( k_t - k^*_t )</td>
<td>( \Delta k^*_t )</td>
</tr>
<tr>
<td></td>
<td>eqn.</td>
<td>eqn.</td>
</tr>
<tr>
<td>Real exch. rate</td>
<td>.62</td>
<td>-.61</td>
</tr>
<tr>
<td>Net worth</td>
<td>-.22</td>
<td>.32</td>
</tr>
<tr>
<td>Real land price</td>
<td>.80</td>
<td>-.63</td>
</tr>
<tr>
<td>&amp; (22)</td>
<td>(.33)</td>
<td>(.32)</td>
</tr>
<tr>
<td>&amp; (49)</td>
<td>(.49)</td>
<td>(.49)</td>
</tr>
<tr>
<td>&amp; (49)</td>
<td>(.49)</td>
<td>(.49)</td>
</tr>
</tbody>
</table>

#### (b) Decomposition of Forecast Error of \( k_t \)

<table>
<thead>
<tr>
<th>Variable (z)</th>
<th>Period</th>
<th>Unrestricted VAR</th>
<th>Restricted VAR</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Forecast</td>
<td>Surprise</td>
<td>Total</td>
</tr>
<tr>
<td></td>
<td>y + c + z</td>
<td>k</td>
<td>y + c + z</td>
</tr>
<tr>
<td>Real exch. rate</td>
<td>1986–91</td>
<td>5.0</td>
<td>1.7</td>
</tr>
<tr>
<td>Net worth</td>
<td>1991–94</td>
<td>4.9</td>
<td>1.9</td>
</tr>
<tr>
<td>Real land prices</td>
<td>1986–91</td>
<td>5.7</td>
<td>1.8</td>
</tr>
<tr>
<td>Net worth</td>
<td>1991–94</td>
<td>4.8</td>
<td>1.9</td>
</tr>
<tr>
<td>Net worth</td>
<td>1991–94</td>
<td>4.8</td>
<td>1.9</td>
</tr>
</tbody>
</table>

**Notes:**
1. Each set of estimates is computed from VARs in the four variables \((y, c, z, k)\), where \( z = \ln(\text{real exchange rate}), \ln(\text{real net worth}), \) or \( \ln(\text{real land prices}) \). The sample period is 1964–94. The unrestricted VAR is computed by transforming the OLS estimates of a VAR in \((k - k^*, \Delta k^*, \Delta c, \Delta z)\). The restricted VAR begins with the unrestricted estimates and imposes restrictions as described in the Appendix.
2. The real exchange rate is computed as: \((\text{nominal yen/dollar exchange rate}) \times (\text{U.S. GDP deflator, 1985 = 100}) / (\text{Japanese GDP deflator, 1985 = 100})\). The deflator for net worth is that for the capital stock; for land prices, the GDP deflator.
3. See notes to Table 9 for an explanation of panel (b); notes to Table 10 for an explanation of panel (a).
cients on the remaining variables are similar to those reported in Table 8; in particular, \( k - k^* \) retains its ability to predict \( \Delta k^* \) and \( \Delta c \) in all three specifications.) For all three variables, the response of \( k \) to a shock to \( y \) is smaller in the restricted than in the unrestricted system. [In all three specifications, the long run has effectively been reached by 10 periods, and shocks to \( y \) still have persistent effects on \( y \). The response to \( y \) is only 0.00 in the net-worth system (for example), because the shock to \( y \) leads to a 10-period-ahead increase in \( c \) as large as that in \( y \).] In general, however, the impulse response functions are similar to those reported in Table 10.

The panel (b) decompositions for the last cycle are not quite as consistent with previous results. The unrestricted estimates for net worth and land prices yield positive shocks to \( k \) in the 1991–1994 [column (6)], and the restricted estimates generally attribute a larger fraction of the movement in \( k \) to \( k \)-shocks [column (10)].

That there is a discrepancy between the unrestricted and restricted impulse response functions for output means that to some degree our present value model fails to capture the dynamics of the VAR. This is perhaps supportive of the view that fluctuations in net worth, or land prices, affect capital accumulation in ways not modeled by us. It is also consistent with the argument in several papers that credit constraints have important influences on business investment in Japan.

However, some of the differences between such papers and ours may be more apparent than real. In the previous section, we found a Q-model to have little explanatory power for investment. It is therefore not clear that there is a conflict between our general conclusions and those of papers that show that the addition of various variables, including ones proxying credit constraints, improve the fit of Q-models (e.g., Hoshi and Kashyap, 1990; Hoshi, Kashyap, and Scharfstein, 1991). In addition, the standard errors in panel (a) of Table 11 are large for net worth and land prices, and we have argued above that if we set the point estimates on net worth or land prices to zero—that is, omit them from the system—the present-value model seems to characterize the data well.

While we find no direct contradiction between our results and some earlier ones, we do feel as well that the results in our and other papers are suggestive of the importance of continuing to analyze the interaction of asset prices and business investment. Other priorities for research using the approach of our paper include use of quarterly data, analysis of the determinants of the cost of capital sufficiently detailed to allow

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20. This is consistent with Brunner and Kamin’s (1995) conclusion that financial factors did not play a very prominent role in the recent period.
explicit treatment of monetary policy, and development of models that derive the behavior of output and the cost of capital endogenously.

Appendix

Here we discuss (1) estimation of the restricted system, and (2) bootstrapping.

1 ESTIMATION OF THE RESTRICTED SYSTEM

Take the case in which \( f = (\Delta k^*, \Delta c)' \); extension to larger information sets is straightforward. Recall that \( Z \) is ordered so \( Z = (k - k^*, \Delta k^*, \Delta c)' \). Let \( \Pi = [\pi_{ij}] \), and let \( a_0 = (b\alpha, b\alpha, 0)' \), \( a_1 = (-1 - \alpha - b\alpha, -\alpha, 0)' \), \( a_2 = (\alpha, 0, 0)' \). Then, ignoring constants, (6.6) and (4.13) together imply \( E[a_0'Z_{t+1} + a_1'Z_t + a_2'Z_{t-1} \mid Z_{t-1}, Z_{t-2}, \ldots] = 0, \)

whence

\[
(0, 0, 0) = a_0'\Pi^2 + a_1'\Pi + a_2 \equiv (g_1(\Pi, b, \alpha), g_2(\Pi, b, \alpha), g_3(\Pi, b, \alpha)). \quad (A.1)
\]

Using an imposed value of \( b = 0.95 \) and the least-squares estimates of the \( \pi_{ij} \)'s \((i = 2,3, j = 1,2,3)\), we solve linearly for the \( \alpha \) that sets \( g_i(\Pi, b, \alpha) = 0 \). (Thus, we ignore the information on \( \alpha \) also contained in \( g_2 \) and \( g_3 \).)

We compute \( \lambda \) as the smaller root of the quadratic implied by \( \lambda/\alpha = (1 - \lambda)(1 - b\lambda) \). To solve for the implied process for \( E[k_t - k^*_t \mid Z_{t-1}, Z_{t-2}, \ldots] \)—call it \( \hat{E}(k_t - k^*_t) \)—we hold \( \alpha \) fixed and use an iterative technique to find \( \pi_{11}, \pi_{12}, \) and \( \pi_{13} \) that, in conjunction with the least-squares estimates of the other \( \pi_{ij} \)'s \((i = 2,3, j = 1,2,3)\) and this fixed estimate of \( \alpha \), yield a stable matrix \( \Pi \) that satisfies (A.1).

For computing forecasts such as in Table 9, estimates of coefficients of deterministic terms are also required. For the \( \Delta k^* \) and \( \Delta c \) equations, the unrestricted estimates are used. For the \( k - k^* \) equation, we use least-squares regressions of the time series \( \{(k_t - k^*_t) - \hat{E}(k_t - k^*_t)\} \) on the deterministic terms.

2 BOOTSTRAPPING

We generated 1000 sets of samples of size 31 (inference about full-sample estimates) and 1000 of size 21 (post-1973 sample). We obtained a given one of the 1000 samples by generating data recursively, using the restricted estimates and sampling with replacement from the \( 3 \times 1 \) vectors of residuals to the restricted system. The actual 1963 (full sample) or 1973 (post-1973 sample) data were used for initial conditions. Obtaining 1000 sets of estimates involved generation of 1082 samples of size 31 and 1010
samples of size 21. The additional samples were ones that produced a negative estimate of \( \alpha \), a signal to us to abort the algorithm used to obtain the restricted estimates (\( \alpha < 0 \) does not guarantee a real and stable).

REFERENCES


Hoshi, T., A. K. Kashyap, and D. Scharfstein. (1991). Corporate structure, liquid-
In their paper Kiyotaki and West (K&W) attempt to explain the dramatic behavior of investment in the recent recession in Japan. Using a conventional neoclassical model of investment as their guide, they estimate a variety of vector autoregressions (VARs), which they then use to decompose forecast errors in capital accumulation. They find that for some of their VARs a large fraction of the unexpected movement in the capital stock over the 1986–1991 and 1991–1994 periods is attributable to shocks

I wish to thank Ken West for his comments on an early draft of this comment. Conversations with Larry Christiano were also helpful in preparing these comments.
to output and the cost of capital. On the basis of this finding they conclude that, given the movements in output and the cost of capital, the movements in investment that occurred over the period in question are consistent with historical experience.

Unfortunately, the authors do not really explain the dramatic behavior of investment. If the behavior of investment is largely accounted for by output and the cost of capital, then to understand the behavior of investment we have to account for the movements in output and the cost of capital. This issue is not addressed by the authors. Since the cost of capital as measured by K&W does not vary much over the period in question, it makes sense to focus on the behavior of output. Here I argue that to understand the behavior of output one has to take into account the conduct of monetary policy and the behavior of stock prices. I find that movements in output are mostly explained by monetary policy and innovations in stock prices. Monetary policy over the period in question appears to have been driven by the extraordinary asset price movements around the time of the onset of the recession. The role of monetary policy and stock prices in the recent recession is largely ignored by K&W.

In the remainder of this comment I briefly review and interpret the empirical work on which K&W's conclusion is based. I then review recent economic history in Japan. Using this review as a guide, I estimate several VARs and use them to support my contention that monetary policy and stock price movements are the key to accounting for the behavior of investment. Finally, I relate the empirical findings discussed here to the findings reported by K&W.

K&W's conclusion is based for the most part on a first-order VAR in terms of the vector \( (k_t - y_t - c_t, \Delta y_t - \Delta c_t, \Delta c_t)' \), where the notation is the same as in their paper. This VAR is derived from a conventional partial equilibrium adjustment cost model of investment and is perfectly reasonable in the context of this model. K&W estimate this model using annual data and then transform it into its level form, which consists of a VAR in the levels of the capital stock, output, and the cost of capital. They focus on two versions of their VAR. In one version, which they call an unrestricted VAR, they do not impose a present-value condition implied by their model. In the other version, which they call a restricted VAR, they impose this present-value condition. Both VARs in fact implicitly impose a further restriction on the dynamic interaction between the variables they consider, which is that two lags of output and the cost of capital appear in the level VAR, but the capital stock appears with only one lag. The residuals in the level VARs are orthogonalized, and historical decompositions of the series are undertaken.
K&W reach their conclusion by observing that innovations to output and the cost of capital account for a large fraction of the deviation of capital from its forecast level in the 1991–1994 period, just as they do in the preceding 1986–1991 interval. From this perspective, one does not have to appeal to the behavior of asset prices or other variables in the periods leading up to the recession to account for the behavior of the capital stock, and thus investment, during the recession.

The robustness of this conclusion will rest principally on whether the econometric models are correctly specified. Output and the cost of capital are included in the estimation because they are postulated to be useful for forecasting future capital stocks, or more precisely future "desired" capital stocks. Within the context of the K&W analysis one is led immediately to wonder whether other variables may be useful for forecasting desired capital and whether including these variables in the estimation may overturn the main conclusion.

In thinking about this issue it is helpful to recall the relationship between VARs and dynamic stochastic models. Under reasonable assumptions, any such model will have as a reduced form a VAR of some form or another. Assuming the data can be accurately characterized in terms of a stationary model driven by exogenous impulses, one can in principle estimate the underlying model and impulses using a VAR. This is one of the virtues of VAR analysis. If the model is correctly specified, then one can disentangle the contribution of the various impulses to the dynamics of the endogenous variables.

There are two potential pitfalls here. The first is that if the VAR representation of the true model involves more variables than included in the estimation, the identification of the exogenous shocks will be problematic. Second, by excluding relevant variables the propagation mechanism implicit in the underlying structural model will be incorrectly estimated. These problems can lead to misleading inference regarding historical decompositions.

K&W recognize this and consider including other variables in the VARs to assess the robustness of their findings based on the three-variable VARs. They find that by including measures of the real exchange rate, net worth, or real land prices in their VARs, own innovations in the capital stock account for a much larger fraction of the capital stock movements than in the three-variable VARs. These findings suggest their main conclusion is too strong and point toward the likelihood that their empirical models are inadequate for explaining the behavior of investment.

Given the ambiguity of K&W's empirical findings, it seems worthwhile to dig more deeply into the question of accounting for the behavior of investment. My strategy for doing this in some ways is similar to
that taken by K&W. In particular I estimate VARs and use them to decom- 
pose forecast errors in key variables. However, my approach involves 
focusing on a different set of variables than considered by K&W. To 
appreciate the approach I take, a brief review of recent Japanese eco-
nomic history is in order. In my review I place considerable emphasis on 
the conduct of Japanese monetary policy over the period in question.¹ 

To begin with, consider the paths of real stock and land prices along 
with a key money market interest rate in the periods leading up to the 
recession, as shown in K&W's Figure 2a, b, and c, respectively. The 
interest rate I consider is the call rate on money market transactions. 
Students of Japanese monetary policy [see for example Yoshikawa (1993)] 
have argued that this interest rate plays a role in the conduct of monetary 
policy similar to that played by the federal funds rate in the United 
always begins with controlling interest rates in short-term money mar-

Starting in 1982, stock prices on the Tokyo stock exchange began a 
dramatic inflation, which ended in equally dramatic fashion a little less 
than two years before the onset of recession at the beginning of 1992. 
Land prices were also growing during this period. Between 1985 and 
1988 the Bank of Japan, after pressure from the United States, conducted 
a deliberate policy of low interest rates. This was to help U.S. efforts to 
contain its budget and current-account deficits. In this period of what 
market observers generally regarded as lax monetary policy, both share 
and land price inflation accelerated.

In 1989 Mr. Yasushi Mieno was appointed the new governor of the 
Bank of Japan. Mr. Mieno, a career central banker, was considered to be 
a Paul Volcker-type tight-money governor. On several occasions in the 
early period of his tenure he made public statements emphasizing his 
concerns about asset price inflation in Japan. These concerns appear to 
have been due to the heavy involvement of banks and nonfinancial firms 
in the stock and property markets around this time. Corporations were 
able to use new equity issues and the steep rise in stock prices as a very 
cheap way of financing capital expenditures.² Many firms were using 
surplus cash to invest in the stock market in order to improve the bottom 
line in a time of slow growth in the returns from operating their capital 

¹. This review of events leading up to the recession in Japan relies heavily on accounts 
given in various issues of The Economist newspaper from 1988 to 1993.
². This appears to be captured to some degree in the cost-of-capital series constructed by 
K&W (Figure 4a), probably because c in the paper includes the call rate. As an aside, 
otice that c works off a constant-risk-premium assumption. This may matter a lot if the 
stock market and the rest of the domestic and international capital market are playing a 
role in the implicit cost of capital.
stocks. In addition, Tokyo banks were using unrealized capital gains in
the stock market to meet capital adequacy requirements, increasingly
important given the staged increases in these requirements stipulated by
the Bank of International Settlements. Lenders generally and banks in
particular were using property increasingly and extensively as collateral
in a growing proportion of their credit provision.

It appears that Mr. Mieno was worried that a version of the U.S.
savings and loan crisis could emerge in Japan and that this could have
serious repercussions for the macroeconomy. He was reported to have
sent delegations to the United Kingdom and the United States to investi-
gate how their financial authorities dealt with the property collapses in
London and the savings and loan crisis, and this was some time before
asset prices peaked. In all of this we should caution that there were
plenty of underlying reasons for the asset price growth besides the li-
quidity in the system provided by the central bank’s lax policy and the
obvious opportunities for speculation at this time. The national saving
rate was growing, indicating growing rates of personal saving, and, as
the capital stock series in K&W’s Figure 1a indicates, saving in the form
of capital spending by firms was high. In a regulatory environment in
which the range of financial instruments was limited mostly to equity,
the stock market was likely to be in for some significant growth.

Mr. Mieno’s concern about the repercussions of perceived unwar-
ranted asset price inflation is one reason given for the steep rise in inter-
est rates that began with his tenure at the central bank. From its trough in
1987 to its peak in 1991 the call rate went from less than 4% to more than
8%. Half way through this rise, share prices peaked and began a steep
descent. Only when land prices peaked did the call rate begin to fall. And
around the time of the beginning of the recession, interest rates peaked.

These facts suggest that monetary policy may have played an impor-
tant role in determining the timing of the recession and that monetary
policy in the period leading up to the onset of the recession was heavily
influenced by concerns about asset price inflation. Before turning to my
VAR analysis it is instructive to examine the behavior of key macro
aggregates over the business cycle in the periods leading up to the reces-
sion. In Figure 1 are plotted HP-filtered macro aggregates starting in
1987:1 (the call rate is unfiltered). Using simple IS–LM analysis to inter-
pret the data, it should be clear from this figure that the recent recession
fits closely a classic response of an economy to a leftward shift in the LM
curve induced by a reduction in the supply of narrow money. Detrended
real balances fall as the call rate rises. In this period inventories accumu-

late relative to trend. Around the time of the peak in inventories, the detrended GDP begins to fall. Interestingly, the peak in plant and equipment investment leads the GDP peak (business investment usually lags the cycle in the United States). This is consistent with the IS–LM view of investment being closely tied to interest rates, given notions of lags in investment decision making, the long runup in the call rate, and the fact that investment peaks when the call rate peaks.

Thus the Japanese data are consistent with the notion that the recession was brought on by "tight" monetary policy as would be predicted at the level of IS–LM analysis. (Interestingly, if we analyze the eight recessions in the interval from 1961:1 to 1994:4, at least five of them appear to be consistent with leftward shifts in the LM curve.) Having confirmed that the monetary policy view of the recession is not obviously inconsistent with the data, it is now necessary to take into account that (1) aggregate variables are determined by a variety of aggregate disturbances, and (2) monetary policy has both exogenous and endogenous elements. This will help us disentangle the behavior of output or investment that is due to exogenous monetary policy disturbances, monetary
policy variation due to asset price movements, and the independent influence of asset prices.

To do this I follow along a line of researchers who have studied U.S. and Japanese monetary policy in the context of reduced-form VARs [see for example Sims (1992), Bernanke and Blinder (1992), Christiano, Eichenbaum, and Evans (1994), Yoshikawa (1993)]. My objective is to specify a VAR which can be used to disentangle monetary policy from other influences. The conventional approach to this problem involves selecting a policy target variable and specifying a reaction function for the monetary authority which depends on current and lagged values of endogenous variables. In deciding which variables to include in my VARs and the manner in which orthogonalizations are conducted, I have tried to incorporate both the information from my short lesson on recent economic history in Japan and the work of scholars who have used this kind of analysis to study Japanese monetary policy before me.

I focus my discussion on two types of quarterly VARs estimated over the period 1964:1 to 1994:4 with four lags. The first type, stock price VARs, include a measure of the real stock price, denoted PK (International Financial Statistics variable FPS6JP divided by the GDP deflator), and the second type, KW VARs, do not. I consider VARs of both types with one expenditure component, GDP, later denoted Y, and with two expenditure components, Y and plant and equipment investment (I). The Y-VARs help address a key unresolved question from K&W's paper. Namely, what is the composition of the output innovations in their empirical models?

In addition to Y, the other variables considered in all the VARs analyzed below are net exports (NX), GDP deflator inflation (INFL), the call rate (R), and the velocity of narrow money (VE). I include NX because there is evidence to suggest this was a key influence on the conduct of policy over the sample period (see Yoshikawa, 1993). The variable INFL is included because, at least since the first oil shock, the Bank of Japan is generally regarded as being quite sensitive to its innovations. I follow Yoshikawa in using the call rate because it appears to be the obvious

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4. The lag length is sufficient to guarantee that the null hypothesis of no serial correlation cannot be rejected at conservative significance levels for all the estimated reduced-form residuals in all the VARs discussed here. Like K&W, I include a dummy for the floating-exchange-rate period. The results are not sensitive to this.

5. Including land prices in the VARs does not influence the results appreciably. This is probably not surprising, given measurement issues.

6. Narrow money velocity equals nominal GDP divided by the IFS measure of the sum of currency outside banks and demand deposits other than those of the central government. Variables PK, Y, I, and VE are in logs, INFL is the log first difference of the GDP deflator, NX is the log difference between exports and imports measured on a GNP basis, and R is the log of the gross call rate.
choice for the monetary policy target variable. Finally, velocity is included for two reasons. First, it is an attempt to capture financial innovations, including ongoing regulatory intervention, which are a potentially important factor in the behavior of asset prices. Second, its innovations account for 14% of the unconditional variance of Y, the largest contribution aside from own innovations to Y.

Consider the KW type Y-VAR first. The Wold causal (Choleski) ordering I work with is NX, Y, ΔP, R, and V. Generally, the ordering does not appear important for the results reported here and below, although I

7. Yoshikawa analyzed Japanese monetary policy and the Japanese monetary transmission mechanism using VARs estimated from monthly data on the call rate, the growth rate of industrial production, CPI inflation, and net exports.
8. Notice that the yen/dollar exchange rate is not included in the VARs even though it is often cited as a key determinant of monetary policy. Including it in the analysis does not change the main findings.
9. Implicit in this ordering is the assumption that lagged values of all the variables appear in the monetary policy authorities’ reaction function for R, and contemporaneous values only of the variables in front of R in the ordering.
have not considered all possibilities. For this case I proceed directly to the historical decomposition of Y plotted in Figure 2. The solid lines in the plots here are the actual values for Y over the period 1987:4 to 1994:4, and the short-dashed line is the forecast as of 1987:3. The long-dashed line is the contribution of the indicated variable’s orthogonalized innovation on Y. Recall that these capture all of the impact of the innovations on the variable being decomposed relative to the expected path assuming no innovations. Immediately we see from the “Effect of Y on Y” plot that output innovations identified with this model roughly speaking account for the recession themselves, via the estimated lag structure in the model of course.

If I is included in the VAR, the decomposition for Y is almost identical (not shown). In Figure 3 I display the decompositions for I for such a VAR with I included after Y in the ordering. Notice the strong role...
played by output innovations in accounting for investment. Exogenous monetary policy plays a role here in dragging investment down, as do I innovations, especially leading up to onset of the recession. Since output innovations and interest-rate innovations play a large role here in the determination of investment over the recent recession, these results could be construed as being generally supportive of K&W's conclusion. However, they suffer from the problem shown in Figure 2 that the recession in output remains unexplained, as in K&W.

Now consider the stock price, Y-VAR. This VAR plays a central role in the analysis, so it is useful to get some sense of the quality of the identification. For this purpose, consider the implied impulse response functions with Monte Carlo one-standard-error bands for orthogonalized R innovations in Figure 4 and PK innovations in Figure 5. The responses to the monetary disturbances conform generally with standard priors on these responses, with the exception of the behavior of inflation, which exhibits the Sims (1992) price puzzle. Here we see that inflation does come down after the call rate peaks in response to an exogenous mone-
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Figure 5 ORDER: NX Y INFL PK R VE.

Figure 6

etary disturbance. The delayed response of inflation may just reflect the typically slow response to inflation by the Bank of Japan in the sample. In Figure 5 we see that PK-innovations have a transitory impact on PK. The other responses seem sensible. Notice the delay in the response of R to these innovations as well. Roughly, the impulse response functions for the other innovations can be explained in an internally consistent way (these are not shown).

In Figure 6 I display the historical decomposition of R, the assumed monetary target, for the asset price Y-VAR. In the period before Mr. Mieno’s tenure at the central bank began, the interest rate appears determined by its own innovations. Relative to what policy would have been without monetary innovations and only output innovations, the interest rate is very low, consistent with the market view of loose monetary policy. When the governorship of the Bank of Japan changes, monetary innovations take interest rates higher, but eventually it is the accumulated effects of PK innovations which drive the call rate to its peak. PK innovations contribute much to keeping interest rates high even as ex-
ogenous policy is pulling them down. Broadly speaking, then, the historical decomposition of $R$ appears consistent with the recent economic history of Japan. Figure 7 shows the decomposition of $PK$. Notice that, with the exception of minor influences due to inflation innovations and monetary policy disturbances, the real stock price seems determined almost entirely by its own innovations. This supports the view that stock price inflation around this time is exogenous in the sense that it is not determined by the historical relationship between $PK$ and its underlying fundamentals.

Now for the main empirical finding of this comment, which is contained in Figure 8. This shows the decomposition of $Y$ in the stock price $Y$-VAR. Notice that in contrast to the KW type, $Y$-VAR output innovations alone would drive output to a peak at a year later than the realized level of output: the recession in output is not explained by output alone. Three variables contribute to the timing of the recession by exerting a
negative influence on output after it peaks: \(NX, PK,\) and \(R\). The influence of \(R\) is minuscule, meaning that exogenous monetary disturbances only play a small part in the timing of the recession. The influence of \(PK\) easily dominates \(NX\). Its peak negative contribution is more than five times the peak of \(NX\) negative contribution to output, and in no period after the onset of the recession does \(NX\) dominate the influence of \(PK\).

An attempt to disentangle the influence of \(PK\) on \(Y\) via endogenous monetary policy and an independent influence via the internal propagation mechanism of the estimated model is given in Figure 9. This figure is the "Effect of \(PK\) on \(Y\)" plot from Figure 8 with one additional (dotted) line. The line convention in this figure is consistent with the previous figures. Here the additional line shows the implied value of output if \(R\) follows the expected path as shown in Figure 6. Thus interest rates do not respond to \(PK\)-innovations for this experiment. Notice that for this case the implied level of \(Y\) is above the long-dashed line, which shows
the effect with policy influence. This suggests that the endogenous response of policy to innovations in PK is important for the behavior of output at the start of the recession. The common shapes of the implied output plots suggest an additional independent influence of PK on Y. Figure 10 shows the investment decomposition for the stock price VAR including both Y and I. Notice the strong leading influence of PK-innovations on investment.

To summarize, apparently exogenous movements in stock prices appear to have exhibited a strong influence on monetary policy in the periods leading up to the onset of the recession. Innovations in PK, via the response of monetary policy, appear to account for much of the behavior of output at the beginning of the recession and the behavior of investment leading up to and during the recession. These results seem consistent with events as they were reported in the financial press at the time. They support the conclusion that monetary policy was an impor-
tant factor in determining both the timing and the severity of the recent recession. The independent influence of PK-innovations adds to the impression that the behavior of stock prices is also important for understanding the recession.

How do these findings relate to the main conclusion arrived at by K&W? The findings do not contradict the conclusion that output and cost of capital movements are largely responsible for the behavior of investment, and in this sense they should be viewed as complementary to K&W's work. The fact that endogenous policy as estimated from past data accounts for a considerable portion of the fall in output (and investment) is also consistent with the view that the recent recession is not anomalous relative to historical experience. The fact that movements in PK are estimated to be largely exogenous, and appear to exert an independent influence on output and investment, is not consistent with this view. In addition, the findings suggest an explanation for the movements in output and in turn the behavior of investment which is absent from K&W's paper. Thus the results may well add to our understanding of the recent recession in Japan.
Figure 10

Effect of NX on I
Order: NX Y I INFL PK R VE

Effect of PK on I
Order: NX Y I INFL PK R VE

Effect of Y on I
Order: NX Y I INFL PK R VE

Effect of I on I
Order: NX Y I INFL PK R VE

Effect of INFL on I
Order: NX Y I INFL PK R VE

Effect of R on I
Order: NX Y I INFL PK R VE

Effect of VE on I
Order: NX Y I INFL PK R VE
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Comment
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The late 1980s were boom years in Japan. GDP growth and fixed investment rates rose to their highest levels since the 1973 oil shock. At the same time, asset prices rose dramatically: stock prices and land prices nearly tripled from 1985 to 1990.

The early 1990s were much different. GDP growth and fixed investment slowed. Stock prices fell by about half, and land prices fell by about a quarter. The Japanese economy of the 1980s—once thought to be a reflection of Japan’s extraordinary economic strength and growth prospects—came to be known as the “bubble economy.”

One of the notable aspects of this recent experience is the extent to which economic growth and investment moved in tandem with asset prices. Of course, it should not be surprising that the two moved together, because asset prices rationally reflect current and future growth prospects (at least partially). But the extreme movements in asset prices led some observers to argue that they may have caused some of the changes in economic growth rather than just reflected those changes.

In particular, given that many companies in Japan own land and stock in other companies, they realized enormous capital gains on those holdings during the late 1980s. These unrealized capital gains served as collateral which enabled Japanese companies to borrow at low interest rates, easing credit constraints and promoting investment and growth. The decline in asset values had the opposite effect in the bust of the 1990s. Of course, this explanation only makes sense if capital markets
are imperfect and firms are credit-constrained in their investment. Thus, with imperfect capital markets, growth affects asset values (through the standard link), but asset values also affect growth. Models along these lines have been presented by Kiyotaki and Moore (1995) and Kashyap, Scharfstein, and Weil (1989).

Kiyotaki and West take a step back and ask the question: Can neoclassical models of investment—in particular the flexible accelerator model in which interest rates and adjustment costs are all that matter—explain the movements in investment over this period? Their answer is yes; one need not cook up more complex models of investment based on imperfect capital markets to explain the recent business cycle.

At one level I agree with Kiyotaki and West. They have done a thoughtful and thorough job of showing that the flexible accelerator model is a rather good empirical model of fixed investment in Japan during the last four decades. However, this evidence does not amount to a rejection of collateral models, because the empirical specification of the collateral model looks much like that of the flexible accelerator model. The collateral model suggests that increases in cash flow and asset values have positive effects on investment. The flexible accelerator model says that increases in output should be associated with increases in investment (due to adjustment costs) and that lower interest rates should increase investment. But output and cash flow are highly correlated, so the empirical effect of output could simply be proxying for cash flow in a collateral model. And since asset prices are inversely related to interest rates—during the boom years interest rates were low, and during the bust years they were high—the negative effect of interest rates on investment could simply be capturing the effect of asset prices on investment in the collateral model. Thus, while it’s true that the flexible accelerator model is a great empirical workhorse, it still does not tell us whether adjustment costs and interest rates drive the results or whether cash flow and asset values drive the results.

At this point, one might ask whether it is important to distinguish between these models. That is, if the flexible accelerator model does the job, why not just use that and forget about the collateral model? I think this is not a good idea, for two reasons. First, the two models have very different efficiency implications. The collateral model implies that during downturns investment inefficiencies rise, while the flexible accelerator model implies that firms are always at the first best. Thus, policies that have no (or possibly negative) effects on welfare in the neoclassical model can be welfare-enhancing in the collateral model. For example, procyclical corporate taxation would have no effect in the neoclassical model, but might raise welfare in the collateral model (because it pro-
vides more cash flow to firms in downturns and enables them to increase investment).

A second reason why it is important to distinguish between the two models is that it helps us understand the distributional effects of downturns. In the neoclassical model, the only effect is through a rise in interest rates which should affect all firms equally. But in a collateral model the firms that are most hurt by the downturn are those that find external finance particularly costly—most likely small and young firms. Sectors of the economy with a large number of such firms are likely to be the most adversely affected by a downturn.

Finally, as argued by Bernanke and Blinder (1988) and Kashyap and Stein (1995), monetary policy has very different effects in the two models. In the neoclassical investment model, monetary policy only affects investment through interest rates. However, in the collateral model, monetary policy affects the costs of making loans if, as Kashyap and Stein argue, banks are also credit-constrained. Credit-constrained firms that relied on banks for funding may then find it difficult to raise alternative sources of funding, which may then induce them to cut investment. This is a very different channel through which monetary policy affects output.

I will conclude by making a point that betrays my own microeconomic bias. It seems to me that there is a limit to what the macroeconomic data can tell us, and, in the end, the only real hope is to use micro, firm-level data. There is now a large literature that examines the differential response of firms to macro shocks. The idea is that some firms face significant difficulties raising external finance, so that a drop in their cash flow or collateral should have a more negative effect on their investment than would a drop in cash flow or collateral of a firm that can more easily adjust by raising external funds. In this spirit, Fazzari, Hubbard, and Petersen (1988) showed that low-dividend-paying firms—which they argue are likely to face greater difficulty raising external capital—seem to cut investment more in response to cash-flow reductions than do high-dividend-paying firms. In the context of Japan, Hoshi, Kashyap, and Scharfstein (1991) showed that firms that are part of a keiretsu—and thus have close ties to banks, their principal suppliers of capital—are less prone to cut investment when cash flow falls. In both datasets, the difference between constrained firms and unconstrained firms is most pronounced during recessions. There are numerous other studies with similar results, some more convincing than others. [For a particularly clever approach to this problem, see Lamont's (1996) paper.] On the whole, I believe that the effects of collateral are real and that they have meaningful macroeconomic implications.
Olivier Blanchard asked the authors to clarify their interpretation of the 1991–1994 results for investment and the user cost of capital. He noted that standard theory predicts that a low user cost will be associated with a high rate of investment, but the authors seem to be arguing for low user cost as a reason for declining investment. Blanchard also found it surprising that the measured cost of capital had been found to decline, since the crash of the Japanese stock market during this period would have implied a rising dividend/price ratio. Finally, Blanchard noted that, although the combination observed in Japan of an upward trend in the capital–output ratio and a downward trend in the relative price of investment goods is consistent with the theory, this relationship is not very robust across countries; in particular, many industrialized countries have seen declines in both the relative price of investment goods and the capital–output ratio, at least since the late 1970s. He suggested that it would be useful to try to reconcile this model with developments in the European countries, for example.

Responding, Kenneth West agreed that, all else equal, a low user cost of capital should indeed be associated with high investment; and he pointed to Table 10 in the paper, which indicates that the estimated level of the desired capital stock did increase. However, he argued that, because of adjustment costs, a decline in the cost of capital will have
important effects on realized investment only if it is expected to persist; and that, historically, the cost of capital in Japan had shown significant mean reversion. In this particular episode, West added, potential investors may have seen the decline in the cost of capital as due largely to monetary policy, which could have increased the perceived likelihood that it was a transitory phenomenon. Following up this comment, Andrew Abel suggested that the authors should point out explicitly that their estimated cost-of-capital effects would change once policies leading to permanent changes in the cost of capital were considered; he expressed interest in seeing what the Kiyotaki–West estimates would imply for such changes, due for example to a change in the tax law.

Addressing Blanchard’s question about the dividend/price ratio, West noted that in their paper the equity-financed portion of the cost of capital is calculated as a constant premium over the cost of short-term debt. West agreed that this methodology implies that the gyrations of the stock market do not enter the cost of capital, but he argued that what matters for the purposes of estimating investment equations is the ex ante, not ex post, return on the market.

James Stock suggested that more extensive stability analyses (using, e.g., a Quandt-type likelihood-ratio test) would be desirable, especially for the capital accumulation equation. He also remarked that a significant number of the paper’s conclusions rest on a particular Choleski decomposition, for which the authors have provided no particular justification. West agreed in principle about the value of testing for stability, but said that for reasons of parsimony they preferred to run all equations over the same sample periods. He defended the ordering used in their VARs as being consistent with the conventional approach to studying investment, which is to de-emphasize simultaneity issues and instead to explain investment conditional on fundamentals, such as output and the cost of capital.

Several participants elaborated on David Scharfstein’s point in the formal discussion, that a model in which investment spending depends on the quantity of borrowers’ collateral could explain Japanese investment as well as the authors’ neoclassical model. Simon Gilchrist said that Kiyotaki and West had imposed insufficient structure to discriminate between the collateral theory and their model; he pointed out that, if collateral effects were a normal part of the Japanese boom-bust cycle, these effects would be reflected in the reduced-form coefficients. He suggested disaggregation by sector as a means of identifying collateral effects. Ben Bernanke noted that there are important differences between the q-theory and the collateral theory which might be exploited in empirical analysis. Some of these relate to the traditional distinction
between average and marginal $q$; investment is related to the former by the collateral theory and to the latter by the neoclassical $q$-theory. He cited Owen Lamont's work on firms with oil and non-oil subsidiaries as an example of research that could distinguish the two approaches; changes in oil prices should affect investment in the non-oil subsidiaries (as Lamont found) according to the collateral theory, but not according to the $q$-theory. In the Japanese context, Bernanke said, one might apply a similar strategy by studying the effects of land prices on the investment of land-holding firms.

Responding to Gilchrist and Bernanke, several people expressed skepticism that the collateral-based and neoclassical theories could be cleanly distinguished empirically. Zvi Griliches noted that the distinction between average and marginal $q$ was muddied in practice by well-known problems in measuring the latter, which depends on the value of future investment opportunities rather than on the current assets of the firm. Abel placed the issue in the broader context of the debate about whether complete-markets or incomplete-markets models provide a better approximation to reality, suggesting that this was a debate that was unlikely to be resolved purely on empirical grounds. Matthew Shapiro and Robert Barsky each discussed the possibility that expectations about future profitability and growth had driven the large fluctuations in both investment and asset values, and noted the difficulty faced by the econometrician in establishing whether those expectations, although unrealized ex post, were unreasonable ex ante. West summarized the discussion by characterizing the paper as showing that a neoclassical specification could explain the Japanese investment data, but not as a definitive rejection of incomplete-markets alternatives such as the collateral theory.

Abel then focused on the fact that, according to the authors' calculations, $q$ is not infrequently negative in the Japanese data, which seems to imply serious measurement error. He thought that analyses of investment in Japan using micro-level data might therefore be more reliable. West replied that finding negative values for $q$ is common in studies of Japan, including micro-level studies: He cited a careful panel data analysis by Takeo Hoshi and Anil Kashyap which found the measured value of $q$ to be negative in some 25% of cases. Nobuhiro Kiyotaki expressed the view that mismeasurement of $q$ is indeed an important issue: For the Japanese case, a major problem is that only a relatively small part of the nonfinancial corporate sector (accounting for about 12% of employment) is publicly traded, so that NIPA data and other statistics largely reflect book values (which are gross underestimates) rather than market values. The lack of market-based valuations, plus analogous problems in obtaining realistic land values, help explain why $q$ is so often found to be negative.