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# DISTRIBUTIONAL EFFECTS OF A SCHOOL VOUCHER PROGRAM: EVIDENCE FROM NEW YORK CITY 

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Distributional Effects of a School Voucher Program: Evidence from New York City
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#### Abstract

We use quantile treatment effects estimation to examine the consequences of a school voucher experiment across the distribution of student achievement. In 1997, the School Choice Scholarship Foundation granted $\$ 1,400$ private school vouchers to a randomly-selected group of low-income New York City elementary school students. Prior research indicates that this program had no average effect on student achievement. If vouchers boost achievement at one part of the distribution and hurt achievement at another, zero or small mean effects may obscure theoretically important but offsetting program effects. Drawing upon prior research related to Catholic schools and school choice, we derive three hypotheses regarding the program's distributional consequences. Our analyses suggest that the program had no significant effect at any point in the skill distribution.


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## Introduction

Excellence and equity goals motivate much of American educational policy. These two goals are not always mutually reinforcing. Some educational policies and practices boost average academic achievement even as they broaden educational inequalities (c.f. Arygs, Rees, \& Brewer 1996). Others have little effect on average achievement but narrow inequalities (c.f. Hong, et al. 2012). The twin goals of excellence and equity should lead policy-makers to be interested in both the average effects of educational policies and their distributional consequences. But although developmental science suggests that many interventions may have heterogeneous effects (Duncan \& Vandell 2012), much educational evaluation research focuses on the estimation of mean treatment effects either for the population at large or for particular subgroups of interest.

In this paper we use a distributional approach to estimate the effects of a school voucher experiment, in which low-income elementary school students in New York City applied for a $\$ 1,400$ private school voucher. Nearly 80 percent of the students who were randomly selected from the pool of eligible applicants to receive the voucher used their vouchers to enroll in private schools (Mayer et al. 2002). However, there is very little evidence to suggest that this voucher offer influenced mean student achievement.

This paper makes three main contributions to the research on vouchers and school choice: First, we argue that estimates of the mean effects of vouchers may obscure theoretically and practically important effects across the distribution of achievement. In particular, we demonstrate that distributional analyses make it possible to test hypotheses that are prominent in the literature on school choice regarding the effects of educational
vouchers on skills inequality. Second, we estimate the effects of the NYC voucher experiment across the distribution of student achievement, as measured by the Iowa Test of Basic Skills (ITBS). Third, we situate NYC voucher experiment participants in the national distribution of student achievement. Doing so provides important context for understanding the external validity of the findings reported here and may inform interpretation of the findings from other voucher experiments.

Our findings are largely consistent with a no-voucher-effects hypothesis. We find some evidence to suggest that the New York City voucher offer had a small negative short-term effect on math achievement at the top of the distribution. However, this effect fades out rapidly and is not precisely estimated. Furthermore, the measured effect of the New York City voucher offer is close to zero throughout the bulk of the study sample's math and reading achievement distribution.

## School choice and the distribution of achievement

Arguing that traditional public schools are monopolistic and inefficient, school voucher proponents aim to create more vibrant educational marketplaces. By broadening the educational choices available to parents and students and creating incentives for schools to improve, vouchers and other school choice programs aim to boost educational outcomes for students who might otherwise have no choice but to enroll in low-quality public schools (Chubb \& Moe 1990; Friedman \& Friedman 1980).

School reformers have launched a handful of voucher programs across the U.S. over the past two decades in an attempt to demonstrate the effectiveness of this approach. In 1997, the School Choice Scholarships Foundation initiated one such program in New York City, offering three-year scholarships worth $\$ 1,400$ a year to a randomly selected
group of low income children then in grades K-4. This program's random assignment design makes it possible to distinguish the effects of a voucher offer from the potentially confounding characteristics of families who self-select into voucher programs. ${ }^{1}$

Mathematica Policy Research (MPR) and the Harvard University Program on Education Policy collected enrollment and achievement data from students in the treatment and control groups.

Analyses of the New York City voucher experiment data clearly indicate that vouchers influence school choice. Students randomly selected to receive a voucher were several times more likely than their peers in the control group to attend private schools. More than three-fourths of voucher recipients used their vouchers to enroll in private schools at some point in the program, and more than half enrolled in private schools for the entire three-year scholarship period. 85 percent of the students who used the voucher enrolled in Catholic schools, where tuition estimates ranged from \$1,200-\$2,500 in 1997 (Hartocollis 1997; Steinberg 1997a; 1997b). Parent surveys clearly indicate that those who received an offer of a voucher had higher levels of satisfaction with their children's schools, compared to those in the control group. Voucher lottery winners - and particularly those who actually used their vouchers to attend private schools - enrolled in smaller schools with smaller classrooms, more computer labs, and more after-school

[^0]programs than their peers in the control group (Mayer et al. 2002).

But to date there is little evidence to suggest that these school resources translated to higher levels of achievement for voucher recipients. While the New York voucher experiment has inspired a vigorous debate about appropriate methods for analyzing experimental data (Barnard et al. 2003; Krueger \& Zhu 2004a; Krueger \& Zhu 2004b; Peterson \& Howell 2004), the results of various analyses of the mean effect of the voucher program on student achievement are strikingly consistent. Voucher recipients score no higher, on average, than students in the control group on standardized measures of math and reading achievement (Krueger \& Zhu 2004a; Mayer et al. 2002; Howell et al. 2002). Voucher programs implemented in other contexts yield somewhat more mixed results. Evaluations of voucher offers in Charlotte, NC (Cowen 2008; Greene 2001), Milwaukee, WI (Rouse 1998), Washington, DC (Howell et al. 2002; Wolf et al. 2013), and Chile (Lara et al. 2011) provide evidence of modest positive average effects on student achievement. (Cowen 2012 provides a comprehensive review of the existing literature on voucher program achievement effects.)

The evidence that the NYC voucher experiment had no average effect does not mean, however, that it had no effect at all. In fact, some evidence suggests that the program had positive effects on African American students' achievement (Barnard et al. 2003; Howell et al. 2002; Mayer et al. 2002; Peterson \& Howell 2004). Furthermore, instrumental variable analyses that use the randomized voucher offer to estimate the causal effect of private school enrollment suggest that private schools particularly benefit African-American students (Howell et al. 2002). While these findings are highly sensitive
to the measurement of student race (Krueger \& Zhu 2004a, Krueger \& Zhu 2004b) ${ }^{2}$, they may indicate that small average effects of voucher programs mask larger heterogeneous voucher program effects for particular types of students. Furthermore, recent studies indicate that both the NYC and the Washington, DC voucher program have larger longrun effects on student attainment than one might expect given their short-term
achievement effects (Chingos \& Peterson 2012; Wolf et al. 2013). Distributional analyses could help make sense of these findings, if voucher receipt helps students at the bottom of the skills distribution acquire a baseline level of skills and successfully progress through their educational career to high school graduation.

In this paper, we investigate the possibility that weak average effects of vouchers disguise larger (and possibly contradictory) voucher program effects for high or low achieving students. We test three competing hypotheses regarding the effects of voucher programs on student achievement.

## (1) Common School Hypothesis: Vouchers mitigate inequality by boosting achievement primarily at the bottom of the distribution

This hypothesis is grounded in the literature on the effects of Catholic schools.
Nearly all of the students in the NYC experiment who used a voucher to attend a private school enrolled in a school with a religious affiliation, and 85 percent enrolled in Catholic

[^1]schools (Howell, Wolf, Campbell, and Peterson 2002). Catholic schools are typically smaller than competing public schools, their curricula are often relatively undifferentiated, and they are often situated in social networks that allow parents and teachers to more closely monitor student achievement and behavior. Additionally, Catholic schools have greater control than public schools over the composition of their student body, since they can admit students selectively and expel students at will. There is some evidence to suggest that enrolling in a Catholic school is particularly beneficial for poor, minority, low-performing and otherwise at-risk students (Coleman \& Hoffer 1987; Evans \& Schwab 1995; Greeley 1982; Hoffer, Greeley \& Coleman 1995; Neal 1997; Morgan 2001), although there have also been concerns raised about selection biasing some of these comparisons.

By providing a mechanism for students to opt out of neighborhood public schools and into Catholic and other private schools, voucher experiments attempt to make the positive achievement effects associated with Catholic schools more broadly available. Assuming that estimated Catholic school effects are both causal and generalize to the schools that voucher recipients chose, the "common school hypothesis" suggests that voucher school programs will have positive effects at the bottom of the academic achievement distribution, but not at the middle or the top of the distribution.
(2) Stratifying Hypothesis: Vouchers exacerbate inequality by boosting achievement primarily at the top of the distribution of applicants

In contrast, the "stratifying hypothesis" suggests that voucher programs magnify educational inequalities. Voucher program advocates take it for granted that parents use school choice to maximize their children's educational success. In practice, however,
many parents make school choice decisions based on the convenience of the school's location, its disciplinary style, and its religious affiliation (e.g., Elacqua, Schneider, \& Buckley 2006). Hastings, Kane, \& Staiger (2005) hypothesize the effects of voucher programs are contingent on the type of the school choices that families make. For students whose families make school choices on the basis of academic quality, voucher programs may have positive effects on achievement. But for students whose families make school choices based on other factors, vouchers may have zero or negative effects on achievement. If educational preferences vary with student academic achievement, voucher programs may boost achievement at the top of the achievement distribution, even as they have no effect or even hurt achievement at the bottom of the achievement distribution.

## (3) No-Effects Hypothesis: Vouchers have no effect across the distribution

While each of the prior two hypotheses are theoretically viable, perhaps the most common-sense hypothesis based on the results of earlier analyses of New York City voucher data is that vouchers simply do not influence the distribution of achievement because vouchers like these do not have very much impact on student achievement. For many students, the voucher program may have amounted to a weak treatment. It did little to change students' home or neighborhood life. Furthermore, the extent to which it influenced the quality of schools to which students were exposed is debatable. Although many voucher recipients used their vouchers to enroll in private schools, the $\$ 1,400$ stipend that the voucher likely provided few students with access to New York City's elite private schools; most of which charge considerably higher tuition levels and have competitive admissions. Rather, most voucher recipients likely attended inexpensive
private schools in their own neighborhoods. If these schools do not differ substantially from the neighborhood public schools that students would have otherwise attended, or if family and neighborhood factors trump the effects of schools on achievement for these students, voucher receipt may have had no effect on either the mean or the distribution of student achievement.

In this paper, we use quantile treatment effect (QTE) estimation to test these competing hypotheses. This technique, which is not widely used in educational research, provides unique insights into the ways in which the treatment influences the distribution of student achievement, making it possible to explicitly investigate this intervention's consequences for educational inequality.

## Data: The New York City School Choice Scholarship Program

The New York City School Choice Scholarship Program (NYCSCSP) was a three year private school choice randomized experiment. Randomization procedures are described in detail in Hill, Rubin, and Thomas (2000). As noted above, low income students (students qualified for free school lunch) currently in grades $\mathrm{K}-4$ were eligible to apply for vouchers of $\$ 1,400$ to be used towards private school tuition for subsequent school years. Initial applications were received in the spring of 2007 from over 20,000 students, with roughly 5,000 of them meeting the eligibility requirements. Of these, approximately 2,600 students were randomized at the family level to treatment and control using two methods of random assignment from separate lottery rounds.

Students from 1,000 families were randomized using a Propensity Matched Pairs Design (PMPD) in the first lottery and a Stratified Block design was used for students from an additional 960 families from a second series of lotteries. The PMPD design was
used for randomization in the first lottery because the number of eligible applicants far exceeded the money available to follow up on all of them. Instead of a randomly selected group of control students, students were selected based on propensity score matching relative to the group of students who were randomly assigned to the treatment condition. Variables used in the estimation of the propensity score model are described in Hill et al. (2000) and Krueger and Zhu (2004a), and included family size and whether the children attended above or below-median test score schools as the two most important variables for matching. Matching was done using a Mahalanobis "nearest neighbor" metric for selecting control families.

The Stratified Block design was created using screened applicants that were invited to a series of four baseline data collection sessions. Invitation to these sessions was weighted such that roughly $85 \%$ of the invitees were from schools with below-median test scores. Families were assigned to treatment and control conditions from each of the testing sessions, creating four stratified blocks.

As described in Krueger and Zhu (2004a), from these two sampling methods, 30 mutually exclusive "random assignment strata" were created from: 5 lottery blocks (1 PMPD block plus 4 stratified blocks) times 2 school types (above- or below-median test scores) times 3 family size groups (1, 2 , or 3 or more students). Within these original strata, assignment is random. Krueger and Zhu (2004a) detail the discovery by Mathematica that some families misreported their family size and were placed in the wrong strata. While revised strata were created and used by Howell and Peterson (2002) and Mayer, Peterson, et al. (2002), because assignment was random within the original strata, we follow Krueger and Zhu's use of the original, rather than the revised strata.

Krueger and Zhu note that differences in results between the two sets of strata are very minor.

Krueger and Zhu also identified two issues with sample weights that were subsequently revised by Mathematica in 2003. ${ }^{3}$ When we attempt to replicate others' findings, we are constrained to either use these revised sample weights, which adjust for non-response, or use no weights. The combined effect of using the original strata and having only the revised weights makes it so that we are unable to exactly replicate any work published prior to Krueger and Zhu (2004a), including Mayer, Peterson, et al. (2002). Thus, replication attempts are primarily concentrated on Krueger and Zhu (2004a) and Jin and Rubin (2009), both of which use the original strata and revised weights.

Baseline student achievement in reading and math was collected for nearly all students, except for applicants in kindergarten, using the Iowa Test of Basic Skills (ITBS). We present results using the National Percentile Rankings (NPR) of these scores ${ }^{4}$. Initial examinations of the distribution of these baseline ITBS scores revealed unexpected differences between treatment and control at the top of the raw ITBS score distribution. Using percentile scores, meanwhile, we found similarly large differences at the bottom of the distribution. Taken at face value, these findings if statistically

[^2]significant would seem to indicate that the randomization procedure failed to generate balanced treatment and control groups.

However, upon closer examination, it became clear that the problem involved the coding of missing data, rather than the treatment assignment process. Figure 1 reports a histogram for baseline scores on the raw ITBS mathematics exam. As it indicates, a large number of students scored 99 on baseline tests in reading and math with the next highest score not exceeding $40 .{ }^{5}$ The distribution of all other baseline and post-tests in reading and math throughout the voucher study show a similar pattern (not shown). Furthermore, participants with a raw score of 99 have NPR scores and normal curve equivalent (NCE) scores of 0 . Communications with the ITBS's publisher indicate that zero is not a valid ITBS NCE score. While analyses reported below indicate that Krueger and Zhu (2004a) and Jin and Rubin (2009) do not set these cases to missing, we do so in our analyses. ${ }^{6}$
[Figure 1 about here]
We create inverse propensity score weights to adjust for nonresponse (including both nonresponse because the observation is missing test scores in the data and non-response from treating the invalid 99 raw scores as missing). First, we predict treatment status as a function of demographics, baseline scores when available, and whether the student has a missing math or reading test score or an invalid 99 math or reading raw test score, using a

[^3]logistic regression. We calculate a predicted probability of being in the treatment group $\hat{p}$, and then construct weights of $1 / \hat{p}$ for those in the treatment group and $1 /(1-\hat{p})$ for the control group. These weights balance the treatment and control group on these observable dimensions.

After accounting for the miscoded nonresponse by treating it as a missing value, roughly 31 percent of the NYC voucher respondents have missing tests in reading or math at baseline. Table 1 provides a detailed description of differences between treatment and control groups in various types of missing data. As the table indicates, there are small but statistically significant differences between the prevalence of missing data mistakenly included as valid in the treatment and control groups using the Mathematica weights (which were constructed while treating the miscoded nonresponse cases as valid data). In particular, students in the treatment group are nearly one-third or 2.1 percentage points more likely to have 99 values on the baseline reading test (although this difference is not statistically significant at the 5 percent level, $\mathrm{p}=0.089$ ). Students in the treatment group were less than half as likely or 3.9 percentage points less likely to have 99 values on the year 1 math test ( $\mathrm{p}<0.01$ ). Finally, treatment group students were 1.9 percentage points more likely to have invalid 99 reading scores in year 3 ( $\mathrm{p}=0.054$ ). As Panels C and D in Table 1 make clear, our inverse propensity score weights thoroughly account for these differences.
[Table 1 about here]
Table 2 indicates that the inverse propensity score weighted data are well balanced on the child's gender, race/ethnicity, gifted or special education status, the family's annual income being low, whether the family speaks English at home, maternal years of
schooling, whether the mother works full time, whether the mother was born in the U.S., whether the family receives some form of public assistance, whether the family has lived in their house for at least one year, and whether the mother is Catholic. Non-response to these questions was quite low, and the only variable with more than 10 percent of the observations missing information was whether the mother was U.S. born (in the 50 states or DC, but not Puerto Rico), with 13.2 percent missing. Checks for whether the share of observations missing information differed between the treatment and control groups suggest that the shares were not significantly different.
[Table 2 about here]
There are no significant differences between treatment and control on either the raw or percentile ITBS scores at baseline, further evidence of balance when the inverse propensity score weights are utilized.

## Methods

The analyses that follow take advantage of randomized assignment into the treatment and control groups in the New York City voucher experiment to estimate the mean effect of the voucher offer as well as its effect on the distribution of student achievement. The potential outcomes model provides a framework for estimation of the effects of a treatment. Each individual i has two potential outcomes, $\mathrm{Y}_{1 \mathrm{i}}$ and $\mathrm{Y}_{0 \mathrm{i}}$ (for our purposes, a test score). Person i has outcome $\mathrm{Y}_{1 \mathrm{i}}$ if assigned to the treatment group and outcome $\mathrm{Y}_{0 \mathrm{i}}$ if assigned to the control group. $\mathrm{D}(\mathrm{i})$ denotes the group that i is assigned to in a randomized experiment. If person i is assigned to the treatment group, then $\mathrm{D}(\mathrm{i})=1$, and if person i is assigned to the control group, $\mathrm{D}(\mathrm{i})=0$; the treatment effect on person i is defined as $d_{i}=Y_{1 i}-Y_{0 i}$.

## Quantiles, Average Treatment Effects, and Quantile Treatment Effects

Let Y be a random variable with a cumulative distribution function (CDF) $\mathrm{F}(\mathrm{y}$ ), where $\mathrm{F}(\mathrm{y})=\operatorname{Pr}[\mathrm{Y} \leq \mathrm{y}]$. Then, the qth quantile of the distribution $\mathrm{F}(\mathrm{y})$ is defined as the smallest value $\mathrm{y}_{\mathrm{q}}$ such that $\mathrm{F}\left(\mathrm{y}_{\mathrm{q}}\right)$ is at least as large as q (e.g., $\mathrm{y}_{0.5}$ is the median). Now consider two (marginal) distributions $\mathrm{F}_{1}$ (the CDF for the potential outcomes if $\mathrm{D}=1$ ), and $\mathrm{F}_{0}$ (the CDF for the potential outcomes if $\mathrm{D}=0$ ). We define the difference between the qth quantiles of these two distributions as $y_{q}=y_{q 1}-y_{q 0}$, where $y_{q d}$ is the qth quantile of distribution $\mathrm{F}_{\mathrm{d}}$.

The joint distribution of $\left(\mathrm{Y}_{0 \mathrm{i}}, \mathrm{Y}_{1 \mathrm{i}}\right)$ is not identified without assumptions. However, if program assignment is independent of the potential outcomes, the difference in means, or average treatment effect, $\mathrm{d}=\mathrm{E}\left[\mathrm{d}_{\mathrm{i}}\right]=\mathrm{E}\left[\mathrm{Y}_{1}\right]-\mathrm{E}\left[\mathrm{Y}_{0}\right]$, is identified because each expectation requires only one of the two marginal distributions. Similarly, identification of the marginal distributions implies identification of the quantiles $\mathrm{y}_{\mathrm{qd}}$, and thus identification of the differences in their quantiles, $\mathrm{y}_{\mathrm{q}}=\mathrm{y}_{\mathrm{q} 1}-\mathrm{y}_{\mathrm{q} 0}$. In this experimental setting, the quantile treatment effect (QTE) is the estimate of this difference in the quantiles of the two marginal distributions. For example, we consistently estimate the QTE at the 0.50 quantile by subtracting the control group's sample median from the treatment group's sample median. Graphically, QTE estimates are the horizontal differences in the CDFs of the outcome for the treatment and control groups.

As an example, we show the CDFs and QTE for the baseline math NPR scores in Figures 2 and 3. Figure 2 shows the CDF for the baseline math scores in the treatment and control groups. The horizontal distance between these CDFs at each point in the distribution is the quantile treatment effect (QTE) at that point or quantile. Figure 3
translates the horizontal differences in the CDFs to a QTE plot, showing the QTE (y-axis) for baseline math NPR scores at each percentile (x-axis), along with $95 \%$ confidence intervals (dashed lines), calculated by bootstrapping families within strata. Figure 3 shows that the bulk of the QTE point estimates are zero or close to zero for the baseline scores, and even when they are not, the confidence intervals clearly include zero. These QTE estimates indicate that the NYC voucher data are well balanced on baseline achievement after addressing weighting and missing data issues.
[Figures 2 and 3 about here]

## Findings/Results

## Revisions to previous mean treatment effect estimates

Since our preliminary analyses indicate that previous analyses using data from the NYC voucher experiment included a substantial amount of miscoded missing data, we begin by reconsidering the mean effect of the NYC voucher experiment. The first column of Table 3 summarizes the results of the Krueger \& Zhu (2004a) mean effect analyses, which includes students who scored zero on the ITBS National Percentile Ranking/99 on the raw test as non-missing cases, taken directly from Table 3b Panel 3. Their analysis indicated that the NYC voucher offer had no mean effect on student mathematics or reading achievement in any of the study's three years. In the second column of Table 3, we report our replication of the Krueger \& Zhu analyses, again including students with zero on the ITBS as non-missing cases. We are able to replicate Krueger \& Zhu coefficients precisely, with only minor differences in the standard errors that do not affect the (lack of) significance of the coefficients.

In the third column of Table 3, we report our estimates of the mean effects of the NYC voucher offer, estimated with out of-range values set to missing and using our inverse propensity-score weights. The results reported in the third column of Table 3 are substantively similar to the results in the prior two columns, indicating that the NYC voucher program had no mean effect on math or reading achievement in any of its three years. This finding suggests that the inclusion of students who were actually missing data on the ITBS due to 99 s but had a National Percentile Ranking score of 0 did not lead to substantively different conclusions about the lack of a mean effect of receiving a voucher in the NYC experiment but did in fact change the point estimates. This third column most accurately captures the true effect of the NYC voucher offer, since these results do not assume that students who were missing ITBS scores would have scored that the very bottom of the test's distribution.
[Table 3 about here]
Previous work by Mayer, et al. (2002) is not replicable with our restricted use data given that weights have been changed since Krueger and Zhu discovered they were being calculated incorrectly, but given Krueger and Zhu's ability to replicate their results and our ability to replicate the Krueger and Zhu results only while including the zeros, it seems likely that results from Mayer and colleagues in their 2002 paper and in their 2003 reply to Krueger and Zhu also include respondents with out-of-range zero ITBS scores in their analyses.

Finally, an additional set of papers, Jin and Rubin (2009) and Jin, Barnard, and Rubin (2010) also use the NYC voucher data in their analyses. Jin, Barnard, and Rubin do not present any basic descriptive statistics to reveal how they handled the missing
data, but Jin and Rubin do. Their Figure 1 presents box-and-whisker plots of total preand year 3 post-test scores of "complete cases" [their term] using the sum of the normal curve equivalent (NCE) math and reading scores. Near replication of these plots is only possible if the NCE scores of zero are treated as valid scores. Once excluded, the mean NCE score increases from 28.7 to 32.2 in reading and 22.7 to 27.6 in math at baseline and 32.6 to 33.7 in reading and 32.5 to 33.8 in math on the year 3 post-test. This suggests that results from Jin and Rubin, and possibly also Jin, Barnard, and Rubin, include out-ofrange test scores as valid data.

In sum, while our re-analysis corrects a data problem with earlier analysis of NYCSCP data, our findings are substantively consistent with earlier findings: the NYCSCSP had no mean effect on student math achievement overall (Howell et al. 2002; Krueger \& Zhu 2004a, 2004b). In supplementary analyses, we consider the consequences of our corrections for the debate about whether the NYC voucher experiment has a disproportionately positive effect for African-American students. While these analyses, reported in Appendix A, do not resolve this dispute, they do draw attention to the considerable skills overlap between racial categories in this sample.

## Quantile treatment effect estimates

Having established that the voucher program had no mean effect on student achievement, we next turn to the QTE, which provides an estimate of the effect of voucher receipt on the distribution of student achievement. Figure 4 shows the QTE for NPR math scores as of spring of the first year, Figure 5 shows NPR math scores for the spring of the second year, and Figure 6 shows NPR math scores for the spring of the third year. In each of these QTE plots, the horizontal differences in the cumulative
distributions of math NPR scores (y-axis) are plotted as a function of the percentile of the distribution at which this difference is calculated (x-axis). Thus, the x -axis ranges from 199 , and the y -value at each percentile q from 1-99 is the difference in the qth quantiles from the treatment and control groups. This difference represents the horizontal distance between the two CDFs for treatment and control.

Figure 4 shows the QTE for differences in math outcomes in year 1. For most of the distribution, there are few test score differences between the voucher recipients and the control students, as the solid line rarely deviates from the zero. This solid line shows the difference between the math scores of the treatment and control children at each percentile. For example, the $25^{\text {th }}$ percentile treatment score is 6 and the $25^{\text {th }}$ percentile control score is 6 , leading to a difference of zero NPR points, and the $75^{\text {th }}$ percentile treatment score is 34 and the $75^{\text {th }}$ percentile control score is 37 , leading to a difference of -3 NPR points. Figure 4 shows that the difference between the treatment and control students' scores at each point along the distribution of math scores remains fairly similar and close to zero. However, at the very top of the distribution, the difference between the treatment and control students becomes larger and negative. For example, the $91{ }^{\text {st }}$ percentile treatment score is 56 and the $91^{\text {st }}$ percentile control score is 60 , leading to a difference of -4 NPR points, and the $97^{\text {th }}$ percentile treatment score is 75 , the $97^{\text {th }}$ percentile control score is 84 , and the difference is -9 NPR points. This difference is significant at the 5 percent level at the $97^{\text {th }}$ percentile, where the confidence interval falls below the zero line, but it is not significant at even the $10 \%$ level for any other percentile, even though the treatment control difference indicated by the solid line is as low as -10 at the $95^{\text {th }}$ percentile. Thus, for the bulk of the distribution of achievement in math, effects
are zero, and we can rule out effects larger than 5 points at the $10 \%$ level for all but a small group of students.
[Figure 4 about here]
Figure 5 shows the QTE for math NPR scores at the end of year 2. As in year 1, in year 2 across most of the distribution, there are few differences between math scores for treatment and control students. The solid line showing the treatment and control differences is at or near zero, or negative but not significant at even the $10 \%$ level, for most of the distribution. At the $93^{\text {rd }}$ percentile, the difference between treatment and control is the largest, at -9 , but it is not significant at the $5 \%$ level as the confidence interval includes zero. Only the difference at the $99^{\text {th }}$ percentile is significantly different from 0 at the $5 \%$ level.
[Figure 5 about here]
Figure 6 shows the QTE for math NPR scores at the end of year 3. Differences in year 3 math scores are even less pronounced than in years 1 and 2 . For most of the distribution, the solid line displaying these differences is very near to the zero line--the difference between treatment and control scores is $-1,0$, or 1 for most of the distribution. There are some larger treatment and control differences above the $89^{\text {th }}$ percentile, with the largest, negative difference of -5 occurring at the $99^{\text {th }}$ percentile. However, none of these differences are statistically significant, suggesting that whatever negative effect emerged in the first two years has reverted to zero by the third year.
[Figure 6 about here]
We also estimated QTE using the same approach for reading at baseline and in years 1 through 3. In each of the three years, the test score differences between treatment
and control were at or near zero for the entire distribution. At no point in any year were these differences larger than three percentage points and at no point were the differences statistically significant. These results are reported in Appendix Figures 1 through 4.

## Discussion

These findings suggest that the NYC voucher experiment had no mean effect as well as no effect on the distribution of student achievement. At first glance, these findings seem to align closely with the predictions of the no-effects hypothesis. Before making this conclusion, however, it is important to consider the extent to which the distribution of achievement for students in the NYC voucher experiment reflects the distribution of students who might be eligible for vouchers if a similar school choice policy were implemented nationwide. Figure 7 places the NYC voucher program participants in the broader context of elementary school achievement across the United States by comparing the frequency of scores at various percentiles of the national distribution for baseline math for students in both the treatment and the control groups of the NYC voucher experiment with the frequency of math achievement scores for all students in the nationally representative Early Childhood Longitudinal Study, Kindergarten Cohort (ECLS-K) who attend Catholic schools as well as all ECLS-K students who come from low-income homes. ${ }^{7}$ This comparison illustrates the stark educational disadvantage that students eligible for the NYC voucher experiment and other poor youth face. While the achievement distribution for the NYC voucher students at baseline is skewed to the left

[^4]relative to that of poor youth nationwide, it is skewed even more sharply to the left compared to Catholic school students nationwide. This fact has potentially important implications for interpreting the results of the NYC voucher experiment. While our analyses clearly indicate that this treatment had no effect for this set of students at the bottom of the skill distribution, it provides little grounds for inference regarding the effects of voucher programs on a broader range of students. Since the NYC voucher study includes few students above the middle of a broader test score distribution, we cannot make strong statements about the effects of vouchers on students at the top of a broader distribution. Distributional analyses of less strictly means-tested voucher programs, such as the statewide programs operating in Indiana, Florida, Georgia, may thus produce very different findings higher up in the achievement distribution.
[Figure 7 about here]
Our findings suggest that the NYC voucher experiment had little effect across the distribution of student achievement, with the possible exception of small negative effects in math at the top of the distribution of students who sought vouchers which fade out over time. This may not be so surprising given the size of the intervention, although the offer had a very large effect on take-up of private school.

These small distributional findings mostly disconfirm both the Common School and Stratifying hypotheses. To the extent that vouchers are used to attend schools with a common curriculum, this seems to have had none of the anticipated positive effects for low-achievers. However, the math findings may be somewhat consistent with the Common Schools hypothesis because the high-achievers (relative to the average achievement in the experimental sample) experienced some small penalties from the
voucher offer. Similarly, any attempts made of the part of parents of high-achievers to pursue schools with challenging coursework did not lead to the hypothesized benefits or the stratification that voucher opponents feared. If anything, the distributional findings confirm our third hypothesis, that vouchers (at least of this magnitude) have no positive or negative effect for the majority of students to whom they were offered.

Put in the context of other interventions, such as KIPP or charter schools, perhaps these null-effects findings are not surprising. These interventions, which involve the development of entirely new schools, have significant impacts, but at much greater expense. For example, evaluations of KIPP Lynn in Massachusetts found that a year of enrollment in KIPP resulted in average effects of 0.35 SD in math and 0.12 SD in reading, with the students entering KIPP with the lowest baseline scores experiencing the largest effects (Angrist et al. 2010). Experimental evaluations of New York City and Boston charter schools found more modest effects on student achievement. In New York, the average effects were 0.09 SD in math and 0.065 SD in reading (Hoxby, Murarka, and Kang 2009). In Boston, the average effects were 0.18 SD in math and 0.09 SD in reading (Abdulkadiroglu et al. 2011). These results, which come from programs that were considerably more comprehensive than the vouchers we evaluate, likely serve as an upper bound of the possible achievement impacts that we might have observed. While the vouchers cost $\$ 1,400$ per child, a year of enrollment at KIPP costs approximately $\$ 13,000$ per student at some of the east coast KIPP schools (Angrist, Dynarski, Kane, Pathak, and Walters 2012). Thus, perhaps it would take a much larger financial investment to see effects that are comparable to a program like KIPP.

Despite the nearly null distributional findings, examining the New York voucher data with a distributional lens yielded other important information that would not have otherwise been discovered. We uncovered unusually large concentrations of test score responses with a raw score of 99 and an NPR or NCE score of 0 when early results returned unbelievably large group differences at the tails of the distribution. Only when we included the observations with these missing data codes in our analyses were we able to replicated previously published analyses of these data. While excluding these codes does not change the substantive conclusions from previous results, it reduces the magnitude of even the most favorable previous findings.

In sum, our distributional analysis of the New York City voucher experiment shows that the offer of a small voucher did little to influence student achievement. The possible exception is a small negative effect for a small group of high-performing students after the first two years of the program, but not after the third. The distributional approach taken here provides additional evidence suggesting that vouchers have a limited impact on student achievement.

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## Appendix A:

One important point of contention in prior analyses of the NYC voucher experiment involves variation in the effect of the voucher offer by race and ethnicity. Several studies find that the voucher offer had a small positive effect on the academic achievement of African-American recipients (Barnard, Frangakis, Hill, \& Rubin, 2003; Howell, Wolf, Campbell, \& Peterson 2002; Peterson and Howell, 2004). However, subsequent analyses suggest that the observed effects for African Americans are sensitive to the definition of racial and ethnic categories and hold only when controlling for students' initial characteristics/omitting students without baseline scores (Krueger \& Zhu, 2004a, 2004b).

This debate is potentially consequential in two regards: first, evidence of a unique positive voucher effect for African-Americans may point toward a strategy to mitigate persistent and troublesome black-white test score gaps. Second, several analysts have suggested that evidence of a unique positive voucher effect for African-Americans is consistent with the idea embedded in the "common school" hypothesis that vouchers may be particularly beneficial for students at the bottom of the skills distribution.

In this appendix, we reconsider the evidence regarding the extent to which NYC voucher offer effects vary by student race and ethnicity in light of the missing data and weighting corrections that we have implemented. In doing so, we note that it is important to consider several distinctive characteristics of the NYC voucher experiment sample. By design, all of the students who participated in the NYC voucher experiment were from low-income families in New York City. As Table 2 makes clear, the vast majority of these students were black or Hispanic. Within these racial categories, however, lies a
great deal of ethnic heterogeneity. 15 percent of students identified as African-American come from immigrant families, with origins primarily from the Caribbean. Similarly, the Hispanic category includes Puerto Rican and Dominican students (many of which may be phenotypically black). This heterogeneity helps to explain the debates concerning the definition of African Americans in these data. While Howell and Peterson categorize all students whose mother indicated her race at baseline as African American as AfricanAmericans, Krueger and Zhu additionally categorize children as African American if their mother indicated her race was African American in a subsequent data collection wave, if the mother indicated her race was other, but wrote in some combination of Black/African American and something else as her race (e.g., Black/Hispanic), or if the father indicated his race was African American in the baseline wave. Our analyses indicate that these definitions likely yield common racial categorizations for 90 percent of students in the sample, but disagree for 10 percent of students in the sample.

Appendix Table 1 summarizes the consequences of these questions of racial categorization for estimating the effect of the NYC voucher experiment on AfricanAmerican students' mathematics achievement. In first model of Panel 1 (column 1), we replicate Howell \& Peterson's estimates of the treatment effect for African-Americans (point estimates are identical, SEs nearly so). This analysis indicates that the voucher offer significantly improved black student math achievement in the study's first and third years. (This analysis yields a positive, but not statistically significant, treatment effect for black students in Year 2.) Similarly, in the first model of Panel 2 (column 1), we attempt to replicate Krueger \& Zhu's racial categorization scheme to estimate of the effects of the voucher offer for African-Americans. While this replication is not perfect (our sample
sizes are 1 observation off from their reported ones), ${ }^{8}$ it returns an estimate of the
African-American treatment effect that is very close to Krueger \& Zhu's published findings. Using the Krueger \& Zhu definition of African-American but treating the 99s as valid percentile scores of 0 , we find a positive significant treatment effect on Math scores in Year 1, but no effects in subsequent years.

The subsequent models (columns) in Appendix Table 1 consider the extent to which these findings are sensitive to corrections for out-of-range values on the ITBS and non-response weighting. Model 2 replicates both analyses with a sample that excludes students who have out-of-range values on the ITBS with the original MPR weights; Model 3 replicates the Howell \& Peterson and Krueger \& Zhu analyses on the original sample (including students who have out-of-range values on the ITBS as non-missing zeros) with our inverse propensity score weights; and model 4 replicates both analyses with a sample that excludes students who have out-of-range values on the ITBS and our inverse propensity score weights.

We focus particular attention on the results reported in Model 4, since we believe that this model most thoroughly accounts for missing data and attrition. In most cases, these analyses return estimates of the effect of the NYC voucher offer for African-

Americans that are between 36 and $99 \%$ of the Howell \& Peterson estimates and between

[^5]41 and $74 \%$ of the size of our replication of the Krueger and Zhu estimates. Using the Howell \& Peterson definition, the Model 4 analysis returns a significant positive treatment effect for African-Americans for math in Year 3, but not in other years. Using the Krueger \& Zhu definition, the Models 2, 3, and 4 return no significant treatment effects for African-Americans for math.

Elsewhere, analysts have viewed this evidence pointing to a unique positive and significant voucher effect for African-Americans as an indication that vouchers may have unique positive consequences for students at the bottom of the skill distribution. However, a distributional analysis suggests that this interpretation may be misleading in the context of the NYC voucher data. In Appendix Figure 5, we show that the blacks (and because the sample is nearly entirely blacks and Hispanics, also Hispanics) are relatively evenly located across the overall baseline test score distribution. The x-axis in Appendix Figure 5 represents the percentiles of the overall baseline test score distribution for the control group. The $y$-axis denotes the share of the observations between the percentiles at which we calculated the QTE that are black using both the Howell and Peterson and Krueger and Zhu definitions. So, if these lines were horizontal, it would be equivalent to the statement that the blacks are uniformly distributed across the baseline score distribution. As Appendix Figure 5 indicates, black students are distributed approximately evenly across the overall test score distribution in the NYC voucher data. This finding may not be particularly surprising, given the fact that all participants in this study are low-income New York City youth. However, it represents an important piece of context to consider in interpreting evidence of heterogeneous effects in this experiment.

Figure 1: Histogram of raw ITBS math items correct at baseline


Notes: Figure shows histogram of raw number of math items correct on baseline ITBS test as reported in the public-use version of the data. The large point mass at 99 represents those individuals with ITBS raw math scores of 99 and associated National Percentile Ranking scores of 0 , and represents a missing data code. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research. Baseline scores unavailable for kindergarten students.

Figure 2: Cumulative distribution functions (CDFs) of math National Percentile Rankings for the treatment and control groups for the baseline year

CDFs for treatment and control groups Baseline math percentile scores


Notes: Figure shows cumulative distribution functions for baseline math National Percentile Ranking scores from the Iowa Test of Basic Skills separately for the treatment (voucher offer) and control (no voucher offer) groups. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Figure 3: Quantile treatment effect estimates of the impact of a voucher offer on math National Percentile Rankings at baseline

QTE for baseline math percentile scores


Notes: Figure shows QTE for the effect of being offered a voucher for private school on baseline math National Percentile Ranking scores from the Iowa Test of Basic Skills. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. $95 \%$ CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research. Baseline scores unavailable for kindergarten students.

Figure 4: Quantile treatment effect estimates of the impact of a voucher offer on math National Percentile Rankings for the first year after random assignment

QTE for Year 1 math percentile scores


Notes:
Figure shows QTE for the effect of being offered a voucher for private school on math National Percentile Ranking scores from the Iowa Test of Basic Skills in the spring after the first year of voucher distribution. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. $95 \%$ CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Figure 5: Quantile treatment effect estimates of the impact of a voucher offer on math National Percentile Rankings for the second year after random assignment

QTE for Year 2 math percentile scores


Notes:
Figure shows QTE for the effect of being offered a voucher for private school on math National Percentile Ranking scores from the Iowa Test of Basic Skills in the spring after the second year of voucher distribution. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. $95 \%$ CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Figure 6: Quantile treatment effect estimates of the impact of a voucher offer on math National Percentile Rankings for the third year after random assignment

## QTE for Year 3 math percentile scores



Notes:
Figure shows QTE for the effect of being offered a voucher for private school on math National Percentile Ranking scores from the Iowa Test of Basic Skills in the spring after the third year of voucher distribution. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. $95 \%$ CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Figure 7: Histogram of scores falling at various points in the overall national distribution for a national sample of lowincome children in public schools (ECLS-K Spring 1st and 3rd), all children in Catholic schools (ECLS-K Spring 1st and 3rd), and New York City School Choice Scholarships Program children at baseline in 1st, 2nd, 3rd and 4th


Notes: Figure shows histogram of percentiles of from the ELCS-K overall public school distribution among poor kids (income low enough for free lunch or on welfare) and for all Catholic school attendees in Spring of first and third grades and well as percentiles of the National Percentile Ranking from the ITBS for the pre-tests for grades $1,2,3$, and 4 from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research. Baseline scores unavailable for kindergarten students in NYCSCSP and scores for end of second grade unavailable in the ECLS K. Statistics weighted to reflect non-response and complex sampling.

Table 1: Imbalance in incidence of "missing data" values across treatment and control groups

|  | Control mean | T-C difference | SE | P-value | N |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Panel A: Differences in missing scores, Mathematica weights |  |  |  |  |  |
| Missing score, baseline, math/reading | 0.310 | -0.015 | 0.020 | 0.444 | 2666 |
| Panel B : Differences in invalid (99) scores, Mathematica | weights |  |  |  |  |
| Invalid (99) score, baseline, math | 0.120 | 0.012 | 0.015 | 0.425 | 2666 |
| Invalid (99) score, baseline, reading | 0.066 | 0.021 | 0.012 | $0.089^{*}$ | 2666 |
| Invalid (99) score, year 1, math | 0.067 | -0.039 | 0.010 | $0.000^{* * *}$ | 2080 |
| Invalid (99) score, year 1, reading | 0.036 | 0.001 | 0.008 | 0.944 | 2080 |
| Invalid (99) score, year 2, math | 0.068 | 0.016 | 0.015 | 0.301 | 1754 |
| Invalid (99) score, year 2, reading | 0.027 | 0.008 | 0.009 | 0.379 | 1754 |
| Invalid (99) score, year 3, math | 0.046 | -0.013 | 0.010 | 0.226 | 1801 |
| Invalid (99) score, year 3, reading | 0.022 | 0.019 | 0.010 | $0.054^{*}$ | 1801 |
| Panel C: Differences in missing scores, authors' inverse p-score weights |  |  |  |  |  |
| Missing score, baseline, math/reading | 0.309 | 0.002 | 0.019 | 0.929 | 2662 |
| Missing score, year 1, math/reading | 0.219 | 0.002 | 0.020 | 0.915 | 2662 |
| Missing score, year 2, math/reading | 0.343 | 0.003 | 0.024 | 0.895 | 2662 |
| Missing score, year 3, math/reading | 0.329 | 0.003 | 0.024 | 0.883 | 2662 |
| Panel D: Differences in invalid (99) scores, authors' inverse | p-score | weights |  |  |  |
| Invalid (99) score, baseline, math | 0.122 | -0.001 | 0.014 | 0.936 | 2662 |
| Invalid (99) score, baseline, reading | 0.075 | -0.0004 | 0.011 | 0.973 | 2662 |
| Invalid (99) score, year 1, math | 0.039 | -0.0004 | 0.008 | 0.964 | 2662 |
| Invalid (99) score, year 1, reading | 0.032 | 0.0006 | 0.007 | 0.937 | 2662 |
| Invalid (99) score, year 2, math | 0.050 | -0.001 | 0.009 | 0.910 | 2662 |
| Invalid (99) score, year 2, reading | 0.022 | -0.0005 | 0.006 | 0.934 | 2662 |
| Invalid (99) score, year 3, math | 0.025 | -0.001 | 0.006 | 0.867 | 2662 |
| Invalid (99) score, year 3, reading | 0.021 | 0.0006 | 0.007 | 0.921 | 2662 |

$\overline{\text { Notes: } \text { Table reports treatment control differences for baseline and year 1-3 missing test scores and the invalid } 99}$ raw/0 percentile test scores. Panels A and B report the differences with the MPR non-response weights, and Panels C and D with our inverse propensity score weights. Column 1 reports the control group mean, column 2 the TC difference, column 3 the SE on this difference, and column 4 the $p$-value. The inverse p -score weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. SEs clustered by family. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Table 2: Balance in $X$ s and test scores at baseline across treatment and control groups, our inverse propensity-score weights

|  | Control mean | T-C difference | SE | P-value |
| :--- | :---: | :---: | :---: | :---: |
| Child characteristics |  |  |  |  |
| Male | 0.496 | 0.001 | 0.019 | 0.951 |
| African-American | 0.438 | -0.002 | 0.019 | 0.932 |
| Hispanic | 0.489 | -0.0001 | 0.019 | 0.994 |
| Labeled gifted | 0.109 | -0.0007 | 0.012 | 0.958 |
| Labeled special education | 0.110 | 0.0007 | 0.012 | 0.958 |
| Speaks English at home | 0.764 | -0.003 | 0.017 | 0.854 |
| Mother /family characteristics |  |  |  |  |
| Mother's years of schooling | 12.977 | -0.006 | 0.069 | 0.932 |
| Mother works full time | 0.215 | 0.0002 | 0.017 | 0.989 |
| Mother born in the US (not PR) | 0.600 | 0.001 | 0.020 | 0.960 |
| Family gets some welfare | 0.779 | 0.001 | 0.016 | 0.947 |
| Mother in same house 1 year ago | 0.914 | 0.0005 | 0.011 | 0.965 |
| Mother is Catholic | 0.539 | -0.00031 | 0.020 | 0.988 |
| Probability income $\leq \$ 15,000$ | 0.502 | -0.001 | 0.025 | 0.958 |
| Baseline test scores (no K scores) |  |  |  |  |
| Math score | 19.79 | 0.012 | 1.004 | 0.990 |
| Reading score | 25.57 | -0.111 | 1.067 | 0.917 |

Notes:
Table reports treatment control differences for baseline demographics and baseline test scores, treating the invalid 99 scores as missing. Column 1 reports the control group mean, column 2 the $\mathrm{T}-\mathrm{C}$ difference, column 3 the SE on this difference, and column 4 the $p$-value. The inverse p-score weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. SEs clustered by family. Mother born in the US denotes born in one of the 50 states and Washington $\mathrm{DC}_{\mathrm{i}}$ and not Puerto Rico, and family welfare use denotes use of Food Stamps, AFDC/public assistance, Social Security, or Medicaid. The probability that income is less than or equal to $\$ 15,000$ is reported in the table, the specifications (following others) control for the natural log of the midpoint of income ranges. A small number of observations are missing demographics. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Table 3: Effect of excluding "missing data" values on mean
treatment effects reported in Krueger and Zhu (2004a)

| K\&Z estimates |  | Mathematica weights | Using our inverse p-score weights |
| :---: | :---: | :---: | :---: |
|  |  | Our replication | Our estimates |
| Os included |  | Os included | Os excluded |
| Panel A: Effects for full sample, math National Percentile Rankings |  |  |  |
| Year 1 | 0.17 | 0.17 | -0.88 |
|  | (1.34) | (1.38) | (1.05) |
| Year 2 | -0.69 | -0.69 | -1.29 |
|  | (1.40 | (1.37) | (1.15) |
| Year 3 | 0.23 | 0.23 | -0.004 |
|  | (1.35) | (1.28) | (1.18) |
| Panel B: Effects for full sample, reading National Percentile Rankings |  |  |  |
| Year 1 | -0.84 | -0.84 | -1.79 |
|  | (1.25) | (1.32) | (1.09) |
| Year 2 | 0.41 | 0.41 | 0.22 |
|  | (1.30) | (1.26) | (1.16) |
| Year 3 | -0.73 | -0.73 | 0.52 |
|  | (1.26) | (1.32) | (1.13) |

Notes: Table reports original results from panel 3 of Table 3B of Krueger and Zhu (2004a), our replication of these results, and then shows the impact of excluding the 0 percentile values (which are invalid percentiles corresponding to the 99 raw scores) and using inverse propensity score weights as an alternative to the non-response adjusted weights provided with the Mathematica data. Dependent variable is the math (Panel A) or reading (Panel B) National Percentile Ranking scores from the Iowa Test of Basic Skills in the spring for years 1-3 of voucher distribution. Regressions also control for dummies for the strata in the initial sampling. Estimates in column 2 use the Mathematica provided non-response weights, while those in 3 use our inverse propensity score weights. The p-score weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, dummies for missing demographics, dummies for invalid scores or missing scores, dummies for strata (sample design) and grade at baseline, and baseline test scores. 95\% CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Appendix Figure 1: Quantile treatment effect estimates of the impact of a voucher offer on reading National Percentile Rankings at baseline

QTE for baseline reading percentile scores


Notes:
Figure shows QTE for the effect of being offered a voucher for private school on baseline reading National Percentile Ranking scoress from the Iowa Test of Basic Skills. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. $95 \%$ CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research. Baseline scores unavailable for kindergarten students.

Appendix Figure 2: Quantile treatment effect estimates of the impact of a voucher offer on reading National Percentile Rankings for the first year after random assignment

QTE for Year 1 reading percentile scores


Notes:
Figure shows QTE for the effect of being offered a voucher for private school on reading National Percentile Ranking scores from the Iowa Test of Basic Skills in the spring after the first year. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. $95 \%$ CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Appendix Figure 3: Quantile treatment effect estimates of the impact of a voucher offer on reading National Percentile Rankings for the second year after random assignment

QTE for Year 2 reading percentile scores


## Notes:

Figure shows QTE for the effect of being offered a voucher for private school on reading National Percentile Ranking scores from the Iowa Test of Basic Skills in the spring after the second year. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. $95 \%$ CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Appendix Figure 4: Quantile treatment effect estimates of the impact of a voucher offer on reading National Percentile Rankings for the third year after random assignment

QTE for Year 3 reading percentile scores


## Notes:

Figure shows QTE for the effect of being offered a voucher for private school on reading National Percentile Ranking scores from the Iowa Test of Basic Skills in the spring after the third year. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. $95 \%$ CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Appendix Figure 5: Share of each one percentile range of control group test distribution that is made up of African American using either the definition of the Mathematica reports or the definition in Krueger and Zhu

## Year 1 Math percentile scores by two definitions of African American Covariate shares



## Notes:

Figure shows the share of each percentile range of the overall control group pre-random assignment math National Percentile Ranking scores from the Iowa Test of Basic Skills at baseline that is made up of African Americans using the Krueger and Zhu and Mathematica report definitions. For example, the value for the 5th percentile is the weighted share of the observations with test scores larger than the 4th percentile of scores but less than or equal to the 5 th percentile of scores that is made of African Americans. Estimates are weighted using inverse propensity score weights. Weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.

Appendix Table 1: Effect of excluding "missing data" values on mean treatment effects for African Americans reported in Krueger and Zhu (2004a) using Peterson and Howell or Krueger and Zhu definition of African American

|  | Using Mathematica weights |  | Using our inverse p-score weights |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Our replication, K\&Z | Our estimates | Our estimates | Our estimates |
|  | 0s included | 0s excluded | 0s included | 0s excluded |
| Panel A: Effects for Peterson $\mathcal{J}$ Howell sample of African Americans, math NPRs |  |  |  |  |
| Year 1 | $4.54{ }^{* * *}$ | $3.65 * *$ | 2.64 | 2.37 |
|  | (1.53) | (1.59) | (1.42) | (1.46) |
| Year 2 | 2.59 | 3.03 | 2.01 | 2.02 |
|  | (2.06) | (2.09) | (1.67) | (1.73) |
| Year 3 | 4.00** | 3.38* | 4.22** | 3.94** |
|  | (1.86) | (1.92) | (1.73) | (1.78) |
| Panel B: Effects for Krueger $\mathcal{B}$ Zhu sample of African Americans, math NPRs |  |  |  |  |
| Year 1 | 3.18** | 2.21 | 1.41 | 1.31 |
|  | (1.53) | (1.57) | (1.38) | (1.41) |
| Year 2 | 1.33 | 1.74 | 0.48 | 0.43 |
|  | (1.97) | (2.01) | (1.65) | (1.72) |
| Year 3 | 2.83 | 2.32 | 2.33 | 2.10 |
|  | (1.76) | (1.81) | (1.66) | (1.70) |

Notes: Table reports original results from panel 3 of Table 3B of Krueger and Zhu (2004a), our replication of these results, and then shows the impact of excluding the 0 percentile values (which are invalid percentiles), as well as the impact of using inverse propensity score weights as an alternative to the non-response adjusted weights in the data. Dependent variable is the math (Panel A) or reading (Panel B) National Percentile Ranking scores from the Iowa Test of Basic Skills in the spring for years $1-3$ of voucher distribution. Estimates in columns 1 and 2 use the MPR provided weights, while those in 3 and 4 use inverse propensity score weights. The p-score weights are $1 / \hat{p}$ for treatment observations and $1 /(1-\hat{p})$ for control observations, where $\hat{p}$ is generated from a logistic regression of treatment status on baseline demographics, sample design variables, and baseline test scores. 95\% CIs are obtained by bootstrapping families with replacement. Data from the New York City School Choice Scholarships Program evaluation conducted by Mathematica Policy Research.


[^0]:    ${ }^{1}$ Other domestic voucher studies that have used random assignment include the voucher experiments in Dayton, OH and Washington DC (Howell and Peterson 2000; Howell et al. 2002; Wolf, Howell, and Peterson 2000). Internationally, experiments were also conducted in Chile (Lara et al. 2011; McEwan and Carnoy 2000) and Colombia (Angrist, Bettinger, and Kremer 2006). The Milwaukee voucher program also took advantage of a legally-required lottery policy to assign vouchers, although voucher assignment was overseen by administrators and not independent evaluators (Greene, Peterson, and Du 1997, 1998; Rouse 1998; Witte 1998). In addition several studies have also examined voucher programs using observational data. Domestically, these include: Cleveland (Greene, Howell, and Peterson 1997; Peterson, Howell, and Greene 1999), Florida (Chakrabarti 2013; Greene and Winters 2003; Kupermintz 2002), Milwaukee (Rouse 1998) and San Antonio (Peterson, Myers, and Howell 1999); and internationally, New Zealand (Ladd and Fiske 2003).

[^1]:    ${ }^{2}$ When analysts consider only students with African-American mothers as African-American, voucher receipt has a positive effect on their achievement. However, this effect is not significantly different from zero when students with either African-American mothers or fathers are included in the pool of AfricanAmerican students (Krueger and Zhu 2004a). Furthermore, Krueger \& Zhu (2004a, 2004b) demonstrate that positive effects for African-Americans (however defined) hold only when controlling for students' baseline test scores. Krueger and Zhu argue that controlling for baseline test scores is not required to gain valid estimates of the effect of voucher receipt on student achievement, since assignment to treatment and control conditions is independent of student test scores. Furthermore, they maintain that controlling for baseline test scores while omitting observations without baseline scores may introduce bias, since a sizable proportion of students are missing these scores and they appear not to be randomly selected from the student population.

[^2]:    ${ }^{3}$ MPR discovered after randomization that some families mis-reported their family size and were placed into the wrong strata. The initial sample weights corrected for the revised sample sizes in the strata. The corrected weights return the families to their originally assigned strata from the point of randomization. Krueger and Zhu (2004a) discovered that the baseline weights did not correctly adjust for the size of the underlying assignment strata. These weights were revised to include poststratification adjustments, which eliminated previously identified baseline test score differences between the treatment and control groups (see p. 663 for a detailed discussion).
    ${ }^{4}$ National Percentile Ranking scores are calculated from raw scores which are then normed based on grade and quarter of the school year (fall, winter, or spring) and converted into rankings as a percentile of the national distribution based on the normed sample of the ITBS. This allows for cross age and cross-grade comparisons of scores.

[^3]:    ${ }^{5}$ According to the ITBS website for the publisher, Riverside Publishing, and confirmed through telephone communication with customer support, students are given tests of increasing difficulty depending on age and skill level in timed sessions that do not exceed 30 minutes. Raw scores are calculated from each test level. Although the total number of questions varies somewhat by level, the highest possible raw score in reading at any level is 44 and the highest possible raw score in math is 50 (Hoover, Dunbar \& Frisbie 2013).
    ${ }^{6}$ Both Krueger and Zhu (2004a) and Mayer et al (2002) identify that many students received an NPR score of 0 . Neither points out that this score corresponds to a raw score of 99 (See Mayer et al. 2002 p. 32 footnote 10 - Students with a score of 0 were included in the generation of composite scores. Page 32 also suggests that they include NPR scores ranging from 0-100. See also Krueger and Zhu (2004a) endnote 4, which identifies the large concentration of scores of 0 that are included in the analysis while suggesting perhaps these are not valid scores.

[^4]:    ${ }^{7}$ For the ECLS-K, we constructed the low income public school distribution so as to best match the children in the voucher experiment while still having sufficient sample size. The voucher children are all eligible for free lunch. Our comparison children are either obtaining free lunch or on welfare or under poverty (the closest proxy in the public use data to being under 130\% of poverty). The ECLS-K scores are for spring of first and third grade, about midway between the baseline voucher scores, which are in grades 1-4.

[^5]:    ${ }^{8}$ The recoding described in Krueger \& Zhu provides some contradictory information about which cases were recoded. In the text, it suggests that students were recoded if: 1 . Their mother listed her race as African American in a subsequent wave; 2. If the father listed his race as African American in the baseline wave; and 3. If a parent indicated that their race was "other" and wrote in an entry that included the words black or African American in combination with something else or abbreviated in an obvious manner. In a footnote, they suggested this recoding only occurred if the mother used a write in response, but not the father. To match their sample sizes within one case, we used only the mother's write-in responses. If the father's write-in responses were included, the sample size was too large. Given that it is not possible to know exactly which write-in cases for either the mother or the father were recoded, our replication of the coefficients in this table is not exact. Their coefficients and standard errors for the alternative version of African American subgroup including the full sample and controls for randomization block presented in Table 5 Panel 2, for reading are $1.36(1.82)$ in year $1,1.57(1.81)$ in year 2, and $0.99(1.84)$ in year 3, and for math, are 3.34 (1.63) in year $1,1.15$ (1.93) in year 2, and $3.04(1.85)$ in year 3.

