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ABSTRACT

The theoretical nature of risk premiums in foreign currency futures markets is derived and studied empirically. Estimation problems encountered in using futures data are discussed. Since forward rates and futures prices are demonstrated to be approximately equal, and because risk premiums in forward markets are highly variable, consistency of the data requires time variation in daily risk premiums in the futures market. Unbiasedness of daily futures prices as predictors of the following day's futures price is rejected for all currencies. Reconciliation of daily and monthly data requires positive serial correlation in daily risk premiums.

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The purpose of this paper is to investigate the nature of risk and return in futures markets for foreign exchange. The paper integrates and extends two relatively unrelated strands of literature. On the one hand, we draw on the predominantly empirical literature on the efficiency of the forward foreign exchange market for motivation and econometric specifications, and on the other hand, we integrate into the international finance literature the predominantly theoretical results on the determination of commodity futures prices and the differences between a futures price and a forward price.

The empirical literature on the efficiency of the forward foreign exchange market is discussed in Hodrick and Srivastava (1984). There, we identify several positions within the profession regarding the evidence on efficiency. We first note the general confusion that has permeated this literature because efficiency is often identified with the proposition that the forward rate is an unbiased predictor of the future spot rate. The unbiasedness hypothesis is rejected in many empirical studies for maturities as short as a day [Dooley and Shafer (1983)] or a week [Cumby and Obstfeld (1981), Hsieh (1984)], to more traditional maturities of one month [Bilson (1981), Hansen and Hodrick (1983), Fama (1984)], or three months [Hansen and Hodrick (1980)]. The reaction to these empirical findings has not been the uniform acceptance of a particular model of risk premiums. Instead, three alternative perspectives have emerged. One perspective questions the findings because of doubt about the statistical validity of the tests that are invariably based on asymptotic distribution theory. Another perspective accepts the validity of the statistical findings but claims that they are evidence of market inefficiency. Most financial economists continue to search for a model of time varying risk premiums that is consistent with the data. Unfortunately, progress in this search has been slow, and several dead ends appear to have been encountered.¹

If the magnitude of the variation in estimated risk premiums relative to the variation in expected rates of change of exchange rates were small, perhaps the unbiasedness hypothesis could be treated as an approximation that is nearly true. This idea is contradicted, though, by the recent studies of Fama (1984) and Hodrick and Srivastava (1986). These studies treat the forward premium as the sum of two unobservable components, the expected rate of depreciation and a normalized risk premium. While the two studies differ in methodology and in interpretation of the empirical results, both demonstrate that the risk premium in the forward foreign exchange market has a larger variance than that of the expected rate of change of the spot exchange rate. These statements are, of course, conditional on the validity of the statistical tests in the sample sizes employed in the studies.

Since futures prices of foreign exchange also can be described as containing predictions of future exchange rates plus risk premiums, this paper seeks to determine whether the rejection of the unbiasedness hypothesis and the nature of time variation in risk premiums found in forward markets carries over into the futures market. The availability of daily futures data also makes this market an attractive one for investigation of the potential importance of small sample size in explaining the results from the forward market.

It is well-known that futures contracts differ in several ways from forward contracts. Forward prices are quoted in an interbank market for delivery at a fixed time of maturity that is typically one, three, six, or twelve months. Futures prices are quoted at an organized exchange like the International Monetary Market (IMM) in Chicago. Contracts are traded for delivery on the third Wednesday of March, June, September, and December, and typically there are four contracts outstanding at a point in time. Futures

contracts are also marked to market daily which induces a theoretical reason why forward prices and futures prices for delivery on the same day in the future may differ. The influence of marking to market on the futures price was first discussed by Black (1976) and has been modeled by Cox, Ingersoll and Ross (1981), Richard and Sundaresan (1981), and French (1983).

Section 2 of the paper extends the theoretical discussion in Hodrick and Srivastava (1984) to the determination of futures prices for foreign exchange within the context of a simple general equilibrium model developed by Lucas (1982). The theoretical difference between a forward contract for foreign exchange and a futures contract is examined.

Although in theory there may be a difference between forward prices and futures prices for delivery on the same day in the future, the initial empirical work in this area by Cornell and Reinganum (1981) found very little difference between the two speculative prices. In Section 3 of the paper we update the study of Cornell and Reinganum with additional data.

Section 4 of the paper examines empirically whether the econometric techniques that were powerful enough to reject the unbiasedness hypothesis in the forward market are powerful enough to find movements in the risk premium with daily data.

The last section of the paper provides an interpretation of the empirical findings, examines what appears to be needed to reconcile the findings with previous research, and discusses possible directions of future research in this area.

2. Futures Pricing Theory

In this section of the paper we extend international intertemporal asset pricing models such as the Lucas (1982) model to consider the pricing of futures contracts for foreign currency. Our argument follows the analysis in

Cox, Ingersoll and Ross (1981) and Richard and Sundaresan (1981) who discuss pricing of futures on commodities. The primary objective of this section is to present the current state of theory in futures pricing and integrate it with exchange rate determination to form a basis for the empirical analysis in later sections.

Cox, Ingersoll and Ross (1981) use arbitrage arguments and the contractual aspects in futures and forward markets to analyze the determinants of futures and forward prices. In order to understand the theoretical difference between these two speculative prices, we consider their arbitrage arguments. We begin with the forward price since it is the easiest to understand. When necessary for clarity, we adopt a dating convention that dates all variables with a primary subscript indicating when they enter the agents' information set and with a secondary subscript to indicate how far into the future or past it is necessary to go in order to define the concept appropriately.

Let S_t be the spot price of foreign currency in terms of dollars at time t , and let $G_{t,k}$ be the forward price of foreign currency set at time t for delivery at time $t+k$. Also, let $R_{t,j}$ be the known dollar return from investing a dollar at time t in a j -period risk-free bill. Then, Cox, Ingersoll and Ross (1981, Proposition 1) demonstrate that $G_{t,k}$ is the present value of a time $t+k$ payoff equal to $S_{t+k}R_{t,k}$. The proof of this proposition is straightforward. Consider an investment strategy of placing $G_{t,k}$ dollars in k -period bills at time t and buying $R_{t,k}$ forward contracts. The time $t+k$ profit per forward contract is $(S_{t+k} - G_{t,k})R_{t,k}$, and the total time $t+k$ payoff on the investment strategy is

$$G_{t,k}R_{t,k} + (S_{t+k} - G_{t,k})R_{t,k} = S_{t+k}R_{t,k} \quad (1)$$

Since the initial investment is $G_{t,k}$ and the payoff is $S_{t+k}R_{t,k}$, equilibrium without arbitrage profits requires that the forward price be the present value of $S_{t+k}R_{t,k}$ where present value must be determined by an appropriate asset pricing paradigm. We delay the discussion of how present values are determined in order to examine the arbitrage argument used in the determination of futures prices.

Let $F_{t,k}$ be the futures price of foreign currency in terms of dollars at time t with maturity date $t+k$. Then, Cox, Ingersoll and Ross (1981, Proposition 2) demonstrate that $F_{t,k}$ is the present value at t of a payoff of $S_{t+k} \prod_{j=t}^{t+k-1} R_{j,1}$ at time $t+k$ where present value is again in reference to an appropriate asset pricing paradigm. The proof of this proposition incorporates the fact that futures contracts are marked to market which provides the investor with a sequence of intermediate cash flows between t and $t+k$. Marking to market requires that the long (short) investor in a contract maturing at time $t+k$ receives (pays) the amount $(F_{j,n} - F_{j-1,n+1})$ if it is positive (negative) at time $j = t+1, \dots, t+k$ where $n = t+k-j$ is the number of periods remaining on the futures contract. Now, consider the arbitrage argument.

At each time $j = t, t+1, \dots, t+k-1$ invest $F_{t,k}$ dollars and the accumulated interest in one period bills with return $R_{j,1}$. Also, at each point in time j , take a long position in $\prod_{i=t}^j R_{i,1}$ futures contracts at price $F_{j,n}$. In each period after the first, liquidate the futures contracts from the previous period to receive the per contract profit or loss and invest the proceeds (which may be negative) and the interest that accumulates in one period bills. Since $F_{t+k,0} = S_{t+k}$ by arbitrage, the time $t+k$ payoff on this investment strategy is

$$F_{t,k} \prod_{j=t}^{t+k-1} R_{j,1} + \sum_{j=t}^{t+k-1} (\prod_{i=t}^j R_{i,1}) (F_{j+1,n-1} - F_{j,n}) (\prod_{i=j+1}^{t+k-1} R_{i,1}) = S_{t+k} \prod_{j=t}^{t+k-1} R_{j,1}. \quad (2)$$

Since the initial investment is $F_{t,k}$ dollars and the final payoff is $S_{t+k} \prod_{j=t}^{t+k-1} R_{j,1}$, the futures price must be set in equilibrium to be equal to the present value of $S_{t+k} \prod_{j=t}^{t+k-1} R_{j,1}$.

Present values are determined by asset pricing paradigms. Intertemporal asset pricing models generally value the payoffs of assets or determine the appropriate equilibrium asset prices by equating the conditional expectation of the marginal utility foregone in making the investment to the conditional expectation of the discounted value of the marginal utility from the payoff of the investment. Consider an asset with dollar price V_t and time $t+k$ payoff of $V_{t+k} + D_{t+k}$, where D_{t+k} is a dividend or coupon payment. The foregone marginal utility of making the investment is $V_t \pi_t E_t(MU_t)$ where π_t is the purchasing power of a dollar at time t , which has units of numeraire good per dollar, and where $E_t(MU_t)$ denotes the conditional expectation of the marginal utility of the numeraire good. We take the conditional expectation of the marginal utility to allow for general specifications of preferences which may not be separable across time periods. The expected marginal utility from the payoff of the investment is $E_t\{(V_{t+k} + D_{t+k})\pi_{t+k} E_{t+k}(MU_{t+k})\}$.² It depends on the purchasing power of the dollar at time $t+k$ and on the expected marginal utility at that time.

Equating the marginal cost of the investment to its expected marginal benefit produces an expression that must be satisfied in equilibrium by all returns:

$$1 = E_t(Q_{t+k,k} r_{t+k,k}) \quad (3)$$

where $r_{t+k,k} = (V_{t+k} + D_{t+k})/V_t$ is a nominal dollar return between time t and time $t+k$, and where

$$Q_{t+k,k} = \pi_{t+k} E_{t+k}(MU_{t+k}) / \pi_t E_t(MU_t) \quad (4)$$

is the intertemporal marginal rate of substitution of dollars between time t and time $t + k$. The dating of $r_{t+k,k}$ and $Q_{t+k,k}$ indicates that they enter the information set at time $t + k$ and are random variables at time t . The intertemporal marginal rate of substitution of money is an index that weights the change in the purchasing power of money between two time periods by the intertemporal marginal rate of substitution of goods between the same two time periods.

As Richard and Sundaresan (1981) note, the asset pricing paradigm in (3) provides a present value operator that converts dollar payoffs at $t + k$ into dollar values at t . The dollar payoffs can be either stochastic or deterministic.

It is established above that the forward price, $G_{t,k}$, is the present value of the payoff $S_{t+k}R_{t,k}$ and the futures price, $F_{t,k}$, is the present value of $S_{t+k} \prod_{j=t}^{t+k-1} R_{j,1}$. Consequently, the following equilibrium pricing relationships are dictated by (3):

$$G_{t,k} = E_t(Q_{t+k,k} S_{t+k} R_{t,k}) \quad (5)$$

and

$$F_{t,k} = E_t(Q_{t+k,k} \prod_{j=t}^{t+k-1} R_{j,1} S_{t+k}). \quad (6)$$

If short-term interest rates were deterministic, arbitrage would require the known k -period return $R_{t,k}$ to be equal to the product of the k one-period returns, $\prod_{j=1}^{t+k-1} R_{j,1}$. Examination of (5) and (6) indicates that forward prices and futures prices would be identical in this case, as Black (1976) noted, because $R_{t,k}$ and $\prod_{j=t}^{t+k-1} R_{j,1}$ would both be elements of the time t information set and could be divided out of the right-hand sides of (5) and (6).

Richard and Sundaresan (1981) note that (5) and (6) provide an interesting insight into why futures prices may differ from forward prices.

The forward price provides the dollar present value of $R_{t,k}$ units of foreign exchange which is known at time t while the futures price provides the dollar present value of a stochastic quantity of foreign currency equal to $\prod_{j=t}^{t+k-1} R_{j,1}$. Clearly, there are two potential reasons why forward prices and futures prices might differ. First, the known return, $R_{t,k}$, is generally not equal to the product of the k one-period returns, $\prod_{j=1}^{t+k-1} R_{j,1}$, and second, the product of the intertemporal marginal rate of substitution of the dollar and the exchange rate, $Q_{t+k,k} S_{t+k}$, may be correlated with the product of the short rates. If we apply a covariance decomposition to (5) and (6), we find the following relationships:

$$\begin{aligned} G_{t,k} &= E_t(Q_{t+k,k} R_{t,k}) E_t(S_{t+k}) + C_t(Q_{t+k,k} R_{t,k}; S_{t+k}) \\ &= E_t(S_{t+k}) + C_t(Q_{t+k,k} R_{t,k}; S_{t+k}) \end{aligned} \quad (7)$$

and

$$\begin{aligned} F_{t,k} &= E_t(Q_{t+k,k} \prod_{j=t}^{t+k-1} R_{j,1}) E_t(S_{t+k}) + C_t(Q_{t+k,k} \prod_{j=t}^{t+k-1} R_{j,1}; S_{t+k}) \\ &= E_t(S_{t+k}) + C_t(Q_{t+k,k} \prod_{j=t}^{t+k-1} R_{j,1}; S_{t+k}) \end{aligned} \quad (8)$$

where $C_t(X; Y)$ is the conditional covariance of two random variables X and Y . The second lines of (7) and (8) follow because the k -period long return and the product of the k short returns must both satisfy (3) in equilibrium. Both forward prices and futures prices of foreign exchange are generally biased predictors of future spot rates as (7) and (8) indicate. If the conditional covariances in (7) and (8) were constant, then forward and futures prices would be characterized by a constant unconditional bias. Obviously, if the conditional distribution of the random variables in (7) and (8) varies over time, no such unconditional bias need characterize the data and a time varying

risk premium may be present.

Equations (5) and (6) also provide a straightforward demonstration of why futures prices may differ from forward prices. The difference between (5) and (6) is

$$F_{t,k} - G_{t,k} = E_t [Q_{t+k,k} S_{t+k} (\prod_{j=t}^{t+k-1} R_{j,1} - R_{t,k})] \quad (9)$$

which is the dollar present value of a random amount of foreign exchange equal to $(\prod_{j=t}^{t+k-1} R_{j,1} - R_{t,k})$.

3. Comparison of Forwards and Futures

Cornell and Reinganum (1981) first compared forward rates to futures prices for delivery on the same day. They concluded that the two prices are essentially the same given the nature of transactions costs in these markets. Since their data set ends in 1979 prior to the increase in the volatility of interest rates during the 1980's, we sought to update their study. In this section we discuss problems we encountered in performing a comparison of futures prices of foreign exchange with forward prices of foreign exchange with a slightly different data set than Cornell and Reinganum (1981). Such a comparison requires careful consideration of the institutional aspects of the two markets and the timing of the observations.

Riehl and Rodriguez (1977) describe the nature of delivery in spot and forward foreign exchange markets. A U.S. dollar purchase of spot foreign currency is for delivery on the spot value day two business days in the future, except for purchases of Canadian dollars and Mexican pesos in which case delivery is in one business day. To find the delivery date for a one-month forward contract one first finds the spot value date then checks whether that numerical date in the next month is a business day in both countries. If it is, that date is the forward value date. If the corresponding date in the

future is not a legitimate value date, forward settlement occurs on the next available business day without going out of the month. If the above procedure would require settlement in the next month, the contract is instead settled on the first business day before the numerical date in the next month corresponding to the spot value date.

As an example, consider the contracts that were written on Thursday, November 15, 1984. Spot contracts were for delivery on Monday, November 19. One-month forward contracts were for delivery on Wednesday, December 19. Three-month forward contracts were for delivery on Tuesday, February 19, 1985.

Futures contracts on the International Monetary Market of the Chicago Mercantile Exchange require delivery on the third Wednesday of March, June, September, and December. Trading in the contracts stops on the Monday preceding the third Wednesday if Monday, Tuesday, and Wednesday are legitimate business days. This is consistent with the two-day delivery procedure in the spot market. In order to compare the forward price to the futures price, one must make sure that both contracts are for delivery on the third Wednesday of the appropriate month. In the example above, the one-month forward rate on Thursday, November 15, 1984, could be compared to the December futures price on that day because both of the contracts are for delivery on the third Wednesday in December. The appropriate date on which the three-month forward contract could be compared to the December 1984 futures contract is Monday, September 17, 1984. On that day, spot contracts were written for delivery on Wednesday, September 19, and three-month forward contracts were written for delivery on Wednesday, December 19.

Since there is a two business day delivery lag in the spot market, it is clear that forward contracts are predicting the spot rate two business days prior to the future delivery day. This is consistent with the futures market

which is also predicting the spot rate two days before the third Wednesday of the delivery month. If one is unhedged in the futures market or the forward market and must enter the spot market to make delivery, one must transact two business days prior to the forward value day or the delivery day in the futures market.

Following the above procedure with one month data, we are able to compare the one-month forward rate to the futures price only for the March and December contracts. While this may seem odd, it is caused by the settlement procedure described above. Consider the September 1984 contract. Futures trading required delivery on September 19. Consequently, in order to compare a futures price to the one-month forward rate, August 19 would have had to have been a spot value day, but that day was a Sunday. On Friday, August 17, one could have made a contract for delivery on Wednesday, September 19, but the contract would have been nonstandard. Our data on one-month forward rates from August 17 are for delivery on September 21. A similar problem occurs with June contracts.³

An additional problem in conducting an interesting comparison arises because our data on forward rates are not sampled at precisely the same time as the closing prices in the futures market. This problem also arose in the study of Cornell and Reinganum (1981). Futures markets for our five currencies close at two minute intervals between 1:16 p.m., Chicago time, for the Swiss franc and 1:26 p.m., Chicago time, for the Japanese yen. Cornell and Reinganum (1981) obtained data on forward prices from the IMM which obtained them from Continental Illinois Bank at 1:00 p.m., Chicago time. Our data are from Data Resources, Inc. which obtains them from Bank of America. The data are on line by 9:30 a.m., San Francisco time, which is 11:30 a.m., Chicago time. Thus, we have a considerably worse problem with errors than did

Cornell and Reinganum (1981).

Because of these problems our comparison is suggestive only. The data are presented in Table 1 through Table 5 for the dollar values of the Japanese yen, the Deutsche mark, the U.K. pound, the Canadian dollar, and the Swiss franc, respectively. Each table presents the closing futures price on the comparison day as reported by the IMM, the bid-ask spread from the forward market, and the raw deviation of the futures price from the bid or the ask forward price. The deviation is expressed as a negative number if the futures price is below the bid and as a positive number if it is above the ask. The tables also contain the deviation expressed as a multiple of the bid-ask spread and the deviation expressed as a percentage of the futures price.

In the case of the Japanese yen, each point in the price and in the raw deviation corresponds to one ten-thousandth of a cent. The raw deviations range from -35 to 25 while the number of spreads ranges as high as 6.5 with nine of the nineteen deviations being more than two bid-ask spreads in absolute value. For the other currencies each point corresponds to hundredths of a cent. Deviations for the Deutsche mark range from -36 to 29, with one observation as large as 9.67 and another equal to 12 bid-ask spreads. Once again, nine of nineteen deviations are larger than two-bid ask spreads. The U.K. pound has several large deviations, one as high as 235 points and another -171 points. Thirteen of the observations are greater than two-bid ask spreads. In contrast deviations of the Canadian dollar range from -17 points to 10 points, although ten of the observations are greater than two bid-ask spreads. Finally, the raw deviations for the Swiss franc range from -40 to 86, the latter being equivalent to 28.67 bid-ask spreads. Seven of the observations have values greater than two spreads.

While these observations seem relatively large and might be deemed to be

far from a well-arbitrated market if one thought that the two prices ought to be equal, an important consideration related to the timing of the data must be examined before conclusions can be drawn. The bid-ask spread is determined in part by the volatility of the underlying series and by the variance of the waiting time between orders. A foreign exchange trader quotes a bid-ask spread to obtain profit from buying and selling currencies. Volatility of the exchange rate induces profits and losses when the trader is exposed to exchange risk. Higher volatility is likely to lead to larger spreads in a risk-averse world. Faster arrival of orders mitigates the need to increase spreads by allowing the trader to take open positions while simultaneously being exposed to less exchange risk since an order of the opposite kind can be expected to arrive relatively sooner. Hence, small bid-ask spreads may be consistent with a high volatility of the exchange rates if orders are arriving quickly enough. Since the data are not measured precisely at the same time, the number of bid-ask spreads is potentially a terrible indicator of the closeness of the two prices. We must ask how much we would expect the series to move in two hours to see if our observations lie outside of this adjustment. Consider the following argument which attempts to place bounds on how much the prices might move in an hour.

The daily volatility of the futures markets differs across currencies and over time. If we take a range of values, as potential candidates for annualized volatilities, of between five and fifteen percent, where by annualized volatility we mean the daily standard deviation of the percentage change in the futures price multiplied by $\sqrt{250}$, we expect a daily standard deviation of between 0.32 and 0.95 percent. Dividing these numbers by $\sqrt{24}$ produces an hourly standard deviation of between 0.065 and 0.19, or a two hour standard deviation of approximately 0.092 to 0.268. Hence, observations of

deviations greater in absolute value than 0.536 might be considered outside of equality. If, on the other hand, we recognize that the hourly volatility of the market may be greater when it is open than when it is closed, as has been documented for NYSE stocks by French and Roll (1984), we might divide by something like $\sqrt{8}$ to get an estimated hourly standard deviation of between 0.11 and 0.33 or a two hour standard deviation of 0.156 to 0.467. We arbitrarily choose 8 implying that volatility during the nineteen hours that the market is closed is 60 percent of the volatility during the five hours it is open. Taking these latter figures as representative of the percentage change possible over an hour, we find that only observations that are more than 0.312 percent or even as much as 0.934 percent are truly economically meaningful deviations. Using the latter figure we find one observation for the Japanese yen, one for the U.K. pound and two for the Swiss franc that are outside this bound.

It is unfortunate that the quality of these data do not allow a more detailed study of the pricing issues raised by Cox, Ingersoll and Ross (1981), but it is our opinion that measurement error would swamp any attempt to estimate the size of the effects. French (1983) investigates these issues with data from the silver and copper markets. The time differential between his observations is as large as five hours. From the arguments presented above, one can see that this introduces an enormous error in the variables problem into his analysis. Consequently, it is not surprising that he found virtually no support for his joint null hypothesis that the Cox, Ingersoll and Ross (1981) effects are present in the data and that the marginal utility of a numeraire commodity is independent of nominal interest rates.

These data problems are comparable to the problem encountered by Frenkel and Levich (1977) who attempt to measure transactions costs with a triangular

arbitrage argument in their study of covered interest arbitrage using data that are measured with up to nine hours difference in time. When McCormick (1979) reexamined their study with data measured precisely at the same point in time, the conclusions of the study changed drastically. It is our opinion that such results would also likely characterize studies of futures and forward prices.

4. Time Varying Daily Risk Premiums

In the previous section we found no evidence to contradict the results first reported in Cornell and Reinganum (1981) of no meaningful statistical difference between forward and futures prices of foreign exchange. This suggests that given the strong rejection of the unbiasedness hypothesis in the forward market, similar findings ought to be found in the futures data. In this section we investigate the properties of futures prices as predictors of futures prices in the future.

Samuelson (1965) argued that the sequence of futures prices in an efficient market would be a martingale with $F_{t,k} = E_t(F_{t+1,k-1})$. If this were true, we know that the futures prices, in contrast to forward prices, would be unbiased predictors of future spot prices. This is easily demonstrated by repeated application of the law of iterated expectations and by use of the arbitrage argument, $F_{t+k,0} = S_{t+k}$:

$$F_{t,k} = E_t(F_{t+1,k-1}) = E_t[E_{t+1}(F_{t+2,k-2})] = E_t(F_{t+2,k-2}). \quad (10)$$

Since the unbiasedness hypothesis is easily rejected for forward exchange rates and since no evidence is available to indicate a strong difference between futures prices and forward prices, it must be the case that Samuelson's argument contains a joint hypothesis. Indeed, if risk premiums are not constant, then Samuelson's argument must be modified, as we now

demonstrate.⁴

Consider the futures price of foreign exchange at time $t + 1$ with $k - 1$ days to maturity. From (6) we know

$$F_{t+1,k-1} = E_{t+1}(Q_{t+k,k-1} S_{t+k} \prod_{j=t+1}^{t+k-1} R_{j,1}) . \quad (11)$$

Also, from the definition of the intertemporal marginal rate of substitution we know that

$$Q_{t+k,k} = Q_{t+k,k-1} Q_{t+1,1} \quad (12)$$

since from (4)

$$Q_{t+k,k-1} = \pi_{t+k} E_{t+k}(MU_{t+k}) / \pi_{t+1} E_{t+1}(MU_{t+1}) \quad (13)$$

and

$$Q_{t+1,1} = \pi_{t+1} E_{t+1}(MU_{t+1}) / \pi_t E_t(MU_t) . \quad (14)$$

Proposition I The futures price, $F_{t,k}$, is equal to the time t conditional expectation of $F_{t+1,k-1}$ plus a risk premium.

Proof: From (6), (11), and (12) find

$$F_{t,k} = E_t [Q_{t+k,k-1} Q_{t+1,1} S_{t+k} \prod_{j=t+1}^{t+k-1} R_{j,1} R_{t,1}] . \quad (15)$$

Covariance decomposition of (15) gives

$$F_{t,k} = E_t(Q_{t+k,k-1} S_{t+k} \prod_{j=t+1}^{t+k-1} R_{j,1}) E_t(Q_{t+1,1} R_{t,1}) + C_t(Q_{t+k,k-1} S_{t+k} \prod_{j=t+1}^{t+k-1} R_{j,1}; Q_{t+1,1} R_{t,1}) . \quad (16)$$

From (3), (11) and the law of iterated expectations, (16) becomes

$$F_{t,k} = E_t(F_{t+1,k-1}) + C_t(F_{t+1,k-1}; Q_{t+1,1} R_{t,1}) . \quad (17)$$

O. E. D.

Whenever the conditional covariance in (17) is not a time invariant function, there will be time varying bias in daily futures prices. The next part of this section investigates statistical tests of the proposition that futures prices are unbiased predictors of the futures price on the next business day.

4.1 The Econometric Specification

Consider the null hypothesis of unbiasedness in daily prices given in (18):

$$E_t(F_{t+1,k-1}) = F_{t,k} \quad (18)$$

Since S_t is in the information set at time t , we may write

$$E_t[(F_{t+1,k-1} - S_t)/S_t] = (F_{t,k} - S_t)/S_t \quad (19)$$

where the transformation makes it more likely that the statistical assumption of stationarity of the data that is necessary for convergence of the asymptotic distributions of parameter estimates is satisfied.⁵

In order to conserve notation let $y_{t+1} = (F_{t+1,k-1} - S_t)/S_t$, and let $x_t = (F_{t,k} - S_t)/S_t$. Since $y_{t+1} = E_t(y_{t+1}) + \epsilon_{t+1}$, where ϵ_{t+1} is the forecast error that is orthogonal to time t information, a test of (19) can be conducted in the usual way by assuming rational expectations and by defining the function $h(y_{t+1}, x_t, \delta_0) \equiv \epsilon_{t+1}$ as

$$h(y_{t+1}, x_t, \delta_0) = y_{t+1} - \alpha - \beta x_t \quad (20)$$

where δ_0 is the true parameter vector (α, β) and the null hypothesis is $\alpha = 0$ and $\beta = 1$. Tests of these hypotheses are performed for five currencies in Table 6. Estimation and testing is accomplished with Hansen's (1982) Generalized Method of Moments (GMM). A nice feature of the GMM procedure is that no additional auxiliary assumption of conditional homoscedasticity need

be made in constructing the covariance matrix of the parameter estimates.⁶

Under the null hypothesis ε_{t+1} can be interpreted as the disturbance term in an econometric estimation. The model provides orthogonality conditions that can be used to estimate α and β in (20). We assume that ε_{t+1} has finite second moment although we do not impose an assumption of conditional homoscedasticity. Let z_t' be the row vector $(1, x_t)$ of instruments that will be used in the estimation. Then, following Hansen and Singleton (1982), define the function f by

$$f(y_{t+1}, x_t, \delta) = h(y_{t+1}, x_t, \delta) \otimes z_t'. \quad (21)$$

The model implies

$$E[f(y_{t+1}, x_t, \delta_0)] = 0 \quad (22)$$

which is a set of two orthogonality conditions when f is evaluated at the true parameter vector. The GMM estimator exploits the sample moment of (22) defined by

$$g_T(\delta) = \left(\frac{1}{T}\right) \sum_{t=1}^T f(y_{t+1}, x_t, \delta) \quad (23)$$

for a sample of size T . The choice of $\hat{\delta}$ in the GMM procedure requires minimization of the criterion function

$$J_T(\delta) = g_T(\delta)' W_T g_T(\delta) \quad (24)$$

for an appropriately chosen weighting matrix W_T that is 2×2 and symmetric.

Notice that in this case

$$g_T(\delta)' = (y - Z\delta)' Z/T \quad (25)$$

where y is a T -dimensional vector of observations on y_{t+1} and Z is a $T \times 2$ matrix of observations on z_t' . Hence, minimization of (23) produces the

ordinary least squares (OLS) estimator

$$\delta_T = (Z'Z)^{-1}Z'y, \quad (26)$$

but the OLS standard errors are not appropriate. Cumby, Huizinga and Obstfeld (1983) demonstrate that any GMM estimator in this linear environment that exploits the orthogonality conditions (21) has the same asymptotic distribution. They demonstrate that

$$\sqrt{T}(\delta_T - \delta_0) \xrightarrow{i.d.} N(0, D_0^{-1} \Omega D_0^{-1}) \quad (27)$$

where $\Omega = \lim_{T \rightarrow \infty} (1/T)E(Z'\varepsilon\varepsilon'Z)$, ε is the T-dimensional vector of true errors, ε_t , and $D_0 = \text{plim}(Z'Z/T)$.

It is interesting that the moment estimator of Ω given by

$$\Omega_T = (1/T) \sum_{t=1}^T z_t' z_t \hat{\varepsilon}_{t+1}^2 \quad (28)$$

is a consistent estimator of Ω even though the daily futures data are not covariance stationary. A similar argument holds for D_0 and its estimator $D_T = (Z'Z/T)$.

We follow Jagannathan (1983, 1985) in deriving the asymptotic distribution of GMM estimators that arise when using data from futures markets with their peculiar contract structure. To understand the problem imagine a fictional vector of daily observations on futures premiums defined in the right-hand side of (19) with between 1 and K days to maturity where K is the longest time period considered in the actual data. Let this K-dimensional vector be denoted X_t with k-th typical element $(F_{t,k} - S_t)/S_t$. The vector process X_t can be thought of as a stationary stochastic process. To facilitate the analysis, also define $w_t' = \varepsilon_{t+1}(1, X_t')$. Then, w_t can also be assumed to be a covariance stationary stochastic process with K + 1 dimensional covariance matrix $\Theta = E(w_t w_t')$. Denote the typical element of Θ by θ_{ij} .

The actual data are sampled from the w_t process. Imagine that the first observation on a regressor, x_1 , corresponds to a contract with K days to maturity, the second observation is on a contract with $K-1$ days to maturity, etc. At the K -th observation, there is one day to maturity, and the next observation begins the second contract with K days to maturity. If there are K days in all the contracts and N total contracts in the sample, the total number of observations is $T = NK$.

In order to determine how Ω corresponds to certain terms of the elements of θ , we write out the terms in the expression:

$$\Omega = \lim_{T \rightarrow \infty} (1/T) E \left\{ \begin{matrix} \varepsilon_2 & T \\ \varepsilon_2 x_1 & \sum_{t=1}^T (\varepsilon_{t+1}, \varepsilon_{t+1} x_t) \end{matrix} + \dots + \begin{matrix} \varepsilon_{T+1} & T \\ \varepsilon_{T+1} x_T & \sum_{t=1}^T (\varepsilon_{t+1}, \varepsilon_{t+1} x_t) \end{matrix} \right\}. \quad (29)$$

Since $E(\varepsilon_{t+1} | \varepsilon_t, \varepsilon_{t-1}, \dots, x_t, x_{t-1}, \dots) = 0$, only contemporaneous terms will be nonzero in (29). In terms of the elements of $w'_t = (w_{1,t} \dots w_{K+1,t})$, the expression in (29) can be rewritten as

$$\Omega = \lim_{N \rightarrow \infty} (1/NK) E \left\{ \begin{matrix} N & K \\ \sum_{n=1}^N & \sum_{k=1}^K \left| \begin{matrix} w_{1, (n-1)K+k} \\ w_{K+2-k, (n-1)K+k} \end{matrix} \right| \left| \begin{matrix} w_{1, (n-1)K+k} \\ w_{K+2-k, (n-1)K+k} \end{matrix} \right|' \end{matrix} \right\}. \quad (30)$$

Hence,

$$\Omega = (1/K) \sum_{k=1}^K \left| \begin{matrix} \theta_{1,1} & \theta_{1,k+1} \\ \theta_{k+1,1} & \theta_{k+1,k+1} \end{matrix} \right|. \quad (31)$$

In (31) Ω is an average covariance of the w_t process. It is straightforward to demonstrate that the Ω_T in (28) is a consistent estimator of Ω in (31).⁷ A similar argument can be used to demonstrate that D_T is a consistent estimator of $\text{plim}(Z'Z/T)$ where convergence again requires the number of days within a contract to be fixed and the number of contracts to grow large. Convergence in this case is again to a type of average covariance of the w_t process.⁸

The results of this estimation procedure are presented in Table 6. The period of estimation is from June 1, 1973 to December 8, 1983. Daily data were followed for the September 1973 contract until it expired on September 17. The next observation on the dependent variable used the futures price on September 18 for the December 1973 contract. The right-hand-side variable was constructed from the futures price on September 17 for the same contract. Data were sampled in this manner from 42 contracts, and the total number of observations is 2420.

For each currency in Table 6 we test the null hypothesis that $\beta = 1$, which allows for a constant risk premium. The data provide convincing evidence that the null hypothesis is violated. Only for the Deutsche mark is the marginal level of significance of the test statistic larger than 0.014. Indeed, the results for the Japanese yen, the U.K. pound, the Canadian dollar and the Swiss franc provide particularly striking evidence against the null hypothesis of unbiased daily futures prices.

The next section of the paper considers estimation of the five equations as a system to allow tests of joint hypotheses.

4.2 System Estimation

Some additional information can be gained by examining the five equations as a system since this allows joint tests of hypotheses across the various currencies. Simultaneous estimation of the ten parameters for the five currencies can be accomplished with a Generalized Method of Moments analogue to Zellner's (1962) seemingly unrelated regression. Also, since the GMM system is overidentified in this case, an additional test on the adequacy of the system is available. This is a joint test that the futures premiums at time t for each of the other four currencies, the right-hand-side variables in the other equations, are not useful in predicting $(F_{t+1,k-1} - S_t)/S_t$. As

above, there is no need to assume a conditionally homoscedastic covariance matrix for the matrix of innovations as is the case with traditional seemingly unrelated regression.

Since it is now necessary to distinguish an observation on a single currency from the vector of observations on all five currencies, let $y_{t+1}^j \equiv (F_{t+1,k-1}^j - S_t^j)/S_t^j$ and $x_t^j \equiv (F_{t,k}^j - S_t^j)/S_t^j$ for $j = 1, \dots, 5$. Define the corresponding vectors y_{t+1} and x_t to be the observations on the five currencies at time t , and let ε_{t+1} represent the vector of innovations in y_{t+1} . Similarly, define the vector function $h(y_{t+1}, x_t, \delta_0) \equiv \varepsilon_{t+1}$ with typical j th element

$$h_j(y_{t+1}, x_t, \delta_0) = y_{t+1}^j - \alpha_j - \beta_j x_t^j$$

where δ_0 is the ten element vector of parameters on α_j and β_j .

The orthogonality conditions are now given by the fact that ε_{t+1} has mean zero and is orthogonal to x_t . Let $z_t' \equiv (1, x_t')$ be the six element vector of instruments, and define the function f by

$$f(y_{t+1}, x_t, \delta) = h(y_{t+1}, x_t, \delta) \otimes z_t' \quad (32)$$

As above, the null hypothesis implies

$$E[f(y_{t+1}, x_t, \delta_0)] = 0 \quad (33)$$

when f is evaluated at the true parameter vector. This is a vector of thirty orthogonality conditions.

The GMM estimator of δ_0 is again found by constructing the sample moment corresponding to (23) and by minimizing the criterion function in (24) where W_T is now a 30 x 30 symmetric weighting matrix.

The system of equations can also be written as

$$y = X\delta_0 + \varepsilon \tag{34}$$

where $y' = (y_1^1, \dots, y_T^1, \dots, y_1^5, \dots, y_T^5)$, $\varepsilon' = (\varepsilon_1^1, \dots, \varepsilon_T^1, \dots, \varepsilon_1^5, \dots, \varepsilon_T^5)$,

$$X = \begin{pmatrix} X_1 & 0 & 0 & 0 & 0 \\ 0 & X_2 & 0 & 0 & 0 \\ 0 & 0 & X_3 & 0 & 0 \\ 0 & 0 & 0 & X_4 & 0 \\ 0 & 0 & 0 & 0 & X_5 \end{pmatrix},$$

and X_j is the $T \times 2$ matrix of observations of $(1, x_t^j)$. If the matrix of instruments is written as

$$Z = I \otimes \begin{pmatrix} z_1' \\ \vdots \\ z_T' \end{pmatrix}$$

where I is an identity matrix of dimension five, the sample orthogonality conditions are

$$g_T(\delta) = Z'(y - X\delta)/T, \tag{35}$$

and the GMM criterion function is

$$J_T(\delta) = (1/T)^2 (y - X\delta)' Z W_T Z' (y - X\delta). \tag{36}$$

This is minimized by choosing

$$\delta_T = (X' Z W_T Z' X)^{-1} X' Z W_T Z' y. \tag{37}$$

The estimate of the asymptotic covariance matrix for $\sqrt{T}(\delta_T - \delta_0)$ is

$$V(\delta_T) = (D_T' W_T D_T)^{-1} \tag{38}$$

where $D_T = Z'X/T$. Hansen (1982) demonstrates that the optimal choice

of W_T is

$$W_T = \left[\frac{1}{T} \sum_{t=1}^T (\hat{\varepsilon}_t \otimes z_t)(\hat{\varepsilon}_t \otimes z_t)' \right]^{-1} \quad (39)$$

where $\hat{\varepsilon}_t$ is a consistent estimate of ε_t .

Tests of joint hypotheses such as all β_j are equal to one or all are equal can be conducted by writing the constraint as $R\delta_T = r$ and employing a Wald test. From the asymptotic distribution theory underlying (38) we know that

$$(R\delta_T - r)' [RV(\delta_T)R'/T]^{-1} (R\delta_T - r) \quad (40)$$

is distributed as a chi-square random variable with degrees of freedom equal to the row dimension of R.

The system estimation of δ_0 is presented in Table 7. Notice that, as is often the case with seemingly unrelated regression, the parameter estimates have not changed in a particularly dramatic way, but the standard errors of the estimates have all fallen. Since the parameter estimates of the slope coefficients are also slightly smaller, there is now even stronger evidence that each β_j is not equal to one. The largest marginal level of significance of this test is only 0.0003 for the Canadian dollar. All other currencies have marginal levels of significance for this test that are smaller than 0.0001. The joint test that all β_j are equal to one is a chi-square statistic with five degrees of freedom. The value of the test statistic in this case is 81.2828 which also corresponds to a marginal level of significance smaller than 0.0001. Hence, this hypothesis is strongly rejected by the data at conventional levels of significance. The test of the hypothesis that all the β_j are equal is a chi-square statistic with four degrees of freedom. The value of the statistic is 11.8578. This indicates that the hypothesis of equality of coefficients is rejected by the data at marginal levels of significance greater than 0.0184.

As an additional test of the restrictions implied by the specification that only a constant and the own value of $(F_{t,k}^j - S_t^j)/S_t^j$ are useful in predicting $(F_{t+1,k-1}^j - S_t^j)/S_t^j$, we calculate T times the value of the minimized criterion function in (36). Hansen's (1982) Lemma 4.2 indicates that this value is distributed as a chi-square random variable with twenty degrees of freedom since this is the number of overidentifying restrictions in the estimation of the system (34). The value of the test statistic is 54.6413 which is greater than the value of a $\chi^2(20)$ associated with the 0.0001 marginal level of significance. Consequently, there is strong additional evidence that the unbiasedness hypothesis is not an appropriate characterization of the data: the other futures premiums would have been useful in predicting each of the dependent variables.

4.3 Subsample Results

The work of Lucas (1976) serves as a warning that the above econometric analysis is probably not structural in the sense that the estimated coefficients may depend upon such things as the government policies pursued by the different countries and changes in the source or type of technological disturbances that generate real growth and aggregative fluctuations. This is particularly true of changes in the variances of the underlying stochastic processes driving the system since these parameters will have a direct influence on the risk premium. An additional reason to investigate whether subperiods provide the same type of inference as the full sample is the possibility that agents may have had to learn about the new international monetary system after the abandonment of the Bretton Woods system in early 1973. It is also often argued in popular discussions that prices in speculative markets such as futures and options possess stochastic properties that correspond to theories of efficient markets only after the markets

are mature. Both of these latter reasons suggest that the results from the first half of the sample might be different from the results of the second half of the sample.

The subsample results are presented in Tables 8 to 11. Tables 8 and 10 present the single equation estimation for the first and second subsamples that corresponds to the single equation technique used in Table 6, and Tables 9 and 11 present the respective subsample system estimation corresponding to the full sample results in Table 7.

There are several interesting differences across the two subsamples in the single equation estimations that are not present in the two system estimations. The single equation results in Table 8 demonstrate evidence against the null hypothesis $\beta = 1$ only for the Canadian dollar and the Deutsche mark, while the single equation results for the second half of the sample in Table 10 indicate strong evidence against the null hypothesis only for the other three currencies, the Japanese yen, the U.K. pound, and the Swiss franc.

The system estimations tell a slightly different story. For subsample one the results in Table 9 indicate strong evidence against the null hypothesis of $\beta = 1$ for all currencies except for the U.K. pound which has an individual marginal level of significance of 0.056. All the other currencies have marginal significance levels smaller than 0.0051. The joint test that all β_j are equal to one has a marginal level of significance smaller than 0.0001. For subsample two the results in Table 11 also indicate strong rejection of the null hypothesis β_j equal to one except for the Canadian dollar which has a marginal level of significance equal to 0.0879. For all other currencies the individual marginal levels of significance are smaller than 0.0001, which is also larger than the significance level of the joint

test that all β_j are equal to one.

In the first subsample there is also strong evidence that the other futures premiums may be useful in predicting the dependent variables since the value of the test statistic for the twenty overidentifying restrictions has a value of 55.6371 which is larger than the $\chi^2(20)$ associated with the 0.0001 level of significance. For the second subperiod this strength of evidence that other data would have been useful in predicting the dependent variables is not present since the test of the overidentifying restrictions has a value of 30.2505 which corresponds to a marginal level of significance of 0.0659.

5. Interpretation

The previous section provides some strong evidence that daily futures prices are not unbiased predictors of futures prices on the following day. This section examines the implications of these findings for the variability of daily risk premiums.

Following Fama (1984), (17) can be written as

$$F_{t,k} = E_t(F_{t+1,k-1}) + P_{t,1} \quad (41)$$

which defines the one-day risk premium as the expected profit on a short position in the futures market. The transformation of variables to induce stationarity in (19) produces a normalized risk premium:

$$(F_{t,k} - S_t)/S_t = E_t[(F_{t+1,k-1} - S_t)/S_t] + p_{t,1} \quad (42)$$

where $p_{t,1} \equiv P_{t,1}/S_t$. Then, the slope coefficient β in (20) can be described as

$$\begin{aligned} \beta &= C[(F_{t+1,k-1} - S_t)/S_t; (F_{t,k} - S_t)/S_t] / V[(F_{t,k} - S_t)/S_t] \\ &= \{V[E_t(F_{t+1,k-1} - S_t)/S_t] + \\ &\quad C[E_t((F_{t+1,k-1} - S_t)/S_t); p_{t,1}]\} / V[(F_{t,k} - S_t)/S_t]. \end{aligned} \quad (43)$$

The average estimated value of β in Table 7 is approximately 0.9, and this provides an indication that $V[E_t((F_{t+1,k-1} - S_t)/S_t)]$ is greater than $V(p_{t,1})$. To see this, notice in (43) that subtracting one from two times β gives an estimate of the difference between the variances of $E_t[(F_{t+1,k-1} - S_t)/S_t]$ and $p_{t,1}$ expressed as a proportion of the variance of the futures premium, $(F_{t,k} - S_t)/S_t$. The calculation is

$$\begin{aligned} 2\hat{\beta} - 1 &= \{V[E_t((F_{t+1,k-1} - S_t)/S_t)] - V(p_{t,1})\} / V[(F_{t,k} - S_t)/S_t] & (45) \\ &= 0.8, \end{aligned}$$

with a standard error of approximately 0.04. Consequently, the data indicate much more variability in $E_t[(F_{t+1,k-1} - S_t)/S_t]$ than in $p_{t,1}$.

As noted in the Introduction, Fama (1984) and Hodrick and Srivastava (1986), using monthly data, document that variability in the risk premium in the one-month forward foreign exchange market across a number of currencies that is greater than the variability of the one-month expected rate of depreciation. We next examine if it is possible to reconcile the findings of the monthly studies with those reported here.

Discussion of these issues is facilitated by considering the logarithmic counterpart to (42) where lower case letters represent natural logarithms of their upper case counterparts:

$$f_{t,k} - s_t = E_t(f_{t+1,k-1} - s_t) + p_{t,1}, \quad (44)$$

where $p_{t,1}$ now represents the logarithmic risk premium as in Fama (1984).

A regression of $(f_{t+1,k-1} - s_t)$ on a constant and the futures premium, $(f_{t,k} - s_t)$, produces a slope coefficient similar to β in (43) which is denoted β_1 to indicate a one day forecast.

Now consider a regression of $(f_{t+2,k-2} - s_t)$ on a constant and $(f_{t,k} - s_t)$ as in

$$f_{t+2,k-2} - s_t = \alpha_2 + \beta_2(f_{t,k} - s_t) + \varepsilon_{t+2,2}, \quad (45)$$

and decompose the dependent variable as

$$f_{t+2,k-2} - s_t = (f_{t+2,k-2} - f_{t+1,k-1}) + (f_{t+1,k-1} - s_t). \quad (46)$$

Consequently, since $E_t(p_{t+1,1}) = -E_t(f_{t+2,k-2} - f_{t+1,k-1})$, we have

$$\beta_2 = \beta_1 - \{C[p_{t,1}; E_t(p_{t+1,1})] + C[E_t(f_{t+1,k-1} - s_t); E_t(p_{t+1,1})]\} / V(f_{t,k} - s_t). \quad (47)$$

Generalizing (45) through (47) to forecasts for H days ahead gives

$$\beta_H = \beta_1 - \{C[p_{t,1}; \sum_{h=1}^H E_t(p_{t+h,1})] + C[E_t(f_{t+1,k-1} - s_t); \sum_{h=1}^H E_t(p_{t+h,1})]\} V(f_{t,k} - s_t). \quad (48)$$

If the nature of the time series properties of the data is that the daily risk premiums are highly positively autocorrelated and they are either positively correlated with $E_t(f_{t+1,k-1} - s_t)$ or not particularly negatively correlated, the estimated β_H falls as we increase the forecast interval. This allows the variability of the risk premium to become large relative to that of the expected rate of depreciation as the forecast interval increases, which allows for a reconciliation of the findings using daily and monthly data.

Empirical support for this interpretation can be obtained by examining the specification

$$(F_{t+30,k-30} - S_t) / S_t = \alpha + \beta(F_{t,k} - S_t) / S_t + \varepsilon_{t+30} \quad (49)$$

which is done in Table 12 with the GMM system estimation. There are 115 nonoverlapping observations in this analysis. On comparing Tables 7 and 12, we find that the coefficient estimates for the five currencies have fallen substantially. For example, for the Canadian dollar the slope coefficient has

fallen from 0.94 to 0.08 while that for the Swiss franc has fallen from 0.89 to 0.19. Notice from (43) that the change in coefficients implies that the variability of the one-month risk premium has increased relative to that of the one month expected rate of depreciation compared to the daily data. Although we do not conduct formal tests, it appears that the monthly coefficients are significantly different from the daily ones. The standard errors further indicate rejection of the null hypothesis $\beta_j = 1$ at below the 0.0001 marginal level of significance for the Japanese yen, the Canadian dollar, and the Swiss franc, at the 0.0007 level for the U.K. pound, and the 0.0655 level for the Deutsche mark. Only the Deutsche mark coefficient is within two standard deviations of unity. The test that all of the β_j are equal to one has a value of 46.5306 which corresponds to a marginal level of significance smaller than 0.0001. If the distributions of the test statistics are appropriate, this is very strong evidence against the null hypothesis.

Of course, an alternative reconciliation of the findings recognizes that the application of asymptotic distribution theory is more appropriate the larger is the sample size. The ten years of daily data in this study provide a sample of 2420 observations whereas the cumulation of these data into changes over H days provides $2420/H$ nonoverlapping observations. The degrees of freedom in the analysis may be increased by employing all the data as was done in Hansen and Hodrick (1980), but one is still left with inherently many fewer degrees of freedom.

Korajczyk (1985) uses bootstrap techniques and Monte Carlo simulations in his study of the forward market in an attempt to assess the validity of his asymptotic distribution theory. He concludes that the fat-tailed nature of the dependent variable in financial studies such as this one may mean that convergence to the asymptotic distribution may be slower than is implied by the theory. His simulations indicate that the asymptotic distribution may

understate the probability of large values of the test statistics in sample sizes such as his 89 monthly observations.

One problem with Korajczyk's simulations involves his treatment of the right-hand-side variables. Bootstrap and Monte Carlo techniques typically employ assumptions that the regressors are fixed in repeated samples or are strictly exogenous. In the bootstrap (see Efron (1982)) a new set of dependent variables is constructed by sampling with replacement from the empirical error distribution by adding the errors to the regressors whose coefficients are constrained by the null hypothesis. If the regressors are merely predetermined endogenous variables, such a technique does not generate new future right-hand-side variables whose values would be simultaneously determined with realizations of the current errors. The degree to which this problem invalidates the simulation results is unknown, but it is clearly an area where interesting research could be done.

This study documents a rejection of the hypothesis that foreign currency futures prices are unbiased predictors of futures prices on the following day. Such a finding is consistent with the findings of studies of the forward foreign exchange market and the fact that there is little difference between forward prices and futures prices on days when they can be compared. Reconciliation of the implied variabilities of risk premiums and expected rates of currency depreciation from the studies of daily futures prices and monthly forward prices is less straightforward. Daily futures prices imply variability of risk premiums that is smaller than variability of expected rates of depreciation while the opposite is found with monthly data. One interpretation of these findings is that daily risk premiums are highly positively autocorrelated. Additional research on the time series properties of risk premiums appears warranted if this explanation is to be confirmed.

Footnotes

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1. Recent work by Korajczyk (1985) and Mark (1985) does show promise in relating rejections of unbiasedness to formal models of risk premiums that include market fundamentals.
2. The development of the preceding argument does not discuss how money is formally introduced into the model in order that it not be an asset whose rate of return is dominated. Townsend (1983) and Lucas (1984) explore the implications of cash-in-advance constraints for a subset of goods. Their theoretical results indicate that the pricing of assets with nominal payoffs is sensitive to this issue. Svensson (1985) explores an alternative timing for the acquisition of goods and assets and reaches similar conclusions. Singleton (1985) discusses how one might address these issues econometrically.
3. Cornell and Reinganum (1981) report four observations per year since the IMM provided them with the appropriate data.
4. Samuelson (1965) was clear about the nature of his joint hypothesis although he seemed more concerned about the neglect of interest rates than of risk aversion.

5. The spot rate data are also from DRI. Hence, they are measured approximately two hours prior to $F_{t,k}$.
6. Evidence in Cumby and Obstfeld (1984), Hodrick and Srivastava (1984), Hsieh (1984) and Domowitz and Hakkio (1985) suggests that conditional heteroscedasticity is present in monthly data.
7. Because the asymptotic distribution depends on the number of contracts growing large, the degrees of freedom in the analysis using daily futures data are inherently less than the number of observations.
8. Samuelson (1976) explores the properties of the variance of changes in futures prices for models with no risk premium and stationary spot prices. He demonstrates that the variance of the change in futures prices must eventually damp as the number of periods till maturity increases, but for a certain number of periods near maturity, variability may "transiently" reverse its direction. A nice feature of the current analysis is its ability to handle the inherent conditional heteroscedasticity present in sequences of futures prices.

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Table 1

Futures vs. Forwards Comparison for the Japanese Yen

Delivery Date	Comparison Date	Futures Price	Bid/Ask Spread	Raw Dev.	No. of Spreads	% of Price
12/19/73	11/15/73	3509	41	-	-	-
3/20/74	2/15/74	3380	10	-35	3.50	1.02
12/18/74	11/14/74	3317	6	-10	1.67	0.30
3/19/75	2/14/75	3423	4	7	1.75	0.20
12/17/75	11/13/75	3315	5	1	0.20	0.03
3/17/76	2/13/76	3330	5	-	-	-
12/15/76	11/11/76	3404	3	11	3.67	0.32
3/16/77	2/14/77	3505	4	-	-	-
12/21/77	11/17/77	4106	6	25	4.17	0.61
3/15/78	2/13/78	4167	2	13	6.50	0.31
12/20/78	11/16/78	5224	9	- 2	0.22	0.04
3/21/79	2/16/79	5005	4	-11	2.75	0.22
12/19/79	11/15/79	4066	4	-14	3.50	0.34
3/19/80	2/15/80	4139	7	14	2.00	0.34
12/17/80	11/13/80	4721	4	-21	5.25	0.44
3/18/81	2/13/81	4838	12	-22	1.83	0.45
12/16/81	11/12/81	4429	5	- 3	0.60	0.07
3/17/82	2/12/82	4228	6	2	0.33	0.05
12/17/82	11/11/82	3761	8	16	2.00	0.43

Table 2

Futures vs. Forwards Comparison for the Deutsche Mark

Delivery Date	Comparison Date	Futures Price	Bid/Ask Spread	Raw Dev.	No. of Spreads	% of Price
12/19/73	11/15/73	3861	4	- 7	1.75	0.18
3/20/74	2/15/74	3665	5	-	-	-
12/18/74	11/14/74	3979	6	-	-	-
3/19/75	2/14/75	4305	4	1	0.25	0.02
12/17/75	11/13/75	3865	3	-36	12.00	0.93
3/17/75	2/13/76	3933	3	6	2.00	0.15
12/15/76	11/11/76	4144	4	-	-	-
3/16/77	2/14/77	4186	2	12	6.00	0.29
12/21/77	11/17/77	4467	2	12	6.00	0.27
3/15/78	2/13/78	4787	3	29	9.67	0.61
12/20/78	11/16/78	5282	5	-	-	-
3/21/79	2/16/79	5427	4	1	0.25	0.02
12/19/79	11/15/79	5631	5	-10	2.00	0.18
3/19/80	2/15/80	5775	3	- 2	0.67	0.03
12/17/80	11/13/80	5292	4	- 6	1.50	0.11
3/18/81	2/13/81	4536	5	-23	4.60	0.51
12/16/81	11/12/81	4535	3	- 9	3.00	0.20
3/17/82	2/12/82	4211	4	-	-	-
12/15/82	11/11/82	3858	3	-10	3.33	0.26

Table 3

Futures vs. Forwards Comparison for the U.K. Pound

Delivery Date	Comparison Date	Futures Price	Bid/Ask Spread	Raw Dev.	No. of Spreads	% of Price
12/19/73	11/15/73	23780	20	- 20	1.00	0.08
3/20/74	2/15/74	22500	35	235	6.70	1.04
12/18/74	11/14/74	23000	24	- 66	2.75	0.29
3/19/75	2/14/75	23800	18	40	2.20	0.17
12/17/75	11/13/75	20360	14	-171	12.20	0.84
3/17/76	2/13/76	20160	9	- 9	1.00	0.04
12/15/76	11/11/76	16080	15	- 30	2.00	0.19
3/16/77	2/14/77	16780	9	-136	15.10	0.81
12/21/77	11/17/77	18250	9	23	2.55	0.13
3/15/78	2/13/78	19400	34	-	-	-
12/20/78	11/16/78	19515	12	- 38	3.17	0.19
3/21/79	2/16/79	19990	10	-	-	-
12/19/79	11/15/79	21445	27	85	3.15	0.40
3/19/80	2/15/80	22930	20	- 46	2.30	0.20
12/17/80	11/13/80	24070	18	-126	7.00	0.52
3/18/81	2/13/81	22950	40	- 95	2.38	0.41
12/16/81	11/12/81	18910	15	45	3.00	0.24
3/17/82	2/12/82	18370	20	- 7	0.35	0.04
12/15/82	11/11/82	16530	14	- 19	1.36	0.11

Table 4

Futures vs. Forwards Comparison for the Canadian Dollar

Delivery Date	Comparison Date	Futures Price	Bid/Ask Spread	Raw Dev.	No. of Spreads	% of Price
12/19/73	11/16/73	10000	4	-10	2.50	0.10
3/20/74	2/19/74	10275	5	6	1.20	0.06
12/18/74	11/15/74	10100	5	-17	3.40	0.17
3/19/75	2/18/75	9980	4	8	2.00	0.08
12/17/75	11/14/75	9823	4	- 7	1.75	0.07
3/17/76	2/13/76	10008	4	2	0.50	0.02
12/15/76	11/12/76	10191	4	11	2.75	0.11
3/16/77	2/15/77	9739	4	13	3.25	0.13
12/21/77	11/18/77	9011	4	4	1.00	0.04
3/15/78	2/14/78	8993	4	-12	3.00	0.13
12/20/78	11/17/78	8520	5	4	0.80	0.05
3/21/79	2/20/79	8361	3	- 1	0.33	0.01
12/19/79	11/16/79	8475	3	10	3.33	0.12
3/19/80	2/15/80	8606	4	-	-	-
12/17/80	11/13/80	8451	4	-10	2.50	0.12
3/18/81	2/13/81	8307	5	-15	3.00	0.18
12/16/81	11/12/81	8374	4	- 9	2.25	0.11
3/17/82	2/12/82	8248	5	-	-	-
12/15/82	11/11/82	8141	13	- 6	0.46	0.07

Table 5

Futures vs. Forwards Comparison for the Swiss Franc

Delivery Date	Comparison Date	Futures Price	Bid/Ask Spread	Raw Dev.	No. of Spreads	% of Price
12/19/73	11/15/73	3161	3	- 3	1.00	0.09
3/20/74	2/15/74	3126	6	- 2	0.33	0.06
12/18/74	11/14/74	3633	7	-40	5.71	1.10
3/19/75	2/14/75	4066	6	8	1.33	0.20
12/17/75	11/13/75	3774	3	-32	10.67	0.85
3/17/76	2/13/76	3937	5	2	0.40	0.05
12/15/76	11/11/76	4112	2	-	-	-
3/16/77	2/14/77	4010	3	7	2.33	0.17
12/21/77	11/17/77	4546	3	3	1.00	0.07
3/15/78	2/13/78	5221	3	86	28.67	1.65
12/20/78	11/16/78	6013	9	-39	3.55	0.65
3/21/79	2/16/79	6024	7	-13	1.86	0.22
12/19/79	11/15/79	6080	6	-28	4.67	0.46
3/19/80	2/15/80	6200	11	-	-	-
12/17/80	11/13/80	5893	9	-10	1.11	0.17
3/18/81	2/13/81	4997	9	-11	1.22	0.22
12/16/81	11/12/81	5721	9	7	0.78	0.12
3/17/82	2/12/82	5254	9	-	-	-
12/15/82	11/11/82	4490	6	18	3.00	0.40

Table 6
Full Sample Single Equation Estimates

$$(F_{t+1,k-1} - S_t)/S_t = \alpha + \beta [(F_{t,k} - S_t)/S_t] + \varepsilon_{t+1}$$

Currency	$\hat{\alpha}$	$\hat{\beta}$	R ²	Test $\beta = 1$	SEE
1. Japanese yen	.0001 (.0001) [.3747]	.9496 (.0158) [.0000]	.72	10.2167 [.0014]	.0063
2. Deutsche mark	.0002 (.0001) [.1940]	.9292 (.0290) [.0000]	.46	5.9730 [.0145]	.0061
3. U.K. pound	-.0003 (.0001) [.0206]	.9330 (.0195) [.0000]	.58	11.7977 [.0006]	.0059
4. Canadian dollar	-.0001 (.0001) [.0089]	.9412 (.0175) [.0000]	.61	11.2927 [.0008]	.0024
5. Swiss franc	-.0006 (.0002) [.0085]	.9191 (.0241) [.0000]	.53	11.2870 [.0008]	.0075

Notes: The sample period is 6/1/73 to 12/8/83 and contains 2420 observations. Standard errors are in parenthesis, and marginal levels of significance are in brackets. The test statistic in the column labelled Test $\beta = 1$ is $[(1 - \hat{\beta})/\sigma(\hat{\beta})]^2$ where $\sigma(\hat{\beta})$ is the standard error of the estimated coefficient. The test statistic is distributed as a chi-square with one degree of freedom. The marginal levels of significance below the coefficients concern the hypothesis that the value of the coefficient is zero.

Table 7
Full Sample System Estimates

$$(F_{t+1,k-1}^j - S_t^j)/S_t^j = \alpha_j + \beta_j [(F_{t,k}^j - S_t^j)/S_t^j] + \varepsilon_{t+1}^j, \quad j = 1, \dots, 5$$

Currency	$\hat{\alpha}_j$	$\hat{\beta}_j$	R ²	Test $\beta_j = 1$	SEE
1. Japanese yen	.0001 (.0001) [.3095]	.9303 (.0139) [.0000]	.72	25.3290 [.0000]	.0063
2. Deutsche mark	.0005 (.0001) [.0007]	.8665 (.0195) [.0000]	.45	47.0878 [.0000]	.0063
3. U. K. pound	-.0003 (.0001) [.0197]	.9258 (.0170) [.0000]	.58	19.1229 [.0000]	.0059
4. Canadian dollar	-.0001 (.0001) [.0074]	.9395 (.0169) [.0000]	.62	12.8669 [.0003]	.0024
5. Swiss franc	.0007 (.0002) [.0000]	.8940 (.0171) [.0000]	.53	38.5584 [.0000]	.0075

Notes: See Table 6. Test all $\beta_j = 1$, $\chi^2(5) = 81.2868$ [.0000]. Test of equality of

β_j , $\chi^2(4) = 11.8578$ [.0184]. Test of overidentifying restrictions,

$\chi^2(20) = 54.6413$ [.0000].

Table 8
Subsample One Single Equation Estimates

$$(F_{t+1,k-1} - S_t)/S_t = \alpha + \beta [(F_{t,k} - S_t)/S_t] + \varepsilon_{t+1}$$

Currency	$\hat{\alpha}$	$\hat{\beta}$	R ²	Test $\beta = 1$	SEE
1. Japanese yen	.0002 (.0001) [.0995]	.9785 (.0205) [.0000]	.87	1.0987 [.2945]	.0043
2. Deutsche mark	.0004 (.0002) [.0244]	.8973 (.0418) [.0000]	.36	6.0396 [.0140]	.0054
3. U. K. pound	-.0002 (.0002) [.1777]	.9620 (.0264) [.0000]	.66	2.0590 [.1513]	.0049
4. Canadian dollar	-.0001 (.0001) [.0067]	.9373 (.0198) [.0000]	.73	10.0443 [.0015]	.0019
5. Swiss franc	.0005 (.0003) [.0352]	.9477 (.0392) [.0000]	.47	1.7808 [.1821]	.0062

Notes: The sample period begins at 6/1/73 and contains the first 1210 observations.

Also, see Table 6.

Table 9
Subsample One System Estimates

$$(F_{t+1,k-1}^j - S_t^j)/S_t^j = \alpha_j + \beta_j [(F_{t,k}^j - S_t^j)/S_t^j] + \varepsilon_{t+1}^j, \quad j = 1, \dots, 5$$

Currency	$\hat{\alpha}_j$	$\hat{\beta}_j$	R^2	Test $\beta_j = 1$	SEE
1. Japanese yen	.0002 (.0001) [.0538]	.9509 (.0175) [.0000]	.87	7.8556 [.0051]	.0030
2. Deutsche mark	.0006 (.0002) [.0006]	.8279 (.0330) [.0000]	.36	27.1591 [.0000]	.0038
3. U.K. pound	-.0002 (.0002) [.1973]	.9553 (.0234) [.0000]	.66	3.6520 [.0560]	.0035
4. Canadian dollar	-.0002 (.0001) [.0080]	.9337 (.0192) [.0000]	.73	11.9104 [.0006]	.0014
5. Swiss franc	.0007 (.0002) [.0012]	.8969 (.0298) [.0000]	.47	11.9732 [.0005]	.0044

Notes: See Table 8. Test of all $\beta_j = 1$, $\chi^2(5) = 48.3672$ [.0000]. Test of equality of

β_j , $\chi^2(4) = 12.8075$ [.0123]. Test of overidentifying restrictions,

$\chi^2(20) = 55.6371$ [.0000].

Table 10
Subsample Two Single Equation Estimates

$$(F_{t+1,k-1} - S_t)/S_t = \alpha + \beta [(F_{t,k} - S_t)/S_t] + \varepsilon_{t+1}$$

Currency	$\hat{\alpha}$	$\hat{\beta}$	R ²	Test $\beta = 1$	SEE
1. Japanese yen	.0005 (.0003) [.1091]	.8924 (.0301) [.0000]	.43	12.7688 [.0004]	.0079
2. Deutsche mark	-.0001 (.0003) [.7787]	.9540 (.0397) [.0000]	.48	1.3438 [.2464]	.0068
3. U. K. pound	-.0002 (.0002) [.2294]	.8728 (.0346) [.0000]	.40	13.5555 [.0002]	.0067
4. Canadian dollar	-.0001 (.0001) [.2010]	.9438 (.0321) [.0000]	.50	3.0676 [.0799]	.0028
5. Swiss franc	.0005 (.0004) [.1829]	.9141 (.0325) [.0000]	.51	7.0330 [.0080]	.0086

Notes: The sample period ends at 12/8/83 and contains the last 1210 observations.

Also, see Table 6.

Table 11
Subsample Two System Estimates

$$(F_{t+1,k-1}^j - S_t^j)/S_t^j = \alpha_j + \beta_j [(F_{t,k}^j - S_t^j)/S_t^j] + \varepsilon_{t+1}^j, \quad j = 1, \dots, 5$$

Currency	$\hat{\alpha}_j$	$\hat{\beta}_j$	R ²	Test $\beta_j = 1$	SEE
1. Japanese yen	.0007 (.0003) [.0152]	.8562 (.0262) [.0000]	.43	30.1638 [.0000]	.0056
2. Deutsche mark	.0004 (.0002) [.4239]	.8636 (.0250) [.0000]	.46	29.7165 [.0000]	.0050
3. U. K. pound	-.0002 (.0002) [.2510]	.8664 (.0274) [.0000]	.40	23.8227 [.0000]	.0047
4. Canadian dollar	-.0001 (.0001) [.2867]	.9492 (.0298) [.0000]	.50	2.9132 [.0879]	.0020
5. Swiss franc	.0010 (.0003) [.0018]	.8731 (.0223) [.0000]	.51	32.4438 [.0000]	.0061

Notes: See Table 10. Test of all $\beta_j = 1$, $\chi^2(5) = 59.9767$ [.0000]. Test of equality of

β_j , $\chi^2(4) = 6.8491$ [.1441]. Test of overidentifying restrictions,

$\chi^2(20) = 30.2505$ [.0659].

Table 12
Monthly Data System Estimates

$$(F_{t+30,k-30}^j - S_t^j)/S_t^j = \alpha_j + \beta_j [(F_{t,k}^j - S_t^j)/S_t^j] + \varepsilon_{t+30}^j, \quad j = 1, \dots, 5.$$

Currency	$\hat{\alpha}_j$	$\hat{\beta}_j$	R^2	Test $\beta_j = 1$	SEE
1. Japanese yen	.0001 (.0026) [.9752]	.4552 (.1377) [.0009]	.03	15.6610 [.0000]	.0317
2. Deutsche mark	-.0020 (.0029) [.4944]	.5613 (.2382) [.0184]	.03	3.3927 [.0655]	.0338
3. U. K. pound	-.0059 (.0023) [.0091]	.3691 (.1868) [.0482]	.03	11.4073 [.0007]	.0256
4. Canadian dollar	-.0035 (.0010) [.0003]	.0786 (.2247) [.0727]	.00	16.8086 [.0000]	.0122
5. Swiss franc	.0036 (.0037) [.3365]	.1875 (.1832) [.3061]	.00	19.6647 [.0000]	.0417

Notes: There are 115 nonoverlapping observations. Also, see Table 6. Test of all

$\beta_j = 1, \chi^2(5) = 46.5306$ [.0000]. Test of equality of $\beta_j, \chi^2(4) = 4.9459$ [.2929].

Test of overidentifying restrictions, $\chi^2(20) = 28.128$ [.1064].