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ADJUSTMENT TO MONETARY POLICY AND DEVALUATION  
UNDER TWO-TIER AND FIXED EXCHANGE RATE REGIMES

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ABSTRACT

The purpose of this paper is to determine whether a two-tier exchange rate regime is more effective than a fixed rate regime in increasing a country's ability to pursue an independent monetary policy in the short run. The analysis compares adjustment to a monetary policy and to a devaluation in the two exchange rate regimes in a portfolio model under imperfect asset substitutability. It is shown that the two policies have in the short run larger effects on interest rates under a two-tier regime. The duration of this effect, however, is longer under a fixed rate regime. The analysis is conducted for the case of static and rational expectations, demonstrating that the above results do not depend on the expectation mechanism.

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## I. Introduction Summary

The recent experience of various countries has renewed interest in a two-tier exchange rate regime. In such a regime different exchange rates are applied for current account and capital account transactions. One possible version of a two-tier system pegs the commercial exchange rate, whereas the financial exchange rate is free to fluctuate and to be determined by market forces. A country might adopt a two-tier exchange rate in order to increase its ability to pursue an independent monetary policy, and to reduce its exposure to interest-sensitive and speculative capital flows. The purpose of this paper is to consider to what degree a two-tier regime is capable of performing the first task, i.e., increasing monetary independence.

In some respects, a two-tier exchange rate might be viewed as a compromise between fixed and floating exchange rates. Under fixed exchange rate the adjustment in the market for foreign exchange is a quantity adjustment, whereas under a floating rate it is a price adjustment. In a two-tier exchange rate the adjustment is assigned to quantities in the submarket for foreign exchange that reflects current account transactions, and to prices in the submarket associated with capital account transactions. As a result, a two-tier exchange rate inhibits foreign capital flows. Any excess demand for foreign capital is cleared only by adjustment of the rate of return on foreign capital, and not by actual inflows of foreign capital.

Previous contributions by Marion (1981) and Flood and Marion (1982) have analyzed the isolating properties of a two-tier exchange rate in portfolio balance models.<sup>1</sup> The portfolio approach, developed among others by Branson (1974), Dornbusch (1976) and Kouri (1976) suggests that the short-run equilibrium of the exchange rate and returns of various assets is determined

so as to equilibrate the market for financial assets. Over time, the economy is propelled to its long run equilibrium by accumulation of assets via the current account.

The purpose of this paper is to use a related framework to analyze and compare the adjustment process to monetary shocks under two-tier and fixed exchange rate regimes. More specifically, the paper asks if a two-tier exchange rate regime increases the ability of a country to pursue an independent monetary policy more than a fixed exchange rate regime. In general, the long run effects of the same policy may differ between the two exchange rate regimes. To make the comparison meaningful, therefore, the analysis considers policies that result in the same long run effects under both regimes, assuming that we start from the same equilibrium. We find that there is a short run trade-off between quantity adjustment and the adjustment of rates of return of various assets. Because a two-tier regime constrains the quantity adjustment in the foreign capital market, the short run adjustment of rates of return under a two-tier exchange rate will exceed their adjustment under a fixed exchange rate. Thus, in the short run a monetary injection has a greater effect on interest rates under a two-tier exchange rate than under a fixed rate. The duration of this effect, however, turns out to be longer under a fixed rate than under a two-tier regime. The result of the larger response of rates of return in a two-tier exchange rate is to induce in the short run a larger current account adjustment to the new policy (relative to its adjustment in a fixed rate regime). Because the total accumulative current account adjustment proves to be the same under both exchange rate regimes, we can conclude that the speed of adjustment to the new long run equilibrium is larger under a two-tier exchange rate regime. This result is strengthened by another factor: a fixed exchange rate regime allows a

swap of domestic money balances for foreign assets, whereas such a channel is closed by a two-tier exchange rate. Following an expansion of the money supply we will get under a fixed rate an instantaneous adjustment to composition disequilibrium in the money market, via a swap of money for traded assets. This adjustment will eliminate part of the monetary expansion, having the effect of increasing the service account surplus and reducing the overall current account deficit that resulted from the pursuit of a monetary expansion under a fixed rate regime. Thus, the service account effect works to further reduce the speed of adjustment under a fixed rate regime, relative to a two-tier system.

The speed of adjustment to the new long run equilibrium is interesting because of its implications for the ability of a country to sterilize balance of payments adjustment in the short run. A country which would like to conduct an independent monetary policy might find it desirable to sterilize the balance of payments effects in the short run.<sup>2</sup> A more rapid speed of adjustment reduces the sterilization capacity of the central bank, in turn reducing the ability of monetary policy to significantly influence the economy.

The same type of result is found for a devaluation, which is designed to generate the same long run equilibrium under the two exchange rate regimes. A devaluation of the commercial rate in a two-tier regime will generate short run undershooting of the financial rate, which implies that the rate of return on foreign assets will increase. This paper shows that in a two-tier exchange system rates of return on financial assets will increase more following the devaluation than under a fixed rate system. The devaluation will generate a larger current account surplus in a two-tier regime, implying a quicker adjustment under a two-tier regime towards the new equilibrium.

The analysis is conducted first for the case of static expectations.

Then, it is contrasted with the case of rational expectations. It is shown that the results of the paper hold for both expectation mechanisms. The policies analyzed in the paper for a two-tier regime cause a short run deviation of the financial rate from its long run equilibrium level. It is shown that the effect of rational expectations is to mitigate this deviation, resulting in a smaller change of the return on foreign assets in a two-tier regime, relative to the case of static expectations.

To summarize, a two-tier regime does not necessarily increase the capacity of the economy to pursue an independent monetary policy relative to a fixed rate. The effect of a given monetary injection on interest rates is larger in the short run under a two-tier exchange rate, however the duration of those effects is larger in a fixed rate system. The same implications apply for the effects of a devaluation which extracts the same long run effects in both regimes.

Section II presents the model, Section III applies it to the analysis of a monetary injection, and Section IV evaluates the adjustment to a devaluation. Section V describes the case of rational expectations.

## II. The Model

Let us consider a small, open economy, under either a fixed or a two-tier exchange rate regime. The purpose of the analysis is to compare financial adjustment to various shocks under the two alternative regimes. To focus on those aspects, let us take the case in which output is composed of one traded good, and wage and price flexibility generates full employment, fixing real output at its equilibrium level ( $y$ ). The financial sector is based on the work of Kouri and Porter (1974). There are three assets: domestic bonds, foreign bonds, and domestic money balances. Foreign bonds are of the consol

type (perpetual annuity), whereas domestic bonds are short-term assets. If the domestic bonds are treated as consols, disturbances may create capital gains or losses on domestic bonds. However, this potential transmission does not affect the main results of the analysis.

The domestic money supply consists exclusively of the liabilities of a central bank, which holds both domestic and foreign currency assets. Domestic bonds and money balances are held only by domestic citizens, and the country is assumed to be too small to influence the foreign interest rate,  $r^*$ .

The three assets are gross and imperfect substitutes, and the assets demand functions are given by:

$$\begin{aligned}
 & l(r, \bar{r}^*) \cdot V = \text{demand for money} \\
 (1) \quad & f(r, \bar{r}^*) \cdot V = \text{demand for foreign bonds} \\
 & \chi(r, \bar{r}^*) \cdot V = \text{demand for domestic bonds.}
 \end{aligned}$$

where  $V$  is nominal wealth; and  $l$ ,  $f$ ,  $\chi$  are the desired portfolio shares of domestic money balances, foreign bonds, and domestic bonds. Each is a function of the return on domestic bonds ( $r$ ) and foreign bonds ( $\bar{r}^*$ ) facing domestic citizens.<sup>3</sup> The signs of the partial effects of the various variables are determined by the assumption of gross substitutability.<sup>4</sup> The analysis takes the case in which inflation is zero, assuming real domestic expenditure to be a function of real disposable income and the rates of return on the various assets:

$$(2) \quad E = E(y^d, r, \bar{r}^*) ; \quad 0 < 1 - E_1 < 1 ; \quad E_2, E_3 < 0 .$$

where  $y^d$  is disposable real income. Suppose that interest payments on public debt are financed completely by lump sum taxes. In such a case real disposable income is given by:

$$(3) \quad y^d = y + \Delta$$

where  $\Delta$  is the (real) service account surplus. Let  $M$  and  $X$  denote nominal money balances and domestic bonds. Asset market equilibrium is obtained where:

$$(4) \quad l \cdot V = M$$

$$(5) \quad \chi \cdot V = X$$

Notice that the wealth constraint implies that  $\chi + l + f = 1$ . Thus, clearing two asset sub-markets is enough to ensure that all asset markets clear.

#### II a. A Two-Tier Exchange Rate

Let  $e_c$  denote the exchange rate used for current account transactions. The central bank is committed to pegging its value to a pre-announced level. Let  $e_f$  denote the exchange rate used for financial transactions. It is allowed to fluctuate and to be market determined. In such a system, the principal on foreign bonds must be acquired and repatriated at the financial exchange rate ( $e_f$ ). Interest income, which is a current account item, must be repatriated at the commercial rate. Nominal wealth is given by:

$$(6) \quad V = M + X + e_f \cdot \frac{F}{r^*}$$

where  $r^*$  is the foreign interest rate.<sup>5</sup> The market value of foreign bonds is evaluated using the financial rate. Suppose that the choice of units is such that the international price of the good is one, causing the domestic price to be given by  $e_c$ . In such a case, the real service account surplus is given by:

$$(7) \quad \Delta = r^* \left( \frac{F}{r^*} \right) = F$$

The price of a foreign bond is given by  $e_f \left( \frac{1}{r^*} \right)$ . Such a bond will pay next period interest of one unit of foreign exchange, which will be repatriated at rate  $e_c$ . Thus, the domestic return on foreign bonds  $\bar{r}^*$ , is:<sup>6</sup>

$$(8) \quad \bar{r}^* = \frac{e_c}{e_f} \cdot r^*$$

The net return on foreign bonds should in principle include also the expected capital gain due to expected depreciation. To simplify, let us start the analysis with static expectations. Section V evaluates the case of rational expectations. It is shown that the results of the paper hold for both expectation mechanisms. The current account surplus is given by:

$$(9) \quad e_c (y + F - E)$$

In a two-tier system the stock of foreign bonds is not allowed to adjust. Thus, the current account surplus increases the domestic money supply by increasing the foreign asset component of the central bank's assets.

Assuming no active monetary policy, we get that over time:

$$(10) \quad \dot{M} = e_c(y + F - E) \quad .$$

A short run equilibrium is determined by the clearing of asset markets. Because under a two-tier regime money supply can be adjusted only via a current account surplus, money balances are given in the short run. Therefore there are two endogenous variables in the short run: the two rates of return  $r, r^*$ . They are determined by eq. 4 and 5.

Curve xx, Figure one, describes combinations of the financial exchange rate ( $e_f$ ) and domestic interest rate that are compatible with equilibrium in the domestic market bonds (eq. 5). An increase in the domestic interest rate results in excess demand for domestic bonds. To clear the market for domestic bonds the return on foreign bonds should increase enough to eliminate the excess demand for domestic bonds. Because  $r^*$  is exogenously given, it implies that  $e_f$  should drop. Thus, xx is downward sloping. Curve mm, Figure one, describes combinations of  $(r, e_f)$  that are consistent with money market equilibrium. An increase in the domestic interest rate results in an excess supply of money balances. To clear the money market, the domestic return on foreign bonds should drop, or  $e_f$  should increase. Thus, mm is upward sloping.

The short run equilibrium is determined at the intersection of the two curves. Long run equilibrium occurs only when the current account is balanced. For example, if at point A we have a current account surplus, money balances will increase over time. At a given financial exchange rate ( $e_f$ ), higher money balances induce excess supply in the money market. This excess is cleared by a drop in the interest rate, shifting mm to m'm'. At a given financial exchange rate, higher money balances also imply higher nominal

wealth. This situation induces excess demand for domestic bonds which is cleared by a drop in the domestic interest rate, shifting  $xx$  to  $x'x'$ . This process will continue over time, till we reach current account equilibrium. At this stage, assets holdings are at their long run equilibrium level.

## II b. A Fixed Rate

Let  $e_0$  denote the exchange rate under a fixed rate regime. Because the same rate is used for financial and commercial transactions,  $e_0 = e_f = e_c$ . Because the exchange rate is unified, the domestic return on foreign assets is exogenously given, at a rate  $r^*$ . In the short run only the domestic interest rate is endogenously determined, by eq. 5. Notice that with a fixed rate the sum of money balances plus foreign bonds is a state variable, given in the short run. Their desired composition is achieved by a swap<sup>7</sup> which does not change  $M + e_0 \cdot \frac{F}{r^*}$ . Suppose that the exchange rate is given by  $e_0 = 1$ . A short run equilibrium occurs at a point like A (Figure one), where curve RR defines the interest rate that clears the market for domestic bonds for a given  $M + e_0 \cdot F/r^*$ . Over time,  $M + e_0 \cdot F/r^*$  is affected by a current account surplus :

$$(11) \quad \dot{M} + e_0 \cdot \frac{\dot{F}}{r^*} = e_0 (y + F - E)$$

If at point A we get a current account surplus, RR will gradually shift to the left. The effect of a current account surplus is to accumulate assets over time. The increase in wealth induces excess demand for domestic bonds which is cleared by a drop in the domestic interest rate (RR shifts to R'R'). This process will continue, till we reach current account equilibrium. At this stage we get stock and flow asset market equilibrium.

The long run equilibrium under both regimes is found by adding to the conditions defining short run equilibrium the requirement that the current account should be balanced. Thus, money supply is endogenously determined in the long run in both regimes, and a similar result obtains for the holdings of foreign bonds in a fixed rate regime.

### III. Adjustment to a Monetary Injection

In order to compare the adjustment process in the two exchange rate regimes, suppose that we start from the same point of long run equilibrium, point A (Figure one), where the exchange rate is one ( $e_o = e_f = e_c = 1$ ). To make the comparison meaningful, let us consider policies that will generate the same long run equilibrium under each of the two regimes. As section II has shown, money balances are endogenous in the long run in both regimes. Thus, an unexpected monetary injection, brought about by a lump-sum transfer, is neutral in the long run. Let us compare in this section the impact effect of such an injection and the adjustment to it under each regime.

#### III. a. The Impact Effect

Let us start with the case of a fixed exchange rate. At a given interest rate the increase in money balances increases nominal wealth, resulting in excess demand for domestic bonds. A short run equilibrium is obtained by a decline of the interest rate, which drops enough to clear the domestic bond market. RR shifts to the left, and the short run equilibrium is obtained at point C. The effect of the increase in money balances and the drop in interest rate is to generate excess demand for foreign bonds at point C. Equilibrium is obtained by an instantaneous swap of domestic money for foreign bonds. From eq. 4 and 5 we obtain that under a fixed exchange rate the impact

effect of the monetary injection is:

$$(12) \quad \frac{dr}{dM} = - \frac{\chi}{\chi_r \cdot V} < 0$$

$$(13) \quad \frac{dF}{dM} = \frac{\frac{dr}{dM} [f_r \cdot V] + f}{V_F} > 0$$

The main difference between a fixed rate and a two-tier regime is that under the first regime the domestic return on foreign bonds is given and the holdings of foreign bonds are allowed to adjust; whereas under the second regime the holdings of foreign bonds are given and the domestic return on foreign bonds ( $\bar{r}^*$ ) is allowed to adjust to clear the asset markets. As was described in section II, the impact effect of a monetary injection is to shift both mm and xx curves to the left to m'm', and x'x'; resulting in a lower interest rate.

Notice that at the initial financial rate ( $e_f = 1 = e_0$ ) the value of money plus foreign bonds is the same under a fixed rate and a two-tier regime. Therefore, at the initial financial rate the same domestic interest rate clears the market for domestic bonds under the two regimes. Thus the short run equilibrium under a fixed rate (point C) is on curve x'x'. At point C we get excess demand for foreign bonds resulting from a lower domestic interest rate and higher nominal wealth. Under a fixed rate, this excess demand is cleared by purchase of foreign bonds (via a swap). Under a two-tier exchange rate, however, this channel is not open. The excess demand for foreign bonds will bid up the financial exchange rate, reducing the domestic return on foreign bonds. Therefore, if we wish to clear the market for both

domestic and foreign bonds we should move on curve x'x' upwards, to the left. This process will continue until  $\bar{r}^*$  is depressed enough to clear the excess demand for foreign bonds. During this adjustment, the domestic interest rate will drop to keep the market for domestic bonds in equilibrium. Short run equilibrium will occur at a point like B.

Comparing the impact effect of the monetary injection under the two regimes, we see that rates of return will be depressed more under a two-tier regime. A quantity constraint in the market for foreign bonds magnifies the needed adjustment of rates of return; and there is a trade-off between quantity and rates of return adjustment. Notice that the long run equilibrium is at point A in both regimes. Thus the financial exchange rate overshoots in response to the monetary injection.

### III.b. The Adjustment Process

At point B, the new short run equilibrium under a two-tier regime, we observe lower rates of return on domestic and foreign assets. Lower interest rates will encourage expenditure, generating a current account deficit at point B. Because a two-tier regime prevents the private sector from adjusting its holding of foreign bonds (F), the current account deficit is matched by an equivalent decline in money balances (and depletion of foreign reserves held by the central bank). From eq. 10 we get that the impact effect on the balance of payment is:

$$(14) \quad \frac{d\dot{M}}{dM} = -E_2 \frac{dr}{dM} - E_3 \frac{dr^*}{dM} < 0$$

Over time, the gradual reduction in money balances will slowly shift m'm', x'x' curves to the right, moving us to the long run equilibrium at point

A. During this process we will observe a current account deficit, appreciation of the financial rate, and an upward trend in rates of return  $(r, \bar{r}^*)$ .

Under a fixed rate regime, short run equilibrium occurs at point C. The impact effect of the monetary injection ( $dM$ ) is to generate at this point a current account adjustment, given by:

$$(15) \quad \frac{d\dot{M} + e_0 \cdot \dot{F}/r^*}{dM} = (1-E_1) \frac{dF}{dM} - E_2 \frac{dr}{dM}$$

As eq. 12, 13 demonstrated, the effect of the monetary injection is to increase holdings of domestic bonds  $(\frac{dF}{dM} > 0)$  and to reduce interest rates  $(\frac{dr}{dM}) < 0$ . Increasing the holding of foreign bonds implies a larger service account surplus, whereas a lower interest rate increases expenditure, inducing a current account deficit. To ensure stability, it is assumed that the second effect dominates the first, such that at point C we get a current account deficit. The effect of such a deficit is to reduce wealth gradually and to increase the interest rate, shifting curve R'R' towards the long run equilibrium (A).

Comparing eq. 14 and 15, we find that the monetary injection induces larger current account deficits under a two-tier regime. This occurs because the drop in interest rates  $(r, \bar{r}^*)$  is smaller in the fixed exchange rate regime, implying a larger increase in consumption under a two-tier regime. A second force working to mitigate the current account deficit under a fixed rate regime is the increase in the service account surplus which results from the swap of money balances for foreign bonds that occurs following the monetary injection. Notice that the total accumulative current account deficit during the adjustment to the long run equilibrium is the same under

the two exchange rate regimes, and is equal to the monetary injection. Thus, we can conclude that the speed of adjustment is lower under a fixed rate regime than under a two-tier exchange rate regime.

#### IV. A Devaluation

Let us compare the adjustment process to a devaluation of the same magnitude under the two regimes ( $de_c = de_o > 0$ ). As can be seen from the long run equilibrium conditions, a devaluation is not neutral in the long run because of the existence of a nominal asset whose holdings are exogenously given: domestic bonds.<sup>8</sup> It will be neutral only if it is coupled with an expansion of domestic bonds at the devaluation rate;  $dX = X de_o$ . As in Section III, the analysis in this section will compare the speed of adjustment in the two regimes to the new long run equilibrium. This will be done by means of comparing the resulting current account deficit under the two regimes. This comparison provides information on the speed of adjustment only if the new long run equilibrium following the devaluation is the same for both regimes, because then the needed cumulative current account surplus is the same. To be able to use this strategy, let us design the devaluation such as to yield the same long run equilibrium for both regimes. Consider the case in which we start from an equivalent long run equilibrium in both regimes, and an unexpected devaluation occurs which is coupled with an expansion of domestic bonds at the devaluation rate. (I.e.  $de_o = de_c > 0$ ;  $dX = X de_o$ ).

Alternatively, take the case of a simple devaluation in an economy whose domestic bonds are indexed to the price level, because in such a case a devaluation is neutral in the long run without any expansion of domestic bonds.

#### IV. a. The Impact Effect

Following the devaluation we get an expansion of domestic wealth at a smaller rate than the rate of expansion in the nominal value of domestic bonds. Thus, we get an excess supply of domestic bonds which is cleared in a fixed rate regime by an increase in interest rates:

$$(16) \quad \frac{dr}{de_0} = \frac{\chi^M}{V \cdot \chi^R} > 0$$

In terms of Figure two, we move to a new short run equilibrium at point C. In moving from A to C, we observe a readjustment of the portfolio composition; which is achieved by swapping foreign bonds for money balances. Thus, at the new short run equilibrium we get higher nominal balances and lower holdings of foreign bonds relative to the initial equilibrium.

Under a two-tier regime the devaluation applies only for the commercial rate. At a given financial rate the devaluation generates an excess supply of domestic bonds (because the value of domestic bonds increases at a rate higher than the expansion in wealth). Thus, in order to clear the market for domestic bonds, the domestic interest rate should go up, shifting curve  $xx$  to  $x'x'$ . Notice that for a financial rate that equals the new fixed exchange rate, wealth is equal in both regimes for the same interest rate. Thus, for  $e_f = 1 + de_0$ , the same interest rate clears the market for domestic bonds in both regimes, implying that point C is on curve  $x'x'$ . At point C we get excess demand for money balances and an excess supply of foreign bonds. Under a fixed rate regime this portfolio composition disequilibrium is cleared by an instantaneous swap. Under a two-tier regime, however, the stock of foreign bonds is not allowed to adjust, and money balances can adjust only over time. Therefore the rates of return  $(r, \bar{r}^*)$  should adjust moving us on  $x'x'$

to the new short run equilibrium. Notice that moving on  $x'x'$  upward implies lower rates of return on both domestic and foreign assets, whereas moving downward implies the opposite. Thus, short run equilibrium in a two-tier regime can occur only on the position of  $x'x'$  below C, at points like B or B'.

There are two opposing forces at work on curve  $mm$ : at a given financial exchange rate we get a higher return on foreign assets (because  $de_c > 0$ ), reducing the demand for money. At the same time, the nominal wealth expansion works to increase the demand for domestic money. As a result, curve  $mm$  can shift in either direction, but in any case we can conclude that following the devaluation  $\frac{de_f}{de_c} < 1$ . Because such a devaluation is neutral in the long run, we can conclude that the financial rate will undershoot its new long run equilibrium level (which is  $1 + de_c$ ).

Comparing the short run adjustment in the two regimes, we see that rates of return will adjust upward more under a two-tier regime. As in the case of monetary expansion, we find that quantity constraint on foreign bonds shifts the burden of adjustment in the short run to rates of return.

#### IV. b. The Adjustment Process

The increase in the rates of return will reduce consumption, inducing a current account surplus at the new short run equilibrium. In a two-tier regime this implies a gradual increase in domestic money balances which will gradually shift  $m'm'$ ,  $x'x'$  to the left, moving us over time towards the new long run equilibrium (point D). During this adjustment, both rates of return will decline, assets value will increase, and the financial exchange rate will depreciate.

Under a fixed rate regime, short run equilibrium occurs at point C, where the increase in the domestic interest rate generates a current account

surplus. Over time the resulting accumulation of foreign assets will gradually move us along line CD towards the new long run equilibrium. During this process the domestic interest rate will fall, to accommodate the increase in assets. Final equilibrium under both regimes occurs at point D. The long run effect of the devaluation is to increase the reserve holdings in the central bank, otherwise the devaluation is neutral. Notice that we arrive at the neutrality only because we assumed that the devaluation was accompanied by the right expansion of domestic bonds, or alternatively that domestic bonds were indexed to the price level.

In both regimes the current account surplus following the devaluation is:

$$(17) \frac{d\dot{M} + e \cdot \dot{F}/r^*}{de} = (1 - E_1) \frac{dF}{de} - E_2 \frac{dr}{de} - E_3 \frac{dr^*}{de}$$

where under a fixed rate regime  $de = de_0$ ,  $dr^* = 0$ ; and under a two-tier regime  $de = de_c$ ,  $\dot{F} = 0$ . Using the analysis of this section we conclude that the devaluation will induce a larger current account surplus under a two-tier regime. As in the case of a monetary expansion, there are two reasons explaining this: first, the interest rate will respond more under a two-tier regime. Next, under a fixed rate regime we get an adjustment in the service account surplus following the devaluation. Because of the swap of foreign bonds for money, we find a decrease in the service account surplus which reduces the current account surplus. Such an adjustment does not occur in a two-tier regime. In both regimes the accumulative current account surplus during the adjustment process to the new equilibrium is the same, equal to  $M \cdot de_0$ , where  $M$  is the money holdings at the initial equilibrium. Therefore, we can conclude that the speed of adjustment is lower under a fixed rate regime relative to a two-tier regime.

## V. The Role of Expectations

The previous discussion assumed static expectations. In such a case assets holders in a two-tier regime ignore expected capital gains on foreign bonds due to expected depreciation of the financial rate. The purpose of this section is to analyze how allowing for rational expectations modifies the results. It turns out that all the previous results stay intact. The effect of rational expectation is only to mitigate the short run deviation of the financial exchange rate from its long run level under a two-tier regime. However, even with rational expectations rates of return will adjust more in the short run under a two-tier regime relative to a fixed rate; and the adjustment will be slower in a fixed rate relative to a two-tier regime.

The new aspect of rational expectation is that now the net domestic return on holdings of foreign bonds is:

$$(8') \quad \bar{r}^* = \frac{e_c}{e_f} \cdot r^* + \frac{\dot{e}_f}{e_f}$$

The second term reflects the expected capital gains due to future depreciation of the financial exchange rate. Notice that under a unified exchange rate net domestic return on foreign bonds equals the foreign interest rate. Thus, adding rational expectations under a fixed rate does not alter the discussion. Under a two-tier regime short run equilibrium is defined, as before, by eq. 4 and 5, using eq. 8' as the relevant net rate of return on holding of foreign bonds. The adjustment is governed by eq. 10 (using the modified  $\bar{r}^*$ ). Taking a linear approximation of the economy around the long run equilibrium we can describe the system by the following two-motion equation:

$$(18) \quad \begin{aligned} \dot{e}_f &= g_1(e_f, M) \\ \dot{M} &= g_2(e_f, M) \end{aligned}$$

For given values of  $M$ ,  $e_f$ , we get the interest rate that clears the domestic bonds market by means of eq. 5. Assuming that the necessary conditions for saddle path stability hold, we get that around the long run equilibrium

$$(19) \quad \dot{e}_f = \theta(\bar{e}_f - e_f)$$

where  $\bar{e}_f$  is the long run value of the financial exchange rate.<sup>9</sup> Thus, for a given financial exchange rate  $e_f$  we get

$$(20) \quad r^* = \frac{e_c \cdot r^* + \theta(\bar{e}_f - e_f)}{e_f}$$

As in section II, we can plot curves  $xx$ ,  $mm$  describing the short run equilibrium. The slope of  $xx$  is given by:

$$\frac{de_f}{dr} = - \frac{\chi_r \cdot V}{\chi \cdot V_{e_f} - \chi_{r^*} \cdot [\bar{e}_f \cdot \theta + e_c \cdot r^*] / e_f^2}$$

The case of static expectation is where  $\theta = 0$ . Notice that allowing for rational expectation ( $\theta > 0$ ) will make  $xx$  flatter. Let  $x_s x_s$  be the  $xx$  curve under static expectations, and point H some point on it, with  $e_f > \bar{e}_f$  (see figure 3). For  $e_f > \bar{e}_f$  we expect appreciation, implying a lower net return on foreign assets under rational expectations. This works to increase the demand for domestic bonds. Thus, at point H we get excess demand for domestic bonds

under rational expectations. Thus, for a given  $e_f$  a lower interest rate will clear the market for domestic bonds, at a point like H'. In a similar way, for  $e_f < \bar{e}_f$  we expect depreciation, implying that we need a higher interest rate to clear the domestic bonds market under rational expectations. In a similar way, curve mm is flatter under rational expectations.

Let us analyze the effect of a monetary injection. Suppose that we start with long run equilibrium at point A. As in Section III, under a fixed rate short run equilibrium is at point C. Notice that for  $e_f = \bar{e}_f$  expected depreciation is zero. Thus, for  $e_f = \bar{e}_f$ , the xx and mm curves shift by the same distance under static and rational expectations. Because both curves are flatter with rational expectations, short run equilibrium under a two-tier regime is at a point like B'. Point B is no longer equilibrium because at this point we expect appreciation, implying that at point B we get an excess demand for domestic bonds and an excess supply of foreign bonds. This is cleared by a drop in the financial rate which works to increase net domestic return on foreign bonds sufficiently to clear both markets. Thus, allowing for rational expectation we need smaller overshooting of the financial rate following the monetary injection, because part of the drop in net return on foreign assets is captured by the expected appreciation. Notice, however, that compared with the fixed rate case, we find that under a two-tier exchange rate regime, even with rational expectations, we get in the short run a larger drop in net returns on assets (compare point B' to point c).

Because we observe in the short run lower net rates of return in a two-tier regime, we get a larger current account surplus, and the argument of Section III is not modified by the existence of rational expectations. The discussion of this Section applies also for the case of unexpected depreciation. Allowing for rational expectation, we get that under a two-tier

regime short run equilibrium is at points like  $(H, H')$  instead of  $(B, B')$ , Figure two. All the results of Section IV stay intact. Notice that allowing for rational expectation we get a smaller depreciation of the financial exchange rate following a monetary injection, and a larger depreciation following a devaluation of the commercial rate relative to the case of static expectation. That is because in the first case the long run equilibrium financial rate does not change, whereas it goes up in the second case.

### Comments

1. Their studies showed that a two-tier regime can isolate (under certain conditions) the effects of foreign interest rate disturbances, and that the normative aspect of such isolation is questionable.
2. For a study of sterilization in a fixed exchange rate regime see Herring and Marston (1977).
3. The main results of the analysis stay intact if we allow for a positive but less than unit wealth effect on assets demand (implying that the desired portfolio share itself is a function of wealth).
4. Thus  $l_1, l_2, f_1, \chi_2 < 0$ ;  $\chi_1, f_2 > 0$  (where for  $g(X_1, X_2)$   
$$g_i = \frac{\partial g}{\partial X_i}$$
)
5. It is assumed that the private sector ignores the composition of the central bank's balance sheet in arriving at portfolio decisions, and that agents do not capitalize the stream of tax liabilities associated with the government debt.
6. For a discussion of the domestic return on foreign bonds under a two-tier regime in a stochastic world see Flood and Marion (1982).
7. For a discussion of such an adjustment process in a fixed rate regime see Frenkel and Rodriguez (1975).
8. The non-neutrality is the result of the assumptions described in comment 5.
9. Let  $\lambda$  be the stable root of the above system ( $\lambda < 0$ ). Under a saddle-path adjustment we get that  $M = a + b \cdot e^{\lambda t}$ ,  $e_f = \bar{e}_f + d \cdot e^{\lambda t}$ . Thus,  
$$\dot{e}_f = \theta(\bar{e}_f - e_f)$$
 where  $\theta = -\lambda$ .

## References

- Branson, W.H., 1974, Stocks and Flows in International Monetary Analysis, in : A. Ando, R. Herring and R. Marston, eds. International aspects of stabilization policies (Federal Reserve Bank of Boston, Boston).
- Dornbusch, R., 1976, The Theory of Flexible Exchange Rate Regimes and Macroeconomic Policy, Scandinavian Journal of Economics, 78, 255-75.
- Flood, R.P. and N.P. Marion, 1982, The Transmission of Disturbances Under Alternative Exchange Rate Regime With Optimal Indexing, Quarterly Journal of Economics 95, 45-62.
- Frenkel, J. and Rodriguez, C., 1975, Portfolio Equilibrium and the Balance of Payments: A Monetary Approach, American Economic Review Vol. 65, December, pp. 674-88.
- Herring, R. and Marston R. 1977, National Monetary Policies and International Financial Markets. New York: Elsevier-North-Holland.
- Kouri, P.J.K. and M.G. Porter, 1974, International Capital Flows and Portfolio Equilibrium, Journal of Political Economy 82, 443-467.
- Marion, N.P., Insulation Properties of a Two-Tier Exchange Market in a Portfolio Balance Model, Economica, Feb. 1981, 48(189), pp. 61-70.

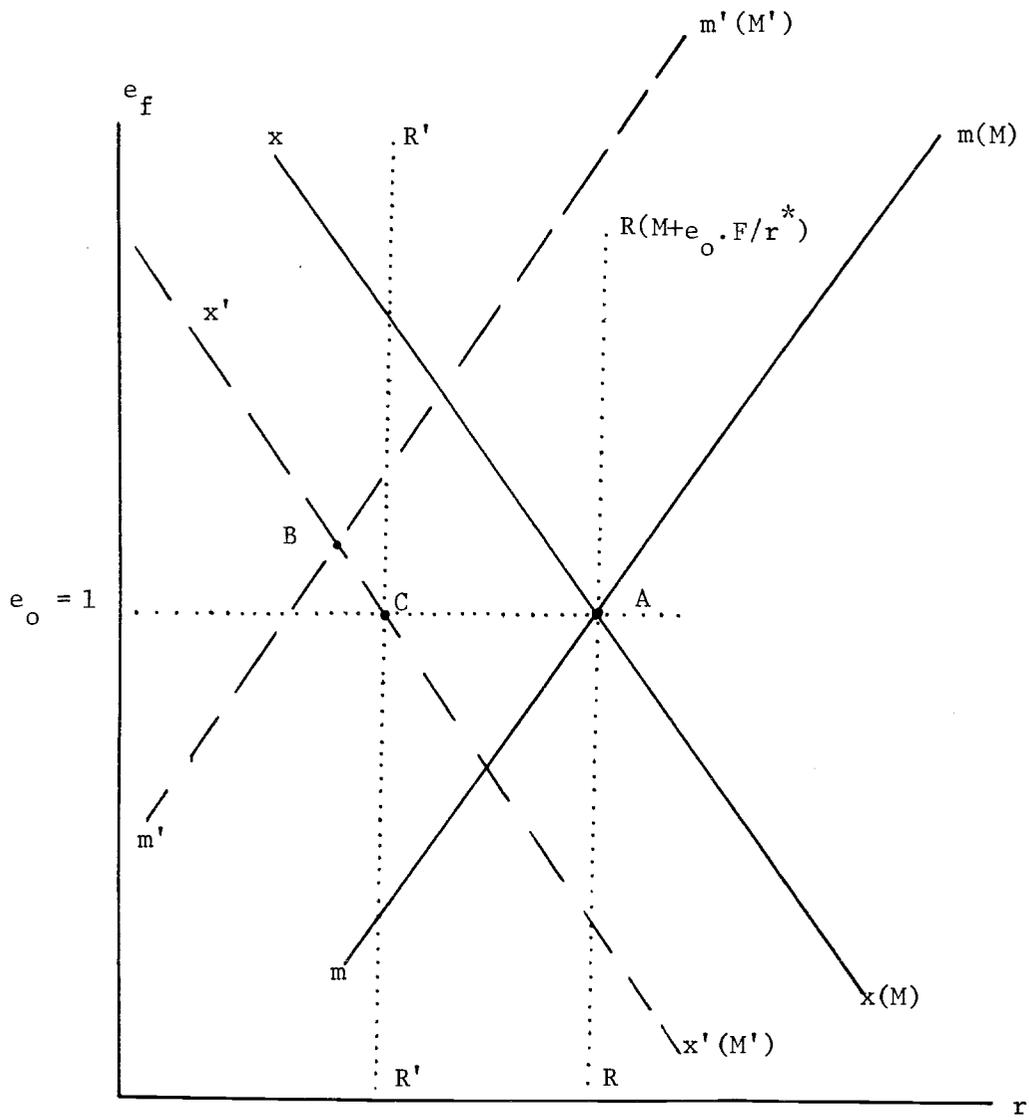


Figure 1

Adjustment to a Monetary Injection

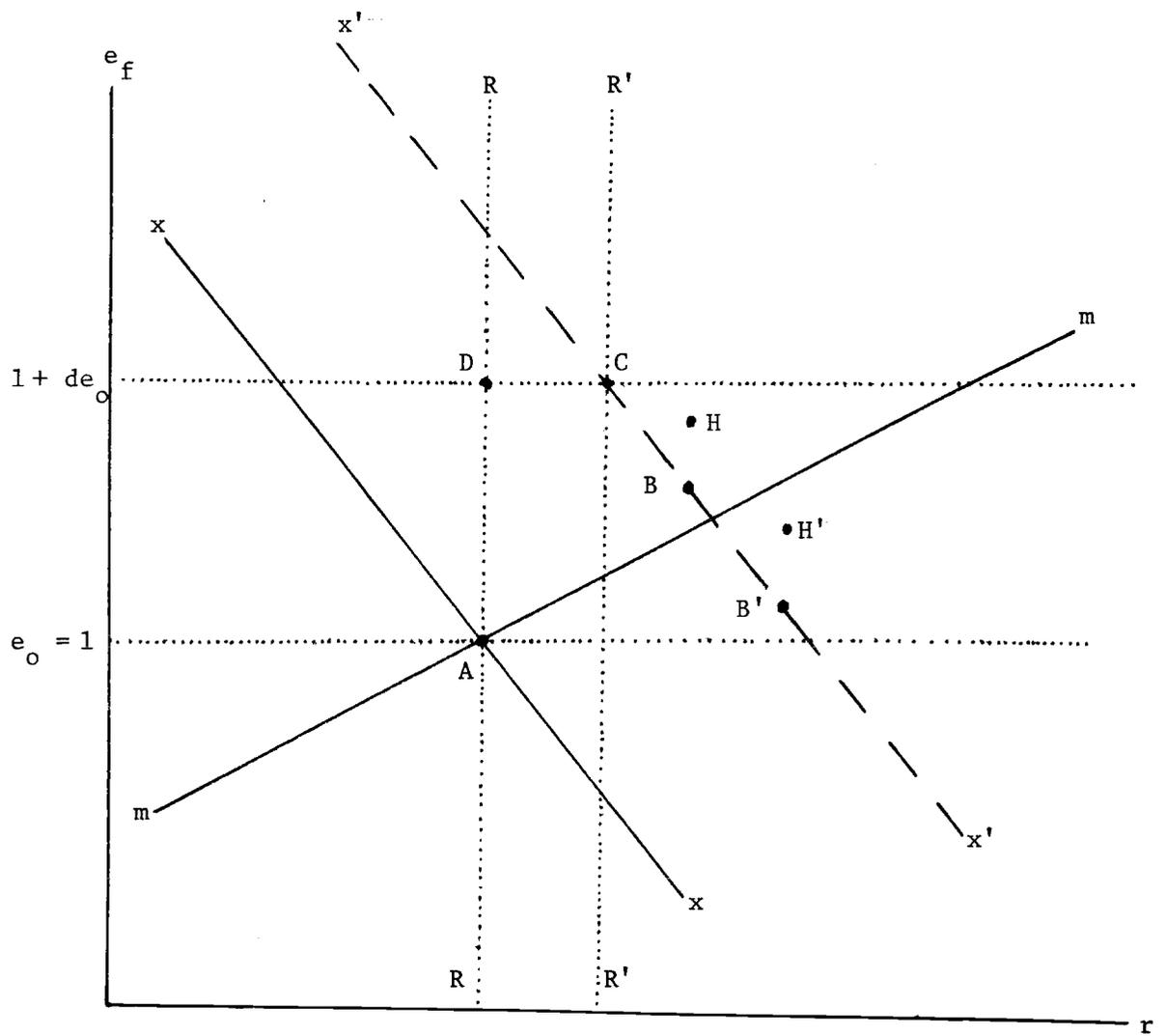


Figure 2

Adjustment to a Devaluation

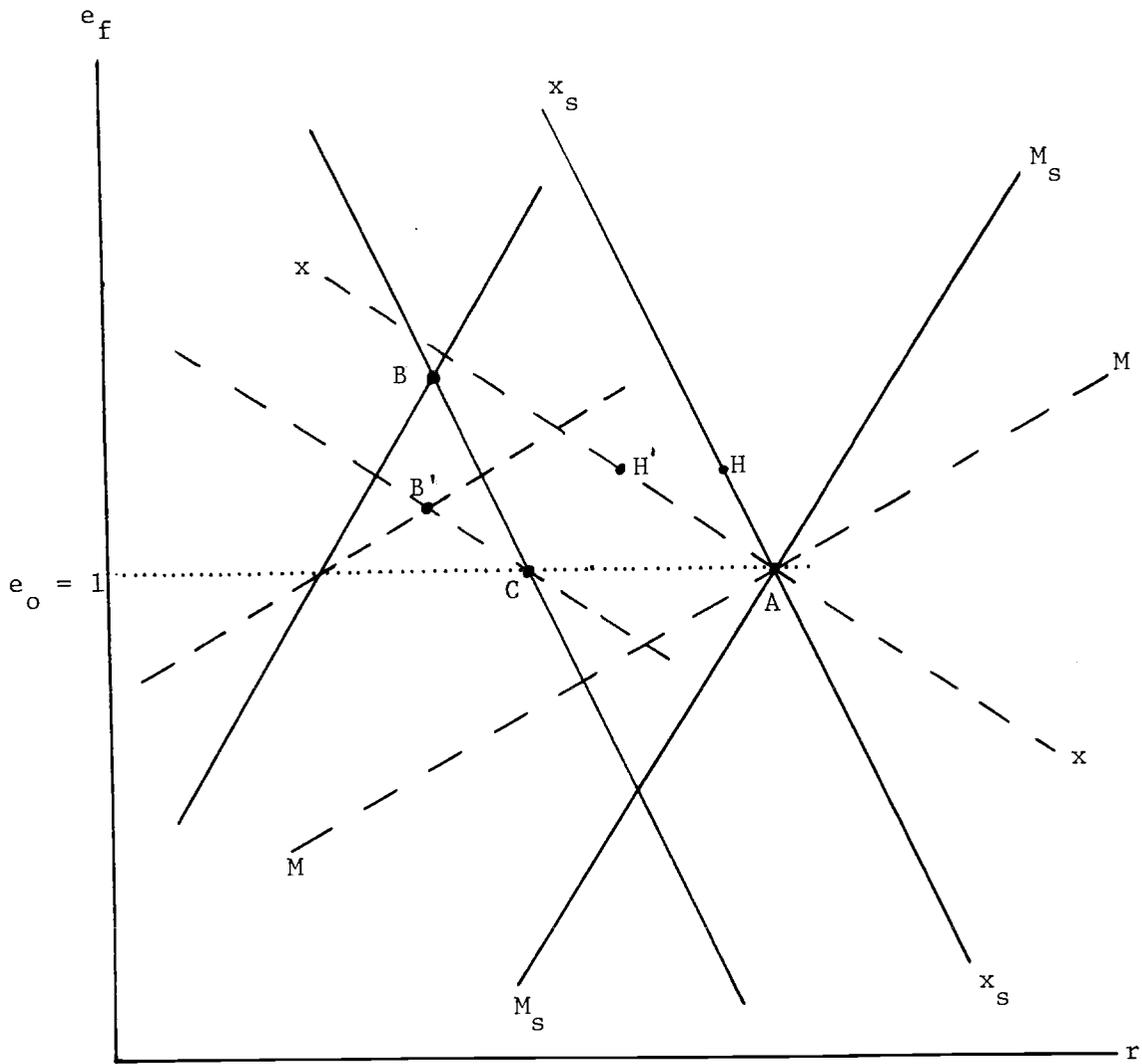


Figure 3

The Role of Expectations