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A MULTICOUNTRY ECONOMETRIC MODEL

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ABSTRACT

A multicountry econometric model is presented in this paper. The theoretical basis of the model is discussed in Fair (1979a), and the present paper is an empirical extension of this work. The model is quarterly and contains estimated equations for 44 countries. Most of the equations have been estimated by two stage least squares. The basic estimation period is 1958I-1980I (89 observations). For equations that are relevant only when exchange rates are flexible, the basic estimation period is 1972II-1980I (32 observations). The trade matrix contains data for 64 countries. The U.S. part of the model is the model described in Fair (1976, 1980b).

The model differs from previous models in a number of ways.

(1) Linkages among countries with respect to exchange rates, interest rates, and prices appear to be more important in the model than they are in previous models. (2) There is no natural distinction in the model between stock-market and flow-market determination of the exchange rate. (3) The number of countries is larger than usual, and the data are all quarterly. (4) I alone have estimated small models for each country and then linked them together, rather than, as Project LINK has done, take models developed by others and link them together. The advantage of this approach is that the person constructing the individual models knows from the beginning that they are to be linked together, and this may lead to better specification of the linkages.

The paper contains (1) a review of the theoretical basis of the model, (2) a description of the econometric model, including presentation and discussion of all the estimated equations, (3) a comparison of the predictive accuracy of the model to that of a fourth order autoregressive model, and (4) a brief discussion of the properties of the model. A much more detailed examination of the properties of the model is presented in Fair (1981).

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A MULTICOUNTRY ECONOMETRIC MODEL*

by

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I. Introduction

A multicountry econometric model is presented in this paper. The theoretical basis of the model is discussed in Fair (1979a), and the present paper is an empirical extension of this work. Quarterly data have been collected or constructed for 64 countries, and the model contains estimated equations for 44 countries. The basic estimation period is 1958I-1980I (89 observations). For equations that are relevant only when exchange rates are flexible, the basic estimation period is 1972II-1980I (32 observations). Most of the equations have been estimated by two stage least squares. The U.S. part of the model is the model described in Fair (1976, 1980b).

The model differs from previous models in a number of ways. First, linkages among countries with respect to exchange rates, interest rates, and prices appear to be more important in the present model than they are in previous models. Previous models have been primarily trade linkage models. The LINK model (Ball 1973), for example, is of this kind, although some recent work has been done on making capital movements endogenous in the model.¹

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Second, the theory upon which the model is based differs somewhat from previous theories. The theoretical model in Fair (1979a) is one in which stock and flow effects are completely integrated. There is no natural distinction in this model between stock-market and flow-market determination of the exchange rate, a distinction that is important in recent discussions of the monetary approach to the balance of payments.² The theoretical model also allows for the possibility of price linkages among countries, something which has generally been missing from previous theoretical work.

Third, the number of countries in the model is larger than usual, and the data are all quarterly. Considerable work has gone into the construction of quarterly data bases for all the countries. Some of the quarterly data had to be interpolated from annual data, and a few data points had to be guessed. The collection and construction of the data bases are discussed in the Appendix.

Finally, there is an important difference between the approach taken in this study and an approach like that of Project LINK. I alone have estimated small models for each country and then linked them together, rather than, as Project LINK has done, take models developed by others and link them together. The advantage of the LINK approach is that larger models for each country can be used. It is clearly not feasible for one person to construct medium- or large-scale models for each country. The

¹See Hickman (1974, p. 203) for a discussion of this. See also Berner *et al.* (1976) for discussion of a five-country econometric model in which capital flows are endogenous.

²See, for example, Frenkel and Johnson (1976), Dornbusch (1976), Frenkel and Rodriguez (1975), and Kouri (1976).

advantage of the present approach, on the other hand, is that the person constructing the individual models knows from the beginning that they are to be linked together, and this may lead to better specification of the linkages. It is unlikely, for example, that the specification of the exchange rate and interest rate linkages in the present model would develop from the LINK approach. Whether this possible gain in the linkage specification outweighs the loss of having to deal with small models of each country is, of course, an open question.

The theoretical basis of the model is reviewed in Section II. Because of data limitations, not all versions of the theoretical model in Fair (1979a) can be estimated, and the primary purpose of Section II is to present the version of the theoretical model that the econometric model most closely approximates. The econometric model is presented and discussed in Section III. The predictive accuracy of the model is then examined in Section IV, and the properties of the model are discussed in Section V. Section VI contains a brief conclusion.

II. The Theoretical Basis of the Model

Data limitations usually make the transition from a theoretical model to an empirical model less than straightforward. This is certainly true in the present case, where much of the international data that one would like to have are of poor quality or do not exist. The transition from the theoretical models in Fair (1974, 1979a) to the present econometric model is discussed in this section. The theoretical models will first be reviewed, and then the modifications needed for the empirical work will be discussed.

The basic theoretical model that has guided my empirical work is

presented in Fair (1974). Individual agents in this model derive their decisions from the solutions of multiperiod maximization problems: households maximize utility and firms maximize profits. The variables that explain the decision variables are the ones that affect these solutions. These problems require that agents form expectations of the future values of a number of variables. Even though the model is deterministic, agents make expectation errors. They do not know the complete structure of the model and must form their expectations on the basis of a limited set of information (usually only the past history of a few variables). These expectation errors lead at times to "disequilibrium" in the labor, goods, and financial markets, and much of the modeling is concerned with the effects of disequilibrium. Another important feature of the modeling is making sure that all flows of funds among the agents are accounted for.

The idea for the two-country model in Fair (1979a) came from considering how one would link the above theoretical model, which is a single-country model, to a model just like it. One way in which the two-country model is distinguished from previous models is in the determination of the exchange rate. The distinction between the stock-market and flow-market determination of the exchange rate, which has played an important role in the literature on the monetary approach to the balance of payments, is not relevant in the model. The exchange rate, like the price level, the wage rate, and the interest rate, is merely one endogenous variable out of many, and in no rigorous sense can it be said to be "the" variable that clears a particular market. Because of the accounting for all flows of funds, the model is one in which stock and flow effects are completely integrated.

There are a number of versions of the two-country model, depending

(1) on whether there are fixed or flexible exchange rates, (2) on whether the bonds of the two countries are perfect substitutes, (3) on the level of aggregation of the sectors in the countries, (4) on whether reaction functions of the monetary authorities with respect to interest rates and the exchange rate are postulated, and (5) on the treatment of the forward rate. Before considering the transition to the empirical model, it will be necessary to outline some of these versions.

Consider first the case in which there are two sectors per country: private (p) and government (g). In what follows capital letters denote variables for country 1; lower case letters denote variables for country 2; and an asterisk (*) on a variable denotes the other country's holdings of the variable. Each country has its own money (M,m) and its own bond (B,b). The bonds are one-period securities. Negative values of B and b denote liabilities. The interest rate on B is R and on b is r. e is the price of country 2's currency in terms of country 1's currency, and F is the (one-period) forward price of country 2's currency. Each country holds a positive amount of the international reserve (Q,q), which is denominated in the currency of country 1.

It is unnecessary for present purposes to consider explicitly the labor and goods markets. Instead, the savings of each sector can be represented by writing one equation per sector:

$$(1) \quad S_p = f_1(R, r, e, \dots),$$

$$(2) \quad S_g = f_2(R, r, e, \dots),$$

$$(3) \quad s_p = f_3(R, r, e, \dots),$$

$$(4) \quad s_g = f_4(R, r, e, \dots).$$

S and s denote savings, the difference between a sector's revenue and its expenditures. In the complete model the savings variables are determined by definitions, where many of the right hand side variables in these definitions are determined in the labor and goods markets. Almost every variable in the model has at least an indirect effect on savings, and so the argument list in the above functions is long. The two interest rates and the exchange rate have been listed explicitly in the functions only for emphasis.

Each sector faces a budget constraint:

$$(5) \quad 0 = S_p - \Delta M_p - \Delta B_p - e\Delta b_p^* ,$$

$$(6) \quad 0 = S_g + \Delta M_g - \Delta B_g - \Delta Q ,$$

$$(7) \quad 0 = s_p - \Delta m_p - \Delta b_p - \frac{1}{e}\Delta B_p^* ,$$

$$(8) \quad 0 = s_g + \Delta m_g - \Delta b_g - \frac{1}{e}\Delta q .$$

For simplicity it is assumed that the countries do not hold each other's money and that the governments do not hold foreign bonds.

Coming out of the solutions of the maximization problems of the private sector are demands for domestic and foreign bonds and domestic money, which can be represented as:

$$(9) \quad B_p = f_9(R, r, e, \dots) ,$$

$$(10) \quad b_p^* = f_{10}(R, r, e, \dots) ,$$

$$(11) \quad M_p = f_{11}(R, r, e, \dots) ,$$

$$(12) \quad b_p = f_{12}(R, r, e, \dots) ,$$

$$(13) \quad B_p^* = f_{13}(R, r, e, \dots) ,$$

$$(14) \quad m_p = f_{14}(R, r, e, \dots) .$$

The equilibrium conditions for the bond and money markets are:

$$(15) \quad 0 = B_p + B_g + B_p^* ,$$

$$(16) \quad M_g = M_p ,$$

$$(17) \quad 0 = b_p + b_g + b_p^* ,$$

$$(18) \quad m_g = m_p .$$

There is finally an equation stating that there is no change in total world reserves:

$$(19) \quad 0 = \Delta Q + \Delta q .$$

One of equations (1), (5), and (9)-(11) is redundant, and one of equations (3), (7), and (12)-(14) is redundant. It will be useful to drop equations (10) and (13). Also, the savings variables satisfy the property that $S_p + S_g + es_p + es_g = 0$, and so one of equations (1)-(8), (15)-(18), and (19) is redundant. It will be useful to drop equation (19). This leaves 16 independent equations. There are 19 variables in the model: $S_p, S_g, s_p, s_g, B_p, b_p^*, M_p, b_p, B_p^*, m_p, M_g, m_g, Q, q, R, r, e, B_g, b_g$.³ In the case of fixed exchange rates e is exogenous and Q is endogenous, and in the case

³There are also, of course, lagged variables in the model because some of the variables enter the equations in change form. All lagged variables are taken to be predetermined.

of flexible exchange rates e is endogenous and Q is exogenous. Given that one of these two variables is taken to be exogenous, the model can be closed by taking B_g and b_g to be the exogenous monetary policy variables.⁴

It should be clear from this representation that e , like R and r , is not determined solely in stock markets or in flow markets. It is simultaneously determined along with the other endogenous variables. When R , r , and e are determined in the above version of the model, they will be said to be "implicitly" determined. An alternative to this version is one in which reaction functions of the monetary authorities are postulated. Reaction functions for R and r can be written:

$$(20) \quad R = f_{20}(\dots),$$

$$(21) \quad r = f_{21}(\dots),$$

where the arguments in the functions are variables that affect the monetary authorities' decisions regarding short term interest rates. In this case monetary policy is explained by equations (20) and (21) and so is endogenous in the model. Adding these equations means that B_g and b_g must be taken to be endogenous. It is also possible to postulate an exchange rate reaction function for one of the monetary authorities, where e is on the left hand side and variables that affect the decision of the

⁴Note that the monetary policy variables are B_g and b_g in this model. The monetary authorities affect the economy by exchanging bonds for money or reserves, subject to the government budget constraints (6) and (8). This in turn affect interest rates and other endogenous variables. There is no banking sector in the version of the model presented here. If a banking sector were added, then two other monetary policy variables would be introduced for each country: the discount rate and the reserve requirement rate. See Fair (1979a) for a discussion of this.

monetary authority regarding e are on the right hand side:

$$(22) \quad e = f_{22}(\dots) .$$

In this case, as in the fixed exchange rate case, Q is endogenous.

The next issue to consider is the case in which the bonds of the two countries are perfect substitutes. The covered interest rate from country 1's perspective on the bond of country 2, say r' , is $(e/F)(1+r) - 1$, where F is the forward rate. If for $R = r'$ people are indifferent as to which bond they hold, then the bonds will be defined to be perfect substitutes. If this is the case, then the above model is modified as follows. First, equations (9) and (12) drop out, since the private sector is now indifferent between the two bonds. Second, arbitrage will insure that $R = r'$, and so a new equation is added:

$$(23) \quad R = (e/F)(1+r) - 1 .$$

Third, the model is underidentified with respect to B_p , B_p^* , b_p , and b_p^* , and so one of these variables must be taken to be exogenous.⁵

A key question to consider in the perfect substitution case is how the forward rate, F , is determined. If F is equal to the expected future spot rate, then one could try to estimate an equation explaining F , where the explanatory variables would be variables that one believes affect expectations. An alternative to this would be to assume that expectations are rational and estimate the model under this constraint.

If F is determined in either of these two ways, it will be said to play

⁵This indeterminacy is analogous to the indeterminacy that arises in, say, a two-consumer, two-firm model in which the two consumers are indifferent between the goods produced by the two firms. It is not possible in this model to determine the allocation of the two goods between the two consumers.

an "active" role in the model. If F is active, then it is obviously not possible to have all three variables-- R , r , and e --implicitly determined or determined by reaction functions. Given equation (23) and the equation (implicit if rational expectations, explicit otherwise) for F , only two of the three variables can be implicitly determined or determined by reaction functions. Also, if exchange rates are fixed, then it is not possible to have both R and r implicitly determined or determined by reaction functions if F is active. An alternative case to F being active is the case in which R , r , and e are implicitly determined or determined by reaction functions and F is determined by equation (23). In this case F will be said to play a "passive" role in the model. Given R , r , and e , F merely adjusts to insure that the arbitrage condition holds.

The version of the model that was used as a basis for the empirical work is the one in which the bonds are perfect substitutes, F is passive, and R , r , and e are determined by reaction functions. Whether this choice, which was partly dictated by data availability, provides an adequate basis for constructing an empirical model is an open question. No direct tests of the assumptions behind this choice are attempted in this paper. The choice is indirectly tested by examining how well the model explains the historical data. The results of this test are presented and discussed in Section IV.

The assumption that is most questionable in this choice is probably the assumption that e is determined by a reaction function. The alternative assumption is that e is implicitly determined, with reserves, Q , exogenous. In practice there is obviously some intervention of the monetary authorities in the exchange markets, and so this alternative

assumption is also questionable. The assumption that e is determined by a reaction function means that intervention is complete: the monetary authority has a target e each period and achieves this target by appropriate changes in Q . This assumption may not be, however, as restrictive as it first sounds. The monetary authority is likely to be aware of the market forces that are operating on e in the absence of intervention (i.e., the forces behind the determination of e when e is implicitly determined), and it may take these into account in setting its target each period. If some of the explanatory variables in the reaction function are in part measures of these forces, then the estimated reaction function may provide a better explanation of e than one would otherwise have thought. Similar arguments apply to the assumption that R and r are determined by reaction functions.

The assumption that F is passive means that the forward market imposes no "discipline" on the monetary authority's choice of the exchange rate. Again, if the monetary authority takes into account market forces operating on e in the absence of intervention, including market forces in the forward market, and if the explanatory variables in the reaction function for e are in part measures of these forces, then the estimated reaction function for e may not be too bad an approximation. Given this assumption and given that F does not appear as an explanatory variable in any of the equations, F plays no role in the empirical model. For each country it is determined by an estimated version of the arbitrage condition, equation (23), but the predictions from these equations have no effect on the predictions of any of the other variables in the model.

The assumption that F is passive is not sensible in the case of fixed exchange rates: for most observations F is equal to or very close

to e when e is fixed. A different choice was thus made for the fixed rate case. This choice was designed to try to account for the possibility that the bonds of the different countries are not perfect substitutes as well as for the fact that F is not passive. The procedure that was followed in the fixed rate case is as follows. The U.S. was assumed to be the "leading" country with respect to the determination of interest rates. Assume in the above model that the U.S. is country 1. Consider the determination of r , country 2's interest rate. If exchange rates are fixed, bonds are perfect substitutes, and F is equal to e , then r is determined by equation (23) and is equal to R . In other words, country 2's interest rate is merely country 1's interest rate: country 1 sets the one world interest rate and country 2's monetary authority has no control over country 2's rate. If the bonds are not perfect substitutes, then equation (23) does not hold and country 2's monetary authority can affect its rate. If, however, the bonds are close to being perfect substitutes, then very large changes in b_g will be needed to change r very much. In the empirical work interest rate reaction functions were estimated for each country, but with the U.S. interest rate added as an explanatory variable to each equation. If the bonds are close to being perfect substitutes, then the U.S. rate should be the only significant variable in these equations and have a coefficient estimate close to 1.0. If the bonds are not at all close substitutes, then the coefficient estimate should be close to zero and the other variables should be significant. The in-between case should correspond to both the U.S. rate and the other variables being significant.

The above discussion about the U.S. rate in the interest rate reaction functions does not pertain to the flexible exchange rate case. One

would thus not expect the interest rate reaction functions to be the same in the fixed and flexible rate cases, and so in the empirical work separate interest rate reaction functions were estimated for each country for the fixed and flexible rate periods. Note that the U.S. rate may still be an explanatory variable in the reaction functions for the flexible rate period. This would be, however, because the U.S. rate is one of the variables that affects the monetary authority's interest rate decision, not because the U.S. rate is being used to try to capture the degree of substitutability of the bonds. It should finally be noted in this regard that the interest rate reaction function for the U.S. was estimated over the entire sample period. This procedure is consistent with the above assumption that the U.S. is the interest rate leader in the fixed rate period. If it is the leader, then it is not constrained as the other countries are, and so there is no reason on this account to expect the function to be different in the fixed and flexible rate periods.

The next issue to consider in the transition to the empirical model is the level of aggregation of the sectors. In the empirical model the private and government sectors are aggregated together, and so there is only one sector per country. In this case the budget constraint for country 1 is the sum of equations (5) and (6):

$$(24) \quad 0 = S - \Delta B - e\Delta b^* - \Delta Q .$$

S is equal to $S_p + S_g$, ΔB is equal to $\Delta B_p + \Delta B_g$, and the p subscript has been dropped from b^* since it is now unnecessary. The budget constraint for country 2 is similarly the sum of equations (7) and (8):

$$(25) \quad 0 = s - \Delta b - \frac{1}{e}\Delta B^* - \frac{1}{e}\Delta q .$$

Note that because of the assumption that a country holds no foreign money, the money supply variables drop out of the sums. Equations (15) and (17) are now written as:

$$(26) \quad 0 = B + B^* ,$$

$$(27) \quad 0 = b + b^* .$$

Consider now a further type of aggregation. Let $\Delta A = \Delta B + e\Delta b^* + \Delta Q$ and $\Delta a = \Delta b + \frac{1}{e}\Delta B^* + \frac{1}{e}\Delta q$. In this notation equations (24) and (25) are:

$$(28) \quad 0 = S - \Delta A ,$$

$$(29) \quad 0 = s - \Delta a .$$

If one adds the first difference of (26), the first difference of (27) multiplied by e , and (19), the result is:

$$(30) \quad 0 = \Delta A + e\Delta a .$$

Equation (30) is redundant, given (28) and (29), because S and s satisfy the property that $S + es = 0$. This aggregation is very convenient because it allows data on A and a to be constructed by summing past values of S and s from some given base period values. Data on S (the balance of payments on current account) are available for most countries, whereas data on B , B^* , b , and b^* (i.e., bilateral financial data) are generally not available. There is, of course, a cost to this type of aggregation, which is that capital gains and losses on bonds from exchange rate changes are not accounted for. Given the current data, there is little that can be done about this. Note that this aggregation is made possible in the model by the assumption that the bonds are perfect sub-

stitutes. If the bonds are not perfect substitutes, then equations (9) and (12) do not drop out, and bilateral financial data would be needed to estimate them.

It will be convenient to rewrite the above model in the form that was used as a basis for the empirical work:

- (i) $S = f_i(R, r, e, \dots)$, [saving of country 1]
- (ii) $s = f_{ii}(R, r, e, \dots)$, [saving of country 2]
- (iii) $0 = S - \Delta A$, [budget constraint of country 1]
- (iv) $0 = s - \Delta a$, [budget constraint of country 2]
- (v) $R = f_v(\dots)$, [interest rate reaction function of country 1]
- (vi) $r = f_{vi}(\dots)$, [interest rate reaction function of country 2]
- (vii) $e = f_{vii}(\dots)$, [exchange rate reaction function]
- (viii) $R = (e/F)(1+r) - 1$. [arbitrage condition]

It should finally be noted that although nothing has been said about the determination of S and s in this section, this determination is an important part of the empirical model. It will be discussed in the next section. The purpose of this section was to try to make clear the assumptions behind the use of the reaction functions and the aggregation.

III. The Econometric Model

The econometric model for all countries except the U.S. is presented in Tables 1 through 4. The variables for a particular country i are presented in alphabetic order in Table 1; the equations for country i are listed in Table 2; the trade and price linkages among the countries are presented in Table 3; and the coefficient estimates for all the countries are presented in Table 4. The purpose of this section is to explain these tables. To conserve space, it is assumed in the following discussion that the tables have been read carefully. Parts of the tables that are self explanatory are not discussed, and the discussion is not self contained without the tables.

The econometric model for the U.S. is the one discussed in Fair (1976, 1980b). It is much larger than the model for an individual country in Table 2, and it captures many more features of the economy. The two key exogenous foreign sector variables in this model are the import price deflator and the real value of exports, and when the U.S. model is embedded in the overall model, these two variables become endogenous. Since the U.S. model is described in detail elsewhere, it will not be discussed in this section. All references to the econometric work in this section pertain only to the non U.S. part of the model.

The Data

The raw data were taken from two of the four tapes that are constructed every month by the International Monetary Fund: the International Financial Statistics (IFS) tape and the Direction of Trade (DOT) tape. The way in which each variable was constructed is explained in brackets in Table 1. Some variables were taken directly from the tapes, and some were constructed from other variables. When "IFS" precedes a number in the

Notes: lc = local currency; all prices are in lc; e and F are units of lc per \$; an * denotes that the variable is in units of lc. † denotes exogenous variable. †† denotes that the variable was used only in the construction of the data.

Eq. No.	Variable	
18	A_{it}^*	= net stock of foreign security and reserve holdings, end of quarter, in lc. [$= A_{it-1}^* + BOP_{it}^*$. Base value of zero was used for the quarter prior to the beginning of the data.]
17	BOP_{it}^*	= total net goods, services, and transfers in lc. Balance of Payments on current account. [See Table A-3.]
2	C_{it}	= personal consumption in 75lc. [IFS96F/CPI _{it} .]
	††CPI _{it}	= consumer price index, 1975 = 1.0. [$= (IFS64 \text{ or } IFS64X)/100$.]
	†e ₁₇₅	= average exchange rate in 1975, lc per \$. [= IFSRF for 1975.]
9b	e _{it}	= exchange rate, average for the quarter, lc per \$. [= IFSRF.]
20	ee _{it}	= exchange rate, end of quarter, lc per \$. [= IFSAE.]
	††EMPL _{it}	= industrial or manufacturing employment index, 1975 = 100. [IFS67 or IFS67EY.]
15	EX _{it}	= total exports (NIA) in 75 lc. [$= (IFS90C \text{ or } IFS90N)/PX_{it}$.]
	†EXDIS _{it}	= discrepancy between NIA export data and other export data, in 75 lc. [$= EX_{it} - e_{175} \times 75\$_{it} - XS_{it}$.]
10b	F _{it}	= three-month forward rate, lc per \$. [= IFSB.]
	†G _{it}	= government purchases of goods and services in 75 lc. [$= (IFS91F \text{ or } IFS91FF)/PY_{it}$.]
3	I _{it}	= gross fixed investment in 75 lc. [= IFS93E/PY _{it} .]
14	IM _{it}	= total imports (NIA) in 75 lc. [= IFS98C/PM _{it} .]
	†IMDIS _{it}	= discrepancy between NIA import data and other import data, in 75 lc. [$= IM_{it} - M_{it} - MS_{it}$.]
	††IP _{it}	= industrial production index, 1975 = 100. [= IFS66.]
1	M _{it}	= merchandise imports (fob) in 75 lc. [= IFS71V/PM _{it} .]
	†MS _{it}	= other goods, services, and income (debit) in 75 lc. BOP data. [$= (IFS77ADD \cdot e_{it})/PM_{it}$.]
	††MS _{it}	= merchandise imports (fob) in \$. [= IFS71V/e _{it} .] [Also equals $(PM_{it} M_{it})/e_{it}$.]
19	M75\$A _{it}	= merchandise imports (fob) in 75\$ from Type A countries. [$= \sum_j XX75\$_{jit}$.]
	†M75\$B _{it}	= merchandise imports (fob) in 75\$ from Type B countries. [$= M_{it}/e_{175} - M75\$A_{it}$.]
6	MI _{it}^*}	= money supply in lc. [= IFS34.]
V	PM _{it}	= import price index, 1975 = 1.0. [IFS75/100.]
IV	PM' _{it}	= import price index from DOT data. [$= (e_{it} \sum_j (PX\$_{jt} \cdot XX75\$_{jit})) / (e_{175} \sum_j XX75\$_{jit})$.]
	†POP _{it}	= population in millions. [= IFS99Z.]
	†PWS _{it}	= world price index, \$/75\$. [$= \{ \sum_{j \neq 1}^* (PX\$_{jt} \cdot X\$_{jt}) \} / \sum_{j \neq 1}^* X\$_{jt}$, where \sum^* denotes summation that excludes Type B countries and countries 26-35.]
11	PX _{it}	= export price index, 1975 = 1.0. [= IFS74/100.]
III	PX\$ _{it}	= export price index, \$/75\$. [$= (e_{175} PX_{it})/e_{it}$.]
5	PY _{it}	= GNP or GDP deflator, 1975 = 1.0. [= (IFS94A or IFS99B)/Y _{it} .]

TABLE 1 (continued)

Eq. No.	<u>Variable</u>	
7a,7b	r_{it}	= three-month interest rate, percentage points. [= IFS60, IFS60B, or IFS60C .]
8	R_{it}	= long-term interest rate, percentage points. [= IFS61 or IFS61A .]
16	S_{it}	= final sales in 75 lc. [= $Y_{it} - \Delta V_{it}$.]
	$^{\dagger}SDIS_{it}$	= discrepancy in real NIA data (in 75 lc) due to use of different deflators. [= $S_{it} - C_{it} - I_{it} - G_{it} - EX_{it} + IM_{it}$.]
	$^{\dagger}TT_{it}^*$	= total net transfers in lc. [See Table A-3.]
12	ΔV_{it}	= inventory investment in 75 lc. [= IFS93I/PY _{it} .]
13	V_{it}	= stock of inventories, end of quarter, in 75 lc. [= $V_{it-1} + \Delta V_{it}$. Base value of zero was used for the quarter prior to the beginning of the data.]
	$^{\dagger}XS_{it}$	= other goods, services, and income (credit) in 75 lc. BOP data. [= (IFS77ACD $\cdot e_{it}$)/PX _{it} .]
	$^{\dagger\dagger}X\$_{it}$	= merchandise exports (fob) in \$. [= IFS70/ e_{it} .]
	$^{\dagger\dagger}XX\$_{ijt}$	= merchandise exports (fob) from i to j in \$. [DOT tape.] [$XX\$_{165t} = X\$_{it}$ - $\sum_{j \neq 65} XX\$_{ijt}$ and $XX\$_{65it} = M\$_{it} - \sum_{j \neq 65} XX\$_{jit}$.] [$XX\$_{ijt} = 0$ if $i = j$.]
I	$XX75\$_{ijt}$	= merchandise exports (fob) from i to j in 75\$. [= ($e_{it} XX\$_{ijt}$)/($e_{175} PX_{it}$) if i is a Type A country; = 0 if i is a Type B country.]
II	$X75\$_{it}$	= merchandise exports (fob) in 75\$. [= $\sum_j XX75\$_{ijt}$.] [Also equals $X\$_{it}/PX_{it}$.] [Equals 0 and is not used if i is a Type B country.]
4	Y_{it}	= real GNP or GDP in 75 lc. [= IFS99AP, IFS99FP, IFS99AR, or IFS99BR .]
	$^{\dagger}a_{jit}$	= share of i's total merchandise imports from Type A countries imported from j in 75\$. [= $XX75\$_{jit}/M75\A_{it} .]
	$^{\dagger}\psi_{1it}$	= (($ee_{it} + ee_{it-1}$)/2)/ e_{it} .
	$^{\dagger}\psi_{2it}$	= PM_{it}/PM'_{it} .

- Notes: 1. For countries with no PM data, PM_{it} was taken to be PM'_{it} (so that $\psi_{2it} = 1$) and M_{it} was taken to be $[e_{it} \sum_j (PX_{jt} XX75\$_{jit})]/PM_{it}$. For these countries it is not the case that $M\$_{it} = (PM_{it} M_{it})/e_{it}$ because the summation $\sum_j (PX_{jt} XX75\$_{jit})$ is only over Type A countries. $M\$_{it}$ pertains to all countries.
2. For the oil exporting countries (countries 26-35), CPI was used in place of PY to deflate IFS91F or IFS91FF (for G_{it}), IFS93E (for I_{it}), and IFS93I (for ΔV_{it}).

Variables Explained by Stochastic Equations

1. $M_{it} = f_1(r_{it} \text{ or } R_{it}, PY_{it}, PM_{it}, Y_{it}, A_{it-1}^*/PY_{it-1}, M_{it-1})$ [merchandise imports in 75 lc]
2. $C_{it} = f_2(r_{it} \text{ or } R_{it}, Y_{it}, A_{it-1}^*/PY_{it-1}, C_{it-1})$ [private consumption in 75 lc]
3. $\Delta I_{it} = f_3(\Delta Y_{it}, \Delta Y_{it-1}, \Delta Y_{it-2}, \Delta Y_{it-3}, I_{it-1}, t)$ [change in gross fixed investment in 75 lc]
4. $Y_{it} = f_4(S_{it}, V_{it-1}, Y_{it-1})$ [GNP in 75 lc]
5. $PY_{it} = f_5(PM_{it}, r_{it} \text{ or } R_{it}, \hat{Y}_{it}, PY_{it-1}, t)$ [CNP deflator]
6. $M1_{it}^* = f_6(r_{it}, PY_{it}, Y_{it}, M1_{it-1}^*, t)$ [money supply in lc]
- 7a. $r_{it} = f_{7a}(PY_{it-1}, M1_{it-1}^*, \hat{Y}_{it}, A_{it}^*/PY_{it}, A_{it-1}^*/PY_{it-1}, PM_{it-1}, r_{it-1}, t, r_{1t}, r_{8t})$ [three-month interest rate]
- 7b. $r_{it} = f_{7b}(\text{same as 7a plus } e_{it})$ [three-month interest rate]
8. $R_{it} = f_8(r_{it}, r_{it-1}, r_{it-2}, (PY_{it} + PY_{it-1} + PY_{it-2})/3, R_{it-1}, t)$ [long-term interest rate]
- 9b. $e_{it} = f_{9b}(PY_{it}, r_{it}, \hat{Y}_{it}, \Delta(A_{it-1}^*/PY_{it-1}), e_{8t}, e_{it-1})$ [exchange rate, average for the quarter]
- 10b. $F_{it} = f_{10b}(ee_{it}, r_{it}/r_{1t})$ [three-month forward rate]
11. $PX_{it} = f_{11}(PY_{it}, PWS_{it}, e_{it})$ [export price index]

Variables Explained by Definitions

12. $\Delta V_{it} = Y_{it} - S_{it}$ [inventory investment in 75 lc]
13. $V_{it} = V_{it-1} + \Delta V_{it}$ [stock of inventories in 75 lc]
14. $IM_{it} = M_{it} + MS_{it} + IMDIS_{it}$ [total imports (NIA) in 75 lc]
15. $EX_{it} = e_{175} \cdot X75_{it} + XS_{it} + EXDIS_{it}$ [total exports (NIA) in 75 lc]
16. $S_{it} = C_{it} + I_{it} + G_{it} + EX_{it} - IM_{it} + SDIS_{it}$ [final sales in 75 l.]
17. $BOP_{it}^* = PX_{it}(e_{175} \cdot X75_{it} + XS_{it}) - PM_{it}(M_{it} + MS_{it}) + TT_{it}^*$ [balance of payments on current account in lc]
18. $A_{it}^* = A_{it-1}^* + BOP_{it}^*$ [net stock of foreign security and reserve holdings in lc]
19. $M75\$A_{it} = M_{it}/e_{it} - M75\B_{it} [merchandise imports in 75\$ from Type A countries]
20. $ee_{it} = 2\psi_{1it} e_{it} - ee_{it-1}$ [exchange rate, end of quarter]

Variables Explained When the Countries are Linked Together (Table 3)

21. $X75_{it}$ [merchandise exports in 75\$]
22. PM_{it} [import price index]

Exogenous Variables

1. e_{175} [average exchange rate for 1975]
2. $EXDIS_{it}$ [discrepancy for export data]
3. G_{it} [government purchases of goods and services in 75 lc]
4. $IMDIS_{it}$ [discrepancy for import data]
5. MS_{it} [non merchandise imports in 75 lc]
6. $M75\$B_{it}$ [merchandise imports from Type B countries in 75\$]
7. POP_{it} [population]
8. PX_{it} for oil exporting countries [export price index]
9. PWS_{it} [world price index]
10. $SDIS_{it}$ [discrepancy for real NIA data]
11. TT_{it}^* [net transfers in lc]
12. XS_{it} [nonmerchandise exports in 75 lc]
13. ψ_{1it} [ratio of $(ee_{it} + ee_{it-1})/2$ to e_{it}]
14. ψ_{2it} [ratio of PM_{it} to PM'_{it}]

- Notes:
1. A \cdot over a variable denotes percentage change.
 2. \hat{Y}_{it} is a function of Y_{it} and is interpreted as a demand pressure variable. It is discussed in the text.
 3. The arguments in the functions are for illustrative purposes only. The exact explanatory variables and functional forms are presented in Table 4.

TABLE 3. Equations That Pertain to the Trade and Price Linkages among Countries

Equations

I	$XX75\$_{jit} = \alpha_{jit} M75\A_{it}	[merchandise exports from j to i in 75\$.] [= 0 if j is a Type B country.]
II	$X75\$_{it} = \sum_j XX75\$_{ijt}$	[merchandise exports of i in 75\$.] [= 0 if i is a Type B country.]
III	$PX\$_{it} = (e_{i75} PX_{it}) / e_{it}$	[export price index of i, \$/75\$.] [= 0 if i is a Type B country.]
IV	$PM'_{it} = \frac{e_{it} \sum_j (PX\$_{jt} XX75\$_{jit})}{e_{i75} \sum_j XX75\$_{jit}}$	[import price index of i from DOT data.]
V	$PM_{it} = \psi_{2it} PM'_{it}$	[import price index of i.]

Notes: α_{jit} = share of i's total merchandise imports from Type A countries imported from j in 75\$.

α_{jit} is exogenous.

TABLE 4. Estimated Equations

A * means that the variable is lagged one quarter. t-statistics in absolute value are in parentheses.

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Equation 1: $\log \frac{M_{it}}{POP_{it}}$ is the dependent variable.

Country	Explanatory Variables										
	$\log PY_{it}$	$\log PM_{it}$	r_{it}	R_{it}	$\log \frac{Y_{it}}{POP_{it}}$	$\frac{A^*_{it-1}}{PY_{it-1} POP_{it-1}}$	$\log \frac{M_{it-1}}{POP_{it-1}}$	R^2	SE	DW	Sample Period
Canada	.086* (0.56)	-.092* (0.78)			.82 (5.45)	.000062 (2.03)	.57 (7.29)	.992	.0374	1.96	581-801
Japan	.12 (1.01)	-.11 (1.78)	-.0034* (1.05)		.15 (1.14)	.00020 (0.78)	.83 (10.29)	.995	.0448	1.98	581-801
Austria	.23 (0.78)	-.19 (0.94)	-.017* (2.09)		1.22 (3.25)	37.4 (1.23)	.36 (2.78)	.990	.0352	2.01	651-793
Belgium	.33 (3.36)	-.37 (4.40)		-.012* (1.50)	1.05 (5.97)		.48 (6.00)	.996	.0323	2.26	581-784
Denmark	.57* (4.04)	-.37* (3.87)	-.0021* (0.87)		.53 (2.55)	.031 (3.12)	.55 (6.58)	.987	.0430	2.38	581-794
France	.23 (1.42)	-.17 (1.54)	-.0012* (0.28)		.54 (2.75)		.70 (6.85)	.993	.0463	1.84	581-784
Germany			-.0050* (3.16)		.94 (4.12)		.58 (5.60)	.995	.0297	1.87	611-801
Italy	.24 (1.71)	-.051 (0.52)		-.016* (1.32)	.88 (2.75)	.00035 (1.38)	.40 (4.08)	.971	.0658	2.20	611-794
Netherlands	.11 (1.11)	-.14 (2.18)			1.10 (4.50)		.39 (3.67)	.992	.0314	2.07	611-794
Norway				-.012 (0.55)	.85 (4.53)	.0042 (2.46)	.57 (6.49)	.966	.0603	2.28	621-794
Sweden			-.0054* (1.21)		1.00 (5.87)	.00077 (0.51)	.50 (5.41)	.980	.0383	2.47	611-794
Switzerland	.074 (1.26)	-.191 (1.86)	-.021* (2.56)	-.0042 (0.37)	1.68 (6.58)	.018 (3.35)	.33 (3.47)	.994	.0289	2.42	581-794
U.K.					1.20 (6.36)	.00011 (0.97)	.36 (3.65)	.982	.0365	2.07	581-801
Finland	.10 (0.37)	-.17 (1.06)			1.33 (5.38)	.000028 (0.93)	.26 (2.65)	.970	.0694	2.27	581-794
Greece	.35 (1.44)	-.16 (0.85)	-.0090* (1.29)		.92 (5.74)		.20 (1.84)	.967	.0960	2.26	581-794
Ireland	.073 (0.60)	-.033 (0.35)		-.0097 (2.16)	1.27 (6.09)	.00026 (1.52)	.47 (5.99)	.987	.0492	2.16	581-794
Portugal				-.0047 (0.54)	1.15 (6.04)		.20 (1.61)	.909	.1542	2.17	581-784
Spain	.16 (1.75)	-.13 (1.49)	-.030 (1.45)		.59 (3.04)		.63 (7.53)	.980	.0568	2.25	621-784
Yugoslavia					.69 (4.44)	.063 (2.41)	.56 (5.56)	.953	.0837	2.07	611-774
Australia				-.041* (4.02)	.79 (4.66)	.00015 (2.60)	.75 (10.40)	.862	.0614	1.93	603-801
New Zealand					.91 (5.87)	.00022 (4.01)	.44 (5.06)	.838	.0803	2.00	582-781
South Africa			-.030* (4.10)		.36 (2.59)		.84 (17.73)	.892	.0660	2.27	621-794
Iran					.51 (2.34)	.0077 (2.75)	.56 (4.34)	.972	.0805	1.48	711-781
Libya					.15 (1.02)		.81 (9.68)	.923	.0755	2.29	721-774
Nigeria						.0023 (4.88)	.77 (13.59)	.977	.0788	1.68	712-781
Saudi Arabia					.026 (2.80)		.69 (6.35)	.992	.0628	2.09	721-782
Venezuela					1.74 (2.99)	.000029 (2.13)	.45 (3.09)	.928	.0721	2.09	711-784
Argentina					.17 (3.41)		.45 (2.96)	.589	.1114	1.89	711-754
Brazil					.60 (1.60)	.19 (1.43)	.83 (7.63)	.828	.0922	1.61	711-784
Chile	.72 (6.64)	-.69 (6.87)			1.04 (1.64)	.00091 (2.38)	.21 (2.35)	.894	.1561	2.33	641-774
Colombia			-.056* (3.14)		.00018 (3.99)		.76 (7.34)	.730	.0781	2.09	711-784
Mexico					1.13 (4.73)	.13 (3.17)	.74 (10.37)	.945	.0411	1.89	711-794
Peru					.049 (0.07)		.95 (8.71)	.781	.1226	1.91	711-784
Egypt					.20 (0.44)		.94 (8.71)	.958	.0916	2.00	721-774
Israel					.55 (1.72)	.000070 (0.50)	.32 (2.05)	.328	.1297	2.30	691-794
Jordan					.88 (3.33)		.59 (4.60)	.838	.1509	2.22	731-784
Syria	.51 (1.72)	-.19 (0.88)			.79 (2.10)	.00011 (0.81)	.25 (1.94)	.818	.1366	2.11	641-784
India					.91 (0.72)		.25 (1.29)	.445	.1213	1.92	722-781
Korea	.16* (0.83)	-.13* (1.33)			.54 (1.87)	.0034 (2.19)	.77 (10.36)	.979	.1079	2.06	641-784
Malaysia	.67* (2.36)	-.42* (2.32)			.51 (2.41)	.00023 (1.25)	.21 (2.63)	.895	.0432	1.05	711-793
Pakistan					.97 (1.14)		.52 (2.33)	.602	.1163	2.66	731-792
Philippines	.93 (5.05)	-.52 (5.67)	-.015 (2.60)		.30 (1.02)	.00039 (4.21)	.28 (3.21)	.688	.0863	2.22	581-794
Thailand	.54 (2.04)	-.38 (2.55)			.40 (1.84)	.0093 (0.20)	.52 (5.59)	.843	.0502	2.11	654-794

Equation 2: $\log \frac{C_{it}}{POP_{it}}$ is the dependent variable.

Country	Explanatory Variables					t	$\hat{\rho}_1$	R ²	SE	DW	Sample Period
	r _{it}	R _{it}	$\log \frac{Y_{it}}{POP_{it}}$	$\frac{A^*_{it-1}}{PY_{it-1} POP_{it-1}}$	$\log \frac{C_{it-1}}{POP_{it-1}}$						
Canada	-.0011 (1.55)		.11 (3.39)	.0000092 (1.53)	.90 (24.18)			.998	.00867	2.43	581-801
Japan	-.0022 (3.06)		.18 (2.68)		.78 (10.00)			.999	.0133	2.36	581-801
Austria	-.0062 (1.75)		.54 (6.13)		.41 (4.36)			.990	.0184	1.87	651-793
Belgium	-.00094 (0.80)	-.0052* (1.73)	.50 (8.02)	.00123 (3.48)	.41 (5.30)			.997	.0123	1.74	581-784
Denmark			.58 (11.20)		.28 (4.43)			.984	.0222	1.18	581-794
France		-.0013* (1.03)	.25 (6.92)		.76 (18.72)			.999	.0091	2.00	581-784
Germany	-.0016 (2.77)		.32 (4.41)	3.79 (0.80)	.71 (11.12)			.998	.00805	2.33	611-801
Italy	-.0012 (1.30)		.23 (2.49)		.71 (9.66)	.0014 (2.19)		.995	.0181	2.11	611-794
Netherlands		-.0048 (1.81)	.44 (4.51)	.010 (2.50)	.63 (8.12)			.996	.0128	2.32	611-794
Norway		-.0060 (0.97)	.45 (6.42)	.000063 (0.17)	.47 (5.98)			.988	.0161	1.77	621-794
Sweden			.29 (4.24)		.64 (8.07)			.979	.0163	2.07	611-794
Switzerland	-.0036 (1.60)		.27 (4.31)	.0021 (1.10)	.79 (15.44)			.996	.0121	2.12	581-794
U.K.	-.00086* (1.00)		.51 (8.63)	.00019 (3.94)	.40 (5.49)			.990	.0123	1.72	581-801
Finland			.36 (5.17)	.0000026 (0.64)	.68 (10.14)			.993	.0238	2.19	581-794
Ireland		-.0043 (5.22)	.58 (11.65)	.000023 (0.58)	.41 (7.54)			.994	.0143	1.55	581-794
Portugal		-.0013 (0.85)	.28 (6.60)		.51 (7.25)			.993	.0104	2.05	581-784
Spain	-.0066 (1.18)		.31 (3.70)		.71 (10.04)			.987	.0230	2.06	621-784
Yugoslavia			.49 (6.48)		.47 (5.69)			.991	.0236	1.52	611-774
Australia	-.0023 (1.47)		.31 (2.64)	.000020 (1.75)	.73 (6.46)			.996	.0107	1.80	603-801
New Zealand			.34 (1.26)	.000057 (1.86)	.71 (2.99)		.69 (2.56)	.984	.0165	1.70	582-781
South Africa	-.0051 (3.28)		.42 (4.41)		.71 (10.32)			.986	.0150	2.14	621-794
Iran			.12 (0.81)	.00047 (0.49)	.83 (3.68)		.52 (1.54)	.991	.0245	1.67	514-781
Libya				.000041 (1.29)	.93 (18.20)			.990	.0351	1.36	651-774
Nigeria			.042 (0.10)	.0014 (1.96)			.62 (1.59)	.679	.0708	1.66	712-781
Saudi Arabia				.013 (1.23)	.70 (2.59)		.71 (2.65)	.970	.0472	1.84	721-782
Venezuela			.24 (1.27)	.0000024 (0.45)	.88 (8.61)		.58 (3.24)	.993	.0152	1.94	621-784
Argentina			.59 (8.79)	.016 (2.97)	.37 (4.48)			.969	.0173	1.31	671-754
Brazil			.14 (3.53)		.87 (24.16)			.997	.0176	1.12	641-784
Chile			.03 (0.20)	.00034 (2.30)	.92 (24.00)			.970	.0640	2.31	641-774
Colombia			.067 (0.86)		.85 (10.62)			.890	.0201	1.40	711-784
Mexico			.43 (7.91)		.45 (6.62)			.972	.0251	1.65	581-794
Peru	-.00071 (0.27)		.54 (3.05)	.0012 (0.42)	.63 (4.87)			.970	.0190	1.94	641-782
Egypt			.12 (1.54)	.00058 (0.81)	.90 (10.46)			.903	.0244	1.40	611-774
Israel			.23 (1.97)		.72 (8.05)			.929	.0290	1.80	691-794
Jordan			.54 (7.01)		.26 (2.31)			.904	.0395	1.22	731-784
Syria			.40 (0.64)		.49 (0.65)		.62 (0.91)	.880	.0593	1.75	641-784
India		-.094 (3.02)	.57 (3.10)	.27 (0.74)	.48 (3.17)			.808	.0287	2.07	722-781
Korea	-.0026 (1.74)		.46 (7.83)		.31 (3.59)			.957	.0558	1.88	641-784
Malaysia			.29 (3.86)		.66 (6.70)			.957	.0212	1.60	711-793
Philippines	-.0024 (1.69)		.66 (13.75)	.000067 (3.48)	.24 (4.33)			.963	.0250	1.06	581-794
Thailand	-.0022 (1.54)		.30 (1.70)		.65 (2.96)		.43 (1.64)	.995	.0108	1.53	654-794

TABLE 4 (continued)

Equation 3: ΔI_{it} is the dependent variable

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Explanatory Variables

Country	ΔY_{it}	ΔY_{it-1}	ΔY_{it-2}	ΔY_{it-3}	I_{it-1}	t	$\hat{\rho}_1$	R ²	SE	DW	Sample Period
Canada	.17 (2.31)	.08 (1.60)	-.09 (1.95)	.07 (0.88)	-.056 (1.83)	5.4 (1.96)		.305	137.5	1.74	581-801
Japan		.21 (3.17)	.17 (2.60)	.17 (2.53)	-.062 (2.34)	7.9 (1.89)		.315	211.5	2.16	581-801
Austria	.54 (5.51)	-.32 (3.76)	-.02 (0.20)	.38 (4.13)	-.15 (2.10)	.049 (1.60)		.981	1.55	2.11	651-793
Belgium	.15 (4.13)	.04 (1.70)	.06 (2.54)	.10 (2.66)	-.15 (2.61)	.16 (2.42)		.506	1.77	1.75	581-784
Denmark	.24 (10.63)	.05 (2.45)	.08 (3.71)	.04 (2.28)	-.064 (1.83)	.0056 (1.34)		.876	.272	2.35	581-794
France	.29 (5.49)	.05 (1.29)	.02 (0.53)	.14 (2.02)	-.013 (0.37)	-.0017 (0.06)		.642	.839	2.07	581-784
Germany	.48 (5.95)	.01 (0.17)	.00 (0.06)	.03 (0.45)	-.051 (1.57)	.015 (1.18)		.647	1.33	1.96	611-801
Italy	.40 (11.03)	.04 (1.50)	.07 (2.52)	.11 (3.85)		.027 (0.05)		.744	96.2	2.12	611-794
Netherlands	.23 (4.71)	-.00 (0.01)	.03 (0.78)	.06 (1.34)	-.093 (2.37)	.0063 (1.90)		.425	.253	1.95	611-794
Sweden	.17 (6.28)	.02 (1.22)	.01 (0.29)	.00 (0.16)	-.054 (2.15)	.0014 (0.72)		.699	.177	2.02	611-794
Switzerland	.45 (4.46)	.06 (0.98)	.07 (1.06)	.31 (3.40)	-.062 (2.76)	.0036 (2.09)		.296	.270	2.27	581-794
U.K.	.06 (1.12)	.13 (3.12)	-.03 (0.68)	.01 (0.16)	-.058 (1.15)	1.4 (0.84)	-.43 (2.96)	.682	140.2	2.10	582-801
Finland	.22 (3.84)	.05 (1.12)	.11 (2.41)	.24 (3.93)	-.0067 (0.22)	-.82 (0.44)		.453	177.4	2.14	581-794
Greece	.24 (5.13)	.05 (1.21)	.03 (0.85)	.01 (0.40)	-.090 (2.18)	.042 (2.08)		.659	1.31	1.89	581-794
Ireland	.31 (6.93)	.08 (1.74)	.10 (2.20)	.13 (2.42)		.018 (0.62)		.799	5.87	2.11	581-794
Portugal	.18 (11.67)	-.00 (0.10)	-.01 (0.39)	.02 (1.30)	-.078 (2.00)	.016 (1.96)		.814	.367	1.92	581-784
Spain	.27 (8.12)	.05 (1.76)	.08 (2.83)	.03 (1.10)	-.023 (0.64)	.018 (0.13)		.775	6.10	2.26	621-784
Yugoslavia	.25 (2.46)	-.01 (0.16)	-.08 (1.21)	-.09 (1.35)	-.0082 (0.19)	.016 (0.80)		.867	.949	1.88	611-774
Australia	.26 (4.98)	.01 (0.21)	.13 (2.93)	.02 (0.43)	-.085 (1.81)	1.9 (1.43)	-.55 (3.73)	.956	99.2	2.20	604-801
New Zealand	.16 (0.52)	.35 (1.55)	.07 (0.36)	.12 (0.61)	-.11 (1.31)	.59 (1.11)	.40 (2.20)	.446	13.7	2.00	583-781
South Africa	.08 (0.61)	.09 (0.86)	.01 (0.07)	.09 (0.90)	-.068 (1.17)	1.1 (0.87)		.153	62.8	2.39	621-794
Libya	.25 (4.57)	-.07 (1.27)	.02 (0.41)	.01 (0.21)	-.093 (2.28)	.57 (2.51)		.386	9.15	0.99	651-774
Nigeria	.18 (10.52)	-.02 (0.99)	-.01 (0.41)	-.01 (0.44)				.833	41.8	1.82	712-781
Argentina	.20 (9.31)	.02 (1.01)	.00 (0.14)	.02 (0.87)	-.13 (1.32)	.12 (1.37)		.962	1.06	1.80	671-754
Brazil	.23 (2.14)	-.01 (0.08)	-.05 (0.72)	.08 (1.32)	-.056 (1.32)	.047 (1.02)		.370	.894	1.60	641-784
Chile	.12 (6.14)	.00 (0.08)	.01 (0.86)	.00 (0.26)	-.128 (2.75)	-1.78 (3.23)		.862	58.0	1.88	641-774
Colombia	.34 (1.65)	-.00 (0.01)	-.10 (0.37)	.03 (0.11)	-.142 (1.71)	52.0 (2.45)		.399	508.0	1.47	711-784
Mexico	.25 (6.24)	.10 (2.86)	.10 (2.99)	.14 (3.69)	-.082 (2.10)	.055 (2.18)		.599	1.16	2.15	581-794
Peru	.28 (1.76)	.05 (0.29)	-.03 (0.19)	.13 (1.04)	-.027 (0.85)	.011 (1.49)		.269	.605	1.61	641-782
Israel	.073 (2.98)	.04 (1.70)	.03 (1.45)	.07 (3.53)	-.33 (3.19)	2.19 (2.40)		.555	56.6	2.03	691-794
India	.10 (1.84)	.07 (1.41)	-.03 (0.53)	.01 (0.11)	-.12 (1.52)	.13 (2.12)		.688	.959	1.82	722-781
Korea	.34 (3.03)	-.02 (0.17)	.17 (1.54)	.19 (1.69)	-.17 (1.85)	1.9 (1.55)		.884	54.0	2.35	641-784
Malaysia	.35 (4.78)	.12 (1.78)	.05 (0.69)	-.04 (0.63)	-.058 (0.59)	1.3 (0.39)		.647	54.9	1.90	711-793
Philippines	.14 (4.66)	-.01 (0.48)	-.03 (0.88)	-.08 (2.52)	-.014 (0.59)	3.1 (1.57)		.457	187.3	2.00	581-794
Pakistan	.23 (6.44)	.03 (0.81)	-.00 (0.12)	-.06 (1.63)	-.019 (0.17)	-5.7 (0.38)		.939	165.9	1.72	731-792

TABLE 4 (continued)

Equation 4: Y_{it} is the dependent variable.

Country	Explanatory Variables				Implied Values				SE	DW	Sample Period
	S_{it}	V_{it-1}	Y_{it-1}	$\hat{\rho}_1$	λ	α	β	R^2			
Canada	.45 (7.23)	-.052 (2.15)	.60 (9.81)		.40	.1300	.96	.9995	221.3	1.84	581-801
Japan	.73 (9.22)	-.0099 (0.32)	.28 (3.70)	.54 (5.67)	.72	.0138	1.01	.9997	217.6	1.94	581-801
Austria	.69 (6.65)	-.083 (1.34)	.43 (5.09)		.57	.1456	1.45	.9949	2.11	1.82	651-793
Belgium	1.00 (30.61)	-.15 (3.23)	.13 (5.64)	.77 (9.42)	.87	.1724	0.87	.9998	1.76	1.71	581-784
Denmark	1.01 (57.07)	-.056 (2.00)	.036 (2.44)	.70 (8.44)	.964	.0581	0.82	.9996	.217	1.70	581-794
France	1.07 (12.98)	-.16 (2.94)	.18 (2.98)	.65 (7.20)	.82	.1951	1.56	.9997	1.29	1.89	581-784
Germany	.99 (10.12)	-.12 (1.23)	.17 (2.77)	.73 (8.11)	.83	.1446	1.33	.9990	1.45	1.99	611-801
Italy	.77 (11.81)	-.0013 (0.06)	.27 (4.77)	.69 (7.45)	.73	.0018	30.77	.9987	211.2	1.79	611-794
Netherlands	.99 (22.02)	-.14 (3.44)	.20 (6.04)	.65 (6.54)	.80	.1750	1.36	.9996	.210	1.78	611-794
Norway	.94 (14.84)	-.034 (0.35)	.073 (1.61)	.81 (6.36)	.927	.0367	0.38	.9982	.293	1.74	621-794
Sweden	1.00 (16.46)	-.053 (1.03)	.059 (1.38)	.83 (9.48)	.941	.0563	1.11	.9977	.471	1.92	611-794
Switzerland	.93 (12.54)	-.056 (2.95)	.20 (3.43)	.69 (8.96)	.80	.0700	2.32	.9985	.240	1.75	581-794
U.K.	1.14 (12.19)	-.18 (2.78)	.11 (1.81)	.35 (3.18)	.89	.2022	1.39	.9960	240.3	1.95	581-801
Finland	1.04 (11.56)	-.086 (1.14)	.12 (1.96)	.89 (10.63)	.88	.0977	1.86	.9979	241.0	1.94	581-794
Greece	1.03 (46.38)		.03 (1.80)	.85 (14.65)	.97	0	--	.9992	1.30	1.74	581-794
Ireland	1.04 (23.92)	-.082 (1.50)	.06 (1.69)	.73 (8.33)	.94	.0872	1.22	.9988	6.72	1.76	581-794
Portugal	1.05 (23.08)	-.033 (1.04)	.051 (1.41)	.75 (9.77)	.949	.0348	3.06	.9972	1.26	1.81	581-784
Spain	1.05 (31.69)	-.035 (1.06)	.013 (0.55)	.86 (10.39)	.987	.0355	1.80	.9996	6.19	1.86	621-784
Australia	.79 (9.80)	-.081 (1.36)	.29 (3.96)		.71	.1141	0.99	.9950	248.8	2.02	603-801
New Zealand	.096 (2.86)	-.019 (3.25)	.97 (28.03)	.75 (9.49)	.03	.6333	3.47	.9997	8.32	1.85	582-781
South Africa	.23 (3.38)	-.038 (1.73)	.83 (11.12)		.17	.2235	1.58	.9965	76.0	2.00	621-794
Libya	.86 (44.83)		.040 (2.08)	.99 (47.94)	.96	0	--	.9998	4.27	0.73	651-774
Saudi Arabia	.99 (29.72)	-.12 (1.05)	.035 (1.06)	.77 (3.83)	.965	.1244	0.21	.9998	.0827	1.00	721-782
Venezuela	.21 (3.03)		.80 (11.22)	.77 (7.95)	.20	0	--	.9998	99.5	1.72	621-784
Argentina	1.04 (48.65)	-.032 (0.79)	.01 (0.32)	.71 (5.08)	.99	.0323	1.56	.999	1.18	1.62	671-754
Brazil	.39 (3.85)	-.043 (1.04)	.65 (3.85)	.74 (7.26)	.35	.1229	0.93	.9994	1.73	1.83	641-784
Mexico	1.02 (40.73)		.013 (0.53)	.74 (10.23)	.987	0	--	.9995	1.54	1.79	581-794
Peru	.47 (4.79)	-.064 (2.35)	.63 (6.96)	.75 (8.30)	.37	.1730	1.56	.9993	.544	1.41	641-782
Egypt	.63 (10.57)		.41 (7.08)	.79 (7.73)	.59	0	--	.999	6.17	1.07	661-774
Jordan	1.08 (42.45)	-.24 (3.45)	.046 (1.58)	.30 (1.79)	.954	.2516	0.53	.999	0.869	1.18	731-784
India	1.03 (15.67)	-.084 (0.08)		.94 (0.99)	1.00	.0840	0.36	.9939	1.18	1.89	722-781
Korea	.85 (7.38)	-.15 (2.29)	.30 (2.64)	-.43 (2.36)	.70	.2143	1.00	.9905	98.9	2.04	641-784
Philippines	1.08 (83.51)	-.013 (1.85)	.040 (3.69)	.92 (19.91)	.960	.0135	9.23	.9998	99.0	2.05	581-794
Thailand	.77 (6.34)	-.18 (2.39)	.43 (4.16)	.87 (9.44)	.57	.3158	1.11	.9996	.408	1.37	621-794

TABLE 4 (continued)

Equation 5: $\log PY_{it}$ is the dependent variable.

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Country	Explanatory Variables										
	$\log PM_{it}$	r_{it}	R_{it}	$\frac{\bar{Y}_{it}}{\log POP_{it}}$	$\log PY_{it-1}$	t	$\hat{\rho}$	R^2	SE	DW	Sample Period
Canada	.061* (4.57)		.0026 (2.40)	.022* (9.29)	.93 (54.42)	.00030 (3.19)		.9998	.0050	1.95	581-801
Japan		.0028 (2.43)			.88 (14.98)	.0019 (2.11)	.69 (6.08)	.9996	.0079	1.98	581-801
Austria	.20* (3.44)			.013 (1.72)	.63 (6.10)	.0031 (3.17)		.997	.0130	2.32	651-793
Belgium	.073 (5.11)			.0098* (3.47)	.89 (40.20)	.00096 (5.50)		.9997	.0057	1.88	581-784
Denmark	.11* (3.58)		.0017 (0.73)	.0050* (0.68)	.75 (12.08)	.0034 (3.71)		.9994	.0119	2.05	581-794
France	.071* (3.97)				.88 (23.41)	.0012 (3.21)	.47 (5.16)	.9997	.0061	2.32	581-784
Germany	.034* (3.10)		.00085* (1.63)	.019* (6.70)	.94 (37.16)	.00039 (1.70)		.9996	.0049	2.30	611-801
Italy	.060 (4.66)	.0019* (2.70)			.91 (51.83)	.00080 (4.32)		.9996	.0099	1.90	611-794
Netherlands	.061* (3.17)			.012 (2.30)	.83 (14.89)	.0022 (2.87)		.9995	.0087	1.87	611-794
Norway	.18 (5.47)		.013* (2.85)		.47 (6.41)	.0061 (7.98)		.999	.0115	1.23	621-794
Sweden	.072* (5.42)	.0018* (2.15)	.0033* (1.17)		.85 (27.29)	.0013 (5.12)		.9997	.0064	1.73	611-794
Switzerland	.025* (0.94)	.00071* (0.40)		.019 (2.33)	.94 (23.76)	.00064 (1.36)		.999	.0088	2.13	581-794
U.K.	.048* (1.99)		.0033* (2.31)	.0018* (0.26)	.92 (25.66)	.00051 (1.48)		.9996	.0103	2.10	581-801
Finland	.068 (3.08)			.016* (2.37)	.90 (22.97)	.00089 (2.34)		.9995	.0111	1.59	581-794
Greece	.073 (2.99)			.0068* (0.70)	.91 (23.03)	.00087 (2.79)		.999	.0163	1.70	581-794
Ireland	.073* (2.35)		.0014* (0.99)	.014* (1.78)	.89 (19.31)	.0012 (2.31)		.999	.0159	1.85	581-794
Portugal	.16 (3.54)			.018* (1.76)	.84 (14.00)	.00072 (2.06)		.998	.0205	2.46	581-784
Spain	.058 (4.67)			.011* (1.19)	.97 (33.50)	-.00012 (0.20)		.999	.0123	2.09	621-784
Yugoslavia				.076 (2.24)	.96 (14.29)	.0016 (0.77)	.25 (1.92)	.997	.0345		611-774
Australia	.046 (1.48)		.0052 (1.69)	.013* (1.15)	.90 (15.96)	.00073 (1.69)		.999	.0150	1.77	603-801
New Zealand	.056* (2.83)				.92 (29.24)	.00076 (2.83)		.9982	.0162	1.94	582-781
South Africa	.12* (2.61)			.027* (1.92)	.83 (11.33)	.0014 (2.13)		.998	.0199	2.36	621-794
Brazil	.058 (1.97)				.90 (29.70)	.0046 (1.77)		.999	.0149	1.66	711-784
Chile	.24 (6.95)				.53 (5.52)	.0548 (1.52)	.94 (13.10)	.9996	.0668	2.11	641-774
Colombia	.068 (1.46)				.73 (7.58)	.0103 (1.88)		.998	.0199	1.86	711-784
Israel	.088 (1.83)			.032* (1.34)	.95 (13.30)	-.00040 (0.22)		.999	.0253	1.93	691-794
Jordan	.073 (0.59)				.50 (2.85)	.014 (2.23)		.853	.0905	1.53	731-784
Syria	.14 (3.24)				.78 (12.39)	.00053 (0.70)		.987	.0385	2.30	641-784
India	.070 (1.16)				.43 (0.75)	.0038 (0.54)	.67 (1.39)	.962	.0269	2.19	722-781
Korea	.11 (3.15)	.0015 (1.35)		.019* (1.43)	.59 (6.14)	.013 (3.84)		.996	.0430	2.46	641-784
Malaysia	.048 (0.95)			.068 (4.17)	.62 (5.68)	.0064 (3.81)		.983	.0253	2.31	711-793
Pakistan	.071 (2.74)				.77 (11.37)	.0036 (2.09)		.996	.0141	2.38	731-792
Philippines	.026 (1.79)	.0031 (2.07)		.022* (2.31)	.96 (32.14)	.00018 (0.34)		.9988	.0196	1.67	581-794
Thailand	.050 (1.09)				.89 (10.38)	.00087 (1.90)		.9949	.0196	1.05	654-794

TABLE 4 (continued)

Equation 6: Ml_{it}^*/POP_{it} is the dependent variable.

Country	Explanatory Variables							Sample Period
	r_{it}	$\frac{PY_{it} - Y_{it}}{POP_{it}}$	$\frac{Ml_{it-1}^*}{POP_{it-1}}$	t	R ²	SE	DW	
Canada	-6.7 (3.67)	.040 (2.72)	.92 (17.86)	.46 (1.55)	.994	19.7	2.65	581-801
Japan	-4.4 (0.82)	.37 (3.18)	.71 (8.09)	.053 (0.35)	.997	9.68	2.53	581-801
Austria		.17 (2.30)	.67 (6.60)	.020 (1.26)	.993	.387	1.90	651-793
Belgium	-.29 (3.90)	.30 (5.44)	.62 (8.82)	.053 (3.57)	.997	.897	2.40	581-784
Denmark	-.064 (5.55)	.45 (10.94)	.44 (7.92)	.0052 (2.09)	.997	.184	1.81	581-794
France	-.028 (2.98)	.33 (5.70)	.59 (7.48)	.0103 (3.40)	.996	.149	2.41	581-784
Germany	-.017 (5.50)	.28 (4.83)	.61 (8.42)	-.0011 (0.92)	.998	.0424	2.56	611-801
Italy	-4.5* (2.95)	.28 (2.47)	.93 (13.67)	.29 (0.57)	.998	30.8	2.53	611-794
Netherlands	-.035 (7.06)	.62 (8.52)	.20 (2.37)	.0033 (2.15)	.997	.0639	2.02	611-794
Norway	-.0042* (0.19)	.51 (5.98)	.18 (1.41)	.016 (3.05)	.990	.257	2.14	621-794
Sweden	-.016* (0.86)	.26* (4.03)	.65 (6.59)	-.0084 (2.46)	.989	.170	2.23	611-794
Switzerland	-.047 (2.25)	.043 (0.55)	.89 (18.31)	.0098 (2.08)	.995	.186	1.90	581-794
U.K.	-1.8 (5.97)	.18 (6.33)	.71 (13.96)	.048 (1.03)	.999	4.46	2.00	581-801
Finland	-4.2* (0.48)	.25* (7.44)	.32 (3.35)	-2.7 (3.76)	.994	56.5	2.23	581-794
Greece	-.061 (1.64)	.64 (9.20)	.05 (0.45)	.011 (1.84)	.996	.400	1.61	581-794
Ireland	-1.6 (4.05)	.10 (3.83)	.90 (21.78)	.085 (1.40)	.997	5.49	1.96	581-794
Portugal	-.074 (0.76)	.30 (1.97)	.85 (12.65)	.0081 (1.21)	.995	.530	2.11	581-784
Spain	-.47 (1.19)	.60 (6.20)	.46 (4.76)	.042 (1.82)	.997	1.25	1.92	621-784
Australia	-6.8* (5.06)	.12 (4.99)	.80 (15.54)	.087 (0.67)	.998	9.40	1.31	603-801
New Zealand	-10.6 (4.89)	.18* (4.23)	.76 (12.02)	-.68 (2.76)	.986	13.6	2.39	582-781
South Africa	-1.4 (3.74)	.049 (2.68)	.84 (14.37)	.23 (3.03)	.994	3.22	2.05	621-794
Iran	-.036 (0.43)	.049 (1.37)	.97 (14.45)	.0044 (0.42)	.991	.593	1.91	614-781
Colombia	-1.5 (0.08)	.26 (2.83)	.58 (3.97)	-9.5 (1.32)	.995	80.4	2.08	711-784
Peru	-.069 (1.34)	.12 (2.94)	.88 (16.03)	.0040 (0.80)	.996	.195	2.17	641-782
Korea	-.013* (0.56)	.086 (5.05)	.83 (16.80)	.025 (1.41)	.997	.995	2.28	641-784
Philippines		.097* (4.60)	.71 (10.35)	.078 (1.24)	.995	6.44	1.85	581-794
Thailand	-.0043* (1.55)	.23 (5.81)	.20 (1.48)	.0024 (3.76)	.992	.0227	1.85	654-794

Equation 7a: r_{it} is the dependent variable.

TABLE 4 (continued)

Country	U.S. Rate r_{it}	German Rate r_{8t}	Explanatory Variables										R ²	SE	DW	Sample Period					
			\dot{M}_{it-1} POP	\dot{Y}_{it} POP	$\frac{A^*_{it}}{PY_{it}}$	$\frac{A^*_{it-1}}{PY_{it-1}}$	$\frac{A^*_{it}}{PY_{it}}$	$\frac{A^*_{it-1}}{PY_{it-1}}$	$\frac{A^*_{it}}{PY_{it}}$	$\frac{A^*_{it-1}}{PY_{it-1}}$	$\frac{A^*_{it}}{PY_{it}}$	$\frac{A^*_{it-1}}{PY_{it-1}}$					$\frac{A^*_{it}}{PY_{it}}$				
Canada	.82 (4.75)		.059 (2.17)														.61 (3.88)	.965	.257	1.36	631-701
Japan																		.793	.769	2.21	581-712
Austria		.15 (5.11)																.915	.132	1.84	651-711
Belgium	.31 (3.47)	.23 (2.43)																.904	.448	1.99	581-712
Denmark	.19 (3.32)																	.926	.333	1.48	581-712
France	.37 (3.87)																	.926	.489	2.09	581-712
Germany	.44 (3.90)																	.954	.419	1.58	611-711
Italy		.12 (5.90)																.936	.167	2.27	611-712
Netherlands	.65 (5.43)																	.962	.401	1.82	611-711
Sweden	.27 (3.29)																	.873	.342	2.16	611-712
Switzerland	.04 (1.28)	.04 (2.00)																.928	.173	2.03	581-711
U.K.	.19 (2.21)																	.907	.418	1.67	581-712
Finland																		.239	.259	1.59	581-712
Greece																		.944	.736	2.11	581-794
Ireland	.16 (1.46)																	.822	.601	1.92	581-712
Portugal	.013 (0.64)																	.941	.117	2.17	581-712
Spain	.12 (3.32)																	.938	.161	2.47	621-712
Australia	.08 (1.83)																	.938	.183	1.94	603-712
South Africa																		.963	.321	1.92	621-794
Iran	.15 (3.22)																	.941	.402	2.10	614-781
Korea																		.856	2.32	1.85	641-784
Pakistan																		.808	.706	1.46	731-792
Philippines	.095 (1.46)																	.877	.739	1.79	581-794
Thailand	.25 (3.50)																	.890	.562	1.76	654-794

TABLE 4 (continued)

Equation 7b: r_{it} is the dependent variable.

Country	Explanatory Variables										R^2	$\hat{\rho}_1$	t	Sample Period		
	U.S. Rate r_{1t}	German Rate r_{8t}	$\frac{M_{it-1}}{POP_{it-1}}$	$\frac{\tilde{Y}_{it}}{POP_{it}}$	$\frac{A_{it}^*}{PY_{it} POP_{it}}$	$\frac{A_{it-1}^*}{PY_{it-1} POP_{it-1}}$	$\frac{\Delta PY_{it} POP_{it}}{PY_{it} POP_{it}}$	$\frac{A_{it}^*}{PY_{it} POP_{it}}$	$\frac{PM_{it-1}}{PY_{it-1}}$	e_{it}					r_{it-1}	
Canada	.35 (3.68)		.023 (2.06)	6.7 (0.71)	-.0086 (1.07)	.0071 (1.04)					.66 (3.99)	.29 (1.20)	.971	.477	1.90	711-801
Japan			.058 (2.95)	1.6* (1.00)	-.12 (5.15)	.13 (6.94)					.81 (13.22)		.976	.451	1.59	722-801
Austria				12.8* (2.55)	-.089 (0.54)	.088 (0.56)					.83 (7.83)		.806	.393	2.02	723-793
Belgium			.041 (0.55)	58.2 (4.78)							.52 (4.05)		.836	.968	2.44	722-784
Denmark			.16 (2.10)	21.5* (1.50)	-5.0* (1.75)	3.2* (1.24)		.037 (1.29)			.45 (3.12)		.749	1.97	2.31	732-794
France	.18 (0.97)	.34 (4.42)		41.1 (3.21)				.0094 (1.28)	.074 (2.01)		.44 (5.24)		.953	.516	1.95	722-784
Germany	.12 (0.68)							-3.1* (0.69)			.67 (5.97)		.870	.966	1.97	722-801
Italy						.11 (8.47)			15.7 (4.04)		.65 (7.68)		.933	.989	1.72	722-794
Netherlands	.63 (3.03)			93.1 (4.04)							.32 (2.80)		.782	1.66	1.73	722-794
Norway			.29 (2.26)	15.9 (0.80)	-1.61 (2.08)	1.05 (1.50)					.22 (1.43)		.584	1.44	2.27	722-794
Sweden			.13 (1.62)	41.3* (5.31)	-4.4 (6.2)	2.1 (3.54)		.018 (3.16)			.34 (3.51)		.918	.502	2.06	722-794
Switzerland	.11 (3.57)			9.1* (3.53)	-3.1* (6.65)	2.3* (5.63)		.0069 (3.43)			.16 (1.36)		.991	.952	2.31	722-794
U.K.			.031 (1.60)	8.9* (0.69)							.72 (1.05)	.59 (0.85)	.831	1.11	1.87	722-801
Finland									-0.00074 (1.39)		.78 (8.32)		.793	.382	1.91	722-794
Ireland			.011 (0.48)								.83 (6.89)		.708	1.43	1.24	722-794
Portugal	.11 (0.46)			6.3 (1.01)							.72 (4.85)		.946	1.01	2.39	722-784
Spain	.069 (2.60)		.021 (2.99)								.56 (4.93)		.970	.176	2.30	722-784
Australia	.077 (1.59)			24.3* (4.57)							.59 (6.78)		.942	.408	2.48	722-801
New Zealand			.017 (1.76)	14.3 (1.07)							.77 (3.06)		.905	.593	1.58	732-781

TABLE 4 (continued)

Equation 8: R_{it} is the dependent variable. $3PY_{it}$ = average percentage change in PY (at an annual rate) for quarters t , $t-1$, and $t-2$.Explanatory Variables

Country	R_{it}	R_{it-1}	R_{it-2}	R_{it-1}	$3PY_{it}$	t	$\hat{\rho}_1$	R^2	SE	DW	Sample Period
Canada	.33 (3.95)	-.27 (2.23)	.04 (0.79)	.84 (11.37)	.014 (1.11)	.0023 (0.54)		.982	.250	1.55	581-801
Belgium	.07 (2.05)	.06 (1.40)	-.05 (2.08)	.70 (14.00)	.014* (1.69)	.0091 (4.52)		.984	.163	1.43	581-784
Denmark	.18 (3.64)	-.06 (1.21)	-.04 (1.05)	.72 (9.64)		.027 (2.90)		.972	.553	1.93	581-794
France	.21 (4.15)	-.11 (1.61)	.05 (1.21)	.72 (13.88)		.0088 (3.67)		.986	.214	2.04	581-784
Germany	.25 (4.94)	-.14 (2.18)	.00 (0.09)	.83 (15.86)		-.00067 (0.37)		.939	.316	1.58	611-801
Italy	.17 (4.29)	-.08 (1.68)	.02 (0.57)	.85 (16.07)		.0034 (0.58)	.39 (3.06)	.993	.255	1.64	611-794
Netherlands	.17 (4.41)	-.11 (2.89)	.05 (2.07)	.73 (9.90)	.043 (2.18)	.0083 (2.35)		.966	.297	1.76	611-794
Norway	.09 (2.47)	-.02 (0.91)	.01 (0.69)	.86 (12.62)	.0098 (0.95)	.00069 (0.15)		.969	.218	1.51	621-794
Sweden	.13 (2.83)	-.05 (0.87)	-.04 (1.21)	.92 (20.45)	.013 (1.81)	.0040 (1.34)		.992	.148	1.43	611-794
Switzerland	.30 (2.42)	-.02 (0.14)	.15 (1.53)	.51 (3.23)		.0084 (2.37)	.57 (3.26)	.983	.155	1.89	581-794
U.K.	.19 (1.66)	-.06 (0.39)	-.02 (0.32)	.79 (10.93)	.029 (1.28)	.011 (1.73)		.979	.483	1.81	581-801
Ireland	-.07 (0.47)	.31 (1.71)	-.09 (0.96)	.76 (9.55)	.026 (0.95)	.018 (2.30)		.966	.716	2.22	581-794
Portugal	.15 (3.01)	.14 (2.30)	-.08 (1.49)	.81 (14.70)		.0025 (1.07)		.991	.297	1.33	581-784
Australia	.39 (5.97)	-.19 (2.41)	-.09 (1.75)	.84 (16.48)	.018 (2.89)	.0023 (1.22)		.994	.158	1.61	603-801
New Zealand	.13 (2.16)	.17 (3.23)	.04 (0.51)	.57 (3.65)	.012 (1.16)	.011 (1.87)		.983	.156	1.96	582-781
South Africa	.50 (3.29)	-.46 (1.92)	.06 (0.49)	.84 (14.57)	.013* (1.83)	.0070 (1.57)		.989	.204	1.52	621-794
India	-.01 (1.70)	.02 (3.11)	-.02 (2.99)	.65 (10.40)		.0030 (1.31)		.987	.0355	1.98	722-781

TABLE 4 (continued)

Equation 9b: $\log e_{it}$ is the dependent variable.

Country	German Rate $\log e_{8t}$	$\log e_{it-1}$	$\log e_{it-1}$	$\log \frac{PY_{it}}{PY_{it-1}}$	$\frac{PY_{it}}{PY_{it-1}} \log \frac{1}{4} \log \frac{(1+r_{it}/100)}{(1+r_{it-1}/100)}$	$\log \frac{Y_{it}/POP_{it}}{Z_{it}^u}$	Explanatory Variables			DW	Sample Period
							$\log \frac{A_{it-1}^*}{PY_{it-1} POP_{it-1}}$	$\log \frac{A_{it-1}^*}{PY_{it-1} POP_{it-1}}$	$\log \frac{A_{it-1}^*}{PY_{it-1} POP_{it-1}}$		
							$\hat{\rho}_1$	R^2	SE		
Canada		.91 (9.09)	.10 (0.88)	-.14 (0.10)			.51 (2.49)	.966	.0121	1.79	711-801
Japan		.83 (8.99)	.064 (1.18)	-.36 (0.24)				.946	.0328	1.88	722-801
Austria	.95 (46.94)	.022 (1.00)	.074 (0.79)	-.042 (4.58)			.84 (8.87)	.999	.00485	1.71	723-793
Belgium	.80 (17.92)	.014 (0.25)		-.042 (2.40)			.76 (6.49)	.988	.0109	1.73	722-784
Denmark	.50 (8.03)	.084 (0.86)	.49 (3.69)					.889	.0195	1.16	732-794
France	.53 (5.04)	.36 (2.34)	.98 (2.85)				.68 (3.73)	.853	.0238	1.52	722-784
Germany		.66 (5.32)	1.3 (2.88)	-4.1 (1.77)				.944	.0395	1.95	722-801
Italy	.32 (4.29)	.66 (6.30)	.47 (4.22)					.974	.0268	1.75	722-794
Netherlands	.78 (22.26)	.092 (2.19)						.995	.0095	1.95	722-794
Norway	.20 (4.08)	.53 (5.41)		-1.0 (1.22)			.47 (2.70)	.879	.0267	1.30	722-794
Sweden	.42 (7.13)	.31 (3.34)	.88 (6.71)	-4.5 (4.73)				.805	.0213	1.13	722-794
Switzerland	.90 (6.28)	.15 (1.16)	.99 (2.69)	-6.3 (1.36)		.082* (1.07)	.68 (4.25)	.987	.0294	1.56	722-794
U.K.	.30 (3.77)	.80 (9.70)	.34 (3.06)			.029* (1.44)		.937	.0332	2.30	722-801
Finland	.27 (2.88)	.78 (8.41)	.31 (3.30)	-2.7 (1.50)				.756	.0233	1.61	722-794
Ireland		.88 (9.13)	.10 (1.00)					.931	.0351	1.70	722-794
Portugal	.42 (4.85)	.63 (8.67)	.68 (6.79)					.983	.0279	2.23	722-784
Spain	.52 (4.79)	.51 (5.40)	.60 (5.60)					.938	.0312	1.69	722-784
Australia		.89 (12.83)	.11 (1.30)					.922	.0287	1.93	722-801
New Zealand		.90 (5.75)	.36 (1.09)			.032 (1.66)		.956	.0344	2.30	732-781
Brazil		.68 (14.56)	.29 (6.37)			.092 (1.68)		.995	.0525	1.32	641-784
Colombia		.90 (9.02)	.070 (0.92)					.992	.0207	2.19	711-784
India		.74 (9.14)	.089 (0.96)					.857	.0237	1.62	722-781

TABLE 4 (continued)

Equation 10b: $\log F_{it}$ is the dependent variable.

For this equation the numbers in parentheses are standard errors rather than t-statistics.

Country	$\log ee_{it}$	Explanatory Variables				Sample Period
		$\frac{1}{4} \log \frac{(1+r_{it}/100)}{(1+r_{1t}/100)}$	R^2	SE	DW	
Canada	.97461 (.00457)	.92 (.083)	.999	.00202	1.57	711-801
Japan	1.00128 (.00228)	1.34 (.40)	.987	.0172	1.17	722-801
Austria	.99954 (.00048)	.83 (.36)	.997	.0083	1.35	723-793
Belgium	.99924 (.00040)	1.45 (.25)	.996	.0069	2.32	722-784
Denmark	.99887 (.00064)	.78 (.24)	.972	.0108	2.28	732-794
France	1.00042 (.00019)	.91 (.14)	.998	.0033	1.86	722-784
Germany	1.00137 (.00025)	.25 (.23)	.998	.0078	1.36	722-801
Netherlands	1.00038 (.00014)	.82 (.13)	.999	.0046	1.92	722-794
Norway	.99843 (.00068)	.65 (.52)	.951	.0176	2.43	722-794
Sweden	.99946 (.00027)	.95 (.23)	.979	.0076	1.45	722-794
Switzerland	1.00058 (.00032)	.93 (.18)	.9996	.0057	1.25	722-794
U.K.	.99911 (.00232)	1.38 (.21)	.998	.0060	1.33	722-801
Finland	1.00509 (.00203)	2.11 (.41)	.950	.0116	1.50	722-794

TABLE 4 (continued)

Equation 11: $\log PX_{it}$ is the dependent variable.

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Country	Explanatory Variables					$\hat{\rho}_1$	R^2	SE	DW	Sample Period
	$\log PY_{it}$	$\log PW_{it}$	$\log e_{it}$	$\log PW_{it} e_{it}$	const.					
Canada	.92 (7.11)	.35 (4.59)	.13 (1.14)			.98 (64.26)	.999	.0137	1.51	581-801
Japan	.74 (3.64)	.38 (3.58)	.64 (8.50)		.69 (2.99)	.98 (67.81)	.988	.0206	1.91	581-801
Austria	.29 (3.41)			.64 (5.28)	2.57 (5.19)	.66 (6.99)	.984	.0217	2.12	651-793
Belgium	.31 (3.56)			.54 (5.39)	1.76 (5.24)	.88 (20.12)	.993	.0166	1.98	581-784
Denmark	.06 (1.37)	.85 (12.58)	.49 (4.67)		2.53 (4.68)	.56 (6.21)	.996	.0195	1.79	581-794
France	.20 (6.59)	.76 (23.91)	.48 (12.84)		2.62 (12.93)	.53 (5.91)	.999	.0114	1.96	581-784
Germany	.38 (3.19)	.43 (6.33)	.20 (4.24)		1.15 (4.05)	.94 (22.85)	.998	.0104	1.68	611-801
Italy	.29 (2.94)	.72 (6.51)	.65 (7.25)		.27 (6.83)	.89 (18.08)	.999	.0184	2.24	611-794
Netherlands	.22 (2.66)			.82 (8.84)	4.91 (8.76)	.92 (20.17)	.995	.0159	1.99	611-794
Norway		1.10 (18.72)	.88 (6.00)		4.57 (6.00)	.75 (9.39)	.994	.0232	1.90	621-794
Sweden	.46 (5.28)	.62 (7.82)	.24 (3.35)		1.26 (3.25)	.92 (22.42)	.999	.0120	1.89	611-794
Switzerland	.50 (16.05)	.29 (4.50)	.28 (4.89)		1.66 (4.83)	.55 (6.05)	.994	.0154	2.23	581-794
U.K.	.56 (11.40)	.54 (9.81)	.32 (7.44)		.29 (7.12)	.94 (26.30)	.9996	.0102	2.00	581-801
Finland	.31 (3.24)			.83 (8.73)	-1.17 (9.00)	.88 (18.59)	.998	.0252	2.07	581-794
Greece	.34 (1.82)	.50 (2.54)	.63 (2.28)		2.11 (2.23)	.66 (7.72)	.983	.0493	2.06	581-794
Ireland	.50 (7.19)	.56 (6.93)	.42 (7.26)		.321 (5.57)	.94 (24.91)	.999	.0147	1.84	581-794
Spain	.10 (1.17)	.72 (6.53)	.66 (5.31)		1.89 (5.49)	.34 (2.95)	.981	.0450	1.94	621-784
Yugoslavia	.21 (3.69)	.75 (9.47)	1.00 (44.09)		4.05 (42.41)	.12 (0.95)	.999	.0386	1.94	611-774
Australia	.32 (1.80)	.60 (3.59)	.15 (0.94)		.087 (1.78)	.89 (16.39)	.991	.0341	1.49	603-801
New Zealand	.60 (3.72)	.24 (1.36)	.25 (1.77)		.161 (2.57)	.91 (15.85)	.989	.0352	1.11	582-781
South Africa	.19 (1.26)	.72 (4.76)	.26 (1.73)		.11 (2.08)	.84 (13.20)	.993	.0327	1.98	621-794
Brazil	.07 (0.56)			.95 (7.66)	4.63 (7.57)	.84 (10.13)	.997	.0583	1.72	641-784
Colombia	1.10 (2.07)			.30 (0.63)	-.92 (0.59)	.75 (4.67)	.982	.0963	1.57	711-784
Israel	.11 (1.09)	.75 (4.41)	1.06 (13.12)		-2.14 (12.81)	.82 (10.28)	.999	.0323	2.08	691-794
Jordan	.35 (1.68)			.17 (1.11)		.86 (9.35)	.886	.0993	1.18	731-784
Syria				1.63 (12.93)	-2.08 (15.56)	.78 (9.42)	.979	.0852	1.10	641-784
India	.21 (0.69)			.78 (4.65)	3.76 (4.62)	.25 (1.20)	.949	.0531	1.79	722-781
Korea		.81 (11.92)	.95 (13.94)		.79 (11.84)	.86 (12.71)	.997	.0292	1.48	641-784
Malaysia	.87 (2.54)	.74 (2.34)	.40 (0.95)		-.278 (0.77)	.71 (5.73)	.970	.0611	1.63	711-793
Pakistan				.54 (1.85)	-1.09 (1.54)	.68 (4.69)	.838	.0702	1.39	731-792
Philippines		.96 (7.77)	.90 (10.37)		-1.83 (10.47)	.87 (15.47)	.992	.0621	1.43	581-794
Thailand	.67 (1.69)	.53 (1.73)	1.28 (0.61)		4.95 (0.60)	.87 (12.50)	.978	.0549	1.95	621-794
U.S.	.94 (8.63)	.29 (5.14)			.30 (7.69)	.96 (31.39)	.999	.0106	1.34	581-801

TABLE 4 (continued)

Regressions for the construction of the demand pressure variable.

$\log \frac{Y_{it}}{POP_{it}}$ is the dependent variable.

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Country	t	Growth Rate (annual rate)	R ²	SE	DW	Sample Period
Canada	.00831 (80.57)	3.4	.986	.0250	0.17	581-801
Japan	.0184 (50.23)	7.6	.966	.0889	0.03	581-801
Austria	.0105 (53.06)	4.3	.982	.0259	0.42	651-793
Belgium	.0100 (75.06)	4.1	.985	.0297	0.43	581-784
Denmark	.00819 (46.06)	3.3	.961	.0423	0.81	581-794
France	.0103 (96.70)	4.2	.991	.0236	0.09	581-784
Germany	.00814 (61.56)	3.3	.980	.0258	0.32	611-801
Italy	.00833 (45.24)	3.4	.964	.0352	0.15	611-794
Netherlands	.00827 (48.56)	3.3	.969	.0325	0.25	611-794
Norway	.00884 (86.90)	3.6	.991	.0179	1.23	621-794
Sweden	.00585 (29.53)	2.4	.920	.0378	0.27	612-794
Switzerland	.00527 (25.76)	2.1	.883	.0487	0.09	581-794
U.K.	.00557 (67.40)	2.2	.982	.0200	0.88	581-801
Finland	.0102 (49.67)	4.1	.966	.0488	0.33	581-794
Greece	.0143 (55.80)	5.8	.973	.0611	0.78	581-794
Ireland	.00812 (60.93)	3.3	.978	.0317	0.71	581-794
Portugal	.0131 (46.15)	5.4	.962	.0632	0.47	581-784
Spain	.0114 (44.99)	4.6	.968	.0409	0.45	621-784
Yugoslavia	.0129 (61.82)	5.3	.983	.0338	0.84	611-774
Australia	.00690 (45.63)	2.8	.969	.0306	0.48	603-801
New Zealand	.00508 (41.85)	2.0	.956	.0250	0.09	582-781
South Africa	.00436 (21.05)	1.8	.861	.0365	0.24	621-794
Iran	.0184 (45.73)	7.6	.969	.0622	0.16	614-781
Libya	.0145 (14.47)	5.9	.802	.1079	0.22	651-774
Nigeria	.0160 (4.39)	6.6	.411	.1539	0.53	712-781
Saudi Arabia	.0146 (12.97)	6.0	.867	.0430	0.28	721-782
Venezuela	.0048 (32.55)	1.9	.940	.0239	0.08	621-784
Argentina	.0085 (16.08)	3.4	.917	.0329	0.88	671-754
Brazil	.0164 (48.79)	6.7	.975	.0450	0.21	641-784
Chile	.00054 (0.93)	0.2	.298	.0701	0.75	641-774
Colombia	.0068 (22.18)	2.7	.940	.0159	0.23	711-784
Mexico	.0072 (36.15)	2.9	.937	.0474	0.47	581-794
Peru	.00399 (16.48)	1.6	.824	.0308	0.11	641-782
Egypt	.0057 (11.87)	2.3	.747	.0462	0.09	661-774
Israel	.00631 (10.47)	2.5	.717	.0505	0.55	691-794
Jordan	.0212 (8.04)	8.8	.739	.0885	0.73	731-784
Syria	.0110 (21.02)	4.5	.881	.0698	0.13	641-784
India	.0048 (7.01)	1.9	.979	.0231	0.98	722-781
Korea	.0203 (37.33)	8.4	.977	.0729	2.83	641-784
Malaysia	.0118 (28.19)	4.8	.961	.0249	1.01	711-793
Pakistan	.0036 (4.47)	1.4	.908	.0308	1.81	731-792
Philippines	.00609 (34.82)	2.5	.933	.0416	1.35	581-794
Thailand	.0113 (61.96)	4.6	.985	.0226	0.22	654-794

table, this refers to the variable on the IFS tape with the particular number. Some adjustments were made to the raw data, and these are explained in the Appendix. The main adjustment that was made was the construction of quarterly National Income Accounts (NIA) data from annual data when the quarterly data were not available. Another important adjustment concerned the linking of the Balance of Payments data to the other export and import data. The two key variables involved in this process are BOP^* and TT^* , and, as noted in Table 1, the construction of these variables is explained in Table A-3 in the Appendix.⁶ Most of the data are not seasonally adjusted.

Note that two interest rates are listed in Table 1, the short term rate (r_{it}) and the long term rate (R_{it}). The notation for these two rates should not be confused with the notation in Section II, where both r and R denoted short term rates. For many countries only discount rate data are available for r_{it} , and this is an important limitation of the data base. The availability of interest rate data by country is discussed in Table A-1 in the Appendix.

A_{it}^* in Table 1 was constructed by summing past values of BOP_{it}^* from a base period value of zero. The summation began in the first quarter for which data on BOP_{it}^* existed. This means that the A_{it}^* series is off by a constant amount each period (the difference between the true value of A_{it}^* in the base period and zero). In the estimation work the functional forms were chosen so that this error was always absorbed in the estimate of the constant term. It is important to note that A_{it}^*

⁶The balance of payments variable is denoted BOP^* rather than S . S is used to denote final sales. This should not be confused with the notation in Section II, where S denotes the balance of payments.

measures only the net asset position of the country vis-a-vis the rest of the world. Domestic wealth, such as the domestically owned housing stock and plant and equipment stock, is not included.

An Outline of the Model

Table 2 contains a complete description of the equations for country i except for the functional forms and coefficient estimates of the stochastic equations. There are up to 11 estimated equations per country, and these are listed first in Table 2. Equations 12 through 20 are definitions.

Equation 1 determines the demand for merchandise imports, and equation 14 provides the link from merchandise imports to total NIA imports. Equations 2 and 3 determine the demands for consumption and investment, respectively. Equation 16 is the definition for final sales. The level of final sales is equal to consumption plus investment plus government spending plus exports minus imports plus a discrepancy term. Government spending is exogenous. Exports are determined when the countries are linked together. The key export variable is $X75_{it}$, and equation 15 links this variable to NIA exports. Equation 4 determines production, and equation 12 determines inventory investment, which is the difference between production and sales. Equation 13 defines the stock of inventories.

Equation 5 is the key price equation in the model. It determines the GNP deflator. The existence of a price equation in the model means that equilibrium is not necessarily assumed to exist in the product market. Any difference between demand and supply in a period is reflected in a change in inventories. The other price equation in the model is equation 11, which determines the export price index as a function of the GNP deflator and other variables.

Equation 17 defines the balance of payments on current account, BOP_{it}^* . Equation 17 and the equations involved in determining its right hand side variables are represented by equation (i) (or (ii)) in Section II. Given BOP_{it}^* , the asset variable A_{it}^* is determined by equation 18. This equation is analogous to equation (iii) (or (iv)) in Section II. The demand for money is determined by equation 6. Although the money supply drops out of the budget constraint when the private and government sectors are aggregated, it is an explanatory variable in the interest rate reaction functions in the model and so needs to be explained. Equation 6 is analogous to equation (11) (or (14)) in Section II.

Equations 7a and 7b are the interest rate reaction functions. They are analogous to equation (v) (or (vi)) in Section II. The "a" denotes that the equation is estimated over the fixed exchange rate period, and the "b" denotes that it is estimated over the flexible rate period. Equation 8 introduces a variable that was not considered in Section II, the long term interest rate. This equation is a standard term structure equation.

Equation 9b is the exchange rate reaction function. It is analogous to equation (vii) in Section II and is estimated only over the flexible exchange rate period. e_{it} in equation 9b is the average exchange rate for the period, whereas ee_{it} in equation 20 is the end-of-period rate. Equation 20 links e_{it} to ee_{it} , where ψ_{lit} in the equation is the historic ratio of e_{it} to $(ee_{it} + ee_{it-1})/2$. ψ_{lit} is taken to be exogenous. ee_{it} is used in equation 10b, along with the interest rates, to determine the forward rate, F_{it} . Equation 10b is an estimate of the arbitrage condition, equation (viii) in Section II. As noted in Section II, F_{it} plays no role in the model, and so neither does ee_{it} .

The trade and price linkages are presented in Table 3. Table 3 takes as input from each country the total value of merchandise imports in 75\$ ($M75\$A_{it}$), the export price index (PX_{it}), and the exchange rate (e_{it}). It returns for each country the total value of merchandise exports in 75\$ ($X75\$_{it}$) and the import price index (PM_{it}). These latter two variables are used as inputs by each country. The model is solved for each quarter by iterating between the equations for each country in Table 2 and the equations in Table 3.

Note from Table 1 that the data taken from the DOT tape are merchandise exports from i to j in \$ ($XX\$_{ijt}$). These data were converted to 75\$ by multiplying $XX\$_{ijt}$ by $e_{it}/(e_{175}PX_{it})$ (see $XX75\$_{ijt}$ in Table 1). This could only be done, however, if data on e_{it} and PX_{it} existed. Type A countries are countries for which these data exist, and Type B countries are the remaining countries. The share variable α_{jit} that is used in Table 3 is defined in Table 1. α_{jit} is the share of i 's total merchandise imports from Type A countries imported from j in 75\$. If j is a Type B country, then α_{jit} is zero. Given the definition of $M75\$A_{it}$ in Table 1, α_{jit} has the property that $\sum_j \alpha_{jit} = 1$. Table 3 deals only with Type A countries. Total merchandise imports of a country from Type B countries, $M75\$B_{it}$ in Table 1, is taken to be exogenous in the model.

The Estimated Equations

The estimated equations are presented in Table 4. Equations 1-6 and 8 were estimated by two stage least squares, and the remaining equations were estimated by ordinary least squares. Lagged dependent variables were used extensively in the estimation work to try to account for

expectational and lagged adjustment effects. This procedure is consistent with the treatment of expectations in the theoretical model discussed in Section II, where expectations are assumed to be formed on the basis of a limited set of information. Explanatory variables were dropped from the equations if they had coefficient estimates of the wrong expected sign. A number of the equations were estimated under the assumption of first order serial correlation of the error term. $\hat{\rho}$ in Table 4 denotes the estimate of the serial correlation coefficient. In many cases variables were left in the equations if their coefficient estimates were of the expected sign even if the estimates were not significant by conventional standards.⁷

Both current and one-quarter lagged values were generally tried for the explanatory price and interest rate variables, and the values that gave the best results were used. Similarly, both the short term and long term interest rate variables were tried, and the variable that gave the best results was used. All the equations except 10b and 11 were estimated with a constant and three seasonal dummy variables. To conserve space, the coefficient estimates of these four variables are not reported in Table 4. In most cases the functional form chosen for the equations was the log form. Data limitations prevented all the equations from being estimated for all countries and also required that shorter sample periods from the basic period be used for many countries. The main part of the model, excluding the U.S., consists of countries Canada through the U.K.

⁷There is considerable collinearity among many of the explanatory variables, especially the price variables, and the number of observations is fairly small for equations estimated only over the flexible exchange rate period. Many of the coefficients are thus not likely to be estimated very precisely, and this is the reason for retaining variables even if their coefficient estimates had fairly large estimated standard errors.

in Table 4. Iran through Venezuela are the primary oil exporting countries.

The specification of the following equations is generally consistent with the theory outlined in Section II. When it is not, such as the use of income as an explanatory variable in the consumption function, this will be noted. No attempt is made in the following discussion to provide a detailed explanation of the transition from the theory to the econometric specifications. Some of this was provided in Section II, particularly with respect to the use of the interest rate and exchange rate reaction functions. Detailed explanation of a number of the other equations is presented in Fair (1976), where the transition from the single-country theoretical model in Fair (1974) to the econometric model of the U.S. is discussed. As with most macroeconometric work, these transitions are not as tight as one would like, but there may be little that can be done about this given the nature of the data.

The asset variable, A_{it}^* , is an important explanatory variable in a number of the equations. One should, however, be aware of the limitations of this variable. As noted earlier, this variable measures only the net asset position of the country vis-a-vis the rest of the world. It does not include the domestic wealth of the country. Also, the value of the asset variable for each country is off by a constant amount, and this required a choice for the functional form of the variable in the equations that one might not have chosen otherwise.

Equation 1: The demand for imports

Equation 1 explains the real per capita merchandise imports of country i . The explanatory variables include the price of domestic goods, the price of imports, the interest rates, per capita income, and the lagged

value of real per capita assets. For the main countries these variables were generally found to be significant. The two price variables are expected to have coefficients of opposite signs and of roughly the same size in absolute value, and this was generally found to be the case.

Equation 2: Consumption

Equation 2 explains real per capita consumption. The explanatory variables include the interest rates, real per capita income, and the lagged value of real per capita assets. These variables were generally found to be significant. The use of income in this equation is inconsistent with the treatment of a household's decision problem in the theoretical model outlined in Section II. If a household is choosing consumption and labor supply to maximize utility, then income is not the appropriate variable to put on the right hand side of the consumption equation. This procedure can be justified if households are always constrained in their labor supply decision, and this is what must be assumed here. This issue is treated consistently in the U.S. model, where income is not used as an explanatory variable in the consumption equations. (See Chapter 4 in Fair (1976).)

The interest rate variables in the import and consumption equations are nominal rates. I added various proxies of expected future rates of inflation to the equations (in addition to the nominal interest rate) to see if their coefficient estimates had the expected positive sign. The proxies consisted of various weighted averages of current and past inflation rates. I also tried subtracting each proxy from the nominal rate and then adding this "real" rate to the equation. The results were not very good, which may be due to the difficulty of measuring expected future inflation rates. In future work more attempts of this kind should be made, but for the present purposes the nominal rates have been used.

Equation 3: Investment

Equation 3 explains the change in gross investment. It is based on the following three equations:

$$(31) \quad I_{it}^{n*} = \alpha_1 \Delta Y_{it} + \alpha_2 \Delta Y_{it-1} + \alpha_3 \Delta Y_{it-2} + \alpha_4 \Delta Y_{it-3} ,$$

$$(32) \quad I_{it}^* = I_{it}^{n*} + DEP_{it} ,$$

$$(33) \quad \Delta I_{it} = \lambda (I_{it}^* - I_{it-1}) , \quad 0 < \lambda \leq 1 .$$

Combining the three equations yields:

$$(34) \quad \Delta I_{it} = \lambda \alpha_1 \Delta Y_{it} + \lambda \alpha_2 \Delta Y_{it-1} + \lambda \alpha_3 \Delta Y_{it-2} + \lambda \alpha_4 \Delta Y_{it-3} - \lambda I_{it-1} + \lambda DEP_{it} .$$

Equation (31) states that desired net investment (I_{it}^{n*}) is a function of past changes in output. The past output variables are taken to be proxies for expected future output. Desired gross investment (I_{it}^*) in equation (32) is equal to desired net investment plus depreciation (DEP_{it}). Equation (33) states that actual gross investment partially adjusts to desired gross investment each period. Data on DEP_{it} are not available, and for the empirical work DEP_{it} was approximated by a constant and linear time trend: $DEP_{it} = \beta_0 + \beta_1 t$. The investment equation thus consists of a regression of the change in gross investment on current and past changes in output, lagged gross investment, a constant, and time. One would expect the output coefficients to be positive, the coefficient for lagged gross investment to be negative, and the coefficient for time to be positive. This is generally the case in Table 4. In many cases not all of the output coefficient estimates are significant, which is not surprising given the likely collinearity among the output variables.

The investment equation estimated here is similar to the investment equation estimated in the U.S. model, with two important exceptions. For the U.S. model a capital stock series and an "excess" capital series were constructed. Desired net investment was assumed to be a function of the amount of excess capital on hand as well as of the output changes. Also, depreciation was assumed to be proportional to the capital stock. This introduces two new explanatory variables into the estimated equation --the amount of excess capital on hand and the measure of depreciation --and subtracts one variable--time. (See Chapter 5 in Fair (1976) for further discussion.)

Equation 4: Production

Equation 4 explains the level of production. It is based on the following three equations:

$$(35) \quad V_t^* = \beta S_t ,$$

$$(36) \quad Y_t^* \equiv S_t + \alpha(V_t^* - V_{t-1}) ,$$

$$(37) \quad Y_t - Y_{t-1} = \lambda(Y_t^* - Y_{t-1}) .$$

Combining the three equations yields:

$$(38) \quad Y_t = \lambda(1 + \alpha\beta)S_t - \lambda\alpha V_{t-1} + (1-\lambda)Y_{t-1} .$$

Equation (35) states that the desired level of inventories is proportional to current sales. Equation (36) states that the desired level of production is equal to sales plus some fraction of the difference between the desired level of inventories and the level on hand at the end of the previous period. Equation (37) states that actual production partially adjusts

to desired production each period. The implied values of λ , α , and β are presented in Table 4 along with the actual coefficient estimates. The values of λ are less than one, and it is generally the case that λ is greater than α for a given country. In a few cases the original estimates implied a negative value of α , and in these cases V_{it-1} was dropped as an explanatory variable. First order serial correlation of the error term is quite pronounced in most of the equations.

Equation 5: The GNP deflator

Equation 5 explains the GNP deflator. It is the key price equation in the model for each country. The explanatory variables include the price of imports, interest rates, and a demand pressure variable, \tilde{Y}_{it}/POP_{it} . It is clear from the results that import prices have an important effect on domestic prices for most countries. The estimated coefficient of the demand pressure variable is also significant for a number of countries, and at least some slight effect of interest rates on prices has been estimated for some countries.

The demand pressure variable was constructed as follows.

$\log(Y_{it}/POP_{it})$ was first regressed on a constant, time, and three seasonal dummy variables, and the estimated standard error, \hat{SE} , and the fitted values, $\log(\hat{Y}_{it}/POP_{it})$, from this regression were recorded. (The results from these regressions are presented last in Table 4.) A new series, Y'_{it}/POP_{it} , was then constructed, where

$$(39) \quad Y'_{it}/POP_{it} = \exp[\log(\hat{Y}_{it}/POP_{it}) + 4 \cdot \hat{SE}] .$$

\tilde{Y}_{it}/POP_{it} was taken to be:

$$(40) \quad \tilde{Y}_{it}/POP_{it} = \frac{Y_{it}/POP_{it}}{\hat{Y}_{it}/POP_{it}} - 1 .$$

The demand pressure variable in equation (40) is equal to zero when the actual value of $\log(Y_{it}/POP_{it})$ is 4 standard errors greater than the value predicted by the above mentioned regression and is less than zero otherwise.⁸ Given that the log of the demand pressure variable is used in the price equation, and assuming that this variable has the expected positive coefficient estimate, this treatment means that as the actual value of real per capita output approaches \hat{Y}_{it}/POP_{it} , the predicted price level approaches plus infinity. Given the other equations in the model, this would never be a solution of the overall model, and so this treatment bounds the output of the country from above. This is a way with limited data of putting supply constraints into the model.

There are a number of theoretical arguments that can be made for the inclusion of import prices in the domestic price equation, and given the seeming empirical significance of import prices on domestic prices, some of these should perhaps be mentioned here. In this discussion of the U.S. model in Fair (1976), it is argued that import prices may affect a firm's expectations of other firms' pricing behavior, which may in turn affect its own price decision. This "expectational" justification is consistent with the profit maximizing model of firm behavior in Fair (1974). On a more practical level, if some wages and prices in a country are indexed and if the index in part includes import prices, then import prices

⁸This is assuming that the actual value of $\log(Y_{it}/POP_{it})$ is never more than 4 standard errors greater than the value predicted by the regression. For no country was the actual value greater than 4 standard errors from the predicted value in any quarter.

may directly or indirectly (through a wage effect on prices) affect domestic prices.

Another implication of the profit maximizing model in Fair (1974) is that interest rates should have a positive effect on prices. This, as noted above, was found to be true for some countries. This was also found to be true for the U.S.

Equation 6: The demand for money

Equation 6 explains the per capita demand for money. Both the interest rate and the income variables are generally significant in this equation. For all countries except Austria and the Philippines the estimated coefficient of the interest rate was of the expected negative sign.

Equations 7a and 7b: The interest rate reaction functions

The candidates for inclusion as explanatory variables in the interest rate reaction functions are variables that one believes may affect the monetary authority's decision regarding short term interest rates. In addition, the U.S. interest rate may be an important explanatory variable in the equations estimated over the fixed exchange rate period if bonds are close substitutes. The variables that were tried include the lagged rate of inflation, the lagged rate of growth of the money supply, the demand pressure variable, the change in assets, the lagged rate of change of import prices, the exchange rate (equation 7b only), and the German interest rate. The form of the asset variable that was tried is $A_{it}^* / (PY_{it} POP_{it})$. Except for division by $PY_{it} POP_{it}$, the change in this variable is the balance of payments on current account. For some countries, depending on the initial results, the current and one period lagged values were entered separately. It may be that the monetary

authorities respond in part to the level of assets and in part to the change, and entering the current and lagged values separately will pick this up.

Although equations 7a and 7b are estimated over fairly small numbers of observations because of the breaking up of the sample periods, a number of significant coefficient estimates were obtained. The estimates vary considerably across countries, but in general it does seem that monetary authorities in other countries "lean against the wind." This conclusion is consistent with the results for the U.S., where the Fed is also estimated to lean against the wind. (See Fair (1978).) The U.S. rate, as expected, is a more important explanatory variable in the fixed exchange rate period than it is in the flexible rate period.

Equation 8: The long term interest rate

Equation 8 is a standard term structure equation. The current and lagged short term interest rates and the rate of inflation term are meant to be proxies for expected future short term interest rates. Many of the current and lagged short term rates are significant. The rate of inflation term is in general not very important.

Equation 9b: The exchange rate reaction function

Equation 9b explains the spot exchange rate. Candidates for inclusion as explanatory variables in this equation are variables that one believes affect the monetary authority's decision regarding the exchange rate. If, as mentioned in Section II, a monetary authority takes into account market forces in choosing its exchange rate target, then variables measuring these forces should be included in this equation. The variables that were tried include the price level of country i relative to the

U.S. price level, the short term interest rate of country i relative to the U.S. rate, the demand pressure variable of country i relative to the demand pressure variable in the U.S. model (ZJ_{1t}^u) , the one-quarter lagged value of the change in real per capita net foreign assets of country i relative to the change in the same variable for the U.S., and the German exchange rate.

As was the case for the interest rate reaction functions, the results vary considerably across countries, but in general significant effects of these variables appear to be found. (Remember that these estimates, like the estimates for the interest rate reaction functions, are based on a relative small number of observations.) The German exchange rate has an important positive effect on the exchange rates of the other European countries. The signs of the effects of the other variables, when they are operating, are (all changes are relative to the U.S.): an increase in a country's price level or demand pressure variable has a positive effect on its exchange rate (a depreciation), and an increase in a country's short term interest rate or change in assets has a negative effect (an appreciation). The change in asset variable, $\Delta(A_{it-1}^*/(PY_{it-1} POP_{it-1}))$, is the per capita balance of payments of the country in 1975 local currency. When subtracting from this variable the similar variable for the U.S., the U.S. variable must be multiplied by the 1975 exchange rate (e_{i75}) to make the units comparable.

Equation 10b: The forward rate

Equation 10b is the estimated arbitrage condition. Although this equation plays no role in the model, it is of interest to see how close the quarterly data match the arbitrage condition. If the condition were

met exactly, the coefficient estimates of $\log ee_{it}$ and $\frac{1}{4} \log \frac{(1+r_{it}/100)}{(1+r_{1t}/100)}$ would be 1.0 and the fit would be perfect. As can be seen, the results do indicate that the data are consistent with the arbitrage condition, especially considering the poor quality of some of the interest rate data.

Equation 11: The export price index

Equation 11 provides a link from the GNP deflator to the export price index. Export prices are needed when the countries are linked together (see Table 3). If a country produced only one good, then the export price would be the domestic price and only one price equation would be needed. In practice, of course, a country produces many goods, only some of which are exported. If a country is a price taker with respect to its exports, then its export prices would just be the world prices of the export goods. To try to capture the in between case where a country has some affect on its export prices, but not complete control over every price, the export price index was regressed on the GNP deflator and a world price index.

The world price index ($PW\$_{it}$) is defined in Table 1. It is a weighted average of the export prices (in dollars) of the individual countries. Type B countries and oil exporting countries (countries 26 through 35) are excluded from the calculations. The weight for each country is the ratio of its total exports to the total exports of all the countries. The world price index differs for different countries because the individual country is excluded from the calculations for itself.

Since the world price index is in dollars, it needs to be multiplied by the exchange rate to convert it into local currency before being used as an explanatory variable in the export price equation for a given country. (The export price index explained by equation 11 is in local currency.)

For some countries, depending on the initial results, this was done, but for others the world price index in dollars and the exchange rate were entered separately. The results in Table 4 show, as expected, that export prices are in part linked to domestic prices and in part to world prices.

It should be stressed that equation 11 is meant only as a rough approximation. If more disaggregated data were available, one would want to estimate separate price equations for each good, where some goods' prices would be strongly influenced by world prices and some would not. This type of disaggregation is beyond the scope of this study.

As noted above, equation 11 is used to link the export price index to the GNP deflator. The world price index is added to the equation to try to lessen the bias of the coefficient estimate of the GNP deflator. The world price index is not meant to be an endogenous variable. Although it is measured as a weighted average of the export price indices of the individual countries, which are endogenous, its use in equation 11 is merely as a control variable. The export price index of one country is indirectly affected by the export prices of other countries through the effect of import prices on the GNP deflator in equation 5 and the effect of the GNP deflator on the export price index in equation 11. It would be (in a loose sense) double counting to have the export price index of a country also be affected by the export prices of other countries through their effect on the world price index. Again, this treatment, which at best provides only a rough approximation to the truth, is dictated by the use of the aggregated data.

Summary

This completes the discussion of the estimated equations. Given the poor quality of much of the data, especially for the non industrial countries, the results do not seem too bad. The least precise estimates in terms of t-statistics are those for the interest rate and exchange rate reaction functions, which are based on relatively few observations. Even for these equations, however, the results do not seem unreasonable. In particular, it is encouraging that a number of explanatory variables were found to be significant (by conventional standards) in the exchange rate equations aside from the lagged dependent variable and the German exchange rate.

IV. The Predictive Accuracy of the Model

The evaluation of macroeconometric models is a difficult problem. Any model is likely to be only an approximation to the true structure of the economy, and one would like to choose that model that provides the best approximation. The problem is deciding what one means by best approximation. It is difficult to compare the fit of one model to the fit of another because models differ in the number and types of variables that are taken to be exogenous. Also, there is a serious danger of data mining with macro time series data, and it is not easy to control for this. A model may be poorly specified (i.e., a bad approximation to the true structure) but fit the data well because of data mining.

I have recently proposed a method (Fair (1980a)) that I think can be used in the long run to compare alternative models. The method provides estimates of forecast error variances that take into account the four main sources of uncertainty: uncertainty due to the error terms,

the coefficient estimates, the exogenous-variable forecasts, and the possible misspecification of the model. It puts each model on an equal footing and so allows comparisons to be made across models. The method is unfortunately expensive to use, since it is based on successive re-estimation and stochastic simulation of the model, and it is beyond the computer budget for this project to apply it to the model.

Because this method has not been used, this paper provides no rigorous comparison of the present model to other models. What was done instead is the following. Three eight-quarter prediction periods were chosen: a fixed exchange rate period, 1970I-1971IV, and two flexible rate periods, 1974I-1975IV and 1976I-1977IV. For each of these periods both static and dynamic predictions were generated using the actual values of the exogenous variables.⁹ Root mean squared errors (RMSEs) were computed for each endogenous variable for each run. The same procedure was followed for what will be called the "autoregressive" model. For the autoregressive model each of the variables on the left hand side of a stochastic equation in the regular model is regressed on a constant, time, three seasonal dummy variables, and the first four lagged values of the left hand side variable. The autoregressive model consists of a set of completely unrelated equations. The predictions and errors in one equation have no effect on any of the other equations. The same estimation periods were used for this model as were used for the regular model. The variables

⁹The model was solved using the Fair-Parke (1981) program, which uses the Gauss-Seidel technique. Iteration occurs for a given quarter both within the countries (the Table 2 part of the model) and among countries (the Table 3 calculations). Convergence was generally quite rapid, requiring between about 3 and 7 Table 3 calculations per quarter. The approximate time on the IBM 370-158 at Yale for one eight-quarter simulation of the complete model (including the U.S. model) was 3.5 minutes.

explained by definitions in the regular model are not part of the autoregressive model.

The results are presented in Tables 5, 6, and 7. For the results in Table 5 a weighted average of the RMSEs across all countries except the U.S. was taken for each variable. The RMSEs were weighted by the ratio of the country's real GNP (in 75\$) in the last (i.e., eighth) quarter of the prediction period to the total real GNP of all the countries. This provides a summary measure of the overall fit of the model with respect to each variable. The RMSEs of the individual countries are presented in Table 6 for one run, the dynamic simulation for the period 1974I-1975IV. This is the period of the large increase in the price of oil by OPEC and is not a particularly easy period to explain. The RMSEs for the U.S. are presented in Table 7.

Each number in parentheses in Tables 5 and 6 is the ratio of the RMSE to the corresponding RMSE for the autoregressive model. Two of the variables in the tables, PM and X75\$, are explained by definitions in the regular model, and so no RMSEs from the autoregressive model are available for these. Each number in parentheses in Table 7 is the ratio of the RMSE to the corresponding RMSE when the rest of the world is taken to be exogenous from the point of view of the U.S.

The following general conclusions can be drawn from Table 5. (1) The model is the same as or less accurate than the autoregressive model for GNP and its two major components, consumption and investment. It is the same as or more accurate than the autoregressive model for the GNP deflator, the two interest rates, the exchange rate, imports, and the price of exports. The two models are about the same for the money supply. (2) The best period for the accuracy of the model relative to that for

TABLE 5. Weighted RMSEs for All Countries Except the U.S.

STA = Static simulation.
 DYN = Dynamic simulation.

Eq. No. in Tables 4 or 5	Variable	701-714		741-754		761-774	
		STA	DYN	STA	DYN	STA	DYN
4	Real GNP	1.95(1.38)	4.32(2.17)	2.10(1.17)	3.29(1.03)	1.90(1.46)	3.71(1.92)
5	GNP Deflator	0.81(0.98)	2.53(1.13)	1.19(0.84)	2.28(0.49)	0.98(1.00)	2.60(1.03)
7a, 7b	Interest Rate	0.56(0.87)	0.91(1.04)	0.75(0.87)	1.14(0.91)	0.88(0.95)	1.80(0.93)
9b	Exchange Rate	a	a	3.80(0.99)	5.26(0.98)	2.56(0.96)	4.32(0.71)
V	Import Price	0.66	1.66	2.97	4.42	2.17	3.85
6	Money Supply	2.99(1.05)	6.60(1.18)	2.85(0.96)	3.87(0.86)	2.55(1.08)	3.83(1.19)
1	Imports	4.70(0.97)	9.43(1.33)	4.79(0.79)	6.44(0.58)	4.30(0.88)	6.56(0.97)
2	Consumption	1.85(1.14)	3.77(1.45)	2.32(1.07)	3.28(0.81)	1.92(1.28)	3.95(1.70)
3	Investment	4.07(1.45)	10.28(1.98)	4.21(1.16)	7.67(1.07)	3.41(1.23)	7.79(1.52)
8	Interest Rate	0.27(0.92)	0.49(1.04)	0.43(0.84)	0.74(0.66)	0.41(0.98)	0.90(0.90)
11	Export Price	1.81(0.83)	3.87(0.63)	3.71(1.03)	5.14(0.51)	2.66(1.09)	4.34(0.70)
II	Exports	1.97	5.21	2.18	3.00	1.50	2.65

Notes: 1. Each number in parentheses is the ratio of the RMSE to the corresponding RMSE for the autoregressive model.

2. All errors are in percentage points.

3. Weights are GNP in 75\$ in the last quarter of the period.

a = fixed exchange rate period for almost all countries.

TABLE 6. RMSEs for the Individual Countries: Dynamic Simulation, 741-754

Country	Real GNP Y	GNP Deflator FY	Interest Rate I	Exchange Rate e	Import Price PM	Money Supply M1*	Imports M	Consumption C	Investment I	Interest Rate R	Export Price PX	Exports X75\$
Canada	0.8(0.56)	2.0(0.67)	0.7(0.72)	2.0(1.07)	3.4	3.1(0.98)	3.7(0.80)	0.9(0.59)	3.0(1.08)	0.5(0.69)	6.2(0.87)	7.9
Japan	3.6(0.78)	0.7(0.27)	0.5(0.96)	3.2(1.04)	2.6	2.4(1.05)	4.0(0.21)	2.8(0.32)	7.5(0.74)	--	4.1(0.34)	2.7
Austria	3.3(1.16)	2.5(0.58)	1.6(1.91)	5.7(0.96)	2.5	3.9(1.42)	4.3(0.52)	3.1(1.84)	8.2(1.55)	--	2.9(0.33)	1.7
Belgium	1.5(0.54)	2.3(0.34)	1.2(0.62)	5.1(0.94)	2.8	2.5(0.93)	2.6(0.23)	1.6(0.66)	6.0(1.29)	0.3(0.56)	4.2(0.43)	2.1
Denmark	1.8(0.32)	1.3(0.33)	1.4(0.30)	4.5(0.85)	3.8	5.3(0.77)	5.5(0.42)	4.3(0.71)	7.4(0.56)	1.4(0.81)	3.5(0.44)	3.3
France	1.3(0.72)	1.0(0.26)	1.4(0.98)	8.0(1.07)	7.0	3.7(0.94)	4.3(0.46)	1.4(1.00)	3.1(1.03)	0.7(0.59)	2.9(0.29)	1.8
Germany	1.6(0.57)	0.7(0.26)	1.7(1.34)	4.6(0.91)	3.5	1.8(0.52)	3.3(0.51)	1.5(3.57)	6.3(0.59)	0.5(0.47)	4.9(0.55)	2.7
Italy	2.5(1.16)	2.0(0.18)	1.9(0.47)	6.4(0.82)	4.1	2.1(0.19)	5.6(0.36)	1.2(0.34)	9.4(2.77)	0.5(0.28)	4.8(0.41)	1.9
Netherlands	0.9(0.39)	1.0(0.31)	1.4(0.68)	5.2(0.92)	3.1	3.2(0.70)	4.0(0.48)	2.5(1.09)	5.3(0.61)	0.7(0.64)	4.1(0.39)	1.8
Norway	1.9(0.95)	1.3(0.45)	2.0(0.99)	6.0(1.14)	1.6	6.4(1.23)	5.6(1.21)	2.1(0.96)	--	0.3(0.73)	2.1(0.21)	3.1
Sweden	3.9(1.60)	1.8(0.52)	2.0(2.45)	5.5(0.91)	3.4	7.7(2.15)	6.2(1.19)	2.8(0.92)	4.5(1.38)	0.5(1.71)	6.0(0.68)	3.1
Switzerland	5.5(0.83)	3.4(1.82)	1.4(1.36)	12.9(2.11)	8.1	4.0(0.53)	7.7(0.46)	3.9(0.64)	14.3(0.80)	0.8(1.27)	3.7(0.56)	2.4
U.K.	2.7(1.16)	5.4(0.63)	0.5(0.74)	5.5(1.09)	7.8	6.1(1.62)	6.5(1.34)	2.9(0.89)	5.4(1.34)	2.0(0.83)	5.6(0.60)	3.0
Finland	8.4(3.96)	6.9(0.82)	0.1(0.34)	3.3(0.72)	5.9	16.5(1.60)	18.1(1.88)	7.9(3.28)	17.0(2.13)	--	13.1(0.71)	3.0
Greece	4.5(0.58)	4.2(0.88)	3.3(1.56)	--	3.9	9.9(2.32)	8.1(0.58)	--	27.7(0.93)	--	4.7(0.43)	2.0
Ireland	5.4(2.27)	4.7(0.92)	1.0(1.11)	4.3(0.79)	5.1	3.5(0.51)	11.0(0.69)	5.3(0.97)	10.3(0.66)	1.9(0.79)	2.2(0.43)	5.1
Portugal	8.9(1.25)	2.5(0.44)	0.7(0.59)	7.6(1.36)	5.3	4.5(1.46)	17.1(0.64)	4.6(0.92)	9.1(0.93)	0.1(0.07)	2.5(0.44)	3.4
Spain	5.8(1.84)	1.6(1.37)	0.2(0.65)	6.7(0.87)	4.3	5.9(2.22)	10.5(2.59)	3.7(1.19)	12.6(2.34)	--	5.4(0.60)	2.9
Yugoslavia	3.7(2.25)	9.3(1.90)	--	--	4.5	--	4.3(0.57)	3.4(0.99)	8.5(1.10)	--	5.9(0.77)	1.3
Australia	3.0(1.76)	6.6(1.02)	1.4(2.21)	8.2(3.63)	10.0	4.8(0.53)	12.1(1.28)	2.0(1.22)	5.7(3.37)	1.0(2.42)	3.7(0.69)	3.0
New Zealand	0.7(1.04)	4.1(0.82)	0.6(0.96)	9.6(3.05)	9.9	4.3(0.81)	11.2(0.69)	4.2(3.47)	11.8(0.77)	0.4(0.96)	20.7(1.76)	4.4
South Africa	5.8(1.81)	3.4(2.36)	1.6(2.14)	--	3.8	3.3(0.89)	7.5(0.51)	3.9(2.23)	14.5(1.38)	1.0(1.76)	2.4(0.32)	2.2
Iran	3.5(0.99)	--	0.6(1.25)	--	3.9	14.0(1.29)	10.5(0.56)	3.4(0.75)	--	--	--	2.5
Libya	5.5(0.60)	--	--	--	3.8	--	14.6(1.13)	11.2(1.17)	10.0(0.70)	--	--	3.9
Nigeria	7.8(0.81)	--	--	--	3.4	--	5.1(0.42)	10.2(0.68)	16.4(1.29)	--	--	4.6
Saudi Arabia	3.4(1.18)	--	--	--	3.7	--	7.6(1.89)	9.9(1.62)	--	--	--	3.2
Venezuela	3.5(2.83)	--	--	--	4.5	--	8.5(1.40)	13.0(0.99)	--	--	--	5.2
Argentina	8.8(2.03)	--	--	--	2.7	--	14.9(0.70)	8.2(2.39)	8.9(2.61)	--	--	2.5
Brazil	5.4(1.16)	2.4(1.26)	--	5.1(0.41)	2.2	--	14.6(1.08)	5.5(0.97)	10.6(2.04)	--	9.8(0.76)	2.8
Chile	8.1(0.54)	17.3(0.21)	--	--	3.1	--	24.8(0.27)	10.7(1.04)	11.8(0.67)	--	17.7(0.21)	4.4
Colombia	5.7(1.86)	2.2(1.09)	--	5.4(1.41)	8.8	5.5(0.50)	19.8(1.42)	3.1(0.95)	12.6(2.32)	--	9.2(0.72)	4.5
Mexico	2.3(1.08)	--	--	--	5.1	--	6.0(0.53)	5.5(1.03)	4.3(2.01)	--	--	7.4
Peru	10.8(3.38)	--	--	--	4.0	11.5(1.58)	25.4(1.04)	11.5(2.45)	37.0(1.97)	--	--	0.8
Egypt	2.7(0.46)	--	--	--	3.0	--	23.1(2.11)	7.1(1.98)	--	--	--	1.2
Israel	5.7(0.95)	6.5(0.65)	--	--	4.5	--	7.7(0.86)	5.0(1.16)	17.8(1.23)	--	6.1(0.88)	3.2
Jordan	9.0(0.79)	16.4(1.13)	--	--	3.6	--	7.4(0.33)	8.9(1.10)	--	--	36.7(1.17)	3.8
Syria	17.7(1.63)	6.9(0.46)	--	--	4.0	--	15.7(1.25)	29.5(1.91)	--	--	22.5(0.79)	0.8
India	6.9(2.84)	4.8(0.91)	--	3.4(0.97)	4.4	--	6.6(0.99)	6.9(0.89)	5.9(1.04)	0.0(0.18)	4.0(0.49)	2.4
Korea	15.3(3.37)	4.4(0.51)	1.1(1.02)	--	2.7	4.6(0.58)	15.6(0.90)	13.1(2.83)	28.2(1.97)	--	9.0(1.20)	4.5
Malaysia	2.1(1.48)	4.2(0.88)	--	--	3.0	--	6.0(0.50)	4.8(0.73)	13.7(1.18)	--	11.9(1.35)	2.8
Pakistan	2.4(1.21)	2.0(0.69)	1.0(1.27)	--	2.6	--	5.7(1.13)	--	11.1(1.23)	--	13.8(2.24)	1.9
Philippines	7.4(1.54)	4.0(0.72)	2.7(1.20)	--	3.1	2.1(0.45)	8.3(1.38)	6.0(1.04)	24.6(1.45)	--	19.8(0.93)	4.8
Thailand	3.4(0.74)	3.6(1.22)	0.7(1.10)	--	3.0	2.3(0.45)	6.0(0.34)	3.1(0.88)	--	--	9.6(1.13)	2.3
Weighted	3.3(1.03)	2.3(0.49)	1.1(0.91)	5.3(0.98)	4.4	3.9(0.86)	6.4(0.58)	3.3(0.81)	7.7(1.07)	0.7(0.66)	5.1(0.51)	3.0

Notes: 1. Each number in parentheses is the ratio of the RMSE to the corresponding RMSE for the autoregressive model.
2. All errors are in percentage points.

TABLE 7. RMSEs for the U.S.

STA = Static simulation.
DYN = Dynamic simulation.

Variable	701-714		741-754		761-774	
	STA	DYN	STA	DYN	STA	DYN
Real GNP	0.50(1.05)	0.25(0.76)	0.81(1.04)	2.31(1.07)	0.74(1.05)	1.32(1.02)
GNP Deflator	0.27(0.98)	0.32(0.53)	0.33(1.06)	1.23(2.31)	0.37(1.08)	0.80(1.20)
Interest Rate	0.54(1.01)	0.84(0.98)	0.57(1.02)	0.83(1.10)	0.25(1.00)	0.31(1.00)
Import Price	0.65	2.06	1.28	3.53	0.61	0.95
Money Supply	1.15(1.00)	3.37(0.99)	1.02(1.00)	0.83(0.96)	0.66(1.00)	1.07(1.02)
Imports	2.48(1.02)	4.44(1.13)	4.40(0.99)	8.06(1.08)	2.32(1.01)	4.48(1.05)
Interest Rate	0.28(1.01)	0.37(1.01)	0.28(1.02)	0.33(1.12)	0.12(1.01)	0.31(1.01)
Export Price	1.03(1.00)	1.87(1.18)	1.97(1.03)	6.01(1.14)	1.15(1.03)	2.32(1.07)
Exports	1.14	1.87	1.68	2.64	1.33	2.20

Notes: 1. Each number in parentheses is the ratio of the RMSE to the corresponding RMSE when the rest of the world is taken to be exogenous.

2. All errors are in percentage points.

the autoregressive model is 1974I-1975IV. (3) In going from a static simulation to a dynamic simulation, the accuracy of the model improves relative to that for the autoregressive model for the 1974I-1975IV period. The relative accuracy worsens for the 1970I-1971IV period. It is about the same for the 1976I-1977IV period.

The RMSEs in Table 6 give a general idea of how well the model explains the individual countries. The RMSEs are generally larger for the smaller countries, which is as expected given, among other things, the poor quality of much of the data for the smaller countries.

The main conclusion to be drawn from the results for the U.S. in Table 7 is that the fit of the U.S. model is not very sensitive to whether or not the U.S. model is included in the overall model, i.e., to whether or not the rest of the world is taken to be exogenous in the U.S. model. Note also that the U.S. RMSEs for a given variable are generally much smaller than the corresponding RMSEs for the other countries in Table 5.¹⁰

Although the results in this section give one a general idea of the accuracy of the model, they do not, as mentioned above, provide a test of the model. It is unclear how the model would compare to the autoregressive model if the method in Fair (1980a) were used. This method takes into account exogenous variable uncertainty, whereas the procedure followed in this section does not, which biases the current results against the autoregressive model. The autoregressive model has no non trivial exogenous variables. The important exogenous variables in the regular model are the government spending variable (G_{it}) and the price of exports of the oil exporting countries. On the other hand, the

¹⁰The U.S. model is compared to an autoregressive model in Fair (1980a), and so no comparisons of this kind are presented here.

autoregressive model may be more misspecified than the regular model, which would bias the current results, which are all within sample, against the regular model. The method has been used to compare the U.S. model and an autoregressive model (Fair (1980a)), and the results in general indicate that the autoregressive model is more misspecified. In future work it will be of interest to use the method to compare the present model not only to the autoregressive model but also to other structural models.

V. The Properties of the Model

A useful way of examining the properties of the model is to consider the effects of changing government policy variables. The results of one experiment are reported in this section: an increase in the purchase of U.S. goods by the U.S. government. This experiment was performed in both a fixed exchange rate period (1970I-1971IV) and a flexible rate period (1976I-1977IV). The results of other experiments are reported in a sequel to this paper, Fair (1981). This paper provides much more discussion of the properties of the model than space limitations allow in this section.

Before discussing the results of the experiment, it will be useful to explain some of the ceteris paribus effects in the model. In what follows a variable is said to have a "direct" effect on another variable if it appears on the right hand side of the equation (either a stochastic equation or a definition) explaining the other variable. Most endogenous variables have at least an indirect effect on the other endogenous variables--either contemporaneously or with a lag of one quarter. Because of this, it is difficult to explain the properties of the model in a

systematic way. The following discussion is designed to try to give a general idea of the properties of the model without going into every possible indirect effect. The experiment, of course, takes all effects into account, and so the experimental results provide a check on the less rigorous discussion of the properties.

It should also be kept in mind in the following discussion that not all of the effects operate for all countries. To conserve space, no distinction is made across countries. Each effect is discussed as if it applied to all countries. All interest rates referred to in the discussion are short term interest rates unless otherwise noted.

Trade Effects Among Countries

There is a standard trade multiplier effect in the model. An autonomous increase in GNP in country i increases its demand for imports, which increases the exports of other countries and thus their GNP and demand for imports, which then increases the exports of country i and thus its GNP. In short, exports affect imports and vice versa.

Price Effects Among Countries

There is also a price multiplier effect in the model. An autonomous increase in country i 's domestic price level increases its export prices, which increases the import prices of other countries, which increases their domestic prices, including their export prices, which then increases country i 's import prices and thus its domestic and export prices. In short, export prices affect import prices and vice versa.

Direct Interest Rate Effects Among Countries

The U.S. short term interest rate appears as an explanatory variable in the interest rate reaction functions of a number of countries. The U.S. rate is more important in the fixed exchange rate period than it is in the flexible rate period, but even in the flexible rate period it has an effect on some countries. This means that an increase in the U.S. interest rate directly increases other countries' rates. The German interest rate appears as an explanatory variable in the interest rate reaction functions of a few other European countries, and so an increase in the German interest rate also directly increases other countries' rates.

Direct Exchange Rate Effects Among Countries

The German exchange rate appears as an explanatory variable in the exchange rate equations of the other European countries. The German exchange rate thus directly affects other exchange rates. All exchange rates are relative to the U.S. dollar, and so each explanatory variable in the exchange rate equations (other than the lagged dependent variable and the German exchange rate) is the particular variable of the country relative to the same variable for the U.S. This means that the following U.S. variables appear as explanatory variables in the exchange rate equations: the GNP deflator, the short term interest rate, the demand pressure variable, and the change in net foreign assets.

Direct Effects Within a Country

The short term interest rate directly affects the long term rate (equation 8). The short term rate or the long term rate has a direct negative effect on imports and consumption (equations 1 and 2) and a direct positive effect on the GNP deflator (equation 5). The short term

rate has a direct negative effect on the demand for money and the exchange rate (equations 6 and 9b). (Remember that an increase in the exchange rate is a depreciation of the country's currency.)

The asset variable, which is a measure of the net asset position of the country vis-a-vis the rest of the world, has a direct positive effect on imports and consumption (equations 1 and 2) and a direct negative effect on the short term interest rate and the exchange rate (equations 7a, 7b, and 9b).

The exchange rate has a direct positive effect on the price of imports and the price of exports, both of which are in units of the local currency (equations V and 11). It also has a direct negative effect on the price of exports in dollars (because the coefficient estimate of the log of the exchange rate in equation 11 is less than 1). It has a direct positive effect on the short term interest rate for three countries (equation 7b).

The price of imports has a direct negative effect on imports (equation 1), a direct positive effect on the GNP deflator (equation 5), a direct negative effect on the asset variable (equations 17 and 18), and a direct positive effect on the short term interest rate for four countries (equation 7b). The price of exports has a direct positive effect on the asset variable (equations 17 and 18). The GNP deflator has direct positive effects on imports, the demand for money, the short term and long term interest rates, the exchange rate, and the price of exports (equations 1, 6, 7a, 7b, 8, 9b, and 11).

The level of imports has a direct negative effect on final sales and the asset variable, and the level of exports has a direct positive effect on these two variables (equations 16, 17, and 18). The level of

final sales has a direct positive effect on GNP (equation 4). Any deviation of GNP from final sales in a period is absorbed by a change in inventories (equation 12). The stock of inventories has a direct negative effect on production (equation 4).

GNP or the demand pressure variable (which is a nonlinear function of GNP) has a direct positive effect on imports, consumption, investment, the GNP deflator, the demand for money, the short term interest rate, and the exchange rate.

Some Indirect Effects Within a Country

It should be clear that there are very few unambiguous indirect effects in the model with respect to sign. The signs depend on the relative sizes of the coefficient estimates. It will nevertheless be useful to consider the likely signs of some indirect effects, even though these signs are not necessarily logical consequences of the model.

Consider first the indirect effect of the exchange rate on GNP. The main direct effect of the exchange rate is on the price of imports, at least in the short run. The price of imports has a direct negative effect on imports, and the level of imports has a direct positive effect on GNP. In other words, an increase in the price of imports causes substitution from imports to domestically produced goods, which raises GNP. The exchange rate thus has an indirect positive effect on GNP through this channel (i.e., depreciation increases GNP).

Depreciation also lowers the dollar price of exports, which lowers the import price indices of countries that import from the given country, which in turn increases the demand for the given country's exports. Therefore, depreciation also increases GNP through this channel.

Depreciation is likely to have a negative indirect effect on GNP through a third channel. The likely initial effect of a depreciation on the balance of payments is negative. Depreciation raises the local currency price of imports more than it does the local currency price of exports, which, other things being equal, has a negative effect on the balance of payments. Depreciation also lowers imports and raises exports, which has a positive effect on the balance of payments. This latter effect is, however, likely to be smaller initially than the price effect, and so the initial net effect is likely to be negative. (This is, of course, the "J curve" effect.) A decrease in the balance of payments decreases net foreign assets, which directly decreases imports and consumption and directly increases the short term interest rate. Although the decrease in imports raises GNP, the decrease in consumption and the increase in the interest rate lower GNP, and the net effect is likely to be negative. Depreciation is thus likely to have an initial indirect negative effect on GNP through this "asset" effect channel.

Depreciation has two main indirect effects on the GNP deflator, one positive and one ambiguous. The positive effect is through the price of imports, which has a direct positive effect on the GNP deflator. The second effect is through GNP. If the net effect of depreciation on GNP is positive, this will have a positive effect on the GNP deflator through the direct positive effect of the demand pressure variable on the GNP deflator. If the net effect of depreciation on GNP is negative, the indirect effect on the GNP deflator is negative.

There are three main effects of the short term interest rate on GNP, one negative, one ambiguous, and one positive. The negative effect is through consumption. An increase in the short term rate increases the

long term rate. An increase in the short term rate or the long term rate decreases consumption, which lowers GNP. The ambiguous effect is through the exchange rate. An increase in the short term rate has a negative effect on the exchange rate (an appreciation), which has an ambiguous effect on GNP. The positive effect is through imports. An increase in the short term or long term rate lowers imports, which, other things being equal, raises GNP. The consumption effect is likely to be the dominant one, and so the net effect of the short term rate on GNP is likely to be negative.

An increase in interest rates has three main effects on the GNP deflator, one positive and two negative. The positive effect is a direct one: interest rates appear as explanatory variables in the price equation (equation 5). The first negative effect is the negative indirect effect of interest rates on GNP and thus on the demand pressure variable. The other negative effect is the effect on the exchange rate: the exchange rate appreciates, which lowers the price of imports, which lowers the GNP deflator.

The Results of the Experiment

The effects of increasing U.S. government expenditures on some of the key variables in the model are presented in Tables 8 and 9 for the main countries. Each number in the tables is the percentage difference between the two- or six-quarter-ahead predicted value of the variable before and after the change divided by the percentage change in autonomous income. For these results the estimated residuals were added to the stochastic equations and treated as exogenous. This means that when the model is simulated using the actual values of the exogenous variables, a perfect tracking solution is obtained. The base path before the change

is thus the perfect tracking solution, and so the predicted values after the change are merely compared to the actual values.¹¹

Consider first the results in Table 8, which are for the fixed exchange rate period. The increase in U.S. government spending increased U.S. income, which in turn increased U.S. imports. This increased other countries' exports, which in turn increased their income and imports. This is the trade multiplier effect. The increase in U.S. income also led to an increase in the U.S. price level, which increased other countries' import prices. This led to an increase in other countries' export prices, which resulted in further increases in other countries' import prices. This is the price multiplier effect.

The other important effect in this case is the interest rate effect. The increase in U.S. income and prices led to an increase in the U.S. interest rate through the reaction function of the Federal Reserve. This offset some of the increase in U.S. income that would otherwise have occurred and also led to an increase in other countries' interest rates. The interest rates for all countries except Japan were higher after two quarters. This worldwide increase in interest rates offset some of the increase in world income that would otherwise have occurred. In the case of the Netherlands this effect was large enough to lead to a net negative effect on GNP in the second quarter.¹²

¹¹Each number in Tables 8 and 9 is thus $[(\hat{y}_{jt} - y_{jt})/y_{jt}]/[\Delta G_{1t}/Y_{1t}]$, where \hat{y}_{jt} is the two- or six-quarter-ahead predicted value of y_{jt} after the change. ΔG_{1t} is the change in U.S. government spending in quarter t , and Y_{1t} is the actual value of U.S. GNP in quarter t .

¹²Some multiplier results for other multicountry econometric models are presented in Tables 1 and 2 in Fair (1979b), and these provide a rough basis of comparison for the results from the present experiment (U.S. increase in a fixed exchange rate period). In general, the present income multipliers are smaller and the price multipliers are larger than those of the other models. This is, of course, as expected, since the other models are primarily trade multiplier models and so have weak or non-existent price multiplier and interest rate effects.

TABLE 8. Percentage Change in the Variable after Two and Six Quarters Induced by a Sustained One Percent Autonomous Increase in U.S. Real GNP

Country	Initial Change in 1970I (fixed exchange rate period).						Short Term Interest Rate						Money Supply						Imports						Consumption						Investment						Long Term Interest Rate						Export Price						Exports						Balance of Payments					
	Real GNP		GNP Deflator		Short Term Interest Rate		Import Price		Money Supply		Imports		Consumption		Investment		Long Term Interest Rate		Export Price		Exports		Balance of Payments																																					
	Y	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6																										
U.S.	1.25	1.32	0.20	0.11	0.49	0.76	0.03	0.15	0.01	-0.29	1.65	3.91	0.10	0.05	1.89	4.75	0.11	0.33	0.20	0.08	0.04	0.40	-134.751	6	0.04	0.40	0.20	0.08	0.04	0.40	0.04	0.40	-435.691																											
Canada	0.19	0.71	0.10	0.44	0.52	-0.39	0.15	0.04	-0.82	-0.55	0.20	1.28	-0.04	0.20	0.19	0.59	0.17	-0.04	0.09	0.40	1.32	3.34	49.767	6	0.65	1.78	-0.00	0.01	0.00	0.01	0.65	1.78	127.197																											
Japan	0.06	0.30	-0.00	0.01	-0.01	0.03	0.08	0.07	0.03	0.18	0.00	0.10	0.02	0.14	0.01	0.24	--	--	-0.00	0.01	0.65	1.78	9.155	6	0.09	0.13	0.00	0.02	0.00	0.02	0.09	0.13	0.047																											
Austria	0.03	0.16	0.00	0.05	0.17	0.04	0.01	0.06	0.01	0.07	-0.16	-0.78	-0.05	-0.23	0.03	0.18	0.07	0.13	0.00	0.01	0.09	0.39	0.047	6	0.09	0.13	0.00	0.01	0.00	0.01	0.09	0.39	0.629																											
Belgium	0.03	0.22	0.01	0.04	0.56	0.08	0.03	0.04	-0.23	-1.16	0.01	-0.06	-0.01	-0.04	0.02	0.18	0.07	0.13	0.00	0.01	0.09	0.39	0.047	6	0.09	0.13	0.00	0.01	0.00	0.01	0.09	0.39	0.014																											
Denmark	0.06	0.21	0.01	0.04	0.18	-0.11	0.02	0.05	-0.71	0.21	0.03	0.19	0.04	0.15	0.06	0.25	0.04	-0.01	0.00	0.00	0.09	0.33	0.014	6	0.09	0.13	0.00	0.01	0.00	0.00	0.09	0.33	0.014																											
France	0.02	0.08	0.00	0.01	0.33	-0.25	0.03	0.05	-0.11	-0.26	-0.01	-0.02	0.00	-0.00	0.03	0.12	0.08	0.02	0.00	0.00	0.09	0.33	0.014	6	0.09	0.13	0.00	0.01	0.00	0.00	0.09	0.33	0.014																											
Germany	0.05	0.21	0.01	0.18	0.38	-0.27	0.03	0.03	-0.54	0.24	-0.05	0.09	-0.02	-0.04	0.08	0.34	0.11	0.01	0.00	0.00	0.09	0.33	0.014	6	0.09	0.13	0.00	0.01	0.00	0.00	0.09	0.33	0.014																											
Italy	0.04	0.15	0.02	0.25	0.17	0.25	0.03	0.04	-0.07	-0.86	-0.02	-0.02	0.00	-0.00	0.03	0.12	0.04	0.14	0.00	0.00	0.09	0.33	0.014	6	0.09	0.13	0.00	0.01	0.00	0.00	0.09	0.33	0.014																											
Netherlands	-0.02	0.04	0.00	-0.02	0.50	-0.36	0.03	0.05	-1.02	0.59	-0.02	-0.02	-0.06	-0.10	-0.01	0.07	0.36	0.04	0.14	0.00	0.07	0.47	0.014	6	0.17	0.47	0.01	0.07	0.00	0.07	0.17	0.47	14.192																											
Norway	0.02	0.11	0.00	0.02	--	--	0.02	0.07	0.02	0.09	0.03	0.13	0.01	0.07	--	--	0.09	0.02	0.00	0.00	0.07	0.25	0.003	6	0.07	0.25	0.00	0.00	0.00	0.07	0.25	0.003	0.021																											
Sweden	0.05	0.17	0.03	0.17	0.23	-0.21	0.02	0.04	-0.07	0.11	-0.02	0.17	0.02	0.10	0.03	0.13	0.04	0.00	0.00	-0.00	0.14	0.57	0.001	6	0.14	0.57	0.00	-0.00	0.00	0.14	0.57	0.001	0.008																											
Switzerland	0.04	0.40	0.01	0.18	0.10	0.13	0.03	0.05	-0.10	-0.39	-0.04	0.18	-0.03	0.21	0.06	0.75	0.04	-0.01	0.01	0.08	0.13	0.48	0.010	6	0.13	0.48	0.00	0.01	0.00	0.13	0.48	0.010	0.036																											
U.K.	0.05	0.16	0.01	0.09	0.17	-0.13	0.04	0.07	-0.23	0.02	0.08	0.27	0.03	0.12	0.04	0.11	0.04	0.01	0.00	0.09	0.17	0.45	0.010	6	0.17	0.45	0.00	0.09	0.00	0.17	0.45	0.010	0.017																											
Finland	0.03	0.12	0.00	0.02	0.00	0.00	0.01	0.05	0.01	0.09	0.04	0.18	0.01	0.07	0.02	0.11	0.04	0.01	0.00	0.05	0.23	0.68	1.621	6	0.23	0.68	0.00	0.05	0.00	0.23	0.68	1.621	9.557																											
																							0.722	6									0.722	2.363																										

^a Change is absolute change, not percentage change, in units of local currency.

TABLE 9. Percentage Change in the Variable after Two and Six Quarters Induced by a Sustained One Percent Autonomous Increase in U.S. Real GNP

Initial Change in 1976I (flexible exchange rate period)

Real GNP Y	GNP Deflator PY		Short Term Interest Rate Y		Exchange Rate e		Import Price PM		Money Supply M1*		Imports M		Consumption C		Investment I		Long Term Interest Rate R		Export Price PX		Exports X75\$		Balance of Payments ^a BOP*				
	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6	2	6			
U.S.	1.43	1.39	0.17	0.54	0.36	0.89	--	--	0.05	0.55	-0.07	-0.33	1.68	2.95	0.31	-0.01	2.36	5.26	0.16	0.41	0.08	0.41	0.09	0.60	-452.807	-985.274	
Canada	0.18	0.55	0.05	0.56	0.22	0.60	-0.00	0.01	0.07	0.50	-0.16	-0.89	0.20	1.14	-0.00	0.04	0.15	0.44	0.07	0.27	0.04	0.51	1.32	2.67	114.732	182.173	
Japan	0.06	0.18	-0.02	-0.12	-0.04	-0.14	-0.80	-3.42	-0.74	-3.08	0.02	0.08	0.12	1.12	0.03	0.17	0.02	0.22	--	--	-0.53	-2.31	0.51	1.09	30.555	41.713	
Austria	0.04	0.10	0.01	0.22	0.00	0.03	0.44	-0.52	0.35	0.15	0.01	0.15	-0.00	0.11	0.02	0.06	0.07	0.14	--	--	0.29	-0.27	0.09	0.27	-0.016	-0.308	
Belgium	0.06	0.09	0.00	0.01	0.01	0.14	0.07	-0.87	0.06	-0.25	-0.00	-0.01	0.06	0.24	0.04	0.04	0.04	0.10	0.00	0.03	0.04	-0.67	0.11	0.31	0.117	-1.245	
Denmark	0.04	-0.01	-0.01	-0.09	-0.04	-0.11	-0.04	-0.95	-0.13	-0.41	0.04	0.04	0.09	0.32	0.03	-0.00	0.04	-0.01	0.04	0.04	0.12	-0.02	-0.46	0.17	0.39	0.036	-0.013
France	0.03	0.01	-0.01	-0.12	0.15	0.30	-0.11	-1.71	-0.15	-1.21	-0.02	-0.20	0.05	0.30	0.01	-0.01	0.04	0.04	0.04	0.12	-0.05	-0.84	0.12	0.32	0.138	0.358	
Germany	0.05	0.19	0.01	0.10	0.12	0.43	0.17	-0.94	0.18	-0.46	-0.06	-0.25	0.04	0.00	-0.00	-0.02	0.11	0.41	0.03	0.16	0.04	-0.15	0.15	0.46	-0.007	0.546	
Italy	0.04	0.19	-0.01	-0.27	-0.05	-0.40	-0.10	-1.68	-0.12	-1.18	0.01	0.17	0.05	0.42	0.02	0.18	0.08	0.46	-0.01	-0.11	-0.07	-1.16	0.17	0.40	16.022	-11.398	
Netherlands	0.03	-0.03	-0.00	0.03	0.44	0.82	0.15	-0.79	0.14	-0.21	-0.43	-0.80	0.02	0.01	-0.03	-0.23	0.03	-0.02	0.08	0.25	0.12	-0.64	0.10	0.30	0.019	-0.107	
Norway	0.03	0.11	0.03	0.26	0.04	0.28	0.22	0.07	0.16	0.67	0.04	0.28	0.03	0.05	0.02	0.03	--	--	0.00	0.06	0.19	0.08	0.14	0.44	0.012	-0.111	
Sweden	0.04	0.21	0.02	0.36	0.11	0.44	0.52	0.05	0.51	0.64	0.00	0.13	0.04	0.01	-0.02	0.11	0.04	0.17	0.02	0.10	0.14	0.18	0.15	0.41	-0.069	-0.042	
Switzerland	0.07	0.26	0.02	0.11	0.09	0.13	0.43	-0.97	0.42	-0.27	-0.06	-0.21	-0.02	0.17	-0.02	0.04	0.16	0.84	0.03	0.10	0.13	-0.21	0.17	0.45	-0.008	0.024	
U.K.	0.07	0.21	0.00	-0.09	0.00	0.04	-0.13	-2.04	-0.12	-1.54	0.03	0.07	0.10	0.40	0.04	0.23	0.04	0.16	0.00	0.00	-0.04	-0.69	0.23	0.53	16.041	110.061	
Finland	0.05	0.24	0.03	0.37	-0.00	0.00	0.55	1.21	0.44	1.77	0.02	0.45	0.00	0.09	0.02	0.18	0.04	0.28	--	--	0.46	1.11	0.09	0.29	5.837	-64.815	

^aChange is absolute change, not percentage change, in units of local currency.

The U.S. increase had a negative effect on the U.S. balance of payments and a positive effect on the other countries' balance of payments. This has, other things being equal, a negative effect on other countries' interest rates. For some of the countries the net effect on the interest rate after six quarters was negative. This reverses at least part of the initial negative effect of the world wide increase in interest rates on world income.

Although GNP increased for all countries except the Netherlands, imports declined for some countries. This is due in part to the effects of higher initial interest rates and in part to the fact that import prices increased more initially than domestic prices. An increase in import prices relative to domestic prices leads to a substitution away from imported goods.

Note finally with respect to Table 8 that the money supply decreased for many countries. Although income was higher, interest rates were also higher, and in many cases the negative interest rate effect dominated.

The results in Table 9 are for the flexible exchange rate period. One key difference between the fixed and flexible rate periods is that the U.S. interest rate has smaller direct effects on other countries' interest rates. The changes in the other countries' interest rates after two quarters are smaller in Table 9 than in Table 8. This means that there is less initial offset to the trade multiplier effect from higher interest rates in the flexible rate period.

There are four main effects of the U.S. spending increase on exchange rates, three negative and one positive. The spending increase raised U.S. output and prices relative to those of the other countries, both of which have a negative effect on other countries' exchange rates (an

appreciation). The U.S. balance of payments fell relative to those of the other countries (the balance of payments of other countries generally rose), and this also has a negative effect on exchange rates. The positive effect is the interest rate effect. The U.S. short term interest rate rose relative to other countries' rates, and this has a positive effect on exchange rates (a depreciation). As can be seen in Table 9, the net effect can go either way. For some countries, such as Germany, there is a depreciation after two quarters (the interest rate effect dominating) and an appreciation after six quarters.

The changes in the price of imports are much higher in the flexible rate period. This is, of course, due to the fact that exchange rate changes are no longer zero. The changes in the price of exports are also higher for the same reason. The changes in import prices are negative for countries whose exchange rate appreciates. For most of these countries the fall in import prices led to a fall in the GNP deflator. In other words, the U.S. expansion generally led to a fall in inflation rates in those countries whose exchange rates appreciated. This is contrary to the case in Table 8, where the U.S. expansion led to an increase in almost all countries' inflation rates.

The balance of payments fell for some countries in Table 9, contrary to the case in Table 8. If a country's exchange rate depreciates in response to the U.S. expansion (the interest rate effect dominating), then, as noted above, the initial effect on the balance of payments is likely to be negative (the J curve effect).

The rest of the results in Table 9 should be self explanatory given the above discussion. As a final comment, it would be possible, as some people have suggested to me, to compare the properties of the present model

to the properties of Model A in Fair (1979a). Model A is a "quasi-empirical" two-country model obtained by linking the U.S. model to a model exactly like it. Model A has the advantage of allowing more versions of the theoretical model to be analyzed. This may be of interest in future work, but in general I look on Model A as merely an intermediate step between the theoretical model and the present econometric model.

VI. Conclusion

The econometric model presented in this paper provides quantitative estimates of the trade, price, and interest rate linkages among countries. Some information on these linkages is presented in Section V. Much more information is presented in a sequel to this paper, Fair (1981).

It is clear from the results in Tables 8 and 9 that there are important quantitative differences between the fixed and flexible rate periods, which shows the importance of trying to model exchange rates accurately.

The models of the individual countries can be easily replaced by alternative models within the context of the overall model, and it is hoped that this study will induce work of this kind.¹³ It will be interesting to see how sensitive the properties of the overall model are to the replacement of individual models. As more observations become available under flexible exchange rates, it should be possible to get more precise estimates of the interest rate and exchange rate reaction functions, and it will also be interesting to see how sensitive the properties of the model are to the new estimates. Another important area for future work

¹³It is quite easy in the Fair-Parke program, which estimates and solves the model, to replace one individual country model with another.

is estimating the responsiveness of the trade shares (the α_{jit}) to changes in relative prices.

In the more distant future the overall model will need to be tested using a method like the one in Fair (1980a). A method like this should help decide which version of the model is the best and how this version compares to alternative models. In the meantime, the results from the model must be interpreted with considerable caution.

DATA APPENDIX

The collection of the data for the U.S. model is described in Fair (1976, 1980b), and this discussion will not be repeated here. The data for all the other countries were obtained from the International Financial Statistics (IFS) tape (October 1980) and the Direction of Trade (DOT) tape (October 1980). The following steps were involved in the construction of the data base:

1. A program was written to read the IFS tape and create for each country all the variables in Table 1 except the variables for which DOT data are needed: $M75\$A_{it}$, $M75\$B_{it}$, PM'_{it} , $XX\$_{ijt}$, $XX75\$_{ijt}$, α_{jit} , and ψ_{2it} . Most of the work in constructing the data base was writing this program. No two countries were exactly alike with respect to the availability of the data, and so separate subroutines were written for each country.¹ The individual treatment of the countries is discussed below. The output from this program was stored by country on a tape called IFS1.
2. A program was written to read the DOT tape and create the $XX\$_{jit}$ data (the bilateral trade data). The output from this program was stored by country on a tape called DOT1.
3. The IFS1 and DOT1 tapes were sorted to store the data by quarter.

¹Before these subroutines were written, a program was written to print the IFS data in a convenient format. The information needed to write the individual subroutines was taken from this printout. I am indebted to William Parke for help in writing the initial program that read the tape.

The sorted tapes were then used together to create the variables mentioned in step 1. This completed the construction of the data base.

The individual treatment of the data for each country is outlined in Table A-1. The comments in the table discuss any special treatment of the country. If no comments appear for a particular country, then all the data were available and nothing special needed to be done. Two standard procedures were followed for all the countries, and it is necessary to discuss these before considering the comments in Table A-1. First, if no quarterly National Income Accounts (NIA) data were available, then quarterly data were interpolated from annual data using quarterly data on the industrial production index (IP). If quarterly data on IP were not available, then the procedure in Table A-2 was used to create the quarterly data. One can thus tell from Table A-1 how the quarterly NIA data were constructed (if they were constructed) by noting whether or not IP data were available.

The second standard procedure concerns the construction of the Balance of Payments (BOP) data, and this procedure is presented in Table A-3. The key variable that is created in this process is BOP_{it}^* , the balance of payments on current account. It is used in the construction of the asset variable, A_{it}^* , for each country. Quarterly BOP data do not generally begin as early as the other data, and the procedure in Table A-3 allows data on BOP_{it}^* to be constructed as far back as the beginning of the data for merchandise imports and exports ($M\$_{it}$ and $X\$_{it}$). When all data are available, the procedure is a way of linking the BOP and non-BOP data.

Most of the comments in Table A-1 are self explanatory. Data for

Frenkel, Jacob A. and Harry G. Johnson, eds. The Monetary Approach to the Balance of Payments. Toronto: University of Toronto Press, 1976.

Frenkel, Jacob A. and Carlos A. Rodrigues. "Portfolio Equilibrium and the Balance of Payments: A Monetary Approach." The American Economic Review. 65 (September 1975): 674-88.

Hickman, Bert G. "International Transmission of Economic Fluctuations and Inflation." In International Aspects of Stabilization Policies, edited by Albert Ando, Richard Herring, and Richard Martson. Boston: Federal Reserve Bank of Boston, 1974.

Kouri, Penti J. K. "The Exchange Rate and the Balance of Payments in the Short Run and in the Long Run." Scandinavian Journal of Economics. 2 (May 1976): 280-304.

TABLE A-2. Procedure Used to Create Quarterly Data from Annual Data
When No Quarterly Interpolation Variables Were Available

Let:

$$y_t = \text{(observed) average value of the variable for year } t ,$$

$$y_{it} = \text{(unobserved) average value of the variable for quarter } i$$

of year t ($i = 1, 2, 3, 4$).

Then:

$$(i) \quad y_{1t} + y_{2t} + y_{3t} + y_{4t} = \lambda y_t ,$$

where $\lambda = \begin{cases} 1 & \text{for flow variables (at quarterly rates)} \\ 4 & \text{for stock variables and price variables.} \end{cases}$

Assume that the annual data begin in year 1, and let $\lambda y_1 = a_1$, $\lambda y_2 = a_2$, $\lambda y_3 = a_3$, The key assumption is that the four quarterly changes within the year are the same:

$$(ii) \quad y_{1t} - y_{4t-1} = y_{2t} - y_{1t} = y_{3t} - y_{2t} = y_{4t} - y_{3t} = \begin{cases} \delta_2 & \text{for } t=1,2 \\ \delta_t & \text{for } t \geq 3 \end{cases}$$

Given (i) and (ii) for $t = 1, 2$, one can solve for y_{40} and δ_2 in terms of a_1 and a_2 :

$$y_{40} = \frac{13}{32}a_1 - \frac{5}{32}a_2 ,$$

$$\delta_2 = \frac{a_2 - a_1}{16} .$$

Using y_{40} and δ_2 , one can then construct quarterly data for years 1 and 2 using (ii). Given y_{42} from these calculations and given (i) and (ii) for $t = 3$, one can solve for δ_3 in terms of a_3 and y_{42} :

$$\delta_3 = \frac{a_3 - 4y_{42}}{10} .$$

Using y_{42} and δ_3 , one can then construct quarterly data for year 3. One can then solve for δ_4 in terms of y_{43} and a_4 , and so on.

Note: The annual population data that were collected for the model are mid-year estimates. In order to apply the above procedure to these data, the assumption was first made that each mid-year value is the same as the average value for the year.

TABLE A-3. Construction of the Balance of Payments Data: Data for BOP_{it}^* and TT_{it}^*

Let:

$M\$_{it}'$ = merchandise imports (fob) in \$, BOP data. [= IFS77ABD.]

$M\$_{it}$ = merchandise imports (fob) in \$. [In Table 1.]

$X\$_{it}'$ = merchandise exports (fob) in \$, BOP data. [= IFS77AAD.]

$X\$_{it}$ = merchandise exports (fob) in \$. [In Table 1.]

$MS\$_{it}$ = other goods, services, and income (debit) in \$. BOP data. [= IFS77ADD.]

$XSS\$_{it}$ = other goods, services, and income (credit) in \$. BOP data. [= IFS77ACD.]

$PT\$_{it}$ = private unrequited transfer in \$. BOP data. [= IFS77AED.]

$OT\$_{it}$ = official unrequited transfers in \$. BOP data. [= IFS77ACD.]

A. When quarterly data on all the above variables were available, then:

$$(i) BOP\$_{it} = X\$_{it}' + XSS\$_{it} - M\$_{it}' - MS\$_{it} + PT\$_{it} + OT\$_{it},$$

$$(ii) TT\$_{it} = BOP\$_{it} - X\$_{it}' - XSS\$_{it} + M\$_{it}' + MS\$_{it},$$

where $BOP\$_{it}$ is total net goods, services, and transfers in \$ (balance of payments on current account) and $TT\$_{it}$ is total net transfers in \$.

B. When only annual data on $M\$_{it}'$ were available, interpolated quarterly data were constructed using $M\$_{it}$. Similarly for $MS\$_{it}$.

When only annual data on $X\$_{it}'$ were available, interpolated quarterly data were constructed using $M\$_{it}$. Similarly for $XSS\$_{it}$, $PT\$_{it}$, and $OT\$_{it}$.

When no data on $M\$_{it}'$ were available, then $M\$_{it}'$ was taken to be $\lambda \cdot M\$_{it}$, where λ is the last observed annual value of $M\$_{it}'/M\$_{it}$. Similarly for $MS\$_{it}$ (where λ is the last observed annual value of $MS\$_{it}/MS\$_{it}$).

When no data on $X\$_{it}'$ were available, then $X\$_{it}'$ was taken to be $\lambda \cdot X\$_{it}$, where λ is the last observed annual value of $X\$_{it}'/X\$_{it}$. Similarly for $XSS\$_{it}$ (where λ is the last observed annual value of $XSS\$_{it}/XSS\$_{it}$), for $PT\$_{it}$ (where λ is the last observed annual value of $PT\$_{it}/X\$_{it}$), and for $OT\$_{it}$ (where λ is the last observed annual value of $OT\$_{it}/X\$_{it}$).

Equations (i) and (ii) were then used to construct quarterly data for $BOP\$_{it}$ and $TT\$_{it}$.

C. After data on $BOP\$_{it}$ and $TT\$_{it}$ were constructed, data on BOP_{it}^* and TT_{it}^* were constructed as:

$$(iii) BOP_{it}^* = e_{it} BOP\$_{it},$$

$$(iv) TT_{it}^* = e_{it} TT\$_{it}.$$

D. Notice from $M\$_{it}$ and $X\$_{it}$ in Table 1 and from $MS\$_{it}$ and $XSS\$_{it}$ above that

$$M\$_{it} = (PM_{it} M_{it}') / e_{it},$$

$$X\$_{it} = (PX_{it} X_{it}') / e_{it}.$$

Notice also from Table 1 that

$$M_{it}' = (PM_{it} M_{it}') / e_{it},$$

$$X_{it}' = (e_{175} PX_{it} X_{it}') / e_{it}.$$

Therefore, from (i)-(iv) the equation for BOP_{it}^* can be written

$$BOP_{it}^* = PX_{it} (e_{175} X_{it}' + X_{it}') - PM_{it} (M_{it}' + M_{it}') + TT_{it}^*,$$

which is equation 17 in Table 2.

E. For countries with no PM data it is not the case that $M\$_{it} = (PM_{it} M_{it}') / e_{it}$. (See note 1 to Table 1.) For these countries TT_{it}^* was taken to be

$$TT_{it}^* = BOP_{it}^* - PX_{it} (e_{175} X_{it}' + X_{it}') - PM_{it} (M_{it}' + M_{it}'),$$

where PM_{it} and M_{it}' are defined in note 1 to Table 1.

a variable were "made up" if there were a relatively small gap in an otherwise good series. In these cases the data were usually made up by linearly interpolating between the closest two available observations. In a few cases quarterly data on the consumer price index (CPI) were used for quarterly interpolations of annual data, and for France and Switzerland quarterly data on employment (EMPL) rather than on industrial production were used for the quarterly interpolation of the NIA data. For many countries only discount rate data were available for the short term interest rate (r), and these cases are mentioned in the table. For a few countries the NIA year began other than January 1, and this had to be taken into account in the quarterly interpolations. These cases are also mentioned in the table. For a few countries data on real GNP (Y) were not available, but data on the nominal NIA variables were. In these cases, as indicated in the table, CPI data were used for the GNP deflator. Real GNP was then taken to be nominal GNP divided by the GNP deflator.

Quarterly population data were not available for any country, and the procedure in Table A-2 was used to construct quarterly from annual data. See in particular the note at the bottom of the table.

Quarterly DOT data began only in 1970I, and no attempt was made to construct DOT data before this quarter. Instead, the variables in the model were constructed in such a way (with one exception noted below) that no DOT data were needed in the estimation of the model. In other words, no DOT data were used for the estimates in Table 4. This allowed the estimation periods for most countries to be much longer than would otherwise be the case. The DOT data are needed, of course, for the solution of the model, and so the earliest quarter for which the model can

be solved in 1970I. In a few cases annual but not quarterly DOT data were available, and in these cases the procedure in Table A-2 was used to construct the quarterly data. In a few cases no DOT data existed, and in these cases the observations were assumed to be zero.

For a few countries no data on import prices were available, and for these countries the data were constructed as indicated in note 1 to Table 1 in the text. This construction required the existence of DOT data, and this is the exception mentioned above where DOT data were needed for the estimation work. For countries for which DOT data were used in the construction of the import price index, the estimation period had to begin no earlier than 1970I for the equations that relied on these data.

The links to and from the U.S. model are listed in Table A-4. The two key exogenous foreign sector variables in the U.S. model are the real value of exports (EX^u) and the import price deflator (PIM^u). When the U.S. model is embedded in the overall model, these two variables become endogenous. The endogenous variables in the U.S. model that affect the rest of the model are the real value of imports (IM^u), the export price deflator (PEX^u), the bill rate ($RBILL^u$), the GNP deflator ($GNPD^u$), real GNP ($GNPR^u$), and a demand pressure variable (ZJ^u). The data base for the U.S. model is different from the data base for the U.S. on the IFS tape (among other things, the real variables in the U.S. model are in 72\$, whereas the real variables for the U.S. on the IFS tape are in 75\$), and the δ_{it} variables in Table A-4 are used to link the two data sets.

The sample periods that were used for the estimation work are listed in Table 4 in the text. The beginning of the sample period was usually taken to be four quarters after the beginning of the data, and the end

A. Relevant endogenous variables in the U.S. model (Fair, 1980b):

- IM_t^u = real value of imports (NIA) in 72\$.
 PEX_t^u = implicit price deflator for exports (NIA), 1972 = 1.0.
 $RBILL_t^u$ = three-month treasury bill rate, percentage points.
 $GNPD_t^u$ = GNP deflator, 1972 = 1.0.
 $GNPR_t^u$ = real GNP in 72\$.
 ZJ_t^u = demand pressure variable.

Links from the endogenous variables in the U.S. model to the variables that affect the rest of the world:

- $M75\$A_{1t} = IM_t^u / \delta_{2t} - M75\$B_{1t} - MS_{1t} - IMDIS_{1t}$. [merchandise imports in 75\$ from Type A countries.]
 $PX_{1t} = PEX_t^u / \delta_{3t}$. [export price index, 1975 = 1.0.]
 $PY_{1t} = GNPD_t^u / \delta_{6t}$. [GNP deflator, 1975 = 1.0.]
 $r_{1t} = RBILL_t^u$. [three-month interest rate.]
 $Y_{1t} = GNPR_t^u / \delta_{5t}$. [real GNP in 75\$.]

B. Relevant exogenous variables in the U.S. model:

- EX_t^u = real value of exports (NIA) in 72\$.
 PIM_t^u = implicit price deflator for imports (NIA), 1972 = 1.0.

Links from the rest of the world to the exogenous variables in the U.S. model:

- $EX_t^u = \delta_{1t} EX_{1t} = \delta_{1t} (X75\$_{1t} + XS_{1t} + EXDIS_{1t})$.
 $PIM_t^u = \delta_{4t} PM_{1t}$.

C. New exogenous variables:

- $\delta_{1t} = EX_t^u / EX_{1t} = EX_t^u / (X75\$_{1t} + XS_{1t} + EXDIS_{1t})$.
 $\delta_{2t} = IM_t^u / (M75\$A_{1t} + M75\$B_{1t} + MS_{1t} + IMDIS_{1t}) = IM_t^u / IM_{1t}$.
 $\delta_{3t} = PEX_t^u / PX_{1t}$.
 $\delta_{4t} = PIM_t^u / PM_{1t}$.
 $\delta_{5t} = GNPR_t^u / Y_{1t}$.
 $\delta_{6t} = GNPD_t^u / PY_{1t}$.

D. Other relevant equations:

- $M_{1t} = M75\$A_{1t} + M75\B_{1t} .
 $BOP_{1t}^* = PX_{1t} (X75\$_{1t} + XS_{1t}) - PM_{1t} (M_{1t} + MS_{1t}) + TT_{1t}^*$.
 $A_{1t}^* = A_{1t-1}^* + BOP_{1t}^*$.

of the sample period was usually taken to be the last quarter of the data. One can thus tell from Table 4 approximately how much data are available for each country.

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