# Leverage Cycles and the Anxious Economy Ana Fostel and John Geanakoplos

Discussion by Roberto Chang

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July 2008

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- Significant contribution: clean modeling, a theory of asset pricing with collateral constraints.
- Less clear: empirical applicability of the model for the questions at hand.

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- Ouring closures, the issuance of investment grade EM bonds falls by more than the issuance of sub grade bonds (*issuance rationing*).

#### Average Spreads around Closures

Emerging Markets

US High Yield Spreads

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Average Spread Volatility around Closures

#### Emerging Markets

US High Yield



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- That is, much of the volatility of emerging markets bonds is a result of the behavior *of international investors* reacting, in particular, to news *about US risky bonds*.
- This contrasts with the view that such volatility reflects fundamentals in EMs themselves.
- Radical idea, potentially strong policy implications, certainly worth exploring.

• FG emphasize that they do not focus on *crises driven* behavior. But for at least some cases, such behavior may be the dominant one.



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- E yields 1 unit of fruit with prob. q, or e < 1 with prob. 1 − q, independently of what happens with H.</li>
- Normally, H yields 1 unit of fruit. But there is the possibility of bad news, in whose case H yields *either* 1 with prob. q or h < 1 with prob. (1 q).

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- If bad news arrive about H, price of H naturally falls. But, would the price of E fall also?
- If so, why?
- If there are different kinds of E trees, whose price falls by more when bad news arrive?

- With a representative agent, no contagion can occur.
- With heterogenous agents but complete markets, "only a tiny degree of contagion" (?).
- ==> Need to allow for heterogenous agents and incomplete markets.

• Agent *i* has utility

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- For computed examples, i = optimist or pessimist.

At each t, agent *i*'s budget constraint is:

$$egin{aligned} & x_t, y_{tj} \geq 0 \ & x_t - e_t^j + \sum_j p_{tj}(y_{tj} - y_{t-1,j}) \leq rac{1}{1+r_t} \phi_t - \phi_{t-1} + \sum_j y_{t-1,j} D_{tj} \ & \phi_t \leq \sum_{j \in J^C} y_{tj} \gamma_{tj} \end{aligned}$$

where  $\gamma_{ti}$  is asset j's collateral capacity:

$$\gamma_{tj} = \min_{\sigma} \left[ p_{t\sigma,j} + D_{t\sigma,j} \right]$$

and the min is over the possible states of nature ( $\sigma$ ) at next stage.

## Individual Optimality

Most of my intuition came from looking at these! Let  $\lambda_{it} = u'(x_{it})$  and  $\mu_{it}$  denote *nonnegative* Lagrange multipliers:

• For each tree j (defining  $\gamma_{tj} = 0$  if  $j \notin J^C$ ):

$$\lambda_{it} p_{tj} = \delta^{i} \left[ \sum_{\sigma} q_{t\sigma}^{i} \lambda_{i,t\sigma} (p_{j,t\sigma} + D_{j,t\sigma}) \right] + \mu_{it} \gamma_{tj}$$

i.e.

$$p_{tj} = \delta^{i} \left[ \sum_{\sigma} q_{t\sigma}^{i} \frac{\lambda_{i,t\sigma}}{\lambda_{it}} (p_{j,t\sigma} + D_{j,t\sigma}) \right] + \frac{\mu_{it}}{\lambda_{it}} \gamma_{tj}$$

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POC for borrowing:

$$\frac{1}{1+r_t}\lambda_{it} = \delta^i \sum_{\sigma} q_{t\sigma}^i \lambda_{i,t\sigma} + \mu_{it}$$

$$p_{tj} = \delta^{i} \left[ \sum_{\sigma} q_{t\sigma}^{i} \frac{\lambda_{i,t\sigma}}{\lambda_{it}} (p_{j,t\sigma} + D_{j,t\sigma}) \right] + \frac{\mu_{it}}{\lambda_{it}} \gamma_{tj}$$

- If the term  $\frac{\mu_{it}}{\lambda_{it}}\gamma_{tj}$  is zero, we have a conventional asset pricing formula: the price of asset *j* is equal to its *payoff value*.
- The term  $\frac{\mu_{it}}{\lambda_{it}}\gamma_{tj}$  is a new source of value (j's collateral value)
- Since  $\gamma_{tj} = \min_{\sigma} [p_{t\sigma,j} + D_{t\sigma,j}]$ , j's collateral capacity and its collateral value are endogenous and forward looking.
- But collateral value is zero unless  $\mu_{it} > 0$ .

$$rac{\mu_{it}}{\lambda_{it}} = rac{1}{1+r_t} - \delta^i \sum_\sigma q^i_{t\sigma} rac{\lambda_{i,t\sigma}}{\lambda_{it}}$$

- µ<sub>it</sub> > 0 only if agent i's wants to borrow more than he can at the
   market interest rate (i.e. there is a *liquidity wedge*)
- For given  $r_t$ , changes in  $\mu_{it}$  (the *liquidity wedge cycle*) must be necessarily accommodated by changes in the  $\lambda'_{it}s$ . (This would affect the  $p'_{ti}s$  even in the absence of leverage.)
- When leverage is possible, the impact of the liquidity wedge cycle on prices can be amplified through the term  $\frac{\mu_{it}}{\lambda_{\mu}}\gamma_{ti}$  (*leverage cycle*).
- Very complex interactions, resulting in new and unexpected behavior, appear possible.

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- It is unclear (at least to me) how informative this exercise can be. Example economies are too stylized (only three periods, only two types of agents, a very particular information structure...) to argue that the outcomes are robust. Parameters are postulated with only a minimal attempt at linking them to observable data.
- Some of the assumptions in the examples appear counterfactual (e.g. emerging markets bonds can be used as collateral but U.S. junk bonds cannot)

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- What do we learn for policy and welfare?
- Next versions of this model should be much more user friendly.

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- The model, however, is a useful step towards the understanding of the role of financial frictions and incomplete markets in asset pricing.
- Developing more potentially realistic versions of this model is, hence, a promising endeavor.