

International Trade in Durable Goods: Understanding Volatility, Cyclical, and Elasticities *

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June 16, 2008

Abstract

Data for OECD countries document: 1. imports and exports are about three times as volatile as GDP; 2. imports and exports are pro-cyclical, and positively correlated with each other; 3. net exports are counter-cyclical. Standard models fail to replicate the behavior of imports and exports, though they can match net exports relatively well. Inspired by the fact that a large fraction of international trade is in durable goods, we propose a two-country two-sector model, in which durable goods are traded across countries. Our model can match the business cycle statistics on the volatility and comovement of the imports and exports relatively well. The model is able to match many dimensions of the data, which suggests that trade in durable goods may be an important element in open-economy macro models.

JEL Classifications: E32 F3 F4

Keywords: Durable Goods, International Real Business Cycles, Elasticity Puzzle, Backus-Smith Puzzle

*We thank David Backus, Paul Bergin, Martin Boileau, Lukasz Drozd, Jonathan Heathcote, Enrique Martinez-Garcia, Mark Wynne, Kei-Mu Yi and seminar participants at Boston College, Chicago GSB, Dartmouth College, Tufts University, the Federal Reserve Bank of Dallas, NBER IFM Meeting, 2008 Midwest Macro Meetings, and HEC/CIRPEE Real Business Cycle Conference for helpful comments. All views are those of the authors and do not necessarily reflect the views of the Federal Reserve Bank of Dallas or the Federal Reserve System. Engel acknowledges support for this research from a grant from the National Science Foundation.

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1 Introduction

One of the most established empirical regularities in international real business cycle (IRBC) analysis is the counter-cyclical behavior of net exports. Backus, Kehoe, and Kydland (1992, 1994) (BKK henceforth) explain this empirical finding with the dynamics of capital formation: in the face of a positive productivity shock, the increase of investment exceeds the increase in saving.¹ In contrast, the behavior of imports and exports themselves has been largely neglected in the literature.² They are much more volatile than GDP and both are pro-cyclical, facts which are at odds with the predictions of standard models. Inspired by the evidence that a large fraction of international trade is in durable goods, we propose a two-country two-sector model, in which durable goods are traded across countries. Simulation results show that our model can match the trade sector data much better than the standard models.

We first document two robust empirical findings: 1. Real imports and exports are much more volatile than total output. Their standard deviations are on average about two to three times as large as GDP's in our OECD-country dataset.³ 2. Real imports and exports are pro-cyclical and also positively correlated with each other. We label the first finding "trade volatility", and the second one "positive comovement". These findings are very robust across our 25-OECD-country data. We also confirm in our dataset the well-documented negative correlation between net exports and output.

In standard international business cycle models, imports and exports are far less volatile than in the data. They are actually even less volatile than GDP. We demonstrate this in a variety of standard models—real business cycle and sticky-price dynamic models. We emphasize that the issue is not resolved by building versions of the model with high real exchange rate volatility. Although a more volatile exchange rate helps to increase the volatility of imports and exports, it generates a negative correlation between imports and exports. This is at odds with the finding of "positive comovement".

We propose a model in which countries trade durable goods only. This setup is inspired by the fact that a large portion of international trade is durable goods. We find in OECD country data that trade in durable goods on average accounts for about 70% of imports and exports for OECD countries.⁴ The importance

¹Raffo (2006) modifies BKK's model with a preference function proposed by Greenwood, Hercowitz, and Huffman (1988) (GHH henceforth). He finds that the modified model can also replicate the counter-cyclical net exports measured at constant prices.

²The only paper that examines import and export volatility to our knowledge, is Zimmermann (1999). That paper uses exogenous exchange rate shocks to generate the volatility of imports and exports. This explanation is contradictory to the positive correlation between imports and exports. We give more details later.

³Similar results are also reported in Table 11.7 of Backus, Kehoe, and Kydland (1995), Heathcote and Perri (2002), and Zimmermann (1999).

⁴Baxter (1995) shows that about two thirds of trade is in durable goods (including capital goods) for the US. Erceg, Guerrieri, and Gust (2006) document a more recent (year 2004) breakdown of US imports and exports. They find that consumer non-durables account for only 28% of non-energy imports and 25% of non-energy exports. In contrast, consumer durables and capital goods account for 32% and 30% of non-energy imports. For non-energy exports, they account for respectively, 16% and 45%. Non-energy industrial supplies, which are used in producing durables, account for the remaining 10% of imports and 14%

of capital goods in international trade has also been documented by Eaton and Kortum (2001). Boileau (1999) examines an IRBC model with trade in capital goods. He finds that allowing direct trade in capital goods improves the model’s performance in matching the volatility of net exports and the terms of trade. Boileau’s model shares some characteristics of the one we examine. It does not include consumer durable goods, which we suggest below are necessary to include to understand some aspects of the data. Moreover, Boileau (1999) does not examine the implications of his model for imports and exports individually, which is the focus of our study. Erceg, Guerrieri, and Gust (2006) also emphasize that trade in capital goods helps model to replicate trade volatility. They argue that trade balance adjustment may be triggered by investment shocks from either home or foreign country and such adjustment may not cause substantial real exchange rate fluctuations. Warner (1994) finds that global investment demand has been an important determinant of U.S. exports since 1967. However, we find that a model with trade in capital goods but not consumer durables is inadequate. In order to match the volatility of the trade data, a large share of traded goods must be durable. But if we take all of those traded goods to be capital, then the model would require, for example, that the U.S. obtains almost all capital goods from imports while simultaneously exporting large quantities of capital.

Our model goes further by including both capital and durable consumption goods in international trade.⁵ In our two-country two-sector model, nondurable goods are nontraded. Durable consumption flows require both home and foreign durable goods varieties and capital goods are aggregated from home and foreign varieties of capital. Simulation results show that the benchmark model can successfully replicate “trade volatility” and “positive comovement”. In addition, net exports in our model are counter-cyclical and as volatile as in the data. So our model can match the trade sector data much better than the standard models. This improvement is not at the cost of other desirable features of standard models. The aggregate variables such as output, consumption, investment and labor, can also match the data well.

An important empirical puzzle that has confronted international trade economists is the mismatch between estimated short-run and long-run elasticities of import demand. As Ruhl (2005) and others have discussed, typically short-run elasticities are estimated to be near unity, but long-run elasticities are generally found to be considerably higher. That pattern arises naturally in any model such as ours in which durable capital and consumer goods are traded, because durable stocks cannot be adjusted quickly in response to price changes. Another interesting feature of our model is its implications for understanding comovements

of exports.

⁵Baxter (1992) has durable consumption in a two-sector model. The model setup is very different from ours and is used to address different issues. Sadka and Yi (1996) build a simple small-country real-business-cycle model with durable consumption goods. They use this model to demonstrate that the increase of consumption durables due to a permanent decrease in their prices may be an important element in explaining the 1980s US trade deficits.

of relative consumption and real exchange rates, as in the Backus-Smith (1993) puzzle. Our model suggests that it may be important to distinguish carefully consumption purchases (which include purchases of consumer durable goods) and consumption flows (which include the flow of services delivered from previously purchased durables.)

Our model’s success in accounting for several aspects of international trade data suggests that it may be important to incorporate trade in durable goods when constructing an open-economy model for policy analysis. There are several challenges remaining, however. A well-known departure of the IRBC model from the data is that cross-country outputs have low correlation in those models, while this correlation is positive and relatively high in the data. We explore this issue, but do not fully resolve the puzzle. In this paper, we also take trade in durable goods as exogenously given. Future work might endogenize the durability of traded goods, relating the types of goods traded to the cost of storage and time to ship.

The remainder of the paper is organized as follows: Section 2 displays statistics on “trade volatility” and “positive comovement”. We show that the standard models and their simple extensions cannot simultaneously replicate those empirical findings. Section 3 describes our two-country two-sector benchmark model. Section 4 explains our calibration of the model. Section 5 shows simulation results of the benchmark model and Section 6 concludes.

2 Empirical Findings and Performance of Standard Models

In this section, we first show some facts about international real business cycles: 1. Real imports and exports are about two to three times as volatile as GDP. 2. Both real imports and exports are pro-cyclical and positively correlated with each other. 3. Real net exports are counter-cyclical. Then we investigate whether standard models in the literature can replicate those features. We also present evidence that trade in durable goods accounts for a large portion of imports and exports in OECD countries.

2.1 Empirical Findings

Our data-set includes quarterly real GDP, real imports, real exports, and real net exports of OECD 25 countries during the period between 1973Q1 and 2006Q3.⁶ The data are from *OECD Economic Outlook* database. All variables are logged except net exports⁷ and H-P filtered with a smoothing parameter of 1600.

⁶Due to data limitation, Austria starts from 1988Q1, Czech Republic starts from 1993Q1, and Hungary starts from 1991Q1. The data of Germany are for West Germany only which end in 1991Q1. The data after unification (1991Q1-2006Q3) show similar patterns.

⁷Following the literature, we divide the net exports by GDP.

Table 1 shows the volatility of those variables and comovement of real imports and real exports with GDP. The standard deviation of GDP on average, is 1.51%. Both real imports and exports are much more volatile than GDP. On average, the imports are 3.3 times, and exports are 2.7 times as volatile as GDP. This result is not driven by outliers. The sample median is very close to the sample mean. The volatilities of imports and exports in the US are close to the sample mean. However, the ratio of net exports to GDP in the US is less volatile than it is in any other countries.

Two things stand out for comovement of real imports and real exports with GDP. First, both imports and exports are pro-cyclical. This result is very robust: the imports are positively correlated with GDP in all 25 countries. The average correlation is 0.63. The same is true for exports except in two countries: Denmark and Mexico. The average correlation between exports and GDP is 0.39. Second, imports and exports are positively correlated in all countries except Australia, Mexico, New Zealand and Spain. The average correlation between imports and exports is 0.38. In this table, we also confirm a well-documented finding in previous studies: net exports are counter-cyclical. This is true in all countries except Austria and Hungary. The average correlation between net exports and GDP is -0.24.

2.2 Performance of Standard Models

We investigate whether some standard models can replicate the facts presented in Table 1. Table 2 shows simulation results for these models. These simulations demonstrate that the standard models and their extensions cannot replicate trade volatility and positive comovement simultaneously. Since the model setups are very standard in the literature, we leave them in the appendix.

We consider two types of models: the IRBC model and the DSGE model. We use exactly the structure of the bond-economy model in Heathcote and Perri (2002) as our standard IRBC model (labeled HP in Table 2.) This model has the same structure as BKK's model, but limits the financial market to a real-bond market only. Baxter and Crucini (1995) compare this incomplete financial market model with the model with perfect risk-sharing and find they behave very similarly if the productivity shock is not extremely persistent or the cross-country spillover of productivity shocks is high. Table 2 also reports results for the DSGE model. This is the extension of the IRBC model that assumes monopolistic competition, trade in nominal bonds, Calvo staggered price setting, and a monetary policy (Taylor) rule. Those models are often used in the studies of monetary policy in open economies.

GHH is the DSGE model with the preference function proposed by Greenwood, Hercowitz, and Huffman

(1988). The function takes a form of

$$u_t = \frac{(C_t - \rho L_t^\nu)^{1-\sigma}}{1-\sigma}, \quad (1)$$

where C_t is the consumption and L_t is the labor supply. We use the same class of utility function in our benchmark model. We include this model to show that our benchmark model results are not driven by this choice of utility function. We also report the results for two more extensions of the DSGE model: the model with low intertemporal elasticity of substitution (Lo-elast) and one with an uncovered interest rate parity shock (UIP). The standard international RBC model and DSGE models cannot replicate the volatility of the real exchange rate. We use those two methods to increase this volatility to see if it helps the model's performance in matching the behavior of imports and exports.

Panel A of Table 2 reports the standard deviations of aggregate variables relative to that of GDP. In our standard IRBC model (HP), imports and exports are even less volatile than GDP. The same discrepancy has also been reported in Table 2 of Heathcote and Perri (2002).⁸ They find that the assumption of financial autarky can improve the volatility of imports and exports in a very limited way. The added features in DSGE model and GHH models cannot solve this problem. Imports and exports are still far less volatile than what they are in the data. However, the GHH utility function does make the volatility of net exports much closer to the data. This follows because imports and exports are more volatile (due to more variable consumption in the GHH model), and imports and exports are less correlated than what they are in the DSGE model.

Panel B shows the correlations of real imports, real exports, and real net exports with GDP, as well as the correlation between real imports and exports. Imports and exports are measured at their steady state prices (constant price). The models of HP, DSGE and GHH match the data in that real imports and exports are pro-cyclical and positively correlated with each other. Net exports are counter-cyclical in these models. That is, the standard models can replicate the "positive comovement" feature, though they fail the "trade volatility".⁹ Panel C reports the same statistics as Panel B, but imports, exports and net exports are measured in terms of final consumption goods, instead of constant prices. The results are similar to those in Panel B.

Besides the volatility of imports and exports relative to GDP, another feature missing from the standard DSGE model is the high volatility of the real exchange rate. A natural question is whether we can increase the volatility of imports and exports in a model with more volatile real exchange rates. We follow Chari,

⁸Zimmermann (1999) finds similar results in a sticky price model.

⁹Raffo (2006) finds that the real net exports measured with constant prices are pro-cyclical under the standard utility function of $u_t = \frac{[C_t^\mu (1-L_t)^{1-\mu}]^{1-\sigma}}{1-\sigma}$. We find that this conclusion may be sensitive to the volatility of investment and the elasticity of substitution between home and foreign goods.

Kehoe and McGrattan’s (2002) “elasticity method” to increase real exchange rate volatility by decreasing the value of the intertemporal elasticity of substitution $1/\sigma$. Some authors have also used an uncovered interest rate parity (UIP) shock to generate exchange rate variations in DSGE models.¹⁰ In our simulation results, we find that the volatilities of real imports, exports and the exchange rate all increase in those models. Under certain calibrations of the UIP shock, the model can also replicate the pro-cyclical movement of imports and exports, though the correlation between exports and output is nearly zero. However, there is a striking departure of these models from the data: real imports and exports are highly negatively correlated in those models.

Figure 1 shows the production structure in the standard models. Home and foreign intermediate goods are used to produce final goods. The final goods are used for consumption and investment. There are two factors affecting the volatility of imports: 1. the volatility of demand for final goods and, 2. the substitution between home and foreign goods. Under the standard calibration, the majority (about 75%) of final goods (and therefore imports) goes to consumption. Consumption is less volatile than GDP in the data. So if we want to match the volatility of consumption, demand for final goods will not be very volatile. Given the low volatility of demand for final goods, we can still have very volatile imports and exports if there is a lot of substitution between home and foreign goods. This is actually what the low elasticity and the UIP models do.

Exchange rate movements induce fluctuations in the relative price of imports and exports. In return, the substitution between home and foreign goods increases the volatility of imports and exports. But when the terms of trade changes, the imports and exports move in opposite directions. So this method produces a negative correlation between imports and exports, which is contradictory to the data. Baxter and Stockman (1989) find little evidence of systematic difference in the volatilities of real imports and exports when countries switch from fixed to flexible exchange rate regimes, though the real exchange rates became substantially more variable during this period. This finding also suggests that the high volatility of international trade flows is unlikely to come from the exchange rate fluctuations.

2.3 Trade in Durable Goods in OECD Countries

Here we present some descriptive statistics on trade flows that help to motivate our model of trade in durables. We obtain our 25 OECD country data from NBER-UN World Trade Data and use the latest available data (year 2000) to calculate the share of durable goods in international trade. Table 3 reports our

¹⁰For instance, see Kollmann (2004), Wang(2007). This approach is similar to Zimmerman’s (1999), which adds an exogenous source of exchange-rate volatility.

results. On average durable goods account for about 70% of imports and exports (excluding energy products SITC 3) in these countries. Results are similar if we also exclude raw materials (right panel of Table 3). We find that about three quarters of trade is in durable goods in the US, which is in line with the finding of Erceg, Guerrieri, and Gust (2006). In particular, machineries and transportation equipments (SITC 7) on average account for more than 40% of trade for OECD countries.¹¹

SITC categories 0 (FOOD AND LIVE ANIMALS), 1 (BEVERAGES AND TOBACCO), and 4 (ANIMAL AND VEGETABLE OILS, FATS AND WAXES) are nondurable goods. Category 7 (MACHINERY AND TRANSPORT EQUIPMENT) belongs to durable goods. Category 2 is raw materials that exclude fuels such as petroleum. Category 3 contains energy products such as coal, petroleum, gas, etc. The remaining categories are more difficult to classify. This is particularly true for category 5 (CHEMICALS AND RELATED PRODUCTS, N.E.S.). Even if we go down to the 3-digit level, it is still unclear which categories belong to durable goods. We find that this category includes many nondurable goods, such as fertilizers, medicines, cleaning products, etc. To avoid exaggerating the share of durable goods, we put the whole category 5 into nondurable goods. But we note that this category does include some durable goods, such as plastic tubes, pipes, etc.

For categories 6, 8 and 9, we go down to the SITC 2-digit levels for more information about the durability of goods. Category 6 (MANUFACTURED GOODS CLASSIFIED CHIEFLY BY MATERIALS) classifies goods according to their materials. We assume that goods produced from leather, rubber, or metals are durables (61-62 and 66-69). Goods produced from wood (other than furniture), paper, or textile (63-65) are nondurables. Category 8 includes other manufactured products that are not listed in categories 6 and 7. We assume that construction goods (81), furniture (82), professional instruments (87), photographic equipments (88) are durable goods. Travel goods (83), clothing (84), footwear (85) and remaining goods (89) are classified as nondurables. Category 9 includes products that are not classified elsewhere. In this category, we assume that coins and gold (95-97) are durables. All remaining products are classified as nondurables.

We also examine the volatility of durable goods trade and other categories of trade in a data set for US trade only. We use quarterly nominal US trade data at the 2-digit SITC level from the US International Trade Commission (<http://www.usitc.gov/>). Import and export price indexes at 2-digit SITC level are obtained from Bureau of the Census through Haver Analytics. Nominal trade data are deflated by corresponding price indexes to calculate real imports and exports. In the end, we have real import and export data at 2-digit SITC level for 1997Q1-2006Q2. Imports and exports are classified into three categories: raw materials,

¹¹We note two outliers for exports. Exports of New Zealand and Iceland are mainly in categories zero (FOOD AND LIVE ANIMALS).

durable goods and nondurable goods according to the standard described above. Real imports and exports are logged and H-P filtered with a smoothing parameter of 1600.

We calculate the standard deviation for each category. In exports, raw materials and durable goods are much more volatile than nondurable goods: the standard deviations of raw materials and durable goods are respectively 7.78% and 6.54%, but only 2.86% for nondurable goods. Imports show less dispersion in volatility: the standard deviations of raw materials and durable goods are 5.02% and 5.00% respectively. It is 4.89% for nondurable goods. We note that these statistics are not precise given our rough classification of goods into the durable and nondurable categories, and given that we use only 38 observations of H-P filtered data.

Durable goods also show stronger correlation with GDP in our data. For imports, the correlation between durable goods and GDP is 0.53. It is -0.35 for raw materials and -0.17 for nondurable goods. For exports, the correlation between durable goods and GDP is 0.82. It is -0.02 for raw materials and 0.65 for nondurable goods.

3 A Two-country Benchmark Model

There are two symmetric countries in our model, Home and Foreign. We depart from the standard models in Section 2.2 by having two production sectors in each country: the nondurable good and durable good sectors. All firms are perfectly competitive with flexible prices. Nondurable goods can only be used for domestic consumption. This setup is motivated by our finding that nondurable goods only account for a small part of international trade for OECD countries. As we note above, durable goods account for much of the volatility and procyclicality of imports and exports. In addition, there is no guidance from the literature on the calibration of the productivity shocks in an open economy with both tradable and nontradable nondurables. Durable goods are traded across countries and used for durable consumption and capital accumulation. Because of the symmetry between these two countries, we describe our model focusing on the Home country.¹²

Our modeling strategy is motivated by the empirical regularities discussed in Section 2.1. As we have noted, in order to explain the high volatility of imports and exports, it is not promising to rely on the response of these variables to price changes. That would tend to make imports and exports negatively correlated, but in fact they are positively correlated. Instead, we note that changes in capital stocks can be very volatile in response to persistent changes in productivity. It is well known that investment is very volatile and

¹²We list all equilibrium conditions for both countries in Appendix A.2.

pro-cyclical. However, it would be unrealistic to attribute all of the movements in imports and exports to trade in capital goods. In order to match the movements in trade volumes, we would need to ascribe an unrealistically high share of trade to trade in capital goods, so we add trade in durable consumption goods to the model.

The standard RBC models are able to capture the pro-cyclicality of imports and exports, and the counter-cyclicality of the trade balance by introducing capital goods. But they are unable to match the volatility because most trade is in consumption goods, so the fraction of trade accounted for by investment goods is too small to account for the overall volatility of trade volumes. However, recognizing that much of trade in consumption goods is trade in consumer durables, we are able to simultaneously reconcile the volatility and cyclical behavior of imports and exports.

We are able to match the business cycle facts on trade without giving up realism in other dimensions, particularly in the characteristics of consumption behavior over the business cycle. That is because we recognize that a large fraction of consumption is in services, which we model as a nondurable nontraded good.

Trade in capital goods and consumer durables would introduce too much volatility in trade if we did not allow for some sort of installation cost. This is a well-known feature of international RBC models. But this also allows us to build a model consistent with another widely-recognized fact: that trade elasticities are higher in the long run in response to persistent shocks than they are in the short run. In our model, home and foreign durable consumption and capital goods are close substitutes, but the sensitivity over the business cycle to relative price changes is low because of these costs of adjustment.

In addition, we introduce an iceberg cost of trade. Here, we want to capture the idea that there is “home bias” in consumption of durables, as well as in the use of capital goods in production. Especially for large economic areas such as the US or the European Union, imports are a relatively small component of the overall consumption basket, or mix of inputs used in production. Because we model traded goods as being highly substitutable in the long run, it does not seem natural to simultaneously introduce home bias directly into the utility function or production function. Instead, and consistent with much of the recent literature in trade, we posit that there are costs to trade which lead to this home bias even in the long run.

We note that there is a tension in modeling the behavior of trade volumes over the business cycle. Imports and exports are pro-cyclical and their standard deviation (in logs) is much larger than that of GDP. At the same time, they are apparently not very responsive in the short run to price changes. The model of consumer durables and investment goods captures these features for reasonable parameter values. We discuss the calibration in Section 4 below, after the presentation of the model.

3.1 Firms

There are two production sectors in each country: the nondurable good sector and durable good sector. Nondurable and durable goods in the Home country are produced from capital and labor according to

$$Y_{Ht}^j = A_{Ht}^j (K_{Ht}^j)^\chi (L_{Ht}^j)^{1-\chi}, \quad (2)$$

where $j \in \{N, D\}$ denotes nondurable (N) and durable (D) good sectors. A_{Ht}^j and L_{Ht}^j are respectively the TFP shock and labor in sector j . Capital K_{Ht}^j is a CES composite of Home- and Foreign-good capital

$$K_{Ht}^j = \left(\alpha^{\frac{1}{\gamma}} (K_{Ht}^{jH})^{\frac{\gamma-1}{\gamma}} + (1-\alpha)^{\frac{1}{\gamma}} (K_{Ht}^{jF})^{\frac{\gamma-1}{\gamma}} \right)^{\frac{\gamma}{\gamma-1}}, \quad (3)$$

where in the notation such as K_{it}^{jk} , we use the subscript i to denote the country in which the capital is used, the first superscript j to denote the sector (nondurable or durable) and the second superscript k to denote the origin of the good. For instance, K_{Ht}^{NH} is the Home-country produced durable good that is used in the nondurable good sector of the Home country.

The firm buys labor and rents capital from households in competitive markets. For given wage (W_{Ht}) and rental price of capital (R_{Ht}^{jH} and R_{Ht}^{jF}), the firm chooses capital and labor to minimize the cost of production. Capital is not mobile across sectors though we assume labor can move freely from one sector to another. The nondurable and durable good markets are also competitive, so the price of nondurable and durable goods P_{Ht}^j is equal to the marginal cost

$$P_{Ht}^j = (A_{Ht}^j)^{-1} (R_{Ht}^j)^\chi W_{Ht}^{1-\chi} \chi^{-\chi} (1-\chi)^{\chi-1}. \quad (4)$$

From the firm's cost minimization problem, we can find the standard demand function for capital and labor by equating the marginal productivity to the real factor cost.

3.2 Households

In the Home country, the representative household supplies labor, accumulates and rents capital to firms, chooses nondurable consumption and accumulates durable consumption stock to maximize expected lifetime utility

$$E_t \sum_{j=0}^{\infty} \beta^j u(D_{Ht+j}, C_{Ht+j}, L_{Ht+j}),$$

where the period utility $u(D_{Ht+j}, C_{Ht+j}, L_{Ht+j})$ is a function of durable consumption (D_{Ht+j}), nondurable consumption (C_{Ht+j}), and labor supply (L_{Ht+j}). The period utility function takes the form of

$$u_t = \frac{\left[\left(\mu^{\frac{1}{\zeta}} D_{Ht}^{\frac{\zeta-1}{\zeta}} + (1-\mu)^{\frac{1}{\zeta}} C_{Ht}^{\frac{\zeta-1}{\zeta}} \right)^{\frac{\zeta}{\zeta-1}} - \rho L_{Ht}^\nu \right]^{1-\sigma}}{1-\sigma}. \quad (5)$$

It is an augmented GHH utility function with consumption as a CES composite of durable and nondurable consumption. The stock of durable consumption is a function of the Home (D_{Ht}^H) and Foreign (D_{Ht}^F) durable consumption stocks

$$D_{Ht} = \left[\psi^{\frac{1}{\theta}} (D_{Ht}^H)^{\frac{\theta-1}{\theta}} + (1-\psi)^{\frac{1}{\theta}} (D_{Ht}^F)^{\frac{\theta-1}{\theta}} \right]^{\frac{\theta}{\theta-1}}, \quad (6)$$

where ψ is the weight of Home durable goods in the durable consumption stock and θ is the elasticity of substitution between the Home and Foreign durable goods. The law of motion for durable consumption is

$$D_{Ht+1}^k = (1 - \delta_D) D_{Ht}^k + d_{Ht}^k, \quad (7)$$

where $k \in \{H, F\}$ denotes the Home and Foreign countries. d_{Ht}^k is the k -country durable consumption goods purchased by the household at time t . As in Erceg and Levin (2006) and Whelan (2003), the household also has to pay a cost to adjust the durable consumption stock

$$\Delta_{Ht}^k = \frac{1}{2} \phi_1 (d_{Ht}^k - \delta_D D_{Ht}^k)^2 / D_{Ht}, \quad (8)$$

where Δ_{Ht}^k is the cost of changing durables produced by country k .¹³

If there were no adjustment costs to durables, durable consumption purchases would be very volatile in response to shocks. Empirical work (see for example, Mankiw (1982) and Gali (1993)), finds that durable consumption adjusts more smoothly and is less volatile than a model with no adjustment costs would imply. Gali (1993) suggests that adjustment costs may account for the excess smoothness of durable consumption, and indeed Startz (1989) finds that adjustment costs can account for the behavior of durable consumption in a permanent income model. Bertola, Guiso, and Pistaferri (2005) find support on micro level data for a model with a fixed cost of adjustment. Aggregate consumption is not likely to exhibit the same lumpiness

¹³Adjustment costs are scaled by the total durable consumption stock (D_{Ht}) so that the cost of adding new durable consumption ($d_{Ht}^H - \delta_D D_{Ht}^H$ and $d_{Ht}^F - \delta_D D_{Ht}^F$) is the same for both types of durable consumption. The same format is also used in the capital adjustment cost functions.

as micro data, so we adopt the standard quadratic adjustment cost formulation (as in Startz(1989).)

The law of motion for capital stocks in the durable and nondurable sectors is given by

$$K_{Ht+1}^{jk} = (1 - \delta)K_{Ht}^{jk} + I_{Ht}^{jk}, \quad (9)$$

where $j \in \{D, N\}$ and $k \in \{H, F\}$. We follow the literature to include capital adjustment costs in our model.

In the Home country, it takes the following form

$$\Lambda_{Ht}^{jk} = \frac{1}{2}\phi_2 \left(I_{Ht}^{jk} - \delta K_{Ht}^{jk} \right)^2 / K_{Ht}^j, \quad (10)$$

where $j \in \{D, N\}$ and $k \in \{H, F\}$. Symmetric adjustment costs exist in the Foreign country.

The Home and Foreign countries can only trade real bonds, which are in terms of the Home durable goods. It is well known that transient shocks have a permanent wealth effect in an open-economy model with incomplete international financial markets. To make our model stationary, we follow Heathcote and Perri (2002) to introduce a quadratic bond holding cost $(\frac{1}{2}\Phi B_{Ht+1}^2)$. Φ is very close to zero and the cost does not affect any results in our model.¹⁴

For the given production structure, the household's budget constraint is

$$\begin{aligned} & P_{Ht}^N C_{Ht} + P_{Ht}^{DH} \left(d_{Ht}^H + \Delta_{Ht}^H + I_{Ht}^{NH} + \Lambda_{Ht}^{NH} + I_{Ht}^{DH} + \Lambda_{Ht}^{DH} + \frac{B_{Ht+1}}{1+i_t} + \frac{1}{2}\Phi B_{Ht+1}^2 \right) \\ & + P_{Ht}^{DF} (d_{Ht}^F + \Delta_{Ht}^F + I_{Ht}^{NF} + \Lambda_{Ht}^{NF} + I_{Ht}^{DF} + \Lambda_{Ht}^{DF}) \\ & \leq W_{Ht} L_{Ht} + P_{Ht}^{DH} B_{Ht} + R_{Ht}^{NH} K_{Ht}^{NH} + R_{Ht}^{NF} K_{Ht}^{NF} + R_{Ht}^{DH} K_{Ht}^{DH} + R_{Ht}^{DF} K_{Ht}^{DF}, \end{aligned} \quad (11)$$

where P_{Ht}^{DF} is price of Foreign-country produced durable goods, which is in terms of the Home country's currency. i_t is the return to the real bond B_{Ht+1} . Subject to this budget constraint, the household maximizes expected lifetime utility.

3.3 Other Equilibrium Conditions

Nondurable goods can only be used for domestic nondurable consumption. So the market clearing condition for Home nondurable goods is

$$Y_{Ht}^N = C_{Ht}. \quad (12)$$

¹⁴There are several other techniques used in the literature to deal with this nonstationarity problem. See Schmitt-Grohé and Uribe (2003) for more discussions.

Durable goods are used for durable consumption and capital investment in both countries. We also assume there is an iceberg trade cost for international trade. Only a fraction $1 - \tau$ of goods arrives in the destination country, so the market clearing condition for Home durable goods is

$$Y_{Ht}^D = d_{Ht}^H + \Delta_{Ht}^H + I_{Ht}^{NH} + \Lambda_{Ht}^{NH} + I_{Ht}^{DH} + \Lambda_{Ht}^{DH} + \frac{1}{2}\Phi B_{Ht+1}^2 + \frac{d_{Ft}^H + \Delta_{Ft}^H + I_{Ft}^{NH} + \Lambda_{Ft}^{NH} + I_{Ft}^{DH} + \Lambda_{Ft}^{DH} + \frac{1}{2}\Phi B_{Ft+1}^2}{1 - \tau}. \quad (13)$$

The labor and bond markets clearing conditions are

$$L_{Ht} = L_{Ht}^N + L_{Ht}^D \quad (14)$$

$$B_{Ht} + B_{Ft} = 0. \quad (15)$$

We assume that after taking into account the trade cost, the law of one price holds

$$P_{Ht}^{DF} = \frac{S_t P_{Ft}^{DF}}{1 - \tau} \quad (16)$$

$$\frac{P_{Ht}^{DH}}{S_t(1 - \tau)} = P_{Ft}^{DH}, \quad (17)$$

where P_{Ht}^{DF} is the price of Foreign durable goods in the Home country. S_t is the nominal exchange rate defined as the value of one unit of Foreign currency in terms of the Home currency.

In section 5, we report real exchange rates based on the consumer price index (CPI). In the Home country, the CPI is defined by:

$$P_{Ht} = (P_{Ht}^N)^{\omega_1} (P_{Ht}^{DH})^{\omega_2} (P_{Ht}^{DF})^{\omega_3}, \quad (18)$$

where ω_1 is the steady-state expenditure share of nondurable consumption. ω_2 and ω_3 are respectively the steady-state expenditure shares of Home and Foreign durable consumption. This is not the same as the utility based CPI, but is closer to the CPI measure used in national accounts. The CPI deflated real exchange rate is defined by

$$Q_t = \frac{S_t P_{Ft}}{P_{Ht}}. \quad (19)$$

To solve our model, we divide all nominal prices in the Home country by the price of nondurable goods (P_{Ht}^N). That is, we use the nondurable good as numeraire. In the Foreign country, all nominal prices are divided by the price of Foreign nondurable goods (P_{Ft}^N).

4 Calibration

We calibrate our model such that in the steady state, the structure of the economy is the same as in Figure 2. Details about how to solve the steady state can be found in Appendix A.2.2. In our benchmark economy, nondurable goods account for 60% of total output and durable goods account for the remaining 40%. Among the durable goods, half of them are used for consumption (equivalent to 20% of total output) and the other half are used for investment (equivalent to 20% of total output).¹⁵ Among durable consumption goods, 65% are used for domestic consumption (equivalent to 13% of total output) and 35% are used for exports (equivalent to 7% total output). Among durable investment goods, 70% are used for domestic investment (equivalent to 14% of total output) and 30% are used for exports (equivalent to 6% of total output). In this economy, investment accounts for 20% of total output and consumption (durable plus nondurable) accounts for the remaining 80%. The trade share of output is 13%. Those features match the US data closely.

Table 4 shows parameter values that we use to match our benchmark model with the described economy structure. We set the shares of home goods in capital (α) and durable consumption (ψ) at 50%. That is, there is no home bias exogenously built in our economy structure. Instead, we generate the observed low trade share from the iceberg trade cost τ . We will discuss this more later. As in Backus, Kehoe, and Kydland (1992), the capital share in production ($\chi = \epsilon$) is set to 36%, and the subjective discount factor is set to 0.99, which gives a 4% annual real interest rate. The depreciation rate of durable consumption (δ_D) is set to 0.05, which implies a 20% annual depreciation rate for consumption durables. A similar depreciation rate has been used in Bernanke (1985) and Baxter (1996).

Given those parameters, we choose other parameters to match the economy structure as in Figure 2. We first choose the preference parameter μ and the depreciation rate of capital (δ) jointly to match the relative size of durable and nondurable good sectors, and the size of investment in durable goods. μ is set to 0.23 and δ is set to 0.013 such that 1. the durable good sector accounts for 40% of total output and, 2. the investment accounts for 50% of durable goods, or equivalently 20% of total output. Consumption durables account for the remaining 50% of durable goods, or equivalently 20% of total output.

The trade cost (τ) and the elasticity of substitution between the home and foreign goods are calibrated

¹⁵Durable consumption in our calibration is higher than the US data, which is about 15% of output. However, many goods with characteristics of durables—such as shoes and clothing—are classified as nondurables in the data.

to match two empirical findings: 1. the trade share of total output is about 13%; 2. the long-run elasticity of substitution between the home and foreign goods is high. In our calibration, the long-run elasticity of substitution between the home and foreign capital (γ) is set to 9.1. The elasticity of substitution between the home and foreign durable consumption (θ) is set to 6.85. In the steady state, the trade in capital goods (durable consumption goods) accounts for 46% (54%) of total trade. The above calibration of γ and θ implies an overall elasticity of 7.9, which is the same as in Head and Reis (2001).¹⁶ The trade cost (τ) is calibrated to 0.1, that is, 90% of goods arrive in their destination countries in the international trade. For given γ and θ , this trade cost generates a trade share of 13%.

We use different values for γ and θ to generate different home bias levels for capital and durable consumption. Capital is more biased towards home goods than durable consumption (70% vs 65%). For given trade cost, the degree of home bias increases with the elasticity of substitution. So we assign a higher elasticity of substitution to capital goods. Alternatively, we can assume the same elasticity of substitution, but higher trade cost for capital goods. In either method, capital can have a higher level of home bias than durable consumption. We used the first method because it matches a pattern observed in the data. For a given decrease in trade cost, the first method predicts that the share of investment goods in international trade increases relative to the share of durable consumption. Intuitively, investment goods are more substitutable across countries than durable consumption under this setup. So when the trade cost decreases, there is more substitution for investment goods than for durable consumption. As a result, the share of investment goods in the trade increases. The same pattern is also found in the US data: from 1994 to 2006-the share of capital goods except automotive in total export goods increased from 34.4% to 45.1%.¹⁷

The preference parameters σ and ν are set to their standard levels used in the GHH utility function. The parameter ρ is chosen such that the labor supply is one third in the steady state. We assume that the elasticity of substitution between the durable and nondurable consumption is low ($\zeta = 1.1$).¹⁸ The adjustment cost parameters of durable consumption (ϕ_1) is chosen to match the volatility of durable consumption, which is about three times as volatile as output in the data. The adjustment cost of capital stock (ϕ_2) is calibrated to match the volatility of investment, which is about three times as volatile as output in the data.

We follow Erceg and Levin (2006) in calibrating the productivity shocks in the durable and nondurable goods sectors. However, there is no information about the cross-country spillovers of those shocks in their closed-economy model. Empirical findings usually suggest small cross-country spillovers. For instance,

¹⁶ $9.1 \times 46\% + 6.85 \times 54\% \approx 7.9$.

¹⁷The data are from Haver Analytics (US International Transactions). Of course, this pattern is also consistent with another explanation: the trade cost decreases more for capital goods than for durable consumption goods.

¹⁸Whelan (2003) calibrates this parameter to be 1. Baxter (1996) finds that a reasonable range for this variable is between 0.5 and 2.5.

Baxter and Crucini (1995) find no significant international transmission of shocks, except for possible transmission between US and Canada. In Kollman's (2004) estimate between the US and three EU countries, the spillover is 0.03. In Corsetti, Dedola, and Leduc (forthcoming), the spillover is -0.06 for traded goods and 0.01 for nontraded goods. We will first set those spillovers at zero and then choose some values used in the literature to check whether our results are robust under different shock structures.

Let A_{it}^N and A_{it}^D be respectively, the productivity shocks in nondurable and durable good sectors of country $i \in \{H, F\}$. They follow univariate $AR(1)$ processes in the benchmark model

$$A_{it+1}^N = \Xi_1 A_{it}^N + \varepsilon_{it+1}^N \quad (20)$$

$$A_{it+1}^D = \Xi_2 A_{it}^D + \varepsilon_{it+1}^D. \quad (21)$$

As in Erceg and Levin (2006), the $AR(1)$ coefficient Ξ_1 is set to 0.87 and Ξ_2 is set to 0.9. The variance-covariance matrix of innovations $[\varepsilon_{Ht}^N \ \varepsilon_{Ht}^D \ \varepsilon_{Ft}^N \ \varepsilon_{Ft}^D]'$ takes the form of

$$\Sigma = \begin{bmatrix} \sigma_N^2 & \sigma_{DN} & \rho_N \times \sigma_N^2 & 0 \\ \sigma_{DN} & \sigma_D^2 & 0 & \rho_D \times \sigma_D^2 \\ \rho_N \times \sigma_N^2 & 0 & \sigma_N^2 & \sigma_{DN} \\ 0 & \rho_D \times \sigma_D^2 & \sigma_{DN} & \sigma_D^2 \end{bmatrix} \quad (22)$$

where σ_N^2 is the variance of ε_{Ht}^N (ε_{Ft}^N). σ_D^2 is the variance of ε_{Ht}^D (ε_{Ft}^D) and σ_{DN} is the covariance. As in Erceg and Levin (2006), the standard deviation of ε_{Ht}^N (σ_N) is 0.0096 and it is 0.036 for σ_D . Within each country, the innovations are correlated across sectors. The correlation $\frac{\sigma_{DN}}{\sigma_D \sigma_N}$ is set to 0.29 as in Erceg and Levin (2006). The cross-country correlation of innovations in durable good sector (ρ_D) is 0.258 by following BKK and it is set to zero in nondurable good sector ($\rho_N = 0$). (Corsetti *et. al.* (forthcoming) estimate ρ_N to be zero.) This shock structure corresponds to the Benchmark model in Table 5.

Corsetti, Dedola, and Leduc (forthcoming) find a larger ρ_D in their estimates. In the model High Correlation of Table 5, we change ρ_D to their value of 0.468. We also release the constraint of no spillovers

in the following two exercises. The process of shocks is modified to a $VAR(1)$ format

$$A_{Ht+1}^N = \Xi_1 A_{Ht}^N + \Xi_3 A_{Ft}^N + \varepsilon_{Ht+1}^N \quad (23)$$

$$A_{Ht+1}^D = \Xi_2 A_{Ht}^D + \Xi_3 A_{Ft}^D + \varepsilon_{Ht+1}^D \quad (24)$$

$$A_{Ft+1}^N = \Xi_1 A_{Ft}^N + \Xi_3 A_{Ht}^N + \varepsilon_{Ft+1}^N \quad (25)$$

$$A_{Ft+1}^D = \Xi_2 A_{Ft}^D + \Xi_3 A_{Ht}^D + \varepsilon_{Ft+1}^D, \quad (26)$$

where coefficient Ξ_3 is the cross-country spillover of productivity shocks.¹⁹ BKK find a relatively large spillover of 0.088. In our first exercise, we set Ξ_3 to this value. This corresponds to the model High Spillover in Table 5. In the second exercise, we set Ξ_3 at a medium level of 0.044. Its results are reported under the model Medium Spillover in Table 5.

5 Model Performance

The model is solved and simulated using the first-order perturbation method. The model’s artificial time series are logged (except for net exports) and Hodrick-Prescott (H-P) filtered with a smoothing parameter of 1600. The reported statistics in this section are averages across 100 simulations. Our benchmark model performs well in three broad categories. First, the model can match the observed IRBC statistics, including the “trade volatility” and “positive comovement” of imports and exports as documented in Section 2.1. Second, the model can replicate the elasticity puzzle in the trade literature. Finally, our model can replicate the Backus-Smith puzzle and offers some new insights on this puzzle.

5.1 International RBC Statistics

Table 5 shows simulation results for six models. All of these models can match data fairly well.

5.1.1 Benchmark Model

As standard IRBC models, our benchmark model can replicate the volatility (relative to that of GDP) of aggregate variables such as consumption, investment, durable consumption, and labor. In addition, our model matches the trade sector data much better than the standard models: imports and exports are about three times as volatile as GDP; and both of them are pro-cyclical and positively correlated with each other. Our model can also match the well-known finding that net exports are counter-cyclical.

¹⁹As in Erceg and Levin (2006), we assume the cross-sector spillover is still zero.

When productivity shocks are persistent, it is well understood that investment will be volatile. Agents wish to change the capital stock quickly to take advantage of current and anticipated productivity shocks. This effect contributes to the high volatility our model produces for imports and exports, because capital goods are traded. A positive productivity shock leads to a desire to increase Home’s stock of domestically produced and foreign produced capital. This leads to the increase in demand for imports when there is a positive productivity shock. A positive productivity shock also increases the supply of Home’s export good, lowering its world price, and thus increasing exports.

These effects are standard in RBC models, and explain why the models can generate procyclical imports and exports. However, if only investment goods are durable, and consumption goods are nondurable, the model does not produce sufficient volatility in imports and exports. For instance, if we change the depreciation rate of durable consumption (δ_D) to one and the adjustment cost to zero, the (relative) standard deviation of imports and exports decreases from 2.6 to 2.²⁰ When we introduce a consumer durable sector, there is an additional source of volatility. Demand for consumer durables, like demand for investment goods, is forward looking. It is not expected productivity per se, but rather higher wealth from higher expected future income that leads to volatility in demand for durable consumer goods.

Figure 3 shows impulse response functions of our benchmark model for a one-standard-deviation shock in home durable good sector. In the face of a positive shock in home durable good sector, the price of durable goods (relative to nondurable goods) decreases, which leads to substitution from nondurables to durables. Because the shock is persistent, there is also a significant wealth effect that pushes up demand for both home and foreign durable consumption goods. As a result, consumption of durable goods (both home- and foreign-produced durable consumption goods) in the home country increases while consumption of nondurable goods declines. The aggregate consumption in the home country rises because the increase of durable consumption exceeds the decline of nondurable consumption. The price of foreign-produced durables relative to home-produced durables also increases: the terms of trade (import prices divided by export prices) increases in Figure 3. The change in the terms of trade leads to substitution toward home-produced durables. As a result, the foreign country consumes more home durable goods, though the foreign aggregate consumption declines. Similarly, the home country also shifts from foreign-produced durable goods toward home-produced durable goods because of this substitution effect. Overall, the wealth effect and the effect of the decline in the price of durables relative to nondurables lead to an increase in import demand, despite the increase in

²⁰In this exercise, the capital adjustment cost is changed such that the (relative) standard deviation of investment is the same as in our benchmark model (2.6). We also change the elasticity of substitution between the home and foreign consumption goods to 0.9, which reflects the fact that the short-run elasticity of substitution is low in our benchmark model due to adjustment costs.

the price of foreign durables relative to home durables. Indeed, total expenditure on imports increases more than the value of exports, leading to a decline in the trade balance. However, part of that increase in import expenditure comes from the increased price of imports. But overall, the model still generates procyclical movements of import and export quantities.

Our benchmark model can also match trade dynamics fairly well. Figure 4 shows the correlations between GDP and real imports, exports and net exports at various leads/lags for the US data and the data simulated from our benchmark model. As noted by Ghironi and Melitz (2007), the correlation between GDP and imports exhibits a tent-shaped pattern, while the correlations of exports and net exports with GDP are S-shaped.²¹ Our model captures these qualitative patterns well. Note in particular that the model captures the fact that, while current imports are positively correlated with GDP, imports are negatively correlated with lagged GDP at longer horizons. However, our model's correlation of both imports and exports with lagged GDP declines quickly - too quickly - as the horizon increases. It appears especially that exports increase with a lagged response to a positive shock to GDP. It might be possible to capture this dynamic behavior by incorporating a lag between orders of durable goods and delivery.

5.1.2 Alternative Specifications

The performance of our model is robust under alternative calibrations in Table 5. Simulation results barely change in the model of High Correlation when the cross-country correlation of innovations in durable good sector increases from 0.258 of the benchmark level to 0.468 as in Corsetti, Dedola, and Leduc (forthcoming). A noticeable difference between our benchmark model and the model with high cross-country spillover of technology shocks (High Spillover in Table 5) is that the volatility of imports and exports decreases when we allow spillovers.²² This result is consistent with BKK's finding that net exports become less volatile when cross-country spillovers increase. But even when we set the spillover coefficient at 0.088, which is relatively large in the literature, imports and exports are still about two times as volatile as output. If we set the spillover coefficient to a moderate level of 0.044 (Medium Spillover in Table 5), the simulation results are very close to our benchmark results.

In all of our calibrations, we note the following shortcomings: As in almost all RBC models, real exchange rate volatility is still lower than in the data. However, our model does quite well relative to the literature. The standard deviation of the real exchange rate in our benchmark model is roughly 50% of the standard deviation in the data. Across all specifications, our model produces somewhat lower correlations of real imports with

²¹Ghironi and Melitz (2007) have also implicitly observed the procyclicality of imports and exports in their Figure 1.

²²The difference is more significant if we keep the adjustment costs the same across models.

GDP than appear in the data. And, perhaps as a consequence, net exports are not as negatively correlated with GDP as in the data.

Cross-country output correlation is nearly zero in the standard IRBC models,²³ though this correlation is usually large in the data. Our model provides little insight on this issue. We find that the cross-country correlation of output increases if we allow innovations to be highly correlated across countries. Our motivation here is that Solow residuals measure productivity shocks with considerable error. To the extent that the measurement errors are uncorrelated across countries, the measured cross-country correlation of productivity may be severely downward biased. If we set cross-country correlation of innovations to 0.7 for both durable good and nondurable good sectors (High Correlation 2 in Table 5), the cross-country output correlation increases from 0.01 to 0.56, which is very close to the data. Indeed, most aspects of the model hold up well under this alternative specification, with the notable exception of real exchange rate volatility which is much lower than in other parameterizations. In particular, the volatility of imports and exports and their correlation with GDP do not decline. We emphasize that we have not chosen the correlation of productivity shocks under this parameterization to match data. Further examination of the measurement of productivity shocks is warranted, but we leave this to future work.

We also considered a different model for the adjustment costs of capital and durable consumption stocks (New Costs in Table 5). Under this setup, it is costly to adjust the proportion of home to foreign capital (durable consumption). This is a crude way of capturing the notion that it takes time to change technologies. As a result, the proportion of home to foreign durables only changes gradually. Ramanarayanan (2007) models this idea more explicitly with a putty-clay technology. In addition, we use adjustment costs for the total stock of capital (durable consumption) to match the volatility of investment in capital (durable consumption). This new setup generates results similar to our benchmark model. Cross-country output correlation in New Costs model (0.08) comes slightly closer to the data than in the benchmark model (0.01). However we also need to note that we have more freedom in calibrating “New Costs” model because it has more cost parameters than our benchmark model.

5.2 Elasticity Puzzle

The elasticity of substitution between home and foreign goods is defined as the percentage change of demand for imports relative to home goods, given a one percent change of the import price relative to the home-good price. Two methods have been used in the literature to estimate this elasticity. In the literature of trade liberalization, studies investigate how much the demand for foreign goods increases after a permanent

²³For instance, the cross-country output correlation in BKK (1992) is -0.18.

relative price change caused by tariff reduction. In the data, the trade share of output increases substantially over time after a small but permanent decrease in the tariff. This empirical finding suggests that home and foreign goods are highly substitutable. So the estimates from this strand of literature range from 6 to 15 with an average of 8. For instance, see Feenstra and Levinsohn (1995), Head and Ries (2001), Lai and Trefler (2002).²⁴

In another strand of literature, the same elasticity is estimated from transitory relative price changes at the business cycle frequency. We show with a simple example in Appendix A.3 that under a general setup used in the literature, those two methods are estimating the same parameter. However, estimates from business cycle frequency data are much smaller. For instance, the cross-industry average in Reinert and Roland-Holst (1992) is 0.91 and it is 0.81 in Blonigen and Wilson (1999). In aggregate models, Heathcote and Perri (2002) find a point estimate of 0.9. Bergin (2006) estimates a New Open Economy Macro model and obtains an estimate of 1.13. These findings have been labeled as the “elasticity puzzle” in the trade literature.

Several studies have offered explanations for this puzzle with a common feature that the long-run elasticity of substitution is high, but the short-run elasticity is low due to some market frictions. Ruhl (2005) proposes a model in which firms have to pay a fixed cost to change their export status. Benefits from changing export status are not enough to recover the fixed cost under transitory shocks. So the elasticity of substitution between the home and foreign goods is low when shocks are transitory. However, in the face of persistent shocks, firms will pay the fixed cost and change their export status, which leads to a large increase of trade share even for a small, but permanent price change. Drozd and Nosal (2007) use the friction of international marketing to reduce the response of output to relative price changes. Ramanarayanan (2007) models this problem from the side of importers. In his model, importers use foreign goods as intermediate inputs in production. Home and foreign intermediate goods are perfectly substitutable in the long run, but switching between them in the short run is very costly. Our model is closely related. We follow the same idea in our model, where we assume that the home and foreign goods are highly substitutable in the long run, but in the short run there is a quadratic cost for adjusting the durable consumption and capital stocks. Unlike the above studies, we do not provide a micro-story for the market friction. Our contribution is quantitative. After calibrating the adjustment costs to match the volatility of durable consumption and investment, we investigate whether our model can also deliver a reasonable short-run elasticity of substitution.

²⁴Yi (2003) also points out that to replicate this empirical finding in a general equilibrium (GE) model, we need an elasticity of more than 14, which is counterfactually high. He argues that measured trade grossly overstates the value added component of exports, because many exports include a lot of imported contents due to vertical specialization. This overcounting of trade may be able to explain why a small tariff reduction leads to a large increase of trade share in the data.

To calculate the short-run elasticity of substitution, we regress the (log) relative demand on the (log) relative price. We need the following variables in our regression: demand for foreign goods, domestic demand for home goods and the relative price. The demand for foreign goods is measured by real imports (RIM_t). The domestic demand for home goods is measured by domestic absorption (DA_t), which is calculated by subtracting real imports from the sum of consumption and investment

$$DA_{Ht} = TC_{Ht} + I_{Ht} - RIM_{Ht}, \quad (27)$$

where TC_{Ht} and I_{Ht} are total consumption and investment respectively. We define the price of domestic absorption as

$$P_{Ht}^{DA} = (P_{Ht}^N)^{\frac{\omega_1}{\omega}} (P_{Ht}^{DH})^{\frac{\omega - \omega_1}{\omega}}, \quad (28)$$

where ω_1 is the steady-state expenditure share of nondurable consumption, and ω is the share of domestic absorption in total output. So $\frac{\omega_1}{\omega}$ is the expenditure share of nondurable goods in domestic absorption and $\frac{\omega - \omega_1}{\omega}$ is the expenditure share of durable goods in total absorption.

We simulate our model and regress $\log\left(\frac{RIM_t}{DA_t}\right)$ on $\log\left(\frac{P_{IMt}}{P_{DA_t}}\right)$, where P_{IMt} is import price.²⁵ The estimated short-run elasticity of substitution is 1.05 with a standard error of 0.20. The short-run elasticity of substitution implied by our model is very close to what is found in the empirical studies with business-cycle-frequency data, such as Bergin (2006) and Heathcote and Perri (2002). It is not surprising, of course, that we are able to generate an elasticity that is lower in the short run than in the long run by introducing costs of adjustment. Our point is simply that in a model in which trade is in durables, this is natural and accords with a long tradition in macroeconomics of modeling the gradual accumulation of capital. That is, the trade elasticity puzzle is easy to understand in a context in which trade is in durables which are accumulated slowly over time.

5.3 Backus-Smith Puzzle

When agents can trade a complete set of contingent claims, but face potentially different goods prices, in a variety of contexts models imply that relative cross-country consumption should be perfectly positively correlated with the real exchange rate. Backus and Smith (1993) demonstrate this result in a model with

²⁵A constant is also added in the regression. As in empirical studies, our estimate is subject to the endogeneity problem. We do not control this problem here, because the goal of this exercise is to find whether we can replicate empirical findings instead of obtaining the true elasticity in our model.

nontraded goods, while Chari, Kehoe, and McGrattan (2002) show that even a DSGE model with incomplete financial markets implies a strong but imperfect positive correlation. But, beginning with Backus and Smith (1993), several studies find empirically that the correlation between relative consumption and the real exchange rate is generally low, even negative in many countries. Some recent papers offer models to explain this correlation when capital markets are not perfect, and only bonds are traded, for instance, Corsetti, Dedola and Leduc (forthcoming), and Benigno and Thoenissen (2007). Our model shares some of the features of these models, but also offers some new insight: the introduction of consumer durables raises interesting issues about how consumption should be measured in tests of the Backus-Smith puzzle.

In this paper, we can also replicate the Backus-Smith empirical findings. The dynamics of consumption and the real exchange rate in response to a shock to productivity in the durable sector look very much like those in Benigno and Thoenissen (2007). As shown in Figure 3, a positive shock lowers the price of the durable export (the terms of trade deteriorate), and because of home bias, that tends to work toward a real CPI depreciation. But that effect can be more than offset by the increase in the relative price of nondurable goods, which are not traded across countries. There are two forces working to push up the price of non-traded goods: First, there is the traditional Balassa-Samuelson effect. The increase in productivity pushes up the real wage, thus pushing up the relative price of non-tradables. In addition, overall consumption in the home country increases from a wealth effect, because higher productivity increases lifetime income for the home country. Even if there were no factors mobile between sectors, that would tend to push up the price of the nontradable goods, and help foster a real appreciation. We have that aggregate consumption is increasing, and under our calibrations, a real appreciation – these correspond to the data.

However, our model also offers some new insight on this puzzle. The durable consumption measured in national accounts data is expenditures on new durable consumption goods. However, it is the service flow from the *stock* of durable consumption that enters the utility function. As emphasized by Obstfeld and Rogoff (2006, page 98), the consumer smooths the service flow from the stock of durable consumption, instead of the path of expenditures on durables. As in the data, the total consumption is measured by the sum of nondurable consumption and the investment in durable consumption

$$TC_{Ht} = C_{Ht} + DC_{Ht}, \tag{29}$$

where TC_{Ht} is the total consumption in Home country. C_{Ht} is nondurable consumption and DC_{Ht} is durable

consumption. Durable consumption is defined as the sum of Home- and Foreign-good durable consumption

$$DC_{Ht} = \hat{P}_{Ht}^{DH} (d_{Ht}^H + \Delta_{Ht}^H) + \hat{P}_{Ht}^{DF} (d_{Ht}^F + \Delta_{Ht}^F). \quad (30)$$

From the utility function, we know the “true” consumption (utility consumption) is

$$UC_{Ht} = \left(\mu^{\frac{1}{\zeta}} D_{Ht}^{\frac{\zeta-1}{\zeta}} + (1-\mu)^{\frac{1}{\zeta}} C_{Ht}^{\frac{\zeta-1}{\zeta}} \right)^{\frac{\zeta}{\zeta-1}}. \quad (31)$$

We calculate the correlation of 1. the (log) CPI-based real exchange rate and the (log) relative total consumption ($\log(TC_{Ht}) - \log(TC_{Ft})$), and 2. the utility-based real exchange rate and the (log) relative utility consumption ($\log(UC_{Ht}) - \log(UC_{Ft})$).²⁶ The correlation between the real exchange rate and total consumption differential ($\log(TC_{Ht}) - \log(TC_{Ft})$) is -0.23. So our model can replicate the negative correlation between the real exchange rate and consumption documented in the data. However, the correlation between the utility-based real exchange rate and the utility consumption differential ($\log(UC_{Ht}) - \log(UC_{Ft})$) is 0.26. Based on the fact that the financial market is limited to trade in non-state-contingent real bonds and leisure is nonseparable in the utility function, a correlation of 0.26 still implies a relatively good amount of risk sharing between the Home and Foreign countries.

It is interesting that true consumption acts more like it does in the model with complete contingent claims, though measured relative consumption and the real exchange rate are negatively correlated. We do not see an increase in utility consumption after a positive shock. In fact, it may decrease. First, consumption of services from durables cannot change, because it is predetermined by the stock of durables. While there is a positive wealth effect that would tend to increase the consumption of nondurables, this is more than offset by the increase in their relative price. That is, the substitution effect dominates the wealth effect, and demand for nondurables falls. As shown in the impulse response functions of Figure 3, the consumption of nondurable goods decreases in the face of a one-standard-deviation shock in the durable good sector, in that the substitution effect dominates the wealth effect.²⁷ As a result, nondurable consumption is positively correlated with the real exchange rate in our model. We calculate the correlation between nondurable consumption and the real exchange rate for Canada, Japan, UK, and US.²⁸ It is positive for Canada, Japan and US (0.22 in Canada, 0.09 in Japan, and 0.15 in US), but negative for UK (-0.04). Though our

²⁶Please see Appendix A.4 for details about how to calculate the utility-based real exchange rate.

²⁷If the shock is very persistent, the wealth effect could dominate the substitution effect and the nondurable consumption increases.

²⁸Due to data restrictions, we only consider these four countries. The data for Canada is from Statistics Canada from 1973Q1 to 2007Q4. The data for Japan is from Japan Cabinet Office from 1994Q1 to 2008Q1. The data for UK is from Office for National Statistics from 1972Q1 to 2007Q1. US data is from Bureau of Economic Analysis from 1973Q1 to 2008Q1.

preliminary results are mixed, we believe this is an interesting avenue for exploration in empirical work on the Backus-Smith puzzle.

6 Conclusion

The behavior of imports and exports is, of course, a key component of the linkages among economies. Our model confronts and, to a degree, successfully explains some strong empirical regularities. By modeling trade in durables, we can understand the high volatility of imports and exports relative to output. Trade in durables also offers a natural explanation for the trade elasticity puzzle – that the response of imports to changes in the terms of trade is low at business cycle frequencies, but is high when considering the long-run effect of permanent price changes. Our model performs well compared to other models, because it offers an explanation that is also consistent with the observation that imports and exports are both procyclical, and positively correlated with each other, even when the terms of trade and real exchange rate are as volatile as in the data.

We believe the forward-looking nature of investment decisions and decisions to purchase consumer durables are a key feature of trade behavior. Our model noticeably fails to account for the high correlation of output across countries, which is a failure shared by essentially all rational expectations equilibrium models. However, we think that modeling trade as durables may still be a promising avenue for dealing with this puzzle as well, through channels that are not explored in this paper. One possibility is that while the common (across countries) component of productivity shocks may account for a small share of the variance of productivity, it may be that agents typically receive strong signals about the future common component. If news helps to drive business cycles (as in Beaudry and Portier, 2005), then perhaps news about the common component of productivity shocks helps contribute to the high correlation of business cycles across countries. News about future productivity is especially important for durables, so the impact of news may be especially strong on the investment and consumer durables sectors.

Another avenue that may deserve further exploration is a model with nominal price stickiness, as in DSGE models. Our model of durable trade creates large swings in demand for imports, which indeed is what allows it to account for trade volatility. But an increase in Home demand for Foreign output has only a small effect on Foreign’s output level. Instead, in our model, prices adjust so that more of Foreign’s output is channeled toward Home. In a model with sticky prices, changes in demand may lead to changes in aggregate output, and so create a channel for international spillovers. While these channels do exist in current DSGE models, they are not strong because the models do not account for large procyclical movements in imports

and exports.

It is an empirical fact that a large fraction of trade is in durables. Indeed, we view explaining this phenomenon - rather than assuming it, as we do in this study - to be another interesting topic for future research. What we have accomplished here is to demonstrate that trade in durables significantly alters the behavior of imports and exports in an RBC model in a way that can account for some striking empirical facts.

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Figure 1: Production Structure of Standard Models

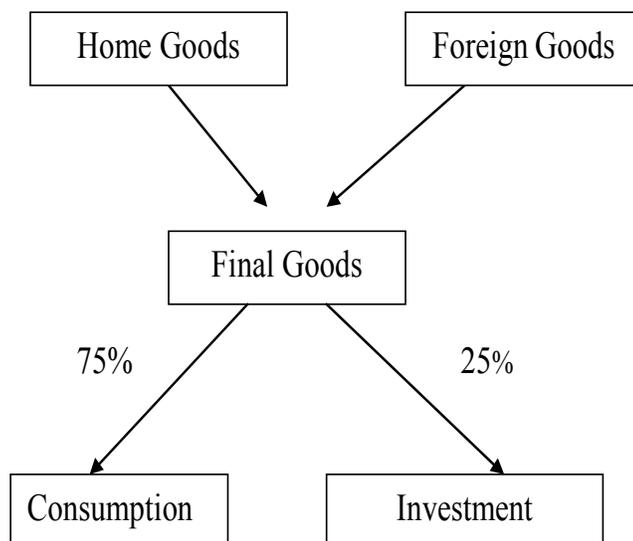


Figure 2: Structure of Benchmark Model

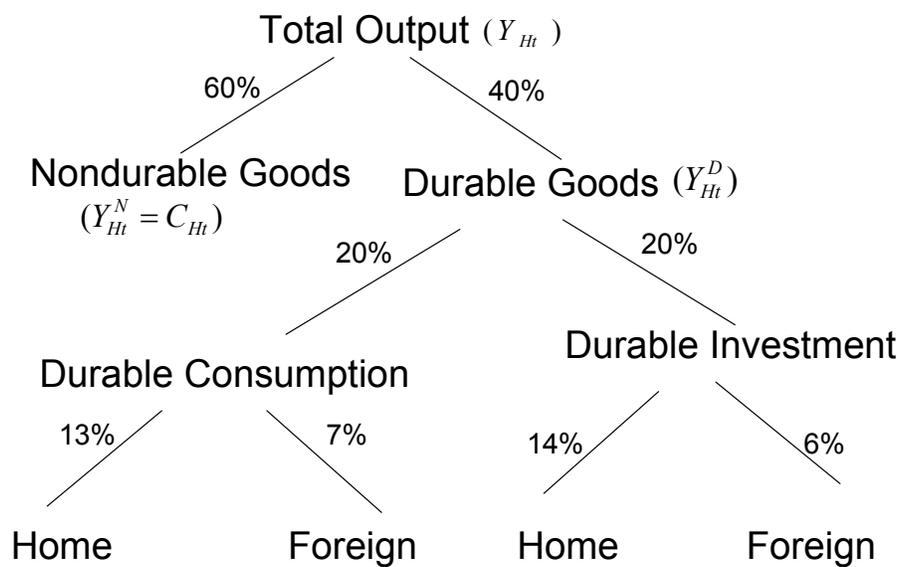
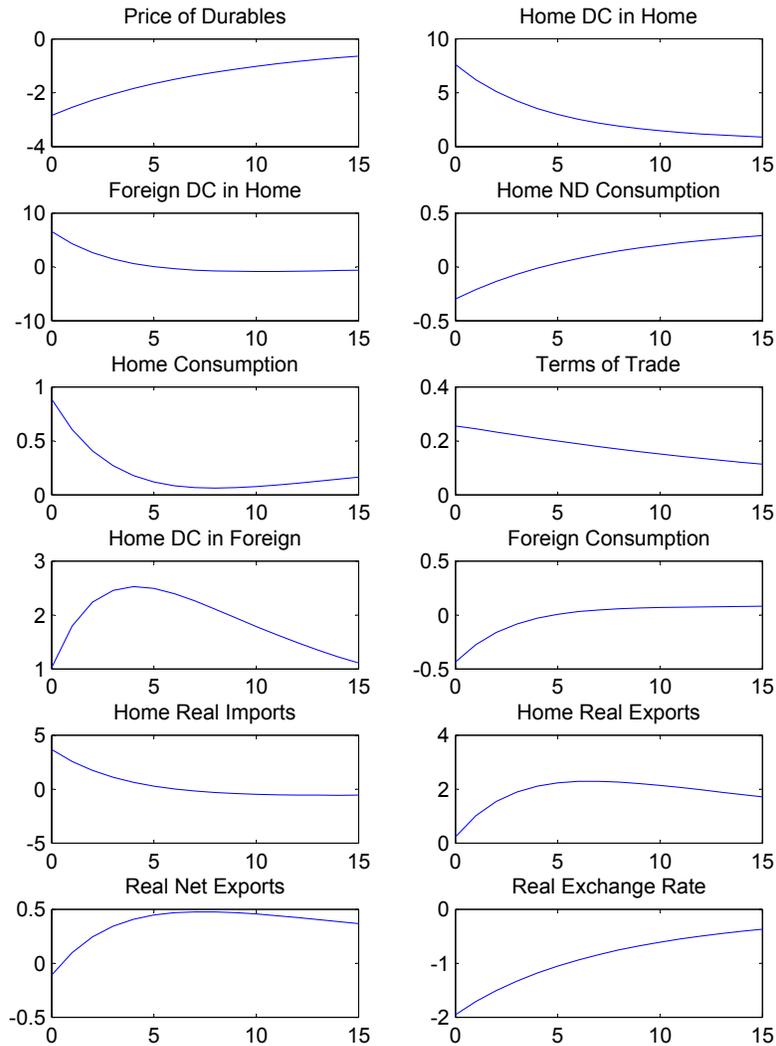


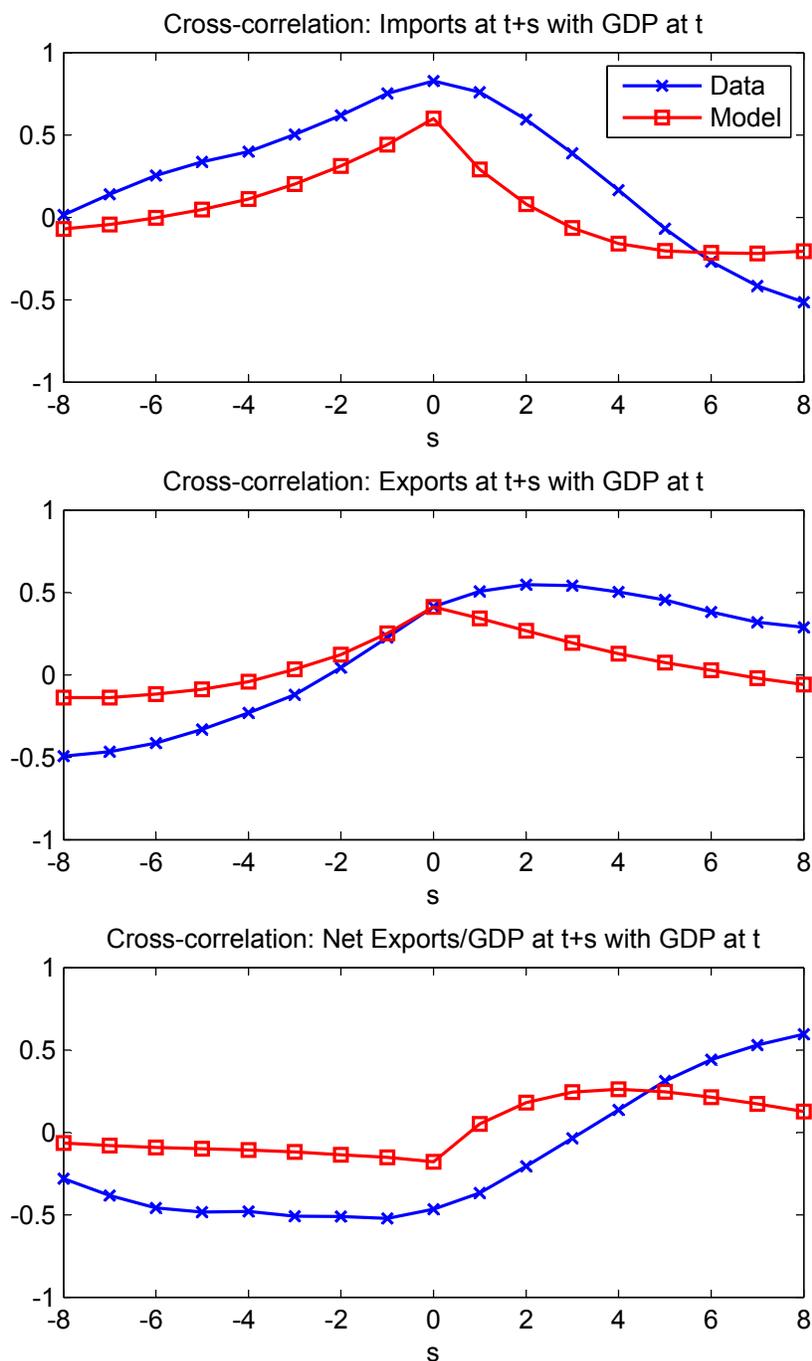
Figure 3: Impulses Response Functions



Note:

- The model is our benchmark model.
- The impulse response functions are with respect to a one-standard-deviation shock in the durable good sector of home country.
- DC is the abbreviation for Durable Consumption. XX DC in YY means XX-country-produced durable consumption goods that are consumed in country YY.
- ND is the abbreviation for Non-Durable.

Figure 4: Cross-correlation in Different Lags



Note:

- The data are quarterly US data from *OECD Economic Outlook* dataset during 1973Q1-2006Q3.
- The model is our benchmark model. Model Statistics are averages over 100 simulations of length 120.
- All variables are logged (except for Net Exports/GDP) and H-P filtered with a smoothing parameter of 1600.

Table 1: Volatility and Comovements of International Trade

Country	SD of GDP (%)	Standard Deviations Relative to That of GDP				Correlation with GDP			
		Real Import	Real Export	$\frac{NetExport}{GDP}$ †	$\frac{NetExport}{GDP}$ †	Real Import	Real Export	$\frac{NetExport}{GDP}$ †	$corr(IM, EX)$ ‡
Australia	1.38	4.23	2.69	0.63	0.49	0.16	-0.33	-0.10	
Austria	0.88	2.10	2.75	0.54	0.60	0.67	0.36	0.85	
Belgium	1.03	2.74	2.36	0.67	0.73	0.74	-0.17	0.92	
Canada	1.42	3.15	2.65	0.66	0.74	0.66	-0.12	0.62	
Czech Republic	1.52	2.39	2.61	1.02	0.53	0.33	-0.09	0.74	
Denmark	1.35	2.65	2.46	0.72	0.55	-0.09	-0.57	0.53	
Finland	2.02	2.74	2.73	0.68	0.73	0.22	-0.41	0.36	
France	0.86	3.97	3.22	0.58	0.77	0.68	-0.27	0.57	
Germany	1.29	2.26	2.86	0.69	0.78	0.52	-0.06	0.40	
Hungary	0.97	4.19	6.53	2.66	0.54	0.53	0.14	0.25	
Iceland	2.18	3.22	1.91	1.28	0.59	0.45	-0.29	0.06	
Ireland	1.62	3.04	1.96	0.73	0.38	0.50	-0.08	0.77	
Italy	1.31	3.44	3.03	0.70	0.70	0.38	-0.26	0.38	
Japan	1.22	4.19	3.51	0.36	0.60	0.16	-0.34	0.21	
Korea	2.43	3.08	2.70	0.82	0.81	0.31	-0.62	0.28	
Mexico	2.36	5.97	2.53	0.89	0.75	-0.20	-0.78	-0.32	
Netherlands	1.28	2.28	1.99	0.62	0.61	0.62	-0.10	0.75	
New Zealand	2.58	2.39	1.53	0.66	0.40	0.22	-0.18	-0.25	
Norway	1.26	4.01	3.22	1.37	0.34	0.36	-0.03	0.13	
Portugal	1.95	2.96	2.72	0.61	0.81	0.51	-0.38	0.44	
Spain	1.04	4.23	2.86	0.77	0.56	0.05	-0.46	-0.14	
Sweden	1.35	3.14	2.54	0.70	0.61	0.46	-0.25	0.53	
Switzerland	1.51	2.78	2.08	0.54	0.66	0.68	-0.10	0.72	
UK	1.36	2.72	2.17	0.39	0.61	0.45	-0.25	0.59	
United States	1.52	3.33	2.63	0.25	0.83	0.41	-0.47	0.19	
Mean	1.51	3.25	2.73	0.78	0.63	0.39	-0.24	0.38	
Median	1.36	3.08	2.65	0.68	0.61	0.45	-0.25	0.40	

Note:

-The data are from *OECD Economic Outlook* database. They are quarterly data of OECD 25 countries during the period between 1973Q1 and 2006Q3. (Due to data limitation, Austria starts from 1988Q1, Czech Republic starts from 1993Q1, and Hungary starts from 1991Q1.)
 -The data of Germany are for West Germany only which end in 1991Q1. The data after unification (1991 Q1-2006Q3) show similar patterns as reported in this table.

†-All variables are logged (except for $\frac{NetExport}{GDP}$), and HP filtered with a smoothing parameter of 1600.

‡- $corr(IM, EX)$ is the correlation of real imports and exports.

-Real imports (exports) are more than twice as volatile as GDP in 22 (19) out of 25 countries at the 5% level in a one-side test. Real imports (exports) are positively correlated with GDP in 25 (21) out of 25 countries at the 5% level in a one-side test. Under the same test, real net exports are negatively correlated with GDP in 15 out of 25 countries and real imports and exports are positively correlated in 19 out of 25 countries. These results are obtained from 1000 bootstraps with replacement.

-Similar volatility and cyclicalilty of imports and exports is also found in aggregate EU data. Results are available upon request.

Table 2: Performance of Standard Models

Panel A: Standard Deviations Relative to That of Real GDP						
	Consumption	Investment	Real Import	Real Export	$\frac{RealNetExport}{RealGDP}$	Real ER [‡]
Data [†]	0.798	2.890	3.335	2.626	0.250	2.432
HP [‡]	0.462	2.663	0.727	0.608	0.087	0.385
DSGE [‡]	0.545	2.830	0.826	0.835	0.077	0.375
GHH [‡]	0.613	2.697	0.935	0.947	0.173	0.284
Lo-elast. [‡]	0.401	2.767	1.651	1.625	0.467	1.216
UIP [‡]	0.925	2.875	3.477	3.466	1.016	1.458

Panel B: Correlation with Real GDP				
	Real Import	Real Export	$\frac{RealNetExport}{RealGDP}$	$corr(RIM_t, REX_t)$ [‡]
Data [†]	0.827	0.415	-0.467	0.194
HP [‡]	0.929	0.588	-0.551	0.628
DSGE [‡]	0.801	0.663	-0.214	0.809
GHH [‡]	0.894	0.278	-0.497	0.252
Lo-elast. [‡]	-0.647	0.973	0.852	-0.799
UIP [‡]	0.286	0.069	-0.112	-0.894

Panel C: Correlation with Real GDP				
	Real Import	Real Export	$\frac{RealNetExport}{RealGDP}$	$corr(RIM_t, REX_t)$ [‡]
HP [‡]	0.999	0.500	-0.819	0.491
DSGE [‡]	0.988	0.601	-0.552	0.634
GHH [‡]	0.985	0.241	-0.608	0.152
Lo-elast. [‡]	0.369	0.984	0.848	0.212
UIP [‡]	0.569	0.070	-0.181	-0.749

Note:

‡-Real ER is the (CPI-based) real exchange rate. $corr(RIM_t, REX_t)$ is the correlation of real imports and exports. In Panels A and B, the imports, exports and net exports are measured in constant (steady-state) prices. They are measured in Panel C in terms of final consumption goods.

†-US data as in Table 1

‡-HP (Heathcote and Perri (2002)) is the standard IRBC model with incomplete financial market (real bonds only). DSGE is the standard DSGE model as described in the appendix. GHH is the DSGE model with GHH utility function. Lo-elast is the DSGE model with low intertemporal elasticity of substitution ($\sigma = 5$), and UIP is the DSGE model with the uncovered interest rate parity shock.

§-Statistics are based on logged (except for $\frac{RealNetExport}{RealGDP}$) and H-P filtered data. Entries are averages over 100 simulations of length 120.

Table 3: Share of Durable Goods in Trade

Country	Exclude Energy Products		Exclude Materials and Energy	
	Import	Export	Import	Export
Australia	0.70	0.56	0.71	0.45
Austria	0.69	0.67	0.70	0.69
Belgium	0.66	0.66	0.67	0.66
Canada	0.77	0.64	0.77	0.69
Czech Rep	0.72	0.75	0.73	0.77
Denmark	0.60	0.47	0.61	0.48
Finland	0.72	0.61	0.73	0.65
France	0.67	0.68	0.68	0.68
Germany	0.69	0.71	0.70	0.71
Hungary	0.74	0.77	0.75	0.78
Iceland	0.55	0.28	0.56	0.28
Ireland	0.73	0.59	0.73	0.59
Italy	0.65	0.64	0.66	0.64
Japan	0.57	0.89	0.58	0.89
Korea	0.76	0.78	0.77	0.78
Mexico	0.73	0.78	0.74	0.78
Netherland	0.68	0.60	0.69	0.61
New Zealand	0.66	0.26	0.66	0.26
Norway	0.70	0.59	0.71	0.61
Portugal	0.65	0.53	0.66	0.54
Spain	0.68	0.65	0.69	0.66
Sweden	0.68	0.73	0.69	0.76
Switzerland	0.65	0.69	0.66	0.69
UK	0.69	0.74	0.70	0.74
US	0.69	0.75	0.70	0.77
Mean	0.68	0.64	0.69	0.65
Median	0.69	0.66	0.70	0.68

Note:

–Data are from International Trade Data, NBER-United Nations World Trade Data (<http://cid.econ.ucdavis.edu>).

–Entries are shares of durable goods in imports and exports (year 2000). Left panel of the table reports results for imports and exports excluding energy products (SITC 3). Raw materials (SITC 2) and energy products (SITC 3) are excluded from imports and exports in the right panel.

–Share of durable goods in bilateral trade among Canada, EU, Japan and US is similar to the results reported in this table. Results are available upon request.

Table 4: Calibration

Parameter	Value	Description
α	0.5	Share of Home Goods in Capital When Trade Cost Is Zero
$\chi = \epsilon$	0.36	Capital Share in Production
γ	9.1	(Long-run) Elasticity of Substitution between Home and Foreign Capital
τ	0.1	(Iceberg) International Trade Cost
β	0.99	Subjective Discount Factor
δ	0.013	Depreciation Rate of Capital
δ_D	0.05	Depreciation Rate of Durable Consumption
μ	0.23	Share of Durable Consumption Stock in Consumption Bundle
ν	1.65	Preference Parameter of Labor Supply
ψ	0.5	Share of Home Goods in Durable Consumption When Trade Cost Is Zero
ρ	5.83	Preference Parameter
σ	2	Preference Parameter
θ	6.85	(Long-run) Elasticity of Substitution b/t Home and Foreign Durable Consumption
ζ	1.1	Elasticity of Substitution b/t Durable and Nondurable Consumption
ϕ_1	1.4 [†]	Durable Consumption Adjustment Cost
ϕ_2	8.5 [†]	Capital Adjustment Cost
Φ	0.00001	Bond Holding Cost
Ξ_1	0.87	AR(1) Coefficient of Technology Shock in Nondurable Good Sector
Ξ_2	0.9	AR(1) Coefficient of Technology Shock in Durable Good Sector
$\sigma(\varepsilon_{Ht}^N)$	0.0096	Standard Deviation of Productivity Shock in Nondurable Good Sector
$\sigma(\varepsilon_{Ht}^D)$	0.036	Standard Deviation of Productivity Shock in Durable Good Sector

Note:

†—Entries are values used in the benchmark model. In other models, they are adjusted to match the volatility of durable consumption and aggregate investment.

Table 5: Simulation Results of Benchmark Model

Panel A: Standard Deviations Relative to That of Real GDP								
	C	I	DC	L	RIM	REX	RNX	Q
Data [†]	0.798	2.890	2.983	0.670	3.335	2.626	0.250	2.432
Benchmark [‡]	0.878	2.594	2.473	0.547	2.633	2.678	0.337	1.262
High Correlation [‡]	0.920	2.750	2.680	0.549	2.880	2.936	0.402	1.058
High Spillover [‡]	0.948	2.905	2.738	0.539	1.826	1.775	0.322	1.297
Medium Spillover [‡]	0.917	2.894	2.754	0.549	2.652	2.615	0.393	1.271
High Correlation 2 [‡]	0.874	2.666	2.381	0.544	2.558	2.596	0.266	0.435
New Costs	0.961	2.828	2.551	0.535	2.726	2.779	0.355	1.041
Correlation with GDP								
	RIM	REX	RNX	$corr(RIM, REX)$		σ_{Y,Y^*}	σ_{C,C^*}	
Data [†]	0.827	0.415	-0.467	0.194		0.68	0.60	
Benchmark [‡]	0.606	0.411	-0.187	0.421		0.01	-0.17	
High Correlation [‡]	0.630	0.337	-0.288	0.265		0.03	-0.20	
High Spillover [‡]	0.576	0.405	-0.129	0.160		-0.03	0.23	
Medium Spillover [‡]	0.599	0.324	-0.228	0.171		-0.01	-0.14	
High Correlation 2 [‡]	0.801	0.554	-0.177	0.577		0.56	0.39	
New Costs	0.560	0.232	-0.292	0.386		0.08	-0.09	

Note:

C–consumption, I–investment, DC–durable consumption, L–labor, RIM–real imports, REX–real exports, RNX–real net exports defined as $\frac{RealNetExport}{RealGDP}$, Q–CPI-based real exchange rate. $corr(RIM, REX)$ –correlation of real imports and exports, σ_{Y,Y^*} –cross-country correlation of output, σ_{C,C^*} –cross-country correlation of consumption. The cross-country correlations are between the United States and the rest of OECD countries (Corsetti *et. al.* forthcoming).

[†]–US data as in Tables 1

[‡]–The standard deviation of GDP in benchmark model is 2.26%. All variables are logged (except for RNX) and H-P filtered with a smoothing parameter of 1600. Entries are averages over 100 simulations of length 120.

APPENDIX

A.1 Standard Models

In this section, we describe the standard models used in Section 2.2.

A.1.1 IRBC Model

The standard IRBC model is the bond-economy model in Heathcote and Perri (2002). There are two symmetric countries, Home and Foreign. In each country, there are two sectors, the intermediate and final good sectors. Because of symmetry, we focus on the Home country in describing the model. Intermediate goods are produced from capital and labor with a Cobb-Douglas technology

$$Y_{Ht}^H + Y_{Ft}^H = A_{Ht} K_{Ht}^\theta L_{Ht}^{1-\theta}, \quad (\text{A.1.1})$$

where Y_{Ht}^H is the Home intermediate goods used in the Home country and Y_{Ft}^H is the Home intermediate goods used in the Foreign country. A_{Ht} is the TFP shock, K_{Ht} is capital and L_{Ht} is labor supply. Capital follows the law of motion

$$K_{Ht+1} = (1 - \delta)K_{Ht} + I_{Ht}. \quad (\text{A.1.2})$$

Final goods are produced from Home and Foreign intermediate goods

$$Y_{Ht} = \left[\alpha^{\frac{1}{\gamma}} (Y_{Ht}^H)^{\frac{\gamma-1}{\gamma}} + (1 - \alpha)^{\frac{1}{\gamma}} (Y_{Ht}^F)^{\frac{\gamma-1}{\gamma}} \right]^{\frac{\gamma}{\gamma-1}}. \quad (\text{A.1.3})$$

All prices and wage are flexible. The representative household maximizes expected lifetime utility given those prices

$$E_t \sum_{j=0}^{\infty} \beta^j u_{Ht+j},$$

where the period utility function u_{Ht} takes the form

$$u_{Ht} = \frac{1}{1 - \sigma} [C_{Ht}^\mu (1 - L_{Ht})^{1-\mu}]^{1-\sigma}. \quad (\text{A.1.4})$$

The Home and Foreign country can trade real bonds of the Home country's intermediate goods. To make the model stationary, we assume a small bond holding cost as in Heathcote and Perri (2002). We calibrate

the model with the same parameter values as in Heathcote and Perri (2002). Our simulation results are very close to those reported in their paper.

A.1.2 DSGE Model

It is a two-country symmetric model. We will focus on the Home country in describing our model. There is a continuum of differentiated intermediate goods indexed by $i \in [0, 1]$. The Home intermediate good i ($Y_H(i)$) is produced by a single firm with capital $K_t(i)$ and labor $L_t(i)$ in the Home country. Capital and labor are not internationally mobile. Intermediate goods are aggregated into an intermediate good composite according to a CES function

$$Y_{Ht} = \left[\int_0^1 Y_{Ht}^{\frac{\phi-1}{\phi}}(i) di \right]^{\frac{\phi}{\phi-1}} \quad (\text{A.1.5})$$

The intermediate-good market is monopolistically competitive. The firms choose prices to maximize expected discounted profit. We follow Calvo staggered price setting in this sticky-price model. In each period, the firm has a probability of $1 - \lambda$ of changing its price. When $\lambda = 0$, the model reduces to the flexible price setup.

Final goods are produced from the Home and Foreign intermediate good composites according to a CES function

$$Y_t = \left[\alpha^{\frac{1}{\gamma}} Y_{Ht}^{\frac{\gamma-1}{\gamma}} + (1 - \alpha)^{\frac{1}{\gamma}} Y_{Ft}^{\frac{\gamma-1}{\gamma}} \right]^{\frac{\gamma}{\gamma-1}}, \quad (\text{A.1.6})$$

where α is the percentage of Home goods in final goods, and γ is the elasticity of substitution between Home and Foreign goods. The final goods market is competitive with flexible prices.

The household chooses sequences of consumption C_t , capital accumulation I_t , labor supply L_t , Home and Foreign nominal bonds (B_{Ht+1} and B_{Ft+1}) to maximize expected lifetime utility

$$E_0 \left[\sum_{t=0}^{\infty} \beta^t u_t(C_t, 1 - L_t) \right], \quad (\text{A.1.7})$$

where $u_t = \frac{[C_t^\mu(1-L_t)^{1-\mu}]^{1-\sigma}}{1-\sigma}$, subject to the budget constraint

$$\begin{aligned}
C_t + \frac{B_{Ht+1}}{(1+i_t)P_t} + \frac{S_t B_{Ft+1}}{(1+i_t^*)P_t} + I_t + \frac{1}{2}\Phi \left(\frac{I_t}{K_t} - \delta \right)^2 K_t \\
+ \frac{1}{2}\phi_d \left(\frac{B_{Ht+1}}{P_t} \right)^2 + \frac{1}{2}\phi_f \left(\frac{S_t B_{Ft+1}}{P_t} \right)^2 \\
\leq \frac{W_t L_t}{P_t} + \frac{R_t K_t}{P_t} + \frac{B_{Ht}}{P_t} + \frac{B_{Ft} S_t}{P_t} + \frac{\Pi_t}{P_t},
\end{aligned} \tag{A.1.8}$$

where $\frac{1}{2}\Phi \left(\frac{I_t}{K_t} - \delta \right)^2 K_t$ is the capital adjustment cost, $\frac{1}{2}\phi_d \left(\frac{B_{Ht+1}}{P_t} \right)^2$ and $\frac{1}{2}\phi_f \left(\frac{S_t B_{Ft+1}}{P_t} \right)^2$ are bond holding costs for the Home and Foreign nominal bonds. Π_t is the profit of intermediate-good firms. The nominal interest rate follows the Taylor rule

$$i_t = i + \Xi_\pi \log(\pi_t/\pi) + \Xi_y \log(gdp_t/gdp), \tag{A.1.9}$$

where π_t is the inflation rate at time t .

The first order conditions of the household approximately imply uncovered interest rate parity. In the UIP model, we break this condition with an uncovered interest rate parity shock by following Kollmann (2004). The values that we use to calibrate the DSGE model are listed in Table 6. Those parameter values are standard in the literature.

Table 6: Calibration of DSGE Model

Parameter	Value	Description
Intermediate Goods Sector		
ψ	0.36	Capital Share in Production
ϕ	6	Elasticity of Substitution between Differentiated Tradable Goods
λ	0.75	Probability of Not Changing Price.
δ	0.025	Depreciation Rate of Capital
Final Goods Sector		
α	0.85	Share of Home Goods in Final Good
γ	1.5	Elasticity of Substitution between Home and Foreign Goods
Household		
β	0.99	Subjective Discount Factor
Φ	3.2	Investment Adjustment Cost
ϕ_d	0.0001	Domestic Bond Holding Cost
ϕ_f	0.0003	Foreign Bond Holding Cost
σ	2	Preference Parameter
μ	0.36	Preference Parameter
Exogenous Shocks		
$\xi_{11} = \xi_{22}$	0.906	Technology shock AR(1) coefficient
$\xi_{12} = \xi_{21}$	0.088	Technology spillovers
σ_ε	0.0085	Standard Deviation of Productivity Shock

A.2 Benchmark Model

In this section, we give more details about our benchmark model in Section 3. We first list equations that define the equilibrium of the model, then solve for its nonstochastic steady state.

A.2.1 Equilibrium Conditions

We divide all prices by the price of nondurable consumption goods (P_{Ht}^N in the Home country and P_{Ft}^N in the Foreign). That is, we use the nondurable consumption good as numeraire. We use a hat above all prices to denote that they are relative prices in terms of nondurable consumption. The equilibrium of the benchmark model is defined by the following equations.

Nondurable Good Sector

$$1 = (A_{Ht}^N)^{-1} (\hat{R}_{Ht}^N)^\chi \hat{W}_{Ht}^{1-\chi} \chi^{-\chi} (1-\chi)^{\chi-1}, \quad (\text{A.2.1})$$

where \hat{R}_{Ht}^N is defined as

$$\hat{R}_{Ht}^N = \left[\alpha (\hat{R}_{Ht}^{NH})^{1-\gamma} + (1-\alpha) (\hat{R}_{Ht}^{NF})^{1-\gamma} \right]^{\frac{1}{1-\gamma}}.$$

$$K_{Ht}^{NH} = \alpha \left(\frac{\hat{R}_{Ht}^{NH}}{\hat{R}_{Ht}^N} \right)^{-\gamma} K_{Ht}^N \quad (\text{A.2.2})$$

$$K_{Ht}^{NF} = (1-\alpha) \left(\frac{\hat{R}_{Ht}^{NF}}{\hat{R}_{Ht}^N} \right)^{-\gamma} K_{Ht}^N \quad (\text{A.2.3})$$

$$K_{Ht}^N = \chi Y_{Ht}^N / \hat{R}_{Ht}^N \quad (\text{A.2.4})$$

$$L_{Ht}^N = (1-\chi) Y_{Ht}^N / \hat{W}_{Ht} \quad (\text{A.2.5})$$

Symmetric conditions hold in the Foreign country

$$1 = (A_{Ft}^N)^{-1} (\hat{R}_{Ft}^N)^\chi \hat{W}_{Ft}^{1-\chi} \chi^{-\chi} (1-\chi)^{\chi-1}, \quad (\text{A.2.6})$$

where \hat{R}_{Ft}^N is defined as

$$\hat{R}_{Ft}^N = \left[\alpha (\hat{R}_{Ft}^{NF})^{1-\gamma} + (1-\alpha) (\hat{R}_{Ft}^{NH})^{1-\gamma} \right]^{\frac{1}{1-\gamma}}.$$

$$K_{Ft}^{NF} = \alpha \left(\frac{\hat{R}_{Ft}^{NF}}{\hat{R}_{Ft}^N} \right)^{-\gamma} K_{Ft}^N \quad (\text{A.2.7})$$

$$K_{Ft}^{NH} = (1 - \alpha) \left(\frac{\hat{R}_{Ft}^{NH}}{\hat{R}_{Ft}^N} \right)^{-\gamma} K_{Ft}^N \quad (\text{A.2.8})$$

$$K_{Ft}^N = \chi Y_{Ft}^N / \hat{R}_{Ft}^N \quad (\text{A.2.9})$$

$$L_{Ft}^N = (1 - \chi) Y_{Ft}^N / \hat{W}_{Ft} \quad (\text{A.2.10})$$

Durable Good Sector

$$\hat{P}_{Ht}^{DH} = (A_{Ht}^D)^{-1} (\hat{R}_{Ht}^D)^\epsilon \hat{W}_{Ht}^{1-\epsilon} \epsilon^{-\epsilon} (1 - \epsilon)^{\epsilon-1}, \quad (\text{A.2.11})$$

where \hat{R}_{Ht}^D is defined as

$$\hat{R}_{Ht}^D = \left[\alpha (\hat{R}_{Ht}^{DH})^{1-\gamma} + (1 - \alpha) (\hat{R}_{Ht}^{DF})^{1-\gamma} \right]^{\frac{1}{1-\gamma}}.$$

$$K_{Ht}^{DH} = \alpha \left(\frac{\hat{R}_{Ht}^{DH}}{\hat{R}_{Ht}^D} \right)^{-\gamma} K_{Ht}^D \quad (\text{A.2.12})$$

$$K_{Ht}^{DF} = (1 - \alpha) \left(\frac{\hat{R}_{Ht}^{DF}}{\hat{R}_{Ht}^D} \right)^{-\gamma} K_{Ht}^D \quad (\text{A.2.13})$$

$$K_{Ht}^D = \epsilon \hat{P}_{Ht}^{DH} Y_{Ht}^D / \hat{R}_{Ht}^D \quad (\text{A.2.14})$$

$$L_{Ht}^D = (1 - \epsilon) \hat{P}_{Ht}^{DH} Y_{Ht}^D / \hat{W}_{Ht} \quad (\text{A.2.15})$$

Symmetric conditions hold in the Foreign country.

$$\hat{P}_{Ft}^{DF} = (A_{Ft}^D)^{-1} (\hat{R}_{Ft}^D)^\epsilon \hat{W}_{Ft}^{1-\epsilon} \epsilon^{-\epsilon} (1 - \epsilon)^{\epsilon-1}, \quad (\text{A.2.16})$$

where \hat{R}_{Ft}^D is defined as

$$\hat{R}_{Ft}^D = \left[\alpha (\hat{R}_{Ft}^{DF})^{1-\gamma} + (1 - \alpha) (\hat{R}_{Ft}^{DH})^{1-\gamma} \right]^{\frac{1}{1-\gamma}}.$$

$$K_{Ft}^{DF} = \alpha \left(\frac{\hat{R}_{Ft}^{DF}}{\hat{R}_{Ft}^D} \right)^{-\gamma} K_{Ft}^D \quad (\text{A.2.17})$$

$$K_{Ft}^{DH} = (1 - \alpha) \left(\frac{\hat{R}_{Ft}^{DH}}{\hat{R}_{Ft}^D} \right)^{-\gamma} K_{Ft}^D \quad (\text{A.2.18})$$

$$K_{Ft}^D = \epsilon \hat{P}_{Ft}^{DF} Y_{Ft}^D / \hat{R}_{Ft}^D \quad (\text{A.2.19})$$

$$L_{Ft}^D = (1 - \epsilon) \hat{P}_{Ft}^{DF} Y_{Ft}^D / \hat{W}_{Ft} \quad (\text{A.2.20})$$

Households

The law of motion for durable consumption

$$D_{Ht+1}^H = (1 - \delta_D) D_{Ht}^H + d_{Ht}^H \quad (\text{A.2.21})$$

$$D_{Ht+1}^F = (1 - \delta_D) D_{Ht}^F + d_{Ht}^F. \quad (\text{A.2.22})$$

The law of motion for capital

$$K_{Ht+1}^{NH} = (1 - \delta) K_{Ht}^{NH} + I_{Ht}^{NH} \quad (\text{A.2.23})$$

$$K_{Ht+1}^{NF} = (1 - \delta) K_{Ht}^{NF} + I_{Ht}^{NF} \quad (\text{A.2.24})$$

$$K_{Ht+1}^{DH} = (1 - \delta) K_{Ht}^{DH} + I_{Ht}^{DH} \quad (\text{A.2.25})$$

$$K_{Ht+1}^{DF} = (1 - \delta) K_{Ht}^{DF} + I_{Ht}^{DF}. \quad (\text{A.2.26})$$

The budget constraint

$$\begin{aligned} & C_{Ht} + \hat{P}_{Ht}^{DH} (d_{Ht}^H + \Delta_{Ht}^H + I_{Ht}^{NH} + \Lambda_{Ht}^{NH} + I_{Ht}^{DH} + \Lambda_{Ht}^{DH}) \\ & + \frac{Q_t \hat{P}_{Ft}^{DF} \hat{P}_{Ht}}{\hat{P}_{Ft}(1 - \tau)} \left(d_{Ht}^F + \Delta_{Ht}^F + I_{Ht}^{NF} + \Lambda_{Ht}^{NF} + I_{Ht}^{DF} + \Lambda_{Ht}^{DF} + \frac{B_{Ht+1}}{1 + i_t} + \frac{1}{2} \Phi B_{Ht+1}^2 \right) \\ & \leq \hat{W}_{Ht} L_{Ht} + \hat{P}_{Ht}^{DH} B_{Ht} + \hat{R}_{Ht}^{NH} K_{Ht}^{NH} + \hat{R}_{Ht}^{NF} K_{Ht}^{NF} + \hat{R}_{Ht}^{DH} K_{Ht}^{DH} + \hat{R}_{Ht}^{DF} K_{Ht}^{DF}, \end{aligned} \quad (\text{A.2.27})$$

where Q_t is the CPI real exchange rate. The consumer price index (CPI) is defined as

$$\hat{P}_{Ht} = (\hat{P}_{Ht}^{DH})^{\omega_2} \left(\frac{Q_t \hat{P}_{Ft}^{DF} \hat{P}_{Ht}}{\hat{P}_{Ft}(1 - \tau)} \right)^{1 - \omega_1 - \omega_2}, \quad (\text{A.2.28})$$

where ω_1 is the expenditure share of nondurable consumption. ω_2 and ω_3 are the expenditure shares of Home and Foreign durable consumption respectively.

The followings are the first order conditions from the household's lifetime utility maximization problem.

$$\hat{P}_{Ht}^{DH} \left(1 + \frac{\partial \Delta_{Ht}^H}{\partial d_{Ht}^H} \right) = E_t \left[\beta \frac{\partial u_{t+1} / \partial D_{Ht+1}^H}{\partial u_t / \partial C_{Ht}} - \Gamma_{t,t+1} \hat{P}_{Ht+1}^{DH} \left(\frac{\partial \Delta_{Ht+1}^H}{\partial D_{Ht+1}^H} - (1 - \delta_D) \left(1 + \frac{\partial \Delta_{Ht+1}^H}{\partial d_{Ht+1}^H} \right) \right) \right], \quad (\text{A.2.29})$$

where $\Gamma_{t,t+1} = \beta \frac{\partial u_{t+1} / \partial C_{Ht+1}}{\partial u_t / \partial C_{Ht}}$ is the intertemporal elasticity of substitution of nondurable consumption goods. The left hand side of the equation is the cost in terms of nondurable goods, of increasing one unit durable consumption. The right hand side is the benefit, which includes three parts: 1. the increase of period $t + 1$ utility due to the increase of durable consumption stock ($\beta \frac{\partial u_{t+1} / \partial D_{Ht+1}^H}{\partial u_t / \partial C_{Ht}}$); 2. the adjustment cost associated with the increased consumption stock ($\Gamma_{t,t+1} \hat{P}_{Ht+1}^{DH} \frac{\partial \Delta_{Ht+1}^H}{\partial D_{Ht+1}^H}$);²⁹ 3. the value of undepreciated durable consumption goods $\Gamma_{t,t+1} \hat{P}_{Ht+1}^{DH} (1 - \delta_D) \left(1 + \frac{\partial \Delta_{Ht+1}^H}{\partial d_{Ht+1}^H} \right)$. In equilibrium, the marginal cost of increasing durable consumption stock is equal to its marginal benefit.

$$\begin{aligned} & \frac{Q_t \hat{P}_{Ft}^{DF} \hat{P}_{Ht}}{\hat{P}_{Ft}(1 - \tau)} \left(1 + \frac{\partial \Delta_{Ht}^F}{\partial d_{Ht}^F} \right) \\ &= E_t \left[\beta \frac{\partial u_{t+1} / \partial D_{Ht+1}^F}{\partial u_t / \partial C_{Ht}} - \Gamma_{t,t+1} \frac{Q_{t+1} \hat{P}_{Ft+1}^{DF} \hat{P}_{Ht+1}}{\hat{P}_{Ft+1}(1 - \tau)} \left(\frac{\partial \Delta_{Ht+1}^F}{\partial D_{Ht+1}^F} - (1 - \delta_D) \left(1 + \frac{\partial \Delta_{Ht+1}^F}{\partial d_{Ht+1}^F} \right) \right) \right] \end{aligned} \quad (\text{A.2.30})$$

$$\frac{\partial u_t}{\partial L_{Ht}} + \hat{W}_{Ht} \frac{\partial u_t}{\partial C_{Ht}} = 0 \quad (\text{A.2.31})$$

$$\hat{P}_{Ht}^{DH} \left(1 + \frac{\partial \Lambda_{Ht}^{NH}}{\partial I_{Ht}^{NH}} \right) = E_t \left[\Gamma_{t,t+1} \left(\hat{R}_{Ht+1}^{NH} - \hat{P}_{Ht+1}^{DH} \left(\frac{\partial \Lambda_{Ht+1}^{NH}}{\partial K_{Ht+1}^{NH}} - (1 - \delta) \left(1 + \frac{\partial \Lambda_{Ht+1}^{NH}}{\partial I_{Ht+1}^{NH}} \right) \right) \right) \right] \quad (\text{A.2.32})$$

$$\begin{aligned} & \frac{Q_t \hat{P}_{Ft}^{DF} \hat{P}_{Ht}}{\hat{P}_{Ft}(1 - \tau)} \left(1 + \frac{\partial \Lambda_{Ht}^{NF}}{\partial I_{Ht}^{NF}} \right) \\ &= E_t \left[\Gamma_{t,t+1} \left(\hat{R}_{Ht+1}^{NF} - \frac{Q_{t+1} \hat{P}_{Ft+1}^{DF} \hat{P}_{Ht+1}}{(1 - \tau) \hat{P}_{Ft+1}} \left(\frac{\partial \Lambda_{Ht+1}^{NF}}{\partial K_{Ht+1}^{NF}} - (1 - \delta) \left(1 + \frac{\partial \Lambda_{Ht+1}^{NF}}{\partial I_{Ht+1}^{NF}} \right) \right) \right) \right] \end{aligned} \quad (\text{A.2.33})$$

$$\hat{P}_{Ht}^{DH} \left(1 + \frac{\partial \Lambda_{Ht}^{DH}}{\partial I_{Ht}^{DH}} \right) = E_t \left[\Gamma_{t,t+1} \left(\hat{R}_{Ht+1}^{DH} - \hat{P}_{Ht+1}^{DH} \left(\frac{\partial \Lambda_{Ht+1}^{DH}}{\partial K_{Ht+1}^{DH}} - (1 - \delta) \left(1 + \frac{\partial \Lambda_{Ht+1}^{DH}}{\partial I_{Ht+1}^{DH}} \right) \right) \right) \right] \quad (\text{A.2.34})$$

$$\begin{aligned} & \frac{Q_t \hat{P}_{Ft}^{DF} \hat{P}_{Ht}}{\hat{P}_{Ft}(1 - \tau)} \left(1 + \frac{\partial \Lambda_{Ht}^{DF}}{\partial I_{Ht}^{DF}} \right) \\ &= E_t \left[\Gamma_{t,t+1} \left(\hat{R}_{Ht+1}^{DF} - \frac{Q_{t+1} \hat{P}_{Ft+1}^{DF} \hat{P}_{Ht+1}}{(1 - \tau) \hat{P}_{Ft+1}} \left(\frac{\partial \Lambda_{Ht+1}^{DF}}{\partial K_{Ht+1}^{DF}} - (1 - \delta) \left(1 + \frac{\partial \Lambda_{Ht+1}^{DF}}{\partial I_{Ht+1}^{DF}} \right) \right) \right) \right] \end{aligned} \quad (\text{A.2.35})$$

$$\frac{1}{1 + i_t} + \Phi B_{Ht+1} = E_t \left[\Gamma_{t,t+1} \frac{\hat{P}_{Ht+1}^{DH}}{\hat{P}_{Ht}^{DH}} \right] \quad (\text{A.2.36})$$

Symmetric conditions hold in the Foreign country. From Walras' law, one equation is redundant. We eliminate the Foreign country's budget constraint from our equation system. So equations in the Foreign

²⁹It is useful to note that this term is negative.

country are

$$D_{Ft+1}^F = (1 - \delta_D)D_{Ft}^F + d_{Ft}^F \quad (\text{A.2.37})$$

$$D_{Ft+1}^H = (1 - \delta_D)D_{Ft}^H + d_{Ft}^H \quad (\text{A.2.38})$$

$$K_{Ft+1}^{NF} = (1 - \delta)K_{Ft}^{NF} + I_{Ft}^{NF} \quad (\text{A.2.39})$$

$$K_{Ft+1}^{NH} = (1 - \delta)K_{Ft}^{NH} + I_{Ft}^{NH} \quad (\text{A.2.40})$$

$$K_{Ft+1}^{DF} = (1 - \delta)K_{Ft}^{DF} + I_{Ft}^{DF} \quad (\text{A.2.41})$$

$$K_{Ft+1}^{DH} = (1 - \delta)K_{Ft}^{DH} + I_{Ft}^{DH} \quad (\text{A.2.42})$$

$$\hat{P}_{Ft} = (\hat{P}_{Ft}^{DF})^{\omega_2} \left(\frac{\hat{P}_{Ht}^{DH} \hat{P}_{Ft}}{Q_t \hat{P}_{Ht} (1 - \tau)} \right)^{1 - \omega_1 - \omega_2} \quad (\text{A.2.43})$$

$$\hat{P}_{Ft}^{DF} \left(1 + \frac{\partial \Delta_{Ft}^F}{\partial d_{Ft}^F} \right) = E_t \left[\beta \frac{\partial u_{t+1}^* / \partial D_{Ft+1}^F}{\partial u_t^* / \partial C_{Ft}} - \Gamma_{t,t+1}^* \hat{P}_{Ft+1}^{DF} \left(\frac{\partial \Delta_{Ft+1}^F}{\partial D_{Ft+1}^F} - (1 - \delta_D) \left(1 + \frac{\partial \Delta_{Ft+1}^F}{\partial d_{Ft+1}^F} \right) \right) \right] \quad (\text{A.2.44})$$

$$\begin{aligned} & \frac{\hat{P}_{Ht}^{DH} \hat{P}_{Ft}}{Q_t \hat{P}_{Ht} (1 - \tau)} \left(1 + \frac{\partial \Delta_{Ft}^H}{\partial d_{Ft}^H} \right) \\ &= E_t \left[\beta \frac{\partial u_{t+1}^* / \partial D_{Ft+1}^H}{\partial u_t^* / \partial C_{Ft}} - \Gamma_{t,t+1}^* \frac{\hat{P}_{Ht+1}^{DH} \hat{P}_{Ft+1}}{Q_{t+1} \hat{P}_{Ht+1} (1 - \tau)} \left(\frac{\partial \Delta_{Ft+1}^H}{\partial D_{Ft+1}^H} - (1 - \delta_D) \left(1 + \frac{\partial \Delta_{Ft+1}^H}{\partial d_{Ft+1}^H} \right) \right) \right] \end{aligned} \quad (\text{A.2.45})$$

$$\frac{\partial u_t^*}{\partial L_{Ft}} + \hat{W}_{Ft} \frac{\partial u_t^*}{\partial C_{Ft}} = 0 \quad (\text{A.2.46})$$

$$\hat{P}_{Ft}^{DF} \left(1 + \frac{\partial \Lambda_{Ft}^{NF}}{\partial I_{Ft}^{NF}} \right) = E_t \left[\Gamma_{t,t+1}^* \left(\hat{R}_{Ft+1}^{NF} - \hat{P}_{Ft+1}^{DF} \left(\frac{\partial \Lambda_{Ft+1}^{NF}}{\partial K_{Ft+1}^{NF}} - (1 - \delta) \left(1 + \frac{\partial \Lambda_{Ft+1}^{NF}}{\partial I_{Ft+1}^{NF}} \right) \right) \right) \right] \quad (\text{A.2.47})$$

$$\begin{aligned} & \frac{\hat{P}_{Ht}^{DH} \hat{P}_{Ft}}{Q_t \hat{P}_{Ht} (1 - \tau)} \left(1 + \frac{\partial \Lambda_{Ft}^{NH}}{\partial I_{Ft}^{NH}} \right) \\ &= E_t \left[\Gamma_{t,t+1}^* \left(\hat{R}_{Ft+1}^{NH} - \frac{\hat{P}_{Ht+1}^{DH} \hat{P}_{Ft+1}}{Q_{t+1} (1 - \tau) \hat{P}_{Ht+1}} \left(\frac{\partial \Lambda_{Ft+1}^{NH}}{\partial K_{Ft+1}^{NH}} - (1 - \delta) \left(1 + \frac{\partial \Lambda_{Ft+1}^{NH}}{\partial I_{Ft+1}^{NH}} \right) \right) \right) \right] \end{aligned} \quad (\text{A.2.48})$$

$$\hat{P}_{Ft}^{DF} \left(1 + \frac{\partial \Lambda_{Ft}^{DF}}{\partial I_{Ft}^{DF}} \right) = E_t \left[\Gamma_{t,t+1}^* \left(\hat{R}_{Ft+1}^{DF} - \hat{P}_{Ft+1}^{DF} \left(\frac{\partial \Lambda_{Ft+1}^{DF}}{\partial K_{Ft+1}^{DF}} - (1 - \delta) \left(1 + \frac{\partial \Lambda_{Ft+1}^{DF}}{\partial I_{Ft+1}^{DF}} \right) \right) \right) \right] \quad (\text{A.2.49})$$

$$\begin{aligned} & \frac{\hat{P}_{Ht}^{DH} \hat{P}_{Ft}}{Q_t \hat{P}_{Ht} (1 - \tau)} \left(1 + \frac{\partial \Lambda_{Ft}^{DH}}{\partial I_{Ft}^{DH}} \right) \\ &= E_t \left[\Gamma_{t,t+1}^* \left(\hat{R}_{Ft+1}^{DH} - \frac{\hat{P}_{Ht+1}^{DH} \hat{P}_{Ft+1}}{Q_{t+1} (1 - \tau) \hat{P}_{Ht+1}} \left(\frac{\partial \Lambda_{Ft+1}^{DH}}{\partial K_{Ft+1}^{DH}} - (1 - \delta) \left(1 + \frac{\partial \Lambda_{Ft+1}^{DH}}{\partial I_{Ft+1}^{DH}} \right) \right) \right) \right] \end{aligned} \quad (\text{A.2.50})$$

$$\frac{1}{1 + i_t} + \Phi B_{Ft+1} = E_t \left[\Gamma_{t,t+1}^* \frac{\hat{P}_{Ft+1}^{DH}}{\hat{P}_{Ft}^{DH}} \right] \quad (\text{A.2.51})$$

Market Clearing Conditions

The model is closed with market clearing conditions

$$Y_{Ht}^N = C_{Ht} \quad (\text{A.2.52})$$

$$Y_{Ft}^N = C_{Ft} \quad (\text{A.2.53})$$

$$Y_{Ht}^D = d_{Ht}^H + \Delta_{Ht}^H + I_{Ht}^{NH} + \Lambda_{Ht}^{NH} + I_{Ht}^{DH} + \Lambda_{Ht}^{DH} + \frac{1}{2}\Phi B_{Ht+1}^2 + \frac{d_{Ft}^H + \Delta_{Ft}^H + I_{Ft}^{NH} + \Lambda_{Ft}^{NH} + I_{Ft}^{DH} + \Lambda_{Ft}^{DH} + \frac{1}{2}\Phi B_{Ft+1}^2}{1 - \tau} \quad (\text{A.2.54})$$

$$Y_{Ft}^D = d_{Ft}^F + \Delta_{Ft}^F + \frac{d_{Ht}^F + \Delta_{Ht}^F}{1 - \tau} + I_{Ft}^{NF} + \Lambda_{Ft}^{NF} + I_{Ft}^{DF} + \Lambda_{Ft}^{DF} + \frac{I_{Ht}^{NF} + \Lambda_{Ht}^{NF} + I_{Ht}^{DF} + \Lambda_{Ht}^{DF}}{1 - \tau} \quad (\text{A.2.55})$$

$$L_{Ht}^N + L_{Ht}^D = L_{Ht} \quad (\text{A.2.56})$$

$$L_{Ft}^N + L_{Ft}^D = L_{Ft} \quad (\text{A.2.57})$$

$$B_{Ht} + B_{Ft} = 0. \quad (\text{A.2.58})$$

There are 10 equations in the nondurable good sector (from equation (A.2.1) to (A.2.10)), and 10 equations in the durable good sector (from equation (A.2.11) to (A.2.20)). We have 31 equations from the household's problem (from equation (A.2.21) to (A.2.51)). In addition, we have 7 equations in this section (from equation (A.2.52) to (A.2.58)). As a total, we have 58 equations. Those equations define equilibrium conditions for the following 58 variables.

16 variables in nondurable good sector:

$$\begin{bmatrix} \hat{R}_{Ht}^{NH} & \hat{R}_{Ht}^{NF} & \hat{W}_{Ht} & K_{Ht}^{NH} & K_{Ht}^{NF} & K_{Ht}^N & L_{Ht}^N & Y_{Ht}^N \\ \hat{R}_{Ft}^{NF} & \hat{R}_{Ft}^{NH} & \hat{W}_{Ft} & K_{Ft}^{NF} & K_{Ft}^{NH} & K_{Ft}^N & L_{Ft}^N & Y_{Ft}^N \end{bmatrix}$$

16 variables in durable good sector

$$\begin{bmatrix} \hat{P}_{Ht}^{DH} & \hat{R}_{Ht}^{DH} & \hat{R}_{Ht}^{DF} & K_{Ht}^{DH} & K_{Ht}^{DF} & K_{Ht}^D & L_{Ht}^D & Y_{Ht}^D \\ \hat{P}_{Ft}^{DF} & \hat{R}_{Ft}^{DF} & \hat{R}_{Ft}^{DH} & K_{Ft}^{DF} & K_{Ft}^{DH} & K_{Ft}^D & L_{Ft}^D & Y_{Ft}^D \end{bmatrix}$$

26 variables in household's problem

$$\begin{aligned} & [D_{Ht}^H \quad d_{Ht}^H \quad D_{Ht}^F \quad d_{Ht}^F \quad I_{Ht}^{NH} \quad I_{Ht}^{NF} \quad I_{Ht}^{DH} \quad I_{Ht}^{DF} \quad C_{Ht} \quad \hat{P}_{Ht} \quad \hat{B}_{Ht} \quad L_{Ht} \\ & D_{Ft}^F \quad d_{Ft}^F \quad D_{Ft}^H \quad d_{Ft}^H \quad I_{Ft}^{NF} \quad I_{Ft}^{NH} \quad I_{Ft}^{DF} \quad I_{Ft}^{DH} \quad C_{Ft} \quad \hat{P}_{Ft} \quad \hat{B}_{Ft} \quad L_{Ft} \\ & i_t \quad Q_t]. \end{aligned}$$

A.2.2 Solving Steady State of Benchmark Model

From the household's problem, we can solve the return to capital

$$\hat{R}_H^{NH} = \hat{R}_H^{DH} = \hat{P}_H^{DH} \left[\frac{1}{\beta} - (1 - \delta) \right]. \quad (\text{A.2.59})$$

In the steady state, the return to capital in the nondurable-good sector is the same as that in the durable-good sector. This result is intuitive since there is no long-run restriction on moving capital between these two sectors. Similarly, we can find that the return to Foreign capital goods is also the same across these two sectors

$$\hat{R}_H^{NF} = \hat{R}_H^{DF} = \frac{\hat{R}_H^{NH}}{1 - \tau}. \quad (\text{A.2.60})$$

Because of the trade cost, the return to the Foreign-good capital has to be higher than the return to the Home-good capital. As shown in the calibration, this trade cost generates home bias endogenously in the durable good sector.

Substituting equations (A.2.59) and (A.2.60) into the definitions of \hat{R}_H^N and \hat{R}_H^D , we find $\hat{R}_H^N = \hat{R}_H^D$, which says that the return to aggregate capital is the same in those two sectors. Now we assume that the production structure is the same in these two sectors by equalizing the capital share in both sectors ($\chi = \epsilon$).³⁰ If we compare equations (A.2.1) and (A.2.11), the above results and the assumption of equal capital share imply $\hat{P}_H^{DH} = 1$.³¹ That is, in the steady state, durable goods have the same price as nondurable goods. The intuition comes from the fact that the production costs of durable and nondurable goods are the same in the steady state: the same production structure, same cost of capital and same cost of labor. This result gives us the solution to the Home-good capital return

$$\hat{R}_H^{NH} = \hat{R}_H^{DH} = \left[\frac{1}{\beta} - (1 - \delta) \right]. \quad (\text{A.2.61})$$

The return to Foreign-good capital can be solved from equation (A.2.60). The returns to the aggregate capital in both sectors can be solved from their definitions.

$$\hat{R}_H^N = \left[\alpha (\hat{R}_H^{NH})^{1-\gamma} + (1 - \alpha) (\hat{R}_H^{NF})^{1-\gamma} \right]^{\frac{1}{1-\gamma}} \quad (\text{A.2.62})$$

$$\hat{R}_H^D = \left[\alpha (\hat{R}_H^{DH})^{1-\gamma} + (1 - \alpha) (\hat{R}_H^{DF})^{1-\gamma} \right]^{\frac{1}{1-\gamma}}. \quad (\text{A.2.63})$$

³⁰This assumption is also used in other two-sector models, for instance, Erceg and Levin (2006), Whelan (2003).

³¹The steady-state productivity shock is equal to 1 in both sectors.

Now we can solve the wage from equation (A.2.1)

$$\hat{W}_H = \left[(\hat{R}_H^N)^{-\chi} \chi^\chi (1-\chi)^{1-\chi} \right]^{\frac{1}{1-\chi}}. \quad (\text{A.2.64})$$

So far, all prices have been solved and we move to solve quantities of the model.

The utility function in our model is too complicated for us to obtain a recursive solution to quantity variables. Instead we solve them numerically. From the labor demand function in both sectors (equations (A.2.5) and (A.2.15)), we have

$$L_H = L_H^N + L_H^D = (1-\chi)(Y_H^N + Y_H^D)/\hat{W}_H, \quad (\text{A.2.65})$$

in which we used the condition of $\chi = \epsilon$. We assume that in the steady state, labor supply is one third. This gives us the first equation that we will use to solve some variables numerically

$$C_H + Y_H^D = \frac{\hat{W}_H}{3(1-\epsilon)}. \quad (\text{A.2.66})$$

We also used the market clearing condition of nondurable goods ($C_H = Y_H^N$) to get the above equation.

In the symmetric equilibrium, the real exchange rate Q_t is equal to one. The prices of durable goods are the same across countries $\hat{P}_H^{DH} = \hat{P}_F^{DF}$. From the household's first order conditions (equations (A.2.29) and (A.2.30)), we have

$$\frac{1}{\beta} - (1-\delta_D) = \frac{\partial u_t / \partial D_H^H}{\partial u_t / \partial C_H} \quad (\text{A.2.67})$$

$$\frac{1}{1-\tau} \left[\frac{1}{\beta} - (1-\delta_D) \right] = \frac{\partial u_t / \partial D_H^F}{\partial u_t / \partial C_H}. \quad (\text{A.2.68})$$

From the market clearing condition of durable goods, we have

$$Y_H^D = \delta_D \left(D_H^H + \frac{D_H^F}{1-\tau} + \frac{\delta\chi}{\hat{R}_H^N} (C_H + Y_H^D) \left[\alpha \left(\frac{\hat{R}_H^{NH}}{\hat{R}_H^N} \right)^{-\gamma} + \frac{1-\alpha}{1-\tau} \left(\frac{\hat{R}_H^{NF}}{\hat{R}_H^N} \right)^{-\gamma} \right] \right). \quad (\text{A.2.69})$$

From the tradeoff between consumption and labor, we have

$$\frac{\partial u_t}{\partial L_{Ht}} + \hat{W}_{Ht} \frac{\partial u_t}{\partial C_{Ht}} = 0. \quad (\text{A.2.70})$$

Equations (A.2.66), (A.2.67), (A.2.68), (A.2.69) and (A.2.70) are used to solve jointly for consumption

(C_H), durable output (Y_H^D), stock of home-good durable consumption (D_H^H), stock of foreign-good durable consumption (D_H^F) and parameter ρ . ρ is chosen such that the steady state labor supply is one third. With solutions to these variables, we can solve other variables recursively.

$$Y_H^N = C_H \quad (\text{A.2.71})$$

$$K_H^N = \frac{\epsilon}{\hat{R}_H^N} Y_H^N \quad (\text{A.2.72})$$

$$K_H^{NH} = \alpha \left(\frac{\hat{R}_H^{NH}}{\hat{R}_H^N} \right)^{-\gamma} K_H^N \quad (\text{A.2.73})$$

$$K_H^{NF} = (1 - \alpha) \left(\frac{\hat{R}_H^{NF}}{\hat{R}_H^N} \right)^{-\gamma} K_H^N \quad (\text{A.2.74})$$

$$K_H^N = \chi Y_H^N / \hat{R}_H^N \quad (\text{A.2.75})$$

$$L_H^N = (1 - \chi) Y_H^N / \hat{W}_H \quad (\text{A.2.76})$$

$$K_H^{DH} = \alpha \left(\frac{\hat{R}_H^{DH}}{\hat{R}_H^D} \right)^{-\gamma} K_H^D \quad (\text{A.2.77})$$

$$K_H^{DF} = (1 - \alpha) \left(\frac{\hat{R}_H^{DF}}{\hat{R}_H^D} \right)^{-\gamma} K_H^D \quad (\text{A.2.78})$$

$$K_H^D = \epsilon Y_H^D / \hat{R}_H^D \quad (\text{A.2.79})$$

$$L_H^D = (1 - \epsilon) Y_H^D / \hat{W}_H \quad (\text{A.2.80})$$

$$d_H^H = \delta_D D_H^H \quad (\text{A.2.81})$$

$$d_H^F = \delta_D D_H^F \quad (\text{A.2.82})$$

$$I_H^{NH} = \delta K_H^{NH} \quad (\text{A.2.83})$$

$$I_H^{NF} = \delta K_H^{NF} \quad (\text{A.2.84})$$

$$I_H^{DH} = \delta K_H^{DH} \quad (\text{A.2.85})$$

$$I_H^{DF} = \delta K_H^{DF} \quad (\text{A.2.86})$$

$$B_H = 0 \quad (\text{A.2.87})$$

$$i = \frac{1}{\beta} - 1 \quad (\text{A.2.88})$$

A.3 Elasticity Puzzle

In this section, we use a simple example to give more details about the elasticity puzzle in the literature. Suppose the final output is a CES composite of Home and Foreign goods. From the CES aggregation function, we can find demands for imports and the Home goods

$$Y_{Ht}^F = (1 - \alpha) \left(\frac{P_{Ht}^F}{P_{Ht}} \right)^{-\gamma} Y_{Ht} \quad (\text{A.3.1})$$

$$Y_{Ht}^H = \alpha \left(\frac{P_{Ht}^H}{P_{Ht}} \right)^{-\gamma} Y_{Ht}, \quad (\text{A.3.2})$$

where Y_{Ht}^F is the demand for Foreign goods. P_{Ht}^F is the price of Foreign goods and P_{Ht} is the aggregate price. Y_{Ht} is the aggregate demand. Y_{Ht}^H is the demand for Home goods and P_{Ht}^H is the price of Home goods. Dividing one of the above equations by the other, we have

$$\frac{Y_{Ht}^F}{Y_{Ht}^H} = \frac{1 - \alpha}{\alpha} \left(\frac{P_{Ht}^F}{P_{Ht}^H} \right)^{-\gamma}. \quad (\text{A.3.3})$$

By definition, the elasticity of substitution between the Home and Foreign goods is

$$-\frac{d \log(Y_{Ht}^F/Y_{Ht}^H)}{d \log(P_{Ht}^F/P_{Ht}^H)} = \gamma. \quad (\text{A.3.4})$$

If $\log(Y_{Ht}^F/Y_{Ht}^H)$ and $\log(P_{Ht}^F/P_{Ht}^H)$ are stationary, we can regress $\log(Y_{Ht}^F/Y_{Ht}^H)$ on $\log(P_{Ht}^F/P_{Ht}^H)$ to find the elasticity. This exercise has been done with industrial-level data in several papers, for instance, Reinert and Roland-Holst (1992), Blonigen and Wilson (1999), Reinert and Shiells (1993). The estimates from quarterly data are usually small with an average of around 0.85. In aggregate models, this parameter is usually calibrated in the range between 0.5 to 2. Bergin (2006) estimates a two-country general equilibrium model. His estimate is 1.13. Heathcote and Perri (2002) also estimate this parameter with aggregate data and find an estimate of 0.9. So at the business cycle frequency, the empirical findings both at disaggregate and aggregate levels point to a small elasticity of substitution between home and foreign goods.

Ruhl (2005) uses a regression to find the elasticity of substitution in his model. Drozd and Nosal (2007) propose a measurement that follows this spirit, but they do not run a regression. Instead, from equation (A.3.3), the standard deviation of $\log(Y_{Ht}^F/Y_{Ht}^H)$ divided by the standard deviation of $\log(P_{Ht}^F/P_{Ht}^H)$ is also equal to γ under the model's setup. We use both methods in our benchmark model and find our results are robust.

The second strand of literature estimates the elasticity of substitution through the (long-run) response

of trade flows to permanent relative price changes. One example is a tariff reduction. Let's assume that the rate of tariff is τ and the law of one price holds after taking into account the tariff, that is,

$$P_{Ht}^F = (1 + \tau)S_t P_{Ft}^F, \quad (\text{A.3.5})$$

where P_{Ft}^F is the price of foreign goods in the foreign country and S_t is the exchange rate. Substitute this to equation (A.3.3), we have

$$\begin{aligned} \frac{Y_{Ht}^F}{Y_{Ht}^H} &= \frac{1 - \alpha}{\alpha} \left(\frac{P_{Ht}^F}{P_{Ht}^H} \right)^{-\gamma} \\ &= \frac{1 - \alpha}{\alpha} \left((1 + \tau)S_t \frac{P_{Ft}^F}{P_{Ht}^H} \right)^{-\gamma}. \end{aligned} \quad (\text{A.3.6})$$

We use variables without time scripts to denote their steady state values. From equation (A.3.6), we have

$$\Delta \log \left(\frac{Y_{Ht}^F}{Y_{Ht}^H} \right) = -\gamma \Delta \log(1 + \tau) - \gamma \Delta \log \left(\frac{S P_{Ft}^F}{P_{Ht}^H} \right). \quad (\text{A.3.7})$$

Under the assumption that there is no change of relative price $\frac{S P_{Ft}^F}{P_{Ht}^H}$, the increase of trade share is determined by the change of tariff and the elasticity of substitution γ . The equation is identified by regressing it across different industries

$$\Delta \log \left(\frac{Y_{iH}^F}{Y_{iH}^H} \right) = \alpha - \gamma \Delta \log(1 + \tau_i) + \varepsilon_i, \quad (\text{A.3.8})$$

where i is the index of industries. The estimates from industrial level data usually give a large γ , which ranges from 6 to 15. For instance, see Feenstra and Levinsohn (1995), Head and Ries (2001), and Lai and Trefler (2002). Yi (2003) shows that the trade share of output increased substantially for a small decrease in tariffs. He points out that to replicate those findings in a general equilibrium model, the elasticity of substitution between the home and foreign goods must be very large. These results are strikingly different from those obtained from first stand of literature, though under the setup of our example, they are estimating the same parameter γ . This discrepancy has been labeled the elasticity puzzle in the literature.

A.4 Backus-Smith Puzzle

In this section, we describe how to calculate the utility-based real exchange rate used in Section 5.3. The calculation is straightforward if we ignore the frictions in the economy. Suppose that the household is

renting the durable consumption from a competitive market instead of owning it. The rent cost in terms of the nondurable goods will be the marginal utility of durable consumption divided by the marginal utility of nondurable consumption

$$\hat{P}_{Ht}^{RH} = \frac{\partial u_{Ht}/\partial D_{Ht}^H}{\partial u_{Ht}/\partial C_{Ht}} \quad (\text{A.4.1})$$

$$\hat{P}_{Ht}^{RF} = \frac{\partial u_{Ht}/\partial D_{Ht}^F}{\partial u_{Ht}/\partial C_{Ht}}, \quad (\text{A.4.2})$$

where \hat{P}_{Ht}^{RH} and \hat{P}_{Ht}^{RF} are respectively the rental prices for Home- and Foreign-good durable consumption. All prices with a hat are in terms of nondurable goods.

The aggregate durable consumption stock is a CES function of the Home- and Foreign-good durable consumption stocks

$$D_{Ht} = \left[\psi^{\frac{1}{\theta}} (D_{Ht}^H)^{\frac{\theta-1}{\theta}} + (1-\psi)^{\frac{1}{\theta}} (D_{Ht}^F)^{\frac{\theta-1}{\theta}} \right]^{\frac{\theta}{\theta-1}}, \quad (\text{A.4.3})$$

where ψ is the weight of Home durable goods in the durable consumption composite, and θ is the elasticity of substitution between the Home and Foreign durable goods. It is straightforward for us to find the shadow price of D_{Ht}

$$\hat{P}_{Ht}^R = \left[\psi (\hat{P}_{Ht}^{RH})^{1-\theta} + (1-\psi) (\hat{P}_{Ht}^{RF})^{1-\theta} \right]^{\frac{1}{1-\theta}}. \quad (\text{A.4.4})$$

The utility consumption is a CES function of durable and nondurable consumption

$$UC_{Ht} = \left(\mu^{\frac{1}{\zeta}} D_{Ht}^{\frac{\zeta-1}{\zeta}} + (1-\mu)^{\frac{1}{\zeta}} C_{Ht}^{\frac{\zeta-1}{\zeta}} \right)^{\frac{\zeta}{\zeta-1}}. \quad (\text{A.4.5})$$

It is easy for us to find the utility-based price index

$$\hat{P}_{Ht}^{UC} = \left[\mu (\hat{P}_{Ht}^R)^{1-\zeta} + (1-\mu) \right]^{\frac{1}{1-\zeta}}. \quad (\text{A.4.6})$$

Symmetric equations hold in the Foreign country, from which we can find the utility-based price index in the Foreign country \hat{P}_{Ft}^{UC} . The utility-based real exchange rate is

$$Q_t^{UC} = \frac{Q_t \hat{P}_{Ft}^{UC} \hat{P}_{Ht}}{\hat{P}_{Ht}^{UC} \hat{P}_{Ft}}, \quad (\text{A.4.7})$$

where Q_t is the CPI-based real exchange rate. \hat{P}_{Ht} is the consumer price index in the Home country and \hat{P}_{Ft} is the consumer price index in the Foreign country. To see how to get this equation, it is useful to note that

$$\begin{aligned}
 Q_t^{UC} &= \frac{S_t P_{Ft}^{UC}}{P_{Ht}^{UC}} \\
 &= \frac{\frac{S_t P_{Ft}}{P_{Ht}} \frac{P_{Ht}}{P_{Ft}} \frac{P_{Ft}^{UC}}{P_{Ft}^N} P_{Ft}^N}{\frac{P_{Ht}^{UC}}{P_{Ht}^N} P_{Ht}^N} \\
 &= \frac{Q_t \hat{P}_{Ft}^{UC} \hat{P}_{Ht}}{\hat{P}_{Ht}^{UC} \hat{P}_{Ft}}, \tag{A.4.8}
 \end{aligned}$$

where all prices without a hat are nominal prices and P_{Ht}^N (P_{Ft}^N) is the nominal price of Home (Foreign) nondurable goods.