A Biological Model of Union Politics^a

Michael Kremer Harvard University, Brookings Institution, and NBER

and

Benjamin A. Olken Harvard University

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Abstract

This paper applies principles from evolutionary biology to the study of unions. We show that unions which maximize the present discounted wages of current members will be displaced in evolutionary competition by unions with more moderate wage policies that allow their ...rms to live longer. This suggests that unions with constitutional incumbency advantages that allow leaders to moderate members' wage demands may have a selective advantage. When incumbency advantages are exogenously reduced, the model predicts unions should increase their wage demands. These predictions seem broadly consistent with the evidence.

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Biological models suggest that selection pressure often works against organisms that are too harmful to their hosts. For example, a disease such as the Ebola virus, which kills its hosts in days, has little opportunity to spread from one host to another. In contrast, the viruses that cause the common cold are widespread. Mitochondria, which were probably originally parasites, evolved to become essential to their hosts and are now universal.

This paper applies this basic biological concept from evolutionary biology to the interaction between unions and ...rms and compares the results to a model in which unions maximize the present discounted rents of members. We argue that unions that demand the level of wages optimal for their members will be displaced in competition with more moderate unions. In our model, the dynamics of union coverage depend on both the rate at which unions spread to non-union ...rms and the rate at which unionized ...rms die. Greater rent extraction by a union can increase the spread rate of the union by making the union more attractive to workers in non-unionized ...rms. On the other hand, greater rent extraction by unions can also lead to increases in the death rates of unionized ...rms. The evolutionarily stable level of rent extraction therefore involves a tradeo^m between attractiveness to workers and the e^mect on ...rm death rates.

The model suggests that reducing the level of rent extraction slightly from the level that maximizes the present discounted value of rents to union members causes a second-order reduction in members' welfare, and hence in the spread of unions, but a ...rst-order reduction in the death rate of unionized ...rms. Selection pressure therefore favors unions with lower levels of rent extraction than would be optimal for workers.

In biology, evolutionary pressures may be the ultimate cause of an organism's attributes, but the proximate cause of those attributes are speci...c genes and the resulting chemical processes. Similarly, while evolutionary pressures may select for a union that tends to moderate worker's wage demands, there must be speci...c persistent organizational mechanisms that make unions more moderate. For example, if a union is controlled by its rank and ...le, its members will vote for the policies that maximize their welfare rather than the policies that would survive evolutionary competition. In the presence of incumbency advantages, however, union leaders may choose to moderate wage demands, which would bene...t workers, in return for contract provisions that bene...t the union

leadership. Selection pressure may therefore also favor unions with constitutional incumbency advantages that allow leaders to pursue more moderate wage demands than those preferred by the rank and ...le.

There is evidence for these implications. Most existing unions do, in fact, have constitutions that create strong advantages for incumbents. Furthermore, rank and ...le dissident movements almost always demand more rent extraction than union leadership, suggesting that the policies of unions tend to be more moderate than would be optimal for workers. In several cases in which incumbency advantages have been weakened due to plausibly exogenous factors, dissident movements have become powerful, wage demands have escalated, and industries have declined. The model also suggests that if multiple unions compete for the same workers within ...rms, as in several European countries, incumbency advantages will be weaker and unions will have to adopt more militant policies.

This paper builds on earlier work. Dickens and Leonard [1985] and Freeman [1983] show that unions must continually organize new enterprises in order to o¤set the natural decline in membership due to turnover among ...rms. Freeman [1998] documents sudden spurts in unionization followed by gradual declines. He accounts for this in a model in which as unionization levels increase, it becomes ...rst easier and then more di⊄cult to unionize new ...rms. This means that there will be one steady-state level of unionization at zero, and one positive steady state. Hannan and Freeman [1987, 1988] use a sociological model of organizational ecology to examine how birth and death rates of unions depend on the existing number of unions. This paper di¤ers in explicitly examining the predator-prey population dynamics involving unions and ...rms and in deriving the implications for union politics.

This paper is also related to several papers that apply biological techniques to other economic situations. Dutta and Radner [1999] argue that ...rms that retain more earnings than would be optimal for their shareholders will survive longer and eventually outnumber ...rms that retain the optimal amount. This paper di¤ers in methodology from Dutta and Radner, however, by explicitly modelling the spread of unions within a population of ...rms and by considering competition among unions in determining which unions will survive.

The focus of this paper is on deriving endogenously the evolutionarily stable level of rent extraction and its implications for union politics. In a related paper (Kremer and Olken [2001]), we explore extensions to the model that take the level of rent extraction by unions as given. We show that if negative shocks to ...rms reduce productivity but are not fatal to ...rms, then there can be multiple equilibria–one equilibrium with low productivity and high unionization and one with high productivity and low unionization. We also present empirical evidence documenting the model's implication that increases in the death rate of ...rms should lead to lower unionization levels.

The remainder of the paper is organized as follows. Section 1 provides background on relevant U.S. collective bargaining institutions. Section 2 presents the model and solves for the steady-state level of unionization with a single union and an exogenously given level of rent extraction. Section 3 contrasts economic and evolutionary models of the determination of levels of rent extraction, and ...nds that the evolutionarily stable level of rent extraction is less than that which maximizes the welfare of the workers. Section 4 discusses the model's implications for union institutions, and shows that incumbency advantages for union leaders will be present in the evolutionarily stable union. Section 5 presents evidence from the history of unions that suggests the model's predictions seem consistent with union behavior. Section 6 concludes by arguing that the welfare e¤ects of unions, and of union moderation, are ambiguous under the model, and by discussing the applicability of this biological approach to other institutions.

1 Background on U.S. Collective Bargaining Institutions

Before introducing the model, it is useful to review a few features of U.S. collective bargaining institutions relevant to the model. Outside of construction, music, and a few other industries, most new ...rms begin life without unions. Under the Federal law covering most industries, if thirty percent of workers sign a petition calling for an election, a certi...cation election supervised by the National Labor Relations Board (NLRB) is held. A union is recognized if more than half the workers vote for it in such an election.

Support from existing unions plays an important role in unionizing new ...rms. Not only are

workers more likely to support unions if they have friends or relatives who are union members, but hired union organizers, paid for through dues of existing union members, also play an important role. These paid organizers are often critical in obtaining the signatures required to have an election and in campaigning for union certi...cation, because unlike activists within ...rms, paid organizers are not susceptible to threats from management. Workers at a plant are theoretically protected from retaliation for supporting a union, but penalties for dismissing union supporters are weak, and union activists are often dismissed. In fact, one in twenty workers who vote for a union in an organizing election are later found to have a valid claim for unfair dismissal by the NLRB [Weiler, 1984]. The percentage among union activists is likely to be even higher, making it dangerous for workers in a ...rm to openly campaign for a union in an NLRB election. In addition to making organizing activities hazardous for employees, ...rms also use legal tactics to delay unionization votes, such as challenging de...nitions of the bargaining unit and thus the set of workers who are eligible to vote in the NLRB election. Responding to these challenges requires lawyers and money, which existing unions can help provide.

Once a ...rm unionizes, workers can theoretically deunionize through a decerti...cation election, or vote to change their a¢liation from one union to another. In practice, however, decerti...cations are infrequent, and switching union a¢liations rarely happens, given the organizing costs involved and the reluctance of unions to poach each others' territory. In fact, the AFL-CIO constitution explicitly prohibits member unions from attempting to organize a ...rm currently organized by a di¤erent AFL-CIO member union. When unions decline, it is therefore not primarily because of decerti...cation elections, but rather because the ...rms covered by the union reduce employment or close down a unionized location altogether.

The model in this paper is designed to apply to those U.S. industries covered by the standard NLRB rules: new ...rms start as non-union; paid union organizers play an important role in unionizing new ...rms; and once employees at a ...rm vote in a particular union, the ...rm stays unionized for the remainder of its life.¹ The resulting dynamics of unionization levels bear a similarity to those under the Susceptible-Infected (SI) model of epidemiological dynamics (see Anderson and

¹As discussed above, in a few industries, such as construction, textiles, and music, institutions di¤er, and new ...rms often start out unionized. The model is not intended to apply to these industries.

May [1991]). In that model, new potential hosts are born uninfected; the chance that they become infected increases with the number of hosts already infected; and once hosts are infected, they stay infected until they die. (As discussed in the conclusion, this comparison is purely positive, not normative.)

2 The Model with a Single Union and Exogenous Rent Extraction

This section describes the basic model for the spread of a single union with an exogenously given level of rent extraction. Section 2.1 begins by outlining the entry, investment, and exit behavior of ...rms taking union behavior as given. Section 2.2 then describes how unions spread and characterizes the steady-state level of unionization.

2.1 Firms

We assume that ...rms produce one of a continuum of measure F possible products, and that there is a downward-sloping demand curve for each product. Entry into a sector requires start-up costs, described below, but once these costs have been paid, output is linear in labor and requires no other inputs, i.e. $q(L) = {}^{-}L$. Once there is a ...rm in a market, if a second ...rm were to enter, the two ...rms would engage in Bertrand competition and earn zero pro...ts. Knowing this, only one ...rm enters each market, and the measure of the number of ...rms is equal to F. For simplicity, we will assume that all ...rms face identical production functions, and so behave identically.

In addition, there is a competitive, constant returns to scale home-production sector in which workers can earn some ...xed exective wage, \underline{w} . We assume that there is a su¢cient quantity of workers such that some are always employed in the home-production sector, i.e. N > L^xF, where N is the quantity of workers and L^x is the optimum quantity of workers each ...rm employs at wage \underline{w} .

Given that each ...rm is a monopoly, each ...rm charges the pro...t maximizing price, pays workers the wages \underline{w} , and earns pre-union pro...ts denoted by $\frac{1}{4}$. By "pre-union pro...ts," we mean the surplus of revenues over the wages paid in the absence of a union. (We assume that there is some demand for each product at a price above $\stackrel{\text{\tiny W}}{=}$, so that each ...rm produces a positive amount, and that the pro...ts are maximized at some ...nite price.²) If the ...rm is unionized, the union extracts a ...xed proportion [®] of these pro...ts. Later, we will endogenize [®], but from the perspective of the ...rm, [®] is an exogenous parameter.

Suppose that ...rms are subject to large negative productivity shocks that cause them to exit with hazard rate \pm , where \pm depends in part on unobservable investment, I, such as avoiding negligence that could lead to lawsuits.³ We also assume that $\pm_1 < 0$ and $\pm_{11} > 0$.

The optimal investment for a unionized ...rm depends on the share of pro...ts it can keep if it stays alive. Given the discount rate, r, the ...rm chooses I to maximize its present discounted value given [®]:⁴

$$I(^{(B)}) = \underset{I}{\operatorname{argmax}} \frac{(1 ; {}^{(B)})^{\underline{\lambda}} ; I}{r + \pm(I)}:$$
(1)

Investment is decreasing in rent extraction by unions, ®, since

$$\frac{dI}{d^{(B)}} = \frac{\frac{1}{2} \pm \frac{1}{1}}{\frac{1}{1} \left[(1_{i} \otimes \frac{1}{2}) \frac{1}{4} + \frac{1}{1} \right]} < 0:$$
(2)

It is therefore possible to write $\pm = \pm (I(^{(R)}))$, or more concisely, $\pm = \pm (^{(R)})$, where $\pm \otimes > 0$.

So far, we have said that there will be only one ...rm in each industry, but have not yet speci...ed how a given capitalist gets to own that ...rm. We model the process by which a given capitalist obtains the monopoly on a particular product as an auction or, equivalently, as a lottery. This can be thought of either literally, such as a government auction for a cell-phone license, or as a metaphor for advertising, research and development, or other up-front expenditures that result in some probability of being successful in an industry, as is widespread among Internet ...rms today. Assuming that there is competition among a large number of risk-neutral capitalists, the cost of

²For example, suppose that all consumers had an identical CES utility function equal to $U = \int_{0}^{3} R_{F} x_{1}^{\frac{1}{2}} di^{\frac{1}{2}}$, where x_i represents demand for good i. As long as $\frac{1}{2} > 0$; so that the elasticity of substitution is greater than 1, all ...rms will charge a ...nite price.

³The hazard rate could also depend on observable investment, but since unions and ...rms can contract on the e¢ cient level of observable investment, it would not vary with rent extraction, and hence we abstract from observable investment in this paper.

⁴Note that equation (1) assumes that the owner of the ...rm receives a continuation payo¤ of 0 in the event the ...rm dies. This is because if the ...rm dies, the owner will need to start a new ...rm, and as will be shown below, the ex-ante pro...ts of starting a new ...rm will be 0.

entering an industry will be equal to the expected value of owning a ...rm. The ex ante pro...ts from opening a ...rm will therefore always be zero. Whenever a ...rm dies, an auction is held and a new ...rm enters. The number of ...rms therefore remains equal to F.

2.2 Steady-State Unionization Levels

Under the model, new ...rms are established without unions. Firms di¤er in how easy they are to unionize, depending on factors ranging from the layout of the factory \ddagger oor to the personalities of managers. (In order to keep the model tractable, we consider a simple model in which ...rms, plants, and union bargaining units are coterminous.) Each ...rm is born with a certain di¢culty of being organized, which we denote by c (for cost), and retains that same level of di¢culty until it dies. For simplicity, we will assume that for newborn ...rms c is distributed uniformly on the interval [0,1].⁵

In each unit of time, the union has an organizing budget that it uses to organize new ...rms. We assume that unions are credit constrained, so that the amount they can spend on organizing exorts depends on their current level of dues collection. The union's budget is therefore equal to BU, where B represents the amount that unionized workers in each ...rm contribute toward the overall union's organizing budget and U is the number of unionized ...rms. (We abstract from size dixerences among ...rms.)

The attractiveness of a particular union to workers depends on (, the proportion of the ...rm's total pro...ts it extracts for the workers. The union's exective organizing budget is A(()BU, where A(() indicates the union's attractiveness as a function of (. Workers recognize that ...rms will die ox quickly if unions extract high levels of rents, so A(() will not be monotonic in (.

The analysis in this section will focus on identifying steady states. The transition dynamics outside of the steady state are somewhat more complex, and are discussed in Appendix A.2. There are two criteria that must be satis...ed in the steady state. First, in the steady state, the total number of unionized ...rms, denoted U, must remain constant. Next, note that when a ...rm dies,

⁵In standard epidemiological models, the e \oplus ciency with which infected hosts pass on the disease also declines as disease prevalence increases, but for a di¤erent reason. In epidemiology, e \oplus ciency declines because of random matching between hosts in the population–when the disease becomes very prevalent, many of these matches occur between two infected hosts, so those matches do not contribute to the spread of the disease. In this model, e \oplus ciency declines because ...rms are heterogeneous in the ease in which they can be unionized, and unions focus ...rst on the easiest ...rms to organize.

the ...rm that replaces it has a new di¢culty of unionization c, distributed according to the initial Uniform[0,1] distribution. This leads to the second criteria for the steady state, that the distribution of organizing di¢culties of union and non-union ...rms must also remain constant.

To identify the steady state, in this section we ...rst consider the case in which there is only one union, with an exogenously given level of @. (Section 3 endogenizes @.) We assume that the union can observe the di¢culty of organizing a ...rm before it starts an organizing e¤ort. Therefore, the union will target those ...rms that are the easiest to organize ...rst. Suppose that at a given moment all ...rms with organizing di¢culty below some cuto¤ point p are unionized and all ...rms with di¢culty above p are non-unionized. This will be the case in steady state or if the size of the union is increasing, since unions always target the easiest to organize ...rms that have just been created with di¢culty distributed according to the initial distribution and a "thick" segment of pre-existing ...rms with di¢culties greater than p. Unions will optimally spend their organizing budget ...rst to organize newly emerged ...rms in the thin segment with organizing di¢culty below p. Once the union has organized those ...rms, it will spend what remains of its budget on the remaining previously existing ...rms in the thick segment with marginal di¢culty of organizing p.⁷

A graphical depiction of the steady-state is given in Figure 1. Note that the density of unionized ...rms is lower than the density of non-unionized ...rms in steady-state, because although the cost distribution for newborn ...rms is uniform, unionized ...rms have a higher death rate, and therefore do not live as long as non-union ...rms.

Normalize the number of ...rms, F, to 1, so that U becomes the fraction of ...rms that are unionized. At an instant of time dt, $[\pm (\ensuremath{\circledast}) U + \pm (0) (1_i U)]$ dt ...rms will have just exited due to a negative productivity shock. As those ...rms die, new ...rms will be born with di¢culties of being

⁶During transitions that involve the decline of a union–for example, in response to some kind of shock that reduces the union's e¤ective organizing budget–there will actually be a range of costs where there will be both unionized and non-unionized ...rms. This is discussed in more detail in Appendix A.2. In the steady state, however, there will be some p below which all ...rms are organized and above which no ...rms are organized.

⁷Strictly speaking, this suggests that in the steady state, the percentage of unionized ...rms will be higher among newly-created ...rms than among older ...rms. However, this is an artifact of our assumption of identical ...rms with Poisson death rates. In practice, if ...rms di¤er in intrinsic pro...tability, more pro...table ...rms will be more attractive to unions and longer-lived. To take another example, if ...rms take time to grow and initially face a high death rate, unions may not organize early in the ...rm's life.



Figure 1: Steady-State Unionization

unionized distributed according to the initial distribution. For a union to organize all newborn ...rms with di¢culty level below p, the union will have to spend

$$[\pm (^{((e))}U + \pm (0) (1_{i} U)] dt \int_{0}^{p} c dG (c); \qquad (3)$$

which, since G (c) is Uniform[0,1], is just

$$[\pm (^{(R)})U + \pm (0)(1_{i} U)]dt \frac{p^{2}}{2}$$
: (4)

In order for p; the threshold below which all ...rms are organized, to remain constant, the union's exective organizing budget must exactly correspond to the total cost of organizing all newly created ...rms with cost less than or equal to p, i.e.:

$$A(^{(\text{B})}BU = [\pm (^{(\text{B})}U + \pm (0)(1 + U)]\frac{p^2}{2}:$$
(5)

This condition, that p must not change, is one of the two conditions that must be satis...ed in the steady-state. If the union had a surplus, i.e. if $A(^{(R)})BU > [\pm (^{(R)})U + \pm (0)(1 \mid U)]\frac{p^2}{2}$, then it would spend that surplus organizing non-union ...rms in the "thick" segment with di¢culty greater than

p, and p would increase. Conversely, if the union's budget was not su¢cient to organize all of the newly born ...rms with di¢culty below p, then p would decrease.

The other condition that must be satis...ed in the steady-state is that the number of unionized ...rms, U, must also not change. This means that the number of newly born ...rms the union organizes must exactly equal the number of ...rms the union loses to attrition. This yields the condition

$$[\pm (^{(B)}) U + \pm (0) (1_{i} U)] p = \pm (^{(B)}) U:$$
(6)

These two conditions, that the di¢culty distribution of unionized and non-unionized ...rms does not change and that the number of unionized ...rms does not change, lead us to the following characterization of the steady-state:

Proposition 1 With a single union, there can be two steady-states, the trivial steady-state with no unionization (U = p = 0) and the steady-state with

$$U^{\alpha} = \begin{cases} 8 \\ \frac{2\pm(0)A(^{(0)}B)}{\pm(^{(0)})^{2}i} & \text{if } 2A(^{(0)}B + \pm(^{(0)}) \\ 2A(^{(0)}B + \pm(^{(0)})i \\ 1 & \text{otherwise} \end{cases} ; \qquad (7)$$

$$\begin{cases} 8 \\ 8 \\ 2A(^{(0)}B \\ 2A(^{(0)}B \\ 1 & \text{otherwise} \end{cases}$$

$$p^{\pi} = \frac{12A(@)B \cdot \pm (@)}{2} \qquad (8)$$

Moreover, the trivial steady state with no unionization is locally unstable, and the steady state with partial unionization is locally stable.

Proof. See Appendix A.1.

Note that when $2A(@)B > \pm(@)$, the union's organizing budget is substantial enough to overcome the attrition of member unions, so the model would be at a corner solution with steady state unionization levels of either 0 or 1. For the remainder of the paper we will assume that

$$2A(^{(R)})B \cdot \pm (^{(R)}); \qquad (9)$$

unless otherwise stated, so that we are in the more interesting interior case with only partial unionization in the non-trivial steady-state.

The intuition behind the stability results is that the total resources available for union organizing rise linearly with the number of unionized ...rms, while the cost of replacing ...rms lost to attrition rises faster than linearly given that the easiest ...rms to unionize are unionized ...rst. Given our assumption of a uniform distribution of di¢culty of unionization, the cost of replacing ...rms lost to attrition is quadratic in the level of unionization. The cost of replacing unionized ...rms lost to attrition is less than the resources available for unionization at all unionization levels between 0 and the non-trivial steady-state, and greater than the available resources curve at higher levels of unionization. With a non-uniform cost distribution, there could be multiple stable non-trivial equilibria, but we focus on a simple case here.

Since the distribution of unionization di¢culties is uniform on [0, 1], p^{α} , the di¢culty level below which all newborn ...rms are unionized, is also the percentage of newborn ...rms that are unionized. In steady state, U^{α} , the proportion of unionized ...rms, is less than p^{α} , because unionized ...rms die at a faster rate than non-union ...rms.⁸

Exogenous increases in the death rate of ...rms reduce steady-state unionization. The intuition is that with higher attrition rates, at every level of membership the union must devote a greater share of its resources to replacing ...rms lost to attrition and less to expanding the size of the union. The following proposition states these results formally.

Proposition 2 Increasing the death rate of all union and non-union ...rms by the same proportion reduces the steady-state level of unionization U^{α} .

Proof. See Appendix A.1.

Empirical results supporting this conclusion are presented in Kremer and Olken [2001]. We test whether industries with a high turnover of ...rms have low unionization rates. We ...nd that a 1 percentage point increase in the annual exit rate of ...rms in an industry is associated with a

⁸Of course, in the real world, factors outside the model may obscure this relationship. In particular, ...rms may di¤er in intrinsic pro...tability, and more pro...table ...rms are more likely to attract attention from unions and less likely to exit.

3.4 percentage point decrease in the unionization rate, controlling for average plant size, capital intensity, and industry concentration. These results are of similar magnitude to those predicted by the model when equation (28) is evaluated using mean values for union membership and exit values and a range of parameter values.⁹

3 Rent Extraction Under Optimizing and Evolutionary Models

This section contrasts economic and evolutionary analyses of the determination of the level of rent extraction, [®]. Under a standard economic approach, unions choose [®] to maximize the present discounted value of rents to union members, taking into account the dependence of ...rm investment on [®]. Under the evolutionary approach, unions are endowed with di¤erent values of [®]. Unions with di¤erent levels of [®] compete, and only those unions with evolutionarily stable values of [®] survive. In many circumstances, the economic and evolutionary approaches yield the same steady-state predictions, albeit with di¤erent dynamics (as in Nelson and Winter, 1982). In this model, however, the evolutionarily stable value of [®] will be less than the value of [®] that maximizes the present discounted value of rents to current union members.

The remainder of this section is organized as follows. Subsection 3.1 derives the conditions for the optimal level of [®] for the workers. Subsection 3.2 then shows that the evolutionarily stable level of rent extraction is less than this welfare maximizing level.

3.1 Welfare-Maximizing Level of Rent Extraction

We ...rst consider a fairly conventional setting in which unions choose [®] to maximize the present discounted value of rents accruing to current union members.

We assume that unions cannot commit to a path of rent extraction over time. Otherwise, the optimal contract would involve a one-time payment from the ...rm in exchange for an agreement to never again extract any rents. This would avoid distorting the ...rms's investments in staying

⁹Assuming $U^{\pi} = 0.26$, = 1.5, $\pm (0) = .076$, and 2A ([®]) $B = \frac{\pm (0)}{2}$ yields a predicted value (from equation (28) of the coe¢cient on exit rates of 3.8. Changing any of these assumptions by 25% yields predicted coe¢cients between 2.8 and 5.2.

alive. In fact, it is di⊄cult to contract on rent extraction, since ...rms may not be able to specify in advance the exact tasks needed later and unions may have di⊄culty committing never to extract rents.

Given this, the union chooses how much it will extract each year. Since ...rms' pre-union pro...ts are constant, there is no di¤erence between extracting a lump sum each year and a share of pro...ts each year. We will consider for the moment the case in which unions have all the bargaining power in negotiations with ...rms, in the sense that they can present ...rms with take-it-or-leave-it o¤ers. (Section 4 presents a somewhat more complex bargaining game between unions and ...rms.) This assumption may be reasonable if a single union bargains with many ...rms and has incentives to acquire a reputation for toughness. Although unions cannot commit to a time-path of future rent extraction, bargaining is statically e¢cient, so that all ...rms employ the e¢cient number of workers.

The present discounted value of rents accruing to current union members is

$$\frac{{}^{\textcircled{\sc 8}}}{r + \pm ({}^{\textcircled{\sc 8}})}:^{10}$$
(10)

Since \pm (®) increases with ®, the optimal level of rent extraction for the worker involves a trade-o \approx between the \pm ow of rents and the hazard rate that the ...rm will chose, which would cause workers to cease to obtain any rents.¹¹

The ...rst order condition for the level of $^{\mbox{\tiny B}}$ that maximizes the present discounted value of rents for workers, denoted $^{\mbox{\tiny B}}_{\mbox{\tiny W}}$, is

$$r + \pm ({}^{\mathbb{R}}_{W}) i {}^{\mathbb{R}}_{W} \pm {}^{\mathbb{Q}} ({}^{\mathbb{R}}_{W}) = 0:$$
 (11)

For the remainder of the paper, we assume that the parameter values are such that we have an interior solution for \mathbb{B}_{W} .

We assume that the function A ([®]), which indexes how attractive a union is to potential new

¹⁰Note that the results would not be substantially di¤erent if workers had a higher discount rate than ...rms. For example, workers might have a higher discount rate to incorporate the chance of death of workers or separation from the ...rm.

¹¹Note that this expression assumes implicitly that workers receive no union rents if they leave the ...rm. This will be true if the labor supply, N, is large enough, so that the probability the worker obtains a second job in the potentially unionizable sector, and therefore has a chance of getting a unionized job, approaches 0.

members, is continuously increasing in the present discounted value of rents obtained by workers (i.e., equation (10)). The assumption that $A(^{(R)})$ is increasing in the present discounted value of rents extracted by workers implies that a union that maximizes the welfare of its members, i.e. a union that extracts $^{(R)}_{W}$, has the easiest time organizing unorganized ...rms.¹²

3.2 Evolutionarily Stable Rent Extraction

An alternative approach to understanding how [®] is determined is to assume that [®], the level of rents a union extracts, is ...xed for a given union, but that there are many unions with di¤ering levels of [®]. One can then ask which union will survive in evolutionary competition.

If there are multiple unions, each would like to spend its organizing budget trying to organize the easiest ...rms. Rather than assume that unions waste resources on battles to organize the same unorganized ...rms, we will assume that they divide them so that at every level of di¢culty, c, unions organize ...rms in proportion to their e¤ective organizing budgets.¹³ Since the e¤ective organizing budget is the actual organizing budget (BU) multiplied by how attractive the union is to workers (indexed by the function A (®)), unions that are more attractive to workers can organize disproportionately more ...rms. For example, suppose that there are two unions, a moderate union with M member ...rms and extraction rate $@_M$ and a radical union with R member ...rms and extraction rate $@_R$. The moderate union targets $\frac{A(@_M)BM}{A(@_M)BM+A(@_R)BR}$ of the non-unionized ...rms with di¢culty less than p and the radical union targets the remainder.

We can now identify the evolutionarily stable level of rent extraction and show that it will be

¹²In fact, while we assume that A(@) is maximized at $@_W$, it is plausible that it is maximized at some value less than $@_W$. Firms can employ a wide variety of anti-unionization tactics, including requiring workers to attend anti-union meetings on company time, challenging the proposed de...nition of the bargaining unit, and illegally ...ring union activists, and the more they expect unions to extract, the more vociferously they will oppose unions. Given the response of ...ms' unobservable investment to @, as @ approaches $@_W$, increases in @ hurt ...rms much more than they help workers. Firms' opposition to unionization might therefore increase more rapidly with @ than workers' support for unionization. Firms may even ease the entry of more moderate unions to forestall more radical alternatives. Such e¤ects, however, would only make showing that $@_S < @_W$ easier, so we ignore any e¤ects of this sort in the model.

¹³We thus allow for unions that extract more for their members to be more successful in attracting members, but rather than have a completely general function for union recruiting as a function of the union's level of rent extraction and that of each of its competitors, we consider the case in which each union's recruiting is proportional to its attractiveness to workers and its organizing budget. We conjecture that the main results of the paper (in particular, Proposition 5) would hold for any division of ...rms that is continuously increasing in the e¤ective organizing budget at each di¢ culty level. We model unions dividing ...rms in proportion to their e¤ective organizing budgets for analytical tractability.

smaller than the welfare-maximizing level of rent extraction. First, we specify how the de...nition of evolutionary stability applies in our context.

De...nition 1 A union that extracts a rent level [®] is evolutionarily stable if and only if, starting from the steady state containing only the [®] union, there exists an $^{\circ} > 0$ such that if any other union with size " < $^{\circ}$ invades, the invading union will disappear.

Proposition 3 The union that extracts the level of rent [®] that maximizes the ratio $\frac{2A(\ensuremath{\circledast})B}{\pm(\ensuremath{\circledast})}$ will be evolutionarily stable.¹⁴

Proof. See Appendix A.1.

The key idea of the proof is that $\frac{2A(@)B}{\pm(@)}$ is the steady-state level of p[#], the proportion of newborn ...rms that are unionized in steady-state. This determines the average cost level the union can sustain in steady-state. A union that can bear a higher average cost level than the incumbent will be able to unionize disproportionately more ...rms, and will be able to invade; a union unable to bear as much will experience negative growth and disappear. Therefore, no union can successfully invade a steady-state containing the union with the highest possible steady-state average cost level. The union with the maximum value of $\frac{2A(@)B}{\pm(@)}$ is therefore evolutionarily stable.

Proposition 3 guarantees that, starting from a steady state occupied by only the \circledast_S union, no other union can invade. We now show that facing a steady state containing any other union or combination of unions, the \circledast_S union can successfully invade. Furthermore, if the system then converges to a steady state, that steady state will contain only the \circledast_S union. To show this, it will be useful to …rst state the following lemma.

Lemma 1 If multiple unions coexist in the steady-state, then they must have the same ratio of <u>exective organizing budget to ...rm death</u> rate, i.e. $\frac{2A(\mathbb{B}_M)B}{\pm(\mathbb{B}_M)} = \frac{2A(\mathbb{B}_R)B}{\pm(\mathbb{B}_R)}$. Furthermore, this ratio

¹⁴It is worth noting that while the level of [®] that maximizes $\frac{2A(@)B}{\pm(@)}$ will be unique under most normal parameterizations of A ([®]) and \pm ([®]), this need not hold in general. It is possible to construct functions A ([®]) and \pm ([®]) as that $\frac{2A(@)B}{\pm(@)}$ has multiple global maxima. In this case, there will be several possible levels of rent extraction [®]s that, together or independently, would be evolutionarily stable. However, ...nding examples of functions A ([®]) and \pm ([®]) satisfying all of the conditions above and where $\frac{2A(@)B}{\pm(@)}$ has multiple global maxima requires careful construction, so it seems likely that this will not occur empirically.

will be equal to the organizing cost of the most di¢cult to organize ...rm that is unionized in the steady-state, i.e. $p_M^{\alpha} = \frac{2A(\circledast_M)B}{\pm(\circledast_M)}$.

Proof. See Appendix A.1.

The intuition behind the Lemma is that for two unions to exist in the steady-state, one must be a more moderate union that is less attractive to workers but loses fewer of its member ...rms due to attrition, while the other must be a more militant union that is better able to unionize new ...rms but also loses more of its member ...rms to attrition. Lemma 1 speci...es how precisely to balance this trade-o¤.¹⁵

With this lemma characterizing the steady-state in mind, we can show that an evolutionarily stable union will be able to invade a steady-state containing any other union.

Proposition 4 The \mathbb{R}_{S} union can successfully invade any steady-state other than the one containing another \mathbb{R}_{S} union.

Proof. The proof is essentially similar to the proof of Proposition 3, and is given in Appendix A.1. ■

We have so far shown that, starting from a steady-state containing the $@_S$ union, no union can invade, and starting from a steady-state with any other union, the $@_S$ union can invade and grow. We have not ruled out a limit cycle, but we do know that if there is a steady-state, it must be the steady-state containing only the evolutionarily stable union. To see this, suppose that there are two unions, the stable union S and an incumbent union I. By Lemma 1, the eventual steady state cannot contain both the S union and the I union, since they have di¤erent ratios $\frac{2A(@)B}{t(@)}$. We have already shown that as the world approaches the steady-state with the I union, whatever tiny amount " of the S union that remains will grow, so the " union can not be eliminated entirely. Therefore, we have shown that the $@_S$ union can invade and displace any other union.

¹⁵Note that when the function $\frac{2A(\textcircled{B})B}{\pm(\textcircled{O})}$ is strictly concave, which it will be for many (but not all) concave functions A ([®]) and increasing functions $\pm(\textcircled{O})$, there can be at most two unions in equilibrium. When $\frac{2A(\textcircled{O})B}{\pm(\textcircled{O})}$ is not strictly concave, on the other hand, there can be three or more unions in equilibrium. Even in this case, however, the same argument in Lemma 1 goes through.





Now that we know which union will be evolutionarily stable, we can show our key result: that the evolutionarily stable union it is more moderate than the welfare-maximizing union.

Proposition 5 The evolutionarily stable level of rent extraction, $@_{S}$, is smaller than the level of rent extraction that maximizes the present discounted value of wages of current members, $@_{W}$.

Proof. As shown above, the evolutionarily stable level of rent extraction, $^{(e)}S$, maximizes the ratio $\frac{2A(^{(e)}B}{^{\pm}(^{(e)})}$. Since $^{(e)}W$, the level of rent extraction that maximizes the present discounted value of wages of current union members, maximizes $A(^{(e)})$, and since $^{\pm}$ monotonically increases in $^{(e)}$, $\frac{2A(^{(e)}B}{^{\pm}(^{(e)})}$ is decreasing in $^{(e)}$ at $^{(e)}W$ and at all greater values of $^{(e)}$. Since $^{(e)}S$ maximizes $\frac{2A(^{(e)}B}{^{\pm}(^{(e)})}$, it must be less than $^{(e)}W$.

Figure 2 presents the proof graphically, showing $A(\ensuremath{^{(!)}})$, $\pm(\ensuremath{^{(!)}})$, and $\frac{2A(\ensuremath{^{(!)}})B}{\pm(\ensuremath{^{(!)}})}$ as functions of $\ensuremath{^{(!)}}$. \pm increases monotonically with $\ensuremath{^{(!)}}$, and $A(\ensuremath{^{(!)}})$ increases with $\ensuremath{^{(!)}}$ up to $\ensuremath{^{(!)}}_W$, the level of output that maximizes the welfare of current workers, and then declines. This implies that $\ensuremath{^{(!)}}_S$, the evolutionarily stable level of rent extraction, is less than $\ensuremath{^{(!)}}_W$. If one starts at the level of rent extraction that is optimal for members, a small reduction in $\ensuremath{^{(!)}}$ causes a second-order reduction in attractiveness of the union to potential members, and thus a second-order reduction in the spread rate of the union. However, it causes a ...rst-order decrease in the exit rate of unionized ...rms. Therefore, the evolutionarily stable level of [®] must be less than the welfare-maximizing level of [®]. This result holds as long as the spread rate of unions is continuous in the present discounted value of wages extracted.

Note that the relative shapes of the A ($^{(0)}$) and \pm ($^{(0)}$) functions determines how far $^{(0)}$ s will be from $^{(0)}$ W. If \pm ($^{(0)}$) is steep, so that ...rm survival is sensitive to rent extraction, then $^{(0)}$ s will be far below $^{(0)}$ W, whereas if \pm ($^{(0)}$) is fairly \pm at, then $^{(0)}$ s will be close to $^{(0)}$ W. Similarly, if A ($^{(0)}$) declines gradually as one moves away from $^{(0)}$ W, then $^{(0)}$ s is likely to be considerably less than $^{(0)}$. On the other hand, if A ($^{(0)}$) declines steeply as one moves away from the welfare maximizing level of output, then $^{(0)}$ s will be very close to $^{(0)}$ W. In particular, if there were Bertrand competition among unions for potential members at unorganized ...rms, in which workers joined whichever union delivered greater discounted rents, then the slope of A ($^{(0)}$) would be in...nite at $^{(0)}$ W and the evolutionarily stable level of rent extraction would equal the optimal amount of rent extraction for current workers. However, if workers decide which union to join based not only on the present discounted value of rent extraction but also on other idiosyncratic factors, such as the match between the personality of union organizers and the workers at the ...rm, then workers may join a union other than the one that maximizes the present discounted value of rents. Union recruitment will therefore increase continuously rather than discretely in the present discounted value of rents delivered to members.

As discussed above, we assume that the attractiveness function A (®) is continuously increasing in ®. The assumption that A is continuous is important for the result that the evolutionarily stable level of rent extraction is less than the welfare-maximizing level of rent extraction. If there were simple Bertrand competition among unions for potential members at unorganized ...rms, in which workers joined whichever union delivered greater discounted rents, then the evolutionarily stable level of rent extraction would equal the optimal amount of rent extraction for current workers. However, if workers decide which union to join based not only on the present discounted value of rent extraction but also on other idiosyncratic factors, such as the match between the personality of union organizers and the workers at the ...rm, then workers may join a union other than the one that maximizes the present discounted value of rents. Union recruitment will therefore increase continuously rather than discretely in the present discounted value of rents delivered to members.

The steady-state number of unionized ...rms in society is higher if unions extract $@_S$ than if they extract $@_W$. Furthermore, the level of rent extraction that maximizes the number of unionized ...rms will be less than or equal to the evolutionarily stable level $@_S$, and therefore, by Proposition 5, less than $@_W$. The intuition for this result is that, under any union extracting more rent than the $@_S$ union, a smaller percentage of newly created ...rms are unionized (since $@_S$ maximizes p^x) and the death rate of those ...rms is higher (since \pm (@) increases monotonically with @). The following proposition shows these results formally.

Proposition 6 For any level of rent extraction [®] greater than the evolutionarily stable level of rent extraction [®]_S, the steady-state level of unionization, U^{α} ([®]), will be lower than the steady-state level of unionization under the evolutionarily stable union, U^{α} ([®]_S). This implies that the level of [®] that maximizes the steady-state level of unionization will be less than or equal to the level that maximizes [®]_S.¹⁶

Proof. See Appendix A.1.

Corollary 6.1 The steady-state level of unionization under the evolutionarily stable level of rent extraction, $U^{\alpha}(\mathbb{B}_{S})$, will be greater than that under the welfare-maximizing level of rent-extraction, $U^{\alpha}(\mathbb{B}_{W})$.

Proof. This follows directly from Proposition 6 and from the fact that $\mathbb{B}_S < \mathbb{B}_W$, which was shown in Proposition 5.

It is worth noting, however, that it is ambiguous whether the total \ddagger ow of rent extracted by the union in steady-state, U^{*} , would be higher or lower with the evolutionarily stable union than with the welfare-maximizing union.¹⁷ The reason is that decreasing @ from $@_W$ to $@_S$ increases the number of unionized ...rms, but decreases the amount extracted from each ...rm. It is theoretically ambiguous which of these two exects dominates.

¹⁶Note that technically, if the function $\frac{2A(\textcircled{B})B}{\pm(\textcircled{B})}$ has multiple global maxima, so that the evolutionarily stable level f[®]sg is not unique, then this result holds for the highest [®]s belonging to that set.

¹⁷See Kremer and Olken [2001] for an example demonstrating this point.

In this paper we take B, the amount unions spend per unionized ...rm on organizing, as exogenous, but unions may also di¤er in the amount they spend on organizing e¤orts. The traditional maximizing approach assumes that increased union density increases the union's bargaining power, and asks what level of B would be optimal for members (see Wallerstein [1989]). However, there are certain phenomena that this approach has di¢culty explaining. In particular, many unions devote substantial resources to organizing outside their core industries. For example, the Steelworkers organize employees at Chock Full O'Nuts, the Teamsters represent casino workers in Las Vegas, and as discussed above, the UAW organizes graduate students at NYU. While it is possible to see how a steel worker or auto worker might bene...t from organizing other workers in their industry, it is harder to see why they would prefer to spend their union dues organizing outside their core industries.

By contrast, our approach takes a worker's preferences over the determination of B as given, and ask what level of B is evolutionarily stable. As in the determination of rent extraction, we argue that there may be a selective advantage to unions that encourage leaders to spend more on organizing exorts than would be optimal for members. As a result, unions controlled by leaders may not only have lower ± but also higher B than would be preferred by members. Kremer and Olken [2001] presents a simple extension to the model which shows that, if worker preferences over A and B are separable, then the evolutionarily stable union has both a lower level of ® and a higher level of B than the welfare-maximizing union.

4 Implications for Union Institutions

Evolutionary pressure selects for a certain type of attribute-in this case, for unions that moderate workers' wage demands. However, both in biology and in economics, there must be a mechanism by which that attribute is expressed. In this section, we discuss one possible mechanism-incumbency advantages for leaders-by which a union's institutions might serve to reduce the level of rents received by workers. We show under reasonable assumptions that the greater incumbency advantages for union leaders, the lower the present discounted value of rents received by workers. We then show

that the evolutionarily stable union provides incumbency advantages for union leaders, whereas the union that maximizes the welfare of its workers does not.

We consider a stylized model of union decision making. The key feature of this model is that increases in incumbency advantages lead to both a lower total level of rent extracted from ...rms and a lower amount of rent received by workers. This occurs because union leaders o = r to extract less rent in total from ...rms in return for channeling some of that rent to leaders in the form of private bene...ts, and the greater incumbency advantages for unions, the more they can extract in terms of private bene...ts without being voted out of o cce. This will be true so long as ...rms have at least some bargaining power in the negotiations with union leaders over private bene...ts. The model we present is one stylized form of such a bargaining game; there many be many other similar ways of modelling the bargaining situation that would produce similar results.

In all negotiations, union leaders represent the rank-and-...le in negotiations with ...rms. Union leaders and ...rms bargain over a level of rent extraction, @, which represents the proportion of the ...rms' pro...ts ¼ which are extracted by the union for the rank and ...le, and over -, the proportion of the ...rms' pro...ts paid directly by the ...rm as private bene...ts to union leaders. These private bene...ts - can be literal monetary o¤ers or, as frequently happens, contract provisions that bene...t union leaders, such as preferential seniority for union o¢ cials or a role in grievance procedures. While workers may obtain some bene...t from these provisions, we consider any bene...t obtained by workers to be part of @, so that - captures the bene...t received only by the union leaders.

Workers receive bene...ts only from the ...rst part of the contract-the level of rent extraction ®: As before, workers seek a level of ® that maximizes the present discounted value of rents accruing to current union members, i.e.

$$\frac{^{\ensuremath{\mathbb{R}}\ensuremath{\mathbb{M}}\ensuremath{\mathbb{M}}\ensuremath{\mathbb{R}}\ensuremath{\mathbb{R}}\ensuremath{\mathbb{R}}\ensuremath{\mathbb{R}}\ensuremath{\mathbb{R}}\ensuremath{\mathbb{R}}\ensuremath{\mathbb{M}}\ensuremath{\mathbb{R}}$$

This expression is identical to equation (10), except that the death rate now depends on the total amount extracted from the ...rm, $^{(B)} + ^{-}$, rather than just the amount extracted for workers, $^{(B)}$.

The approval of contracts and selection of union leaders works as follows. Each union without a leader begins by electing one. As will be discussed below, all potential candidates look ex-ante

identical, so electing a candidate can be thought of as drawing one at random from the population of potential union leaders. The elected leader negotiates a contract with the ...rm, and presents it for rati...cation by the workers.

Presented with a contract, the workers have three choices–approve the contract, reject the contract but retain the current union leader, or reject the contract and elect a new union leader. If the workers reject the contract but retain the union leader, the union leader renegotiates the contract, the contract is put up for another vote, and the process repeats. Each worker incurs a cost s (for strike) due to the renegotiation.

If the workers choose to reject the contract and elect a new union leader, a new union leader is elected, a new contract is negotiated, and each worker incur a cost v (for voting). The cost v represents the advantages possessed by incumbents in union elections–a union with no incumbency advantages would have v = 0, and increases in v represent increases in the power of incumbents. We assume that a given union's level of v is determined by its constitutional provisions. Unions vary in the degree of incumbency advantages–i.e. the level of v created by their constitutional provisions. As long as a leader is not voted out of o¢ce, he can anoint a successor who will continue his contract policy.¹⁸

There are two types of union leaders-idealists and opportunists. Idealist union leaders care only about the interests of the rank-and-...le, and therefore in negotiating contracts will demand the welfare-maximizing level of rent extraction and set private bene...ts equal to 0, i.e. $(^{(m_W)}; ^{-}_W) = (^{(m_W)}; ^{(0)})$. By contrast, opportunists seek to maximize only their private gains while in o¢ce, i.e. $^{-}$. Therefore, in negotiating contracts with ...rms, opportunistic union leaders they will trade o^m as much rent-extraction as possible in return for private transfers from ...rms. In the population of potential union leaders, a fraction i are idealistic. However, idealism is not directly observable, so all potential union candidates claim to be idealistic. The union leader's true colors are revealed only when when he is elected and proposes a contract.

¹⁸An opportunist has incentives to pass anoint another opportunist, who (as an opportunist) would o¤er bribes to the incumbent in return for the job. An idealist, by contrast, might not be able to discern idealists from opportunists. Therefore, while there is chance that unions headed by idealist leaders might revert back to being headed by opportunists, it is less likely for a union headed by an opportunistic leader to revert back to being idealistic. Assuming this pattern of transitions only increases the evolutionary convergence to unions with opportunistic leaders.

We model the negotiations between unions and ...rms as follows. In the ...rst stage, union leaders and ...rms Nash bargain over (@; $^-$), where the relative bargaining power is such that the union leader obtains x percent of the surplus. If these initial private negotiations fail, the negotiations enter the "strike" phase. Once the strike has begun, the union can make take it or leave it o ¤ers to the ...rm in terms of @, as once in the public eye it has an incentive to maintain a reputation for toughness, since it will bargain publicly with many other ...rms. On the other hand, because of the public scrutiny caused by the strike, it becomes impossible for the ...rm to o ¤er side payments to the union o¢cials, so any contracts emerging from the strike phase must have $^- = 0$.

To ...nd the Sub-Game Perfect Nash equilibrium of this game, we solve backwards for the case of an opportunistic union leader. (For the case of an idealistic union leader, it is clear that the union will extract the welfare maximizing rent $^{(0)}_{W}$ and set private payments to union leaders $^{-}_{W} = 0$). First, note that the rank and ...le will never choose the second option, i.e. rejecting the contract while retaining the current union leadership. To see this, note that if workers reject a contract ($^{(0)}$) but retain the union leadership, they expect to receive

$$\frac{{}^{\mathbb{R}^{E}}{}^{\mathbb{M}}_{4}}{r + \pm ({}^{\mathbb{R}^{E}}{}^{+}{}^{-E})} i s;$$
(13)

where ${}^{i} {}_{\textcircled{B}} {}^{E}; {}^{-E} {}^{\textcircled{C}}$ represents the contract the rank-and-...le expect to receive in the next period. The rank-and-...le expect that, since future subgames are identical to this game, the union leader will propose the same level of rent extraction ${}^{\textcircled{B}}$ and private payments ${}^{-}$, i.e. ${}^{i} {}^{\textcircled{B}} {}^{E}; {}^{-} {}^{E} {}^{\textcircled{C}} = ({}^{\textcircled{B}}; {}^{-}).^{19}$ Therefore the expected amount received by rejecting the contract but keeping the union leader, expression (13), is strictly less than the amount received by accepting the contract, $\frac{{}^{\textcircled{B}} {}^{E}_{M}}{r_{+\pm} ({}^{\textcircled{B}} {}^{+} {}^{-} {}^{E})}$, so the workers will never choose to reject the contract while retaining the union leadership.²⁰

The other option open to workers besides accepting the contract is to reject the contract and ¹⁹In practice, this seems to be precisely what happens-when contracts are rejected by the rank-and-...le, the union leadership often simply repackages the contract in new language rather than fundamentally altering the contract o¤er.

²⁰We thank Keith Chen for this argument.

change the leadership. Workers will chose to do this if and only if

$$\frac{{}^{\mathbb{R}}{}^{1}}{r + \pm ({}^{\mathbb{R}} + {}^{-})} < (1_{i} i) \frac{{}^{\mathbb{R}}{}^{E}{}^{1}_{4}}{r + \pm ({}^{\mathbb{R}}{}^{E} + {}^{-}{}^{E})} + i \frac{{}^{\mathbb{R}}{}_{W}{}^{1}_{4}}{r + \pm ({}^{\mathbb{R}}{}_{W})} i V;$$
(14)

where ${}^{i} {}_{\textcircled{B}}{E}$; ${}^{-E}{}^{\textcircled{C}}$ represents the contract the rank-and-...le expect to receive if an opportunist is elected in the subsequent period. Once again, rank-and-...le expect that, since future subgames are identical to this game, if an opportunist is elected again he will propose the same level of rent extraction ${}^{\textcircled{B}}$ and private payments ${}^{-}$, i.e. ${}^{i}{}_{\textcircled{B}}{E}$; ${}^{-E}{}^{\textcircled{C}} = ({}^{\textcircled{B}}{;}^{-})$: Since the union leader earns 0 if he is voted out of oCce, he will chose a contract such that workers are just indi¤erent between voting him out of oCce and retaining him, i.e.

$$\frac{^{\otimes}{}_{M}}{r + \pm (^{\otimes} + ^{-})} = \frac{^{\otimes}_{W} ^{1}_{M}}{r + \pm (^{\otimes}_{W})} i \frac{^{\vee}}{i}:$$
(15)

Note also that in equilibrium, opportunists are never voted out of o¢ce.

The intuition for the amount obtained by rank-and-...le in equilibrium is straightforward. Opportunists can reduce the present discounted value of rents by the expected discounted cost of continuing to reject opportunists until an idealist is found and the level of rent $@_W$ is extracted.

Note that while equation (15) determines the present discounted value of rents obtained by the workers, it does not uniquely determine $\[mathbb{B}\]$ and $\[-1\]$. To determine $\[mathbb{B}\]$ and $\[-1\]$, note that Nash bargaining in the ...rst stage implies that the union leaders obtain x percent of the total surplus over not reaching an agreement and having a level of rent extraction $\[mathbb{B}\]$. This implies that

$$x \frac{1}{r + \pm (^{\circledast} + ^{-})} i \frac{1}{r + \pm (^{\circledast}_{W})} = \frac{-}{r + \pm (^{\circledast} + ^{-})}$$
(16)

Together, equations (15) and (16) uniquely determine a level of $^{\mbox{\tiny B}}$ and $^{-}$ extracted by a union with a given level of v and an opportunistic union leader.

Given this relationship between incumbency advantages and rent extraction, we can use the analysis of Section 3 to determine the level of incumbency advantages in the evolutionary equilibrium. To do this, we de...ne the functions $\pm (v) = \pm (^{(B)}(v) + ^{-}(v))$, and A (v) = A ($^{(B)}(v)$), and then

repeat the same analysis above. In particular, we know from Proposition 3 that the evolutionarily stable union will be the union maximizing $\frac{2A(v)B}{\pm(v)}$. The following Proposition shows that such a union will have a constitution that provides incumbency advantages for leaders.

Proposition 7 The evolutionarily stable union will have incumbency advantages for union leaders, i.e. v > 0, whereas the union that maximizes the present-discounted value of rents accruing to workers would have no incumbency advantages, i.e. v = 0.

Proof. See Appendix A.1

It is also worth noting that the level of incumbency advantages present in the evolutionarily stable union depends on the percentage of the surplus from negotiations extracted by union leaders, x. Increases in x, the percentage of the surplus from negotiations extracted by union leaders as opposed to ...rms, decrease the evolutionarily stable level of incumbency advantages, v. The reason is that as x increases, a given increase in v reduces the attractiveness of the union by the same amount as before (since, as shown by equation (15), the presented discounted value of rents from workers does not depend on x). On the other hand, a given increase in v results in a smaller evolutionary gain for the union in terms of reduced death rates of ...rms, because the total amount of rent extracted by the union decreases by less than before. Put another way, increasing x leaves the A (v) curve untouched while making the \pm (v) curve ‡atter. As demonstrated by Figure 2, a ‡atter \pm (v) curve will tend to make the evolutionarily stable level of v closer to the welfare-maximizing level.

The premise of the analysis in this section is that union leaders will take advantages of incumbency advantages to moderate wage demands. In fact, Ross [1950] argues that this is precisely what often occurs–unions are often prepared to sacri...ce worker-oriented provisions, such as wages, for union-oriented provisions, such as union security, automatic checko^m of union dues, the right of the union to participate in all grievance negotiations, and preferential seniority for union o¢cials.

Though we focus on incumbency advantages and the possibility of idealistic union leaders as the mechanism moderating wage demands, there are other possible mechanisms as well. First, just as ...rm managers are often assumed to be empire builders, with a preference for increasing ...rm size, union leaders may prefer to be in charge of larger unions, as leaders of larger unions have more prestige and political power. As was shown in Proposition 6, increasing the steady-state size of the union requires extracting less than the welfare-maximizing level of rent. Therefore, union leaders that care about the size of their union beyond the impact on members will extract less rent than would be preferred by their members. Also, workers may be heterogeneous in their desired level of wage demands, and union institutions may evolve to favor the subset of workers with less aggressive wage demands. Alternatively, union institutions may require a supermajority to call an strike, shifting the critical union member from the median to someone desiring more moderate wage policies.

Of course, in an evolutionary model, there need be no presumption that all union constitutions that create incumbency advantages also create incentives for moderation. If some union constitutions create incumbency advantages but have provisions that encourage leaders to be extract more rent than members would prefer, these unions will die out. Meanwhile, if other union constitutions create incumbency advantages and also encourage leaders to moderate members' wage demands, these unions will grow.

5 Evidence From the History of Unions

The implication of the previous section is that unions should exhibit substantial incumbency advantages. Moreover, exogenous reductions in those incumbency advantages should be associated with increases in union wage demands. This section presents evidence from the history of unions that seems to support these conclusions.

5.1 Presence of Incumbency Advantages

Overall, incumbents have a substantial advantage over their potential challengers in union elections. Table 1 shows the turnover of union presidents for the ten largest U.S. unions since each union's founding. We focus on the chance an incumbent was defeated each year as a measure of incumbency advantages, since this captures both the advantages incumbents have through infrequent elections

						Chance
			Total	Average	Number of	Incumbent
		Year	Number of	Tenure of	Defeated	Defeated
Union		Founded	Presidents	Presidents	Incumbents	Per Year
		100				
1. National	Education Association (NEA)	1934	. 12	5.5	3	4.5%
2. Teamsters (IBT)		1903	6	16	2*	2.1%
3. Food & 0	Commercial Workers (UFCW)	1912	14	6	0	0.0%
4. State, County & Municipal Employees (AFSCME)		1932	3	22	0	0.0%
5. Teachers (AFT)		1916	15	6.5	2	2.4%
6. Auto Workers (UAW)		1947	8	6.5	1	1.9%
7. Electrical Workers (IBEW)		1890	16	7	2	1.8%
8. Communication Workers (CWA)		1938	3	21	1	1.6%
9. Machinists (IAM)		1888	13	9	N/A	N/A
10. Steelworkers (USW)		1894	6	18	0	0.0%
Average:	All Unions		9.6	11.8	1.2	1.5%
	Private Sector Unions**		8.6	13.2	0.9	1.2%
	Public Sector Unions**		10.0	11.3	1.7	2.3%
Comparison	n:					
Presidents of	of the United States (1900-2000)		18	5.6	5***	5.0%
G 11						

Table 1:	Turnover	of union	presidents	for 10	largest	American	unions
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Source: National union offices.

* Both of the defeated Teamsters presidents were defeated after the Federal

government takeover of the union and the imposition of direct elections for the union president.

** The NEA, AFT, and AFSCME are classified as public sector unions; the

remainder are classified as private sector unions.

*** General election defeats.

and the electoral advantages gained once an election is held. Over the history of the nine unions for which data is available, an incumbent union president had only a 1.5% chance of being defeated in an election each year. This ...gure would be even lower-only 1.2%-if one does not include the period under which the Federal government took over the Teamsters union and imposed changes in election procedures that decreased incumbency advantages and led to the defeat of 2 incumbents. To put these numbers in perspective, during roughly the same period, an incumbent President of the United States had a 5% annualized chance of being defeated in a general election.

This data seems generally consistent with the model. In general, the relatively low chance of an incumbent being defeated is consistent with the high levels of incumbency advantages necessary to sustain more moderate wage policies. Furthermore, note that the two unions with the greatest chance of an incumbent being defeated each year were the National Education Association and the American Federation of Teachers, both public sector unions. More broadly, incumbents in public sector unions had a 2.3% chance of defeat, while those in the private sector had a 1.2% chance of defeat (0.8% excluding the two Teamster defeats.) This is consistent with the model's predictions. To see this, note that there is a very small chance that a public employer will be forced out of business. The function \pm (®) is therefore much \pm atter for the public sector than for private sector ...rms.²¹ As discussed in Sections 3 and 4, as a result, ®_S will be very close to ®_W, and incumbency advantages v will be close to 0. Therefore, competition will select for unions with weak incumbency advantages. The fact that the chance of a union president being defeated in public sector unions is almost twice that of private sector unions is consistent with this prediction, though there are other possible explanations as well.

5.2 Sources of Incumbency Advantages

One reason why incumbents are so often reelected is that most existing unions have constitutional features creating substantial incumbency advantages for leaders. This section presents several examples of the sources of incumbency advantages typically found in U.S. labor unions.

First, most unions have indirect leadership elections, in which the president of the union is elected by delegates to a national convention, rather than by the membership at large. At these conventions, the delegates, often local union leaders, face strong pressure to support incumbents in national oCce if they think that the incumbents will win, because local union leaders need several types of services from national unions. For example, the union leadership often controls access to national strike funds and has the power to put local branches in trusteeship. [Geoghegan, 1992; Benson, 1986]. Furthermore, since incumbency advantages are much weaker in some union locals than at the national level, local leaders face the threat of not being re-elected and having to return to the shop ‡oor. Local leaders' insurance against this threat is the possibility of obtaining a job with the national union sta¤, which will be much more likely to occur if they have reliably supported

²¹The function \pm (®) is probably not completely \ddagger at, as militant actions on the part of unions can provoke a government to de-unionize. One classic example of this is President Reagan's confrontation with the air tra¢c controllers. Such situations are, however, relatively rare.

the national leadership. All of these factors encourage the delegates to the national conventions to support the incumbents.

Union incumbents have other direct advantages over challengers as well. Union sta¤ are often not restricted from donating money to support campaigns of current leadership, and laws restricting union sta¤ from campaigning on union time are extremely weak. To take another example, union o¢cers are not often required to give membership lists or even lists of local chapters to opposition candidates. Since unions often represent diverse sets of workers (for example, the United Auto Workers represents graduate students at NYU), this makes it di¢cult for challengers to campaign against incumbent leaders. On the other hand, incumbents can use o¢cial union communications, such as union newsletters, to promote their own candidacies.

Even if there is a viable challenger, local union o¢cers, rather than neutral third parties, are typically in charge of vote counting in union elections [Geoghegan, 1992], so there are few safeguards against fraud. In fact, there is anecdotal evidence of a signi...cant amount of outright vote-stealing in union elections. Moreover, prior to mandated periodic elections under federal law, unions could go for decades without even holding elections. For example, the Laborers' union had no conventions between 1920 and 1941 [Benson, 1986].

5.3 Comparative Statistics of Wage Demands and Incumbency Advantages

In addition to predicting the existence of incumbency advantages for union leaders, the model also predicts that union leaders should use their incumbency advantages to moderate wages. Increases in incumbency advantages should be associated with declines in wage demands, and vice-versa.

Perhaps the most important evidence that union leaders typically favor more moderate policies than would be preferred by members comes from the asymmetry of challenges to established leaders. Union dissidents typically accuse union leaders of being too moderate in their negotiations with the ...rms, not of threatening members' jobs by extracting too much from ...rms. If union leaders sought to represent the typical worker, one would expect challenges to come as often from either direction.

There is also evidence that weaker incumbency advantages are associated with more aggressive

policy. For example, Lipset, Trow, and Coleman [1950] single out the International Typographer's Union as the only major U.S. union to have a functioning two-party system, the result of a split by Progressives during the 1911 union convention. Power in the union subsequently alternated between the Progressive and more the conservative Wahneta party throughout the ...rst half of the century. Consistent with the model, Lipset, Trow, and Coleman note that the union was distinguished by its militance and willingness to strike. For example, during WWII, ITU was one of the few unions that repudiated the no-strike pledge, since it felt that the War Labor Board's policies were drastically hurting the real wages of ITU members. When the Taft-Hartley act was passed in 1947, the union still insisted on the closed shop practice, even though it was made illegal by the law. It is also worth noting that the ITU has substantially declined in membership. While part of this decline was due to technological change in the typesetting industry, unions in other industries have managed to adapt and survive despite similar technological shifts.

While incumbency advantages are strong at the national or international level, union locals vary in the degree of control of incumbency advantages, and in some union locals, there is regular turnover of leadership. We would therefore expect that the weaker the incumbency advantages in the local, the more militant that local will be. Kleiner and Pilarski [2001] ...nd exactly such an exect in a comparison of two similarly-sized locals of the UAW with plausibly exogenous dixerences in incumbency advantages. One local was organized with indirect elections because it was comprised of many plants spread out over the Los Angeles areas, making frequent large meetings di¢cult. The second local, by contrast, was organized with direct elections of union o¢cials because it was comprised primarily of a single large plant which made direct elections more feasible. Kleiner and Pilarski found that the geographically concentrated local with direct elections had a much more vigorous union democracy and much more aggressive wage demands.

To the extent that locals have weaker incumbency advantages than national unions, we should also expect that local unions should advocate stronger wage demands than national unions. In fact, this is generally the case, and there are a number of examples of local unions conducting strikes against the wishes of the national union. For example, the P9 Hormel strike of the mid-1980s strike was conducted by the local union without the support of the national union, as was the 1994-1995

Caterpillar strike.²²

The model also suggests that if incumbency advantages decline exogenously, wages will rise and ...rms will be more likely to fail. It is instructive to examine a case study of two unions that for plausibly exogenous reasons were subject to shocks that reduced incumbency advantages. In the late 1930's, John L. Lewis, the president of the United Mine Workers (UMW) and founder of the CIO, feuded with Roosevelt, going so far as to endorse Wendell Willkie, Roosevelt's Republican opponent. As part of an e^xort to enhance his national political stature, Lewis, who faced no serious opposition within the UMW, instituted direct leadership elections. The Steelworkers, which were created by the UMW, adopted a similar constitutional provision.

By the 1970's, leadership of the UMW had passed to the corrupt Tony Boyle. Just after the 1969 leadership election, Boyle arranged for the murder of his opponent, "Jock" Yablonski, and of Yablonski's family. This over-reaching led to intense federal scrutiny of the 1972 UMW election and the victory of the challenger, Arnold Miller. Miller's victory was followed by much increased militancy on the part of the union, the decline of the Eastern coal industry, and a dramatic decline in union membership.

Following the election defeat of the incumbent UMW leadership, in 1977 a major challenge was also launched to the Steelworkers' leadership, which was similarly vulnerable due to its constitutional provision for direct leadership elections. Before the election, the heir apparent, Lloyd McBride, had promised to make a number of concessions to management in the hopes of saving jobs in the ailing steel industry. Ed Sadlowski, McBride's opponent, challenged McBride as being too close to management, and was explicit about his willingness to sacri...ce union membership for higher wages. Sadlowski said that he did not mind if the Steelworkers' membership dropped from 400,000 to 100,000 or even 60,000, and that it should be a goal of labor to have the steel industry pay high wages that would allow its workers to ...nance education so that they or their children could obtain better jobs. It is hard to imagine typical incumbent union leadership adopting policies that would cut membership to a quarter of its initial level. Though Sadlowski lost the election, as a

²²It is not clear what other models would predict about the relative militancy of the national union and locals. On the one hand, the national has to provide resources to support the local union in strikes, for example through the strike fund. On the other hand, a national union might wish to demonstrate its willingness to strike against other employers by striking against one employer.

result of his challenge McBride was forced to drop his concessions to management and adopt much more aggressive wage demands. With several years, the steel industry had begun a precipitous decline, shedding 56 percent of its workforce in the period from 1979 to 1986, a decline from which it has yet to recover [Tornell, 1997]. Of course, the decline of the Eastern coal industry and the U.S. steel industry was probably the result of a number of other factors as well, but the model is at least consistent with the data.

5.4 Individual vs. Group-Level Competition

Though the model presented here focuses on competition of unions across a group of ...rms, biological models also consider the exects of competition within a single individual. A natural extension of the model would therefore be to consider what would happen if unions continued to compete with one another within a ...rm, rather than having all within-...rm competition end once a union is elected. The prediction of such a model would be that the higher the level of competition within ...rms, the higher the level of rent-extraction. This may be a partial explanation for why unions in the U.S., where labor laws greatly favor incumbent unions, seem to be more moderate than many of their European counterparts, where the threat of entry by competing unions may prevent incumbent leaders from departing too far from the workers' preferred policies. (Of course, this does not apply to the same extent in countries with encompassing unions on the Scandinavian model, where unions may have other incentives to moderate wages.)

Relative to labor law in most of Europe, U.S. labor law enhances incumbency advantages for existing unions. In the US, once a particular union has won a union certi...cation election, it is o¢cially recognized as the sole collective bargaining partner representing the covered workers, and it can only be replaced if the majority of workers vote to decertify it and then certify another union. Decerti...cation, however, is relatively rare. In some European countries, such as France, Italy, and the Netherlands, several di¤erent unions may compete for workers within the same ...rm on an ongoing basis. The threat of entry makes it more di¢cult for incumbents to depart from members' preferred policies.²³ Reducing rent extraction from the level that maximizes the present

²³Ongoing within-...rm competition for members among unions will produce higher long-run rent extraction than

discounted value of rents for current union members may increase the lifespan of ...rms, but it will lead to the loss of workers within the ...rm to rival unions.

As a result, individual-level selection is likely to be a much more potent force in European countries with multiple unions inside a single ...rm than in a U.S.-style system in which a single union is certi...ed to collectively bargain on behalf of a de...ned set of workers. Even in countries such as Britain, where a single union typically represents a given set of workers, the weakness of barriers to entry for competing unions relative to the U.S. means that the implicit threat of competition is likely to constrain unions to represent their members relatively well.

Evolutionary and standard maximizing models di¤er most sharply in their predictions of relative militancy of unions under the U.S. system of multiple craft unions representing di¤erent types of workers within the ...rm and European systems in which di¤erent unions can potentially compete for the same potential members. In the U.S. craft union system, for example, airline pilots, machinists, and ‡ight attendants are all represented by separate unions, and hence under standard maximizing models, if there are many unions each union has no incentive to internalize the e¤ect of its own rent extraction on the ...rm's investment. Standard maximizing models therefore imply that rent extraction should therefore be greater in this craft union environment than under a European environment in which multiple unions compete within a single ...rm but wage concessions to one union apply to all employees. In an evolutionary model, however, the ongoing competition for members among unions in the European system could lead to more rent extraction than under a system of U.S.-style craft unions. The model is consistent with the widespread view that European unions are more militant than their U.S. counterparts.²⁴

A similar comparison can also be made within the U.S. Prior to the merger of the AFL and

restricting competition to the initial choice of union. This is because if unions only compete at some initial stage, unions that initially extract the level of rents which maximizes the present discounted welfare of members, and then gradually lower rent extraction, will be able to attract members with a policy which approaches the evolutionarily stable policy in the long run. Note that this policy does not require a commitment technology for unions, because it does not involve promises to undertake time-inconsistent policies. Extra bene...ts to workers joining a union are provided in the short run, not the long run. For example, unions could make an up-front payment in the form of support for organizers and support for an initial strike if necessary. In contrast, unions must maintain a high level of rent extraction in the long run to retain members in the face of ongoing competition.

²⁴More systematic evidence on relative rent extraction is hard to come by. Wage premia for union members as conventionally measured are higher in the U.S. However, the lower union coverage in the U.S. means that wage premia may not be a good measure of rent extraction. In the U.S., unions may only be present in industries and ...rms with large amounts of rents to extract, whereas in Europe, unions are widespread.

the CIO, unions a Cliated with each of the two umbrella organizations often continually competed to organize a given set of workers. This higher level of competition seems to have coincided with more militant behavior on the part of unions, as the model would predict.

The analysis of how rent extraction di¤ers depending on whether or not unions compete within ...rms is analogous to the analysis of the evolution of virulence in biology. The strength of selective pressures for organisms to become more benign or even symbiotic depends on the mode of transmission of the organism [Ewald, 1994]. For example, if several di¤erent HIV strains are competing within the human body, one that reproduces more rapidly within the human body may be more likely to kill its host, but will also be more likely to be transmitted to another host. Thus individual-level selection within the host favors rapid reproduction while group-level selection favors more benign forms of the disease that are less likely to kill the host. In contrast, mitochondria reproduce only through cell division, so selection among mitochondria favors those that help their cells survive. Similarly, the system of incumbency advantages built into U.S. labor law produces an advantage for unions that help their ...rms survive. The greater ongoing competition for members among several di¤erent unions, the more this e¤ect is counterbalanced by the need to extract more rent to attract members.

6 Conclusion

This paper has applied techniques from biology to model unions. A key implication of the model is that the unions we observe today are likely to extract less rent than would be optimal for current members, because unions that do so will have a selective advantage over unions that better represent their members' interests. For union leaders to moderate workers' wage demands, however, they must be insulated from workers by incumbency advantages. In fact, these incumbency advantages are widespread among today's unions.

In the conclusion, we discuss the relationship between our model and other theories of incumbency advantages in unions, the normative implications of the analysis, and the applicability of the evolutionary analysis here to other institutions, such as ...rms.

6.1 Relationship to Other Theories of Incumbency Advantages

The model outlined in this paper is complementary with other, more traditional explanations of incumbency advantages in unions. Sociological explanations, such as Michel's [1949 (1915)] "Iron Law of Oligarchy," suggest that leaders will inevitably seize control of their organizations and work to preserve the organization itself rather than to advance the original goals of the organization. In contrast, the argument here is not that all union leaders will wrest control away from their members due to internal sociological factors and then work to maximize the membership of the union, but rather that those unions that create structures in which this occurs will grow at the expense of unions that narrowly serve their current members' interests. If Michel's process occurs even in a few unions, we will empirically observe these unions much more frequently than unions that are more responsive to their membership.

Another way to explain the typically more moderate position of union leadership is through models in which union leaders are agents whose interests di¤er from those of their principals, the rank and …le. An example of such an agency model was presented in Section 4, and as we points out, these considerations may well be the proximate cause of moderation of wage demands by union leaders. However, standard agency theory implies that principals should design optimal mechanisms for agents. It thus begs the question of why so many unions have constitutional institutions that exacerbate agency problems in controlling leaders, such as indirect elections, secret lists of locals and members, and no prohibitions on campaign donations from union sta¤. In contrast, this biological model suggests that unions with constitutional procedures that exacerbate agency problems will outcompete others that do not.

6.2 Normative Implications

The normative implications of the analysis are ambiguous. As shown above, the evolutionarily stable level of rent extraction will lead to more unionization in the steady-state than the welfare-maximizing level of rent extraction, but which union will extract more rent overall is ambiguous.

The dimerence in startup-cost expenditure is also ambiguous. On the one hand, since the steadystate chance of a new ...rm being unionized, p^{μ} , is maximized by the evolutionarily stable union,

the chance of a new ...rm being unionized is higher, reducing the expenditure on start-up costs. Furthermore, the death rate of ...rms will be lower, so startup costs will be paid less frequently. However, the cost of being unionized, ®¼, is lower, increasing the ex ante value of the ...rm and thus increasing start-up costs, so the overall e¤ect could go in either direction. In any case, the welfare implications of these changes depend on the interpretation of investment and start-up costs. Investment and start-up costs may be productive, such as investment in research and development of improved products, or unproductive, such as advertising designed to establish market leadership for a dot.com seeking ...rst-mover advantage.

Regardless of these general equilibrium exects, however, the model implies that unions are not extracting the optimal level of rent for their workers. Changing union constitutions to reduce incumbency advantages will likely lead to increased welfare for the union's current members, though it will also reduce long-term unionization.

6.3 Applicability to Other Organizations

Similar evolutionary arguments could be made about organizations other than unions. For example, those religions that grow may be those that are most successful at retaining members, rather than those that maximize members' welfare. Universities whose boards accumulate large endowments may be more likely to survive than universities that pay out from the endowment less conservatively, whether or not this contributes to the universities' educational and research mission. As Dutta and Radner (1999) suggest, ...rms that maximize their stockholders' interests by paying out dividends may eventually be outnumbered by ...rms that retain earnings as a safety net, because paying out dividends makes ...rms more vulnerable to negative shocks.

Reality is likely to lie between the predictions of models in which institutions maximize their owners' welfare and biological models in which organizational characteristics are ...xed. The more that members have opportunities to control their organizations, the closer reality is likely to lie to the welfare-maximizing model. For example, the model presented in this paper suggests that if unions are controlled by opportunistic leaders, these leaders will pass on the leadership to similar opportunistic leaders, and these unions will displace unions with idealistic leaders. One could

consider a more complicated model in which there is some chance that an opportunistic leader is replaced by an idealistic successor, and vice-versa. In this case, there will be a mixture of opportunistic and idealistic union leaders in steady-state. The longer it takes unions with incumbency advantages to displace those that serve their members perfectly, the longer these idealistic unions will survive and the better the economic model of welfare-maximizing unions will describe union behavior.

This suggests that ...rms may be closer to the welfare-maximizing end of the spectrum than unions, since control of unions by members is likely to be weaker than control of ...rms by share-holders. There is a substantial free-rider problem for workers in controlling union management, just as there is an important free-rider problem for shareholders in controlling ...rm management. However, in many cases, ...rms will have one large shareholder with a substantial stake in ...rm governance. In contrast, no single union member has a substantial stake in reforming the union leadership. Moreover, whereas there is a large ...nancial incentive for outsiders to take over ...rms managed against shareholders' interests, there is much less incentive for outsiders to challenge existing unions for the right to represent workers.

A Appendix

The ...rst part of the appendix gives some of the proofs omitted from the main text. The second part discusses the behavior of the model outside of the steady-state.

A.1 Proofs

Proof of Proposition 1. Equations (7) and (8) can be obtained by combining equation (5) and equation (6). The derivation for the condition that guarantees an interior solution, $2A (@) B \cdot \pm (@)$, can be seen by setting the algebraic expressions for U^{\times} and p^{\times} equal to 1, the maximum value they can take, given that the maximum proportion of ...rms that can be unionized is 1 and that the di¢culties of unionization are distributed on the interval [0,1].

To see that the steady-state with U = 0 is locally unstable, consider starting out from the

steady-state of U = 0 and introducing a union of size " > 0. Assume that this union consists of the least-costly " ...rms, so that the remaining non-unionized ...rms have costs uniformly distributed on the interval ["; 1]. This assumption makes it the hardest to show instability, because the cost distribution facing the union is the highest possible. Recall from equation (50) that the budget surplus or de...cit will be given by

A (®) B" i [± (®) " + ± (0) (1 i ")] dt
$$\frac{"^2}{2}$$
 (17)

since p will be equal to ". Note that the average organizing costs faced by the union will be less than " since it will be organizing some newly created ...rms in the thin segment [0; "] and some in the thick segment at ". The growth rate of the union will therefore be greater than it would be if it spent its entire budget organizing ...rms with cost ", i.e.

$$U > \frac{A(^{(R)})B''}{''} + (^{(R)})''$$
(18)

which will be clearly positive for " small enough.

To see that the steady state with positive unionization is locally stable, consider ...rst a union in the steady state where " of the ...rms in the union revert back to non-union status. The union's organizing budget will therefore be A (®) B (U_i "). Denote by f the highest cost level ...rm in the thin segment the union could organize with such a budget, and by p^0 the lowest cost value of ...rms in the thick segment. We know that $p^0 \cdot p$, but the precise value will depend on the cost level of the " ...rms that switched from being unionized to being non-unionized. If $f > p^0$, the union will spend the remaining budget surplus organizing the thick segment of ...rms with cost p^0 ; otherwise it will organize as many ...rms in the thin segment as it can. The growth of the union will therefore be greater than or equal to the growth if it spend its entire organizing budget on ...rms with costs less than or equal to f, i.e.

$$U_{J} = \frac{P_{A(^{(R)})BU^{\alpha}[\pm (^{(R)})U^{\alpha} + \pm (0)(1_{i} U^{\alpha})]}}{2A(^{(R)})BU^{\alpha}[\pm (^{(R)})U^{\alpha} + \pm (0)(1_{i} U^{\alpha})]} + \pm (^{(R)})U^{\alpha}$$
(19)

Substituting in $U^{*}i^{"}$ for U and rearranging terms, we can see that, for " > 0, the growth will be positive (and therefore the steady-state will be stable) if

$$2A(^{(R)})B[\pm (^{(R)})(U^{(n)}) + \pm (0)(1 + U^{(n)}) > \pm^{2}(^{(R)})(U^{(n)})$$
(20)

Since U = 0 at U^{α} , the U^{α} terms in this expression cancel, and we are left with the condition

$$2A(^{(R)})B[\pm (^{(R)})''_{j} \pm (0)''] < \pm^{2}(^{(R)})''$$
(21)

Since condition (9) guarantees that 2A ($^{(R)}$) B · ± ($^{(R)}$), this condition will be satis...ed and the union will return to the steady-state.

Next, consider a union in the steady state where " of the non-union ...rms spontaneously unionize. To make it hardest to show stability, assume that these ...rms are the costliest to unionize, i.e. the h i ...rms with costs from the interval $1_i \frac{"(1_i p)}{(1_i U)}$; 1. This is the most di¢cult assumption for showing stability since we have removed the ...rms that are costliest to organize. The ...rst thing to check is whether the union will have su¢cient organizing funds left over to begin organizing the thick segment, i.e. whether or not equation (50) is positive. The budget surplus will be

$$A(^{(B)})B(U^{''} + '')_{j} [\pm (^{(B)})(U^{''} + '') + \pm (0)(1_{j} U^{''} + '')]\frac{p^{2}}{2}$$
(22)

Since $U^{\alpha} = 0$ at the steady state, the terms from equation (5) cancel, so the surplus will be greater than or equal to 0 if

A ([®]) B" ; [± ([®]) " ; ± (0) "]
$$\frac{p^2}{2}$$
 , 0 (23)

Since p is equal to $\frac{2A(\ensuremath{\$})B}{\pm(\ensuremath{\$})}$ in the steady-state, we know that this condition will hold if

$$\pm (^{(R)})^2 \ _2 A (^{(R)}) B'' [\pm (^{(R)})'' + \pm (0)'']$$
 (24)

which is exactly the same as inequality (??), and holds by the same logic.

Given that there is a budget surplus, the change in U will be given by

$$U = [\pm (^{(\mathbb{R})}) (U^{^{\times}} + ^{^{\times}}) + \pm (^{0}) (1_{i} U^{^{\times}} i^{^{\times}})] p + \frac{A(^{(\mathbb{R})})B (U^{^{\times}} + ^{^{\times}})_{i} [\pm (^{(\mathbb{R})}) (U^{^{\times}} + ^{^{\times}}) + \pm (^{0}) (1_{i} U^{^{\times}} i^{^{\times}})] \frac{p^{2}}{2}}{p} i^{^{\times}} t^{^{(\mathbb{R})}} (U^{^{\times}} + ^{^{\times}}) (25)$$

Once again, since $U^{\pi} = 0$ at the steady state, canceling out the terms from equation (5) and (6) yields

$$U = [\pm (^{\mathbb{B}})"_{i} \pm (0)")]p + \frac{A(^{\mathbb{B}})B"_{i} [\pm (^{\mathbb{B}})"_{i} \pm (0)")]\frac{p^{2}}{2}}{p} i \pm (^{\mathbb{B}})"$$
(26)

Substituting in for p and rearranging terms yields inequality (??) as the condition for U < 0. Since we have already shown that this inequality holds, the growth rate of the union will be negative and it will return to the steady-state.

Proof of Proposition 2. Suppose that the ratio $\frac{\pm(@)}{\pm(0)}$ is ...xed at (@). Then equation 7 can be rewritten as

$$U^{\mu} = \frac{2A(^{(R)}B}{(^{(R)})^{2} \pm (0) + 2A(^{(R)}B[_{(^{(R)})} + 1]};$$
(27)

Taking the derivative with respect to \pm (0) yields

$$\frac{dU^{n}}{d\pm (0)} = \frac{U^{n}}{(R)^{2} \pm (0)} \frac{U^{n}}{(R)^{2} \pm (0)} \frac{(R)^{2}}{(R)^{2} \pm (0)} \frac{(R)^{2}}{(R)} \frac{(R)^{2}}{(R)$$

Condition (9) guarantees that $2A(^{(R)}B \cdot (^{(R)}) \pm (0)$, which in turn guarantees that $\frac{dU^{*}}{d\pm(0)}$ will be less than zero.

Proof of Proposition 3. Denote by \mathbb{B}_S the level of \mathbb{B} that maximizes $\frac{2A(\mathbb{B})B}{\pm(\mathbb{B})}$. Let S represent the number of unionized ...rms in the union that extracts \mathbb{B}_S . Consider a steady-state containing only the \mathbb{B}_S union, and introduce into this steady-state a small union of size " > 0 that extracts $\mathbb{B}_n \in \mathbb{B}_S$. In order to show that \mathbb{B}_S is evolutionarily stable, we need to show that for each \mathbb{B}_n , there exists a minimum size ° such that if the size of the invading union " is less than °, then the invader will have negative growth and die o¤. To see that this will be the case, consider how the " union spends its e¤ective organizing budget of $A(\mathbb{B}_n)B$ ". With such a budget, it can a¤ord to organize the newborn ...rms up to some level $p_{"}$, determined by setting the exective organizing budget equal to the number of newborn ...rms times the proportion organized by the invading union times the average cost of unionization for ...rms with cost less than $p_{"}$:

$$A(^{(B_{n})})B'' = [\pm (^{(B_{n})})S + \pm (^{(B_{n})})'' + \pm (0)(1_{j} S_{j} '')] \frac{A(^{(B_{n})})B''}{A(^{(B_{n})})BS + A(^{(B_{n})})B''} \frac{Z_{p_{n}}}{0} c dc;$$
(29)

which yields

$$p_{"} = \frac{2[A(\mathbb{R}_{S})BS + A(\mathbb{R}_{"})B'']}{\frac{1}{2}(\mathbb{R}_{S})S + \frac{1}{2}(\mathbb{R}_{"})'' + \frac{1}{2}(0)(1|S|'')}$$
(30)

Recall from the single-union case (equations (5) and (8)) that in the steady state,

$$p_{S}^{\mu} = \frac{2A(^{(B}_{S})B}{\pm (^{B}_{S})} = \frac{2A(^{(B}_{S})BS}{\pm (^{B}_{S})S + \pm (0)(1 + S)};$$
(31)

Note that when " is close to 0, $p_{"}$ is approximately equal to p_{S}^{α} . Since in the steady state before the invasion all ...rms with di¢culty level less than p_{S}^{α} are unionized, when " is close to 0 the invading union will exhaust its budget organizing ...rms up to $p_{"}$. The growth rate of the invading union will be

$$= [\pm (\mathbb{R}_{S})S + \pm (\mathbb{R}_{"})" + \pm (0)(1_{i} S_{i} ")] \frac{A(\mathbb{R}_{"})B"}{A(\mathbb{R}_{S})BS + A(\mathbb{R}_{"})B"} p_{"i} \pm (\mathbb{R}_{"})":$$
(32)

Rearranging terms, we ...nd that the growth rate of the invading union " will be less than 0 if

$$\frac{2A(\mathbb{B}_{n})B}{\pm(\mathbb{B}_{n})} < \frac{2[A(\mathbb{B}_{S})BS + A(\mathbb{B}_{n})B'']}{\pm(\mathbb{B}_{S})S + \pm(\mathbb{B}_{n})'' + \pm(0)(1 | S | '')}$$
(33)

Since the RHS equals $p_{"}$ and $p_{"}$ can be made arbitrarily close to p_{S}^{α} by setting " small enough, we can re-write this inequality as

$$\frac{2\mathsf{A}(\mathbb{B}_{"})\mathsf{B}}{\pm(\mathbb{B}_{"})} < \frac{2\mathsf{A}(\mathbb{B}_{\mathsf{S}})\mathsf{B}}{\pm(\mathbb{B}_{\mathsf{S}})}:$$
(34)

Since the ratio $\frac{2A(@)B}{\pm(@)}$ is precisely what $@_S$ maximizes, we know that this inequality will hold and that the $@_S$ union will be evolutionarily stable.

Proof of Lemma 1. For clarity of exposition, this proof will consider the case of a steady-

state with two unions. However, the same arguments go through in the cases when there are more than two unions in the steady-state. As will be shown, however, there can be more than two unions in the steady state only if there is some value q such that there are more than two distinct levels [®] such that $\frac{2A(@)B}{\pm(@)} = q$, which will only occur under parameterizations of A ([®]) and \pm ([®]) such that $\frac{2A(@)B}{\pm(@)}$ has more than 1 critical point.

Recall that in the steady-state in which a single union has organized all …rms with di¢culty levels less than or equal to p, equation (5) stated that a union must spend its entire organizing budget organizing new …rms with di¢culty levels less than or equal to p. Adapting this condition to the case of two unions yields

$$A(^{(\text{B}_{M})}BM = [\pm (^{(\text{B}_{M})}M + \pm (^{(\text{B}_{R})}R + \pm (0) (1_{i} U)] \frac{A(^{(\text{B}_{M})}BM}{A(^{(\text{B}_{M})}BM + A(^{(\text{B}_{R})}BR \frac{p_{M}^{2}}{2})}$$
(35)

If p_M and p_R were di¤erent, then this equation would apply only to the union with the smaller p. Supposing for the moment that M had the lower p (though in practice it could be either M or R), then the union R would be able to organize all unions in the interval $[p_M; p_R]$ instead of just the fraction $\frac{A(\hat{v}_R)BR}{A(\hat{v}_M)BM+A(\hat{v}_R)BR}$ of them. However, rewriting equation (35) shows that

$$p_{M} = \frac{2[A(^{(R)}_{M})B + A(^{(R)}_{R})B]}{\frac{\pm}{(^{(R)}_{M})M + \pm}{(^{(R)}_{R})R + \pm}{(0)}{(1_{j} M_{j} R)}}$$
(36)

Inspection of equation (36) shows that p_M and p_R must be the same for both unions in the steadystate since the equation for p_R would be exactly the same. Therefore we know that in the steady state the set of ...rms being organized each period by both unions have the same di¢culty pro...le. This, in turn, is a consequence of allocating ...rms in proportion to the unions' e¤ective organizing budget.

The second condition for the steady state is that U = 0, so that the size of the union remains the same. Since the union's entire budget is exhausted in organizing newly created ...rms, in the steady state we know that, for U = 0,

$$\pm (^{(8)}_{M})M = [\pm (^{(8)}_{M})M + \pm (^{(8)}_{R})R + \pm (0)(1_{i} M_{i} R)] \frac{A(^{(8)}_{M})BM}{A(^{(8)}_{M})BM + A(^{(8)}_{R})BR} p_{M}$$
(37)

and the equivalent equation for R. This equation states that the number of member ...rms lost due to negative shocks must be exactly replaced by the number of ...rms organized during the same period. There are $[\pm (\ensuremath{\$_M})M + \pm (\ensuremath{\$_R})R + \pm (0) (1 \ensuremath{_I} M \ensuremath{_I} R)]$...rms created each period, of which the M union targets the fraction $\frac{A(\ensuremath{\$_M})BM}{A(\ensuremath{\$_R})BR}$ and from which it organizes all ...rms with di¢culty levels below p_M. Substituting equation (36) for p_M yields the steady-state condition

$$\frac{A(^{(8)}_{M})B}{\pm (^{(8)}_{})} = \frac{A(^{(8)}_{M})BM + A(^{(8)}_{R})BR}{2[\pm (^{(8)}_{M})M + \pm (^{(8)}_{R})R + \pm (0)(1_{i} M_{i} R)]};$$
(38)

By substituting equation (38) into equation (36), we can see that

$$\frac{2A(^{(\mathbb{R}_{M})}B)}{\pm (^{(\mathbb{R}_{M})})} = p_{M} = p_{R} = \frac{2A(^{(\mathbb{R}_{R})}B)}{\pm (^{(\mathbb{R}_{R})})}:$$
(39)

The algebra would have been essentially similar if there had been more than two types of union.

Proof of Proposition 4. Suppose that the steady state contains an incumbent union, $@_1$. Lemma 1 guarantees that if there are additional unions in the steady state with di¤erent @, those unions will have the same value of $p^{\alpha} = p_1^{\alpha}$. Therefore, in the steady-state, all ...rms with di¢culty level less than p_1^{α} will be unionized and all ...rms with higher di¢culty levels will not be unionized. For simplicity, the remainder of the proof focuses on the case where there is only one union in the steady state, but because the ratio $\frac{2A(@)B}{±(@)}$ is the same for all incumbent unions in a steady state, the same arguments go through when there are multiple incumbent unions.

Consider an invasion by a union that extracts \mathbb{B}_S with size S < ", where " is very close to 0. Using a similar argument to the one in Proposition 3, we can see that $p_S \ \ p_I^{\alpha}$. Therefore, the initial growth of the union will be approximately

$$S \frac{1}{4} [\pm (^{\mathbb{B}}_{1}) I + \pm (^{\mathbb{B}}_{S}) S + \pm (0) (1_{i} I_{j} S)] \frac{A (^{\mathbb{B}}_{S}) BS}{A (^{\mathbb{B}}_{1}) BI + A (^{\mathbb{B}}_{S}) BS} p_{1}^{\mu} i \pm (^{\mathbb{B}}_{S}) S:$$
(40)

To see that this growth is positive, observe that S is approximately equal to 0 and recall that in the steady state, $p_1^{\pi} = \frac{2A(\circledast_1)B}{\pm(\circledast_1)} = \frac{\mathbf{Q}_1}{\frac{2A(\circledast_1)BI}{\pm(\circledast_1)I + \pm(0)(1_1 I)}}$. This allows us to simplify this expression and write

$$\frac{S}{S} \frac{V_{A}}{p_{I}^{\alpha}} \frac{2A(^{(\mathbb{R}_{S})}B)}{p_{I}^{\alpha}} = (^{(\mathbb{R}_{S})}B)$$
(41)

which is greater than 0 since $\frac{2A(\mathbb{B}_{S})B}{\pm(\mathbb{B}_{S})} > \frac{2A(\mathbb{B}_{1})B}{\pm(\mathbb{B}_{1})}$. This means that the invading union will grow.

Proof of Proposition 6. Recall from equation (6) that in the steady state, the number of unionized ...rms that die each instant must exactly match the number of newly created forms unionized in that instant. Rearranging equation (6) yields the condition

$$\frac{2A(^{(R)}B_{\pm}(^{(R)})}{\pm(^{(R)})} = U^{^{(R)}} \pm (^{(R)})_{i} \frac{2A(^{(R)}B}{\pm(^{(R)})} [\pm(^{(R)})_{i} \pm(^{(R)})]$$
(42)

Consider a change from [®] to [®]_S. Denote by \protect{P} the dimerence in the fraction of ...rms unionized each period, i.e. $\protect{P} = \frac{2A(\ensuremath{\circledast}_S)B}{\pm(\ensuremath{\circledast}_S)}$; $\frac{2A(\ensuremath{\circledast})B}{\pm(\ensuremath{\circledast})}$, and denote by $\protect{\Phi} \pm$ the same change in $\pm(\ensuremath{\$})$, i.e. $\protect{\Phi} \pm \pm(\ensuremath{\$}_S)$; $\pm(\ensuremath{\$})$; $\frac{2A(\ensuremath{\$})B}{\pm(\ensuremath{\$})}$, and denote by $\protect{\Phi} \pm$ the same change in $\pm(\ensuremath{\$})$, i.e. $\protect{\Phi} \pm \pm \pm(\ensuremath{\$}_S)$; $\pm(\ensuremath{\$})$; $\frac{2A(\ensuremath{\$})B}{\pm(\ensuremath{\$})}$, $\protect{\Phi}$ will be greater than 0, and since $\ensuremath{\$}_S < \ensuremath{\$}$ by assumption, $\protect{\Phi} \pm$ will be less than 0.

Since the left hand side of equation (42) is higher under \mathbb{B}_S than under \mathbb{B} , U^{π} will be higher under \mathbb{B}_S than under \mathbb{B} if the right hand side is lower. The change in the right hand side between \mathbb{B}_S will be

From condition (9), we know that $\frac{2A(\ensuremath{^{\circ}B}\ensuremath{)}B}{\pm(\ensuremath{^{\circ}}\ensuremath{)}} < 1$ for all $\ensuremath{^{\circ}}\ensuremath{,}$ and since $\pm(\ensuremath{^{\circ}}\ensuremath{)}\ensuremath{,}\ \pm(0)$ for all $\ensuremath{^{\circ}}\ensuremath{,}\ we know that <math>\pm(\ensuremath{^{\circ}}\ensuremath{)}\ensuremath{,}\ \pm(0)$ $\ensuremath{,}\ = 0$. Therefore the expression for the change in the right hand side, equation (43), will be less than 0. We can therefore conclude that $U^{\mu}(\ensuremath{^{\circ}}\ensuremath{S}\ensuremath{)}\ensuremath{,}\ = 0$.

Proof of Proposition 7. All that is required to show the result is to show that $\frac{2A(v)B}{\pm(v)}$ is maximized at a point v > 0. Since v = 0 implies $^{(m)} = ^{(m)}W$, $^{-} = 0$, we know that A(v) is maximized at v = 0, and therefore in an "-neighborhood around v = 0 changes in A(v) will be second-order. What remains to be shown is that in an "-neighborhood around v = 0, $\frac{d\pm(v)}{dv} < 0$. Note that it is su¢cient to consider only v = 0 because any v < 0 yields the same $^{(m)}$ and $^{-}$ as v = 0, i.e.

 $^{\mathbb{R}} = {}^{\mathbb{R}}_{W};^{-} = 0.$

To show this, it is convenient to de...ne $\circ = \mathbb{B} + \overline{}$. Rewriting equations (15) and (16) in terms of \mathbb{B} and \circ , we have:

$$x \frac{1}{r+\pm (\circ)} i \frac{1}{r+\pm (\circledast_W)} = \frac{\circ i \circledast}{r+\pm (\circ)}$$
(44)

$$\frac{\mathbb{R}}{r + \pm(^{\circ})} = \frac{\mathbb{R}_{W}}{r + \pm(\mathbb{R}_{W})} i \frac{V}{i\frac{1}{4}} : \qquad (45)$$

We can therefore eliminate ®:

$$\frac{\circ}{r + \pm (\circ)} i \times \frac{1}{r + \pm (\circ)} i \frac{1}{r + \pm (^{\otimes})} i = (1i \times) \frac{\otimes_{W}}{r + \pm (\otimes_{W})} i \frac{v}{i\frac{1}{4}} :$$
(46)

The implicit function theorem implies that

$$\frac{d^{\circ}}{dv} = \frac{\frac{1}{3} \frac{(1 + x)}{\frac{1}{1}}}{\frac{1}{1} \frac{1}{1} \frac{x}{\frac{1}{1}}}{\frac{1}{1} \frac{1}{1} \frac{x}{1}}}{\frac{1}{1} \frac{1}{1} \frac{x}{1} \frac{\frac{1}{1} \frac{1}{1} \frac{x}{1}}{\frac{1}{1} \frac{1}{1} \frac{x}{1}}}{\frac{1}{1} \frac{1}{1} \frac{x}{1} \frac{\frac{1}{1} \frac{x}{1}}{\frac{1}{1} \frac{x}{1}}}$$
(47)

Since $\circ = \circledast_W$ when v = 0, and since \circledast_W maximizes $\frac{\circ}{r + \pm (\circ)}$, $\frac{d}{d \circ} \frac{\circ}{r + \pm (\circ)}$ 1/4 0 in a neighborhood of v = 0. Therefore,

$$\frac{d^{\circ}}{dv} \frac{1}{4} \frac{(1 + x)(r + t^{\circ})^{2}}{\frac{1}{4}ix\frac{dt^{\circ}}{d^{\circ}}} < 0:$$

Since $\frac{d^{\circ}}{dv} < 0$ and $\frac{d\pm(^{\circ})}{d^{\circ}} > 0$, we have shown that $\frac{d\pm(v)}{dv} < 0$ in a neighborhood of v = 0. Therefore, since in a small neighborhood of v = 0; $\frac{dA(v)}{dv}$ 1/4 0 but $\frac{d\pm(v)}{dv} < 0$, the value of v that maximizes $\frac{2A(v)B}{\pm(v)}$ is strictly greater than 0.

A.2 Dynamics

Outside of the steady-state, the state-space can be characterized by the number of union ...rms, U, and the di¢culty distribution of all unorganized ...rms. As discussed above, in the steady-state the distribution of non-unionized ...rms' di¢culties is simply uniform from the threshold p to 1, but in certain kinds of transitions–for example, those in which the di¢culty level below which all

...rms are unionized, p, is shrinking-the distribution can be non-uniform. To track the dynamics, then, one needs keep track not only of the transition equations for U and p, but also the transition equation for the entire di¢culty distribution. These transition equations are used in Section 3 to characterize the evolutionarily stable steady-state.

At any instant, assuming that there is no discontinuous increase in the number of ...rms, there are two di¤erent sets of ...rms that the union may chose to organize: the "thick" set of ...rms that are non-unionized and the "thin" set of ...rms that were created that instant to replace ...rms that exited due to a negative shock. The number of non-unionized ...rms is in the thick set is 1_i U and the number of ...rms in the thin segment is

$$[\pm (^{(8)}) U + \pm (0) (1 + U)] dt$$
 (48)

Facing this pro...le of non-unionized ...rms, the union will organize the easiest ...rms it can. These will be all of the ...rms in the thin segment with cost less than p and then as many ...rms in the thick segment as it can with whatever remains of its organizing budget at that moment. Note that p represents the lower bound of the "thick" set of non-unionized ...rms-it will be possible in certain transitions that there are unionized ...rms whose di¢culties are greater than p. Since the distribution of ...rms in the thin segment is uniform, the cost of organizing all ...rms in the thin segment with cost less than p will be

$$[\pm (^{(R)}) U + \pm (0) (1_{i} U)] dt \frac{p^2}{2}$$
(49)

so that the budget surplus or exective de...cit becomes

A (®) BU_i [± (®) U + ± (0) (1_i U)] dt
$$\frac{p^2}{2}$$
 (50)

If the budget has a surplus, then the growth of the union will be the number of ...rms in the thin segment with di¢culty levels less than or equal to p plus however many older ...rms the union can a¤ord to organize at marginal cost p with whatever remains of its budget, minus the number

of its member ...rms it lost due to negative shocks:

$$U = [\pm (^{(B)})U + \pm (0) (1_{i} U)]p + \frac{A(^{(B)})BU_{i} [\pm (^{(B)})U + \pm (0) (1_{i} U)]\frac{p^{2}}{2}}{p} i \pm (^{(B)})U$$
(51)

On the other hand, if the union's budget is not su⊄cient to organize all ...rms in the thin segment with costs less than or equal to p, the union will organize as many of those ...rms as it can. This will be all newly created ...rms with di⊄culty levels less than or equal to some cuto¤ level I such that the total budget exactly equals the cost of organizing the ...rms, i.e.

$$[A(^{(\text{B})}BU] dt = [\pm (^{(\text{B})}U + \pm (0) (1_{i} U)] dt \frac{l^{2}}{2}$$
(52)

This implies that

$$I = \frac{2A(^{(R)}BU}{[\pm (^{(R)})U + \pm (0)(1 + U)]}$$
(53)

The change in the number of unionized ...rms in this case will therefore be the fraction I of thin ...rms unionized, multiplied by the total number of thin ...rms, less the number of unionized ...rms that exit:

$$U = \frac{P}{2A(^{(B)})BU[\pm (^{(B)})U + \pm (0)(1_{i} U)]}_{i} \pm (^{(B)})U$$
(54)

Keeping track of changes in the distribution of the non-unionized ...rms is somewhat trickier. Suppose that the density of non-union ...rms in the thick segment at some di¢culty level c is f (c). To ...nd f-(c) for those levels c that remain non-unionized (which will be all c _ p) it will be instructive to consider the discrete case and take limits, so suppose that the density is the same over some small segment dz and small amount of time dt. Denote by $f_0(c)$ the density of ...rms in the segment dz before the time starts and $f_1(c)$ the density after the unit of time has passed. De...ne the density so that the total number of ...rms in the segment dz before the change will be $(1 \ U) f_0(c) dz$ and after the change will be $1 \ U \ U \ U dt$ $f_1(c) dz$. The number of ...rms after the change will be equal to the number of ...rms in the segment before the change plus the number of ...rms that are born with costs in the segment minus the number of ...rms in the segment that exit due to the shock:

³
1_i U_i Udt
$$f_1(c) dz = f_0(c) (1_i U) dz +$$

$$[\pm (^{(R)}) U + \pm (0) (1_{i} U)] dt dz_{i} \pm (0) (1_{i} U) f_{0} (c) dt dz$$
 (55)

The change in f will therefore be

$$f_{-}dt = [f_{1}(c) dz_{i} f_{0}(c) dz] dt$$

$$= \frac{f_{0}(c) (1_{i} U) dz + [\pm (^{((())}) U + \frac{1}{3}(0) (1_{i} U)] dt dz_{i} \pm (0) f_{0}(c) (1_{i} U) dt dz}{1_{i} U_{i} U dt} i_{i} f_{0}(c) dz (56)$$

Simplifying and taking limits yields the equation for f-:

$$f(c) = \frac{[\pm (R) U + \pm (0) (1_{i} U)]_{i} \pm (0) (1_{i} U)_{i} U f_{0} (c)}{(1_{i} U)}$$
(57)

Note that substituting in the steady-state value of U and setting f(c) and U equal to 0 yields a steady-state value for $f_0(c)$ of $\frac{1}{1_i p^{\pi}}$, which means that the distribution of costs of non-unionized ...rms in the steady-state is uniform over the range [p; 1], as expected.

We also need to keep track of changes to p, the lower bound of the support set of the thick segment. If the union has a budget surplus (i.e. equation (50) is positive), the union has organizing funds remaining after unionizing all ...rms in the thin segment with costs less than or equal to p. The change in p will therefore be equal to the number of new ...rms unionized at cost p divided by the density of ...rms at that cost level, i.e.

$$\underline{p} = \frac{A(\ensuremath{\circledast})BU_{i} \ [\pm (\ensuremath{\circledast})U + \pm (0) (1_{i} \ U)] \frac{p^{2}}{2}}{p} \frac{1}{(1_{i} \ U) f(c)}$$
(58)

On the other hand, when the union's organizing budget is not su¢cient to unionize all newly created ...rms with costs less than or equal to p, the new value of p will be the highest-cost ...rm that the

union is able to unionize, i.e.

$$p = \frac{S}{\frac{2A(^{(R)})BU}{[\pm (^{(R)})U + \pm (0)(1 + U)]}}$$
(59)

Together, the transition equations U; f-(c), and <u>p</u> completely characterize the dynamics of the system.

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