Global Yield Curve Dynamics and Interactions: A Generalized Nelson-Siegel Approach

Francis X. Diebold
University of Pennsylvania and NBER
fdiebold@sas.upenn.edu

Canlin Li University of California, Riverside canlin.li@ucr.edu

> Vivian Z. Yue New York University zy3@nyu.edu

This revision/print: March 18, 2007

<u>Abstract</u>: The popular Nelson-Siegel yield curve model is routinely fit to intra-country bond yields, facilitating extraction of latent yield factors. In this paper we move to a global context, modeling a potentially large *set* of country yield curves via a generalized Nelson-Siegel model that allows for both global and country-specific yield factors. We extract the global and country-specific factors from term structures of government bond yields for the U.S., Germany, Japan, and the U.K. The results indicate that global yield factors do indeed exist and are economically important, generally explaining significant fractions of country yield curve dynamics, with interesting differences across countries.

<u>Key Words</u>: Yield curve, term structure, interest rate, dynamic factor model, global yield, world yield

JEL Codes: G1, E4, C5

Acknowledgments: This paper is dedicated to Charles Nelson, whose brilliantly creative contributions to financial econometrics and macro-econometrics continue to inspire us. For research support we thank the National Science Foundation and the Wharton Financial Institutions Center. For kindly supplying their bond yield data we thank Michael Brennan and Yihong Xia. For helpful comments we thank the Editor and two anonymous referees, as well as Joachim Grammig, Stefan Mittnik, James Morley, Charles Nelson, Richard Startz, Chuck Whiteman, and conference / seminar participants at the Federal Reserve Bank of Atlanta Conference in Honor of Charles Nelson, the Deutsche Bundesbank Conference on Forecasting, the International Monetary Fund, the Fiftieth Anniversary Conference of the Econometric Institute at Erasmus University Rotterdam, and the McGill Finance Research Centre / Institut de

Finance Mathématique de Montréal Conference on Financial Risk Management.

1. Introduction

The yield curve is of great interest both to academics and market practitioners. Hence yield curve modeling has generated a huge literature spanning many decades, particularly as regards the term structure of government bond yields. Most of that diverse literature is nevertheless unified by the assumption that the yield curve is driven by a number of latent factors (e.g., Litterman and Scheinkman, 1991; Balduzzi, Das, Foresi and Sundaram, 1996; Bliss, 1997a, 1997b; Dai and Singleton, 2000). Moreover, in many cases the latent yield factors may be interpreted as level, slope and curvature (e.g., Andersen and Lund, 1997; Diebold and Li, 2006). The vast majority of the literature studies a single country's yield curve in isolation and relates domestic yields to domestic yield factors, and more recently, to domestic macroeconomic factors (e.g., Ang and Piazzesi, 2003; Diebold, Rudebusch and Aruoba, 2006).

Little is known, however, about whether common *global* yield factors are operative, and more generally, about the nature of dynamic cross-country bond yield interactions. One might naturally conjecture the existence of global bond yield factors, as factor structure is routinely present in financial markets, in which case understanding global yield factors is surely crucial for understanding the global bond market. Numerous questions arise. Do global yield factors indeed exist? If so, what are their dynamic properties? How do country yield factors load on the global factors, and what are the implications for cross-country yield curve interactions? How much of country yield factor variation is explained by global factors, and how much by country-specific factors, and does the split vary across countries in an interpretable way? Has the importance of global yield factors varied over time, perhaps, for example, increasing in recent years as global financial markets have become more integrated?

In this paper we begin to address such questions in the context of a powerful yet tractable yield curve modeling framework. Building on the classic work of Nelson and Siegel (1987) as dynamized by Diebold and Li (2006), we construct a hierarchical dynamic factor model for sets of country yield curves, in which country yields may depend on country factors, and country factors may depend on global factors. Using government bond yields for the U.S., Germany, Japan, and the U.K., we estimate the model and extract the global yield curve factors. We then decompose the variation in country yields and yield factors into the parts dues global and idiosyncratic components. Finally, we also explore the evolution (or lack thereof) of global yield curve dynamics in recent decades.

Our generalized Nelson-Siegel approach is related to, but distinct from, existing work that tends to focus on spreads between domestic bond yields and a "world rate" (e.g., Al Awad and Goodwin, 1998), implicit one-factor analyses based on the international CAPM (e.g., Solnik, 1974, 2004; Thomas and Wickens, 1993), multi-factor analyses of long bond spreads (e.g., Dungey, Martin and Pagan, 2000), and affine equilibrium analyses (e.g., Brennan and Xia, 2006). Instead we work in a rich environment where each country yield curve is driven by country factors, which in turn are driven both by global and country-specific factors. Hence we achieve an approximate global bond market parallel to the global real-side work of Lumsdaine and Prasad (2003), Gregory and Head (1999) and Kose, Otrok and Whiteman (2003).

We proceed as follows. In section 2 we describe our basic global bond yield modeling framework, and in section 3 we discuss our bond yield data for four countries. In section 4 we provide full-sample estimates and variance decompositions for the global yield curve model, and in section 5 we provide sub-sample results. We conclude in section 6.

2. Modeling Framework

Diebold and Li (2006), Diebold, Rudebusch and Aruoba (2006) and Diebold Piazzesi and Rudebusch (2005) show that, in a U.S. closed-economy environment, a generalized Nelson-Siegel model accurately approximates yield curve dynamics and provides good forecasts. Here we extend that framework to a multi-country environment, allowing for both global and country-specific factors.

Single-Country

The Diebold-Li factorization of the Nelson-Siegel yield curve for a single country (at a particular and arbitrary point in time) is

$$y_{i}(\tau) = l_{i} + s_{i} \left(\frac{1 - e^{-\lambda_{i}\tau}}{\lambda_{i}\tau} \right) + c_{i} \left(\frac{1 - e^{-\lambda_{i}\tau}}{\lambda_{i}\tau} - e^{-\lambda_{i}\tau} \right) + v_{i}(\tau), \qquad (1)$$

where $y_i(\tau)$ denotes the continuously-compounded zero-coupon nominal yield on a τ -month bond, l_i , s_i , c_i and λ_i are parameters, and $v_i(\tau)$ is a disturbance with standard deviation $\sigma_i(\tau)$. Following Diebold and Li, we dynamize the model by allowing the parameters to vary over time,

$$y_{it}(\tau) = l_{it} + s_{it} \left(\frac{1 - e^{-\lambda_{it}\tau}}{\lambda_{it}\tau} \right) + c_{it} \left(\frac{1 - e^{-\lambda_{it}\tau}}{\lambda_{it}\tau} - e^{-\lambda_{it}\tau} \right) + v_{it}(\tau), \qquad (2)$$

and we interpret l_{it} , s_{it} , and c_{it} as *latent factors*. In particular, as shown by Diebold and Li, they are level, slope and curvature factors, respectively, because their factor loadings are a constant, a decreasing function of τ , and a concave function of τ . (Hence the notation l, s and c.) As the yield factors vary over time, this generalized Nelson-Siegel model can generate a variety of time-varying yield curve shapes.

Henceforth we will work with a simplified version of the yield curve (3). First, we will assume constancy of the λ_{it} parameters over countries and time. Following Diebold and Li (2006), there is little loss of generality from doing so, because λ simply determines the maturity at which the curvature loading is maximized. Second, because the curvature factor is normally estimated with low precision due to missing data at very short and/or very long maturities in most of the countries used in our study, and because curvature lacks clear links to macroeconomic fundamentals as shown in Diebold, Rudebusch and Aruoba (2006), we focus on the model with level and slope factors only. Hence we write

$$y_{it}(\tau) = l_{it} + s_{it} \left(\frac{1 - e^{-\lambda \tau}}{\lambda \tau} \right) + v_{it}(\tau). \tag{3}$$

Note that (3) is effectively the measurement equation of a state space system with state vector $(l_{ii}, s_{ii})'$, as emphasized by Diebold, Rudebusch and Aruoba (2006). Effectively, the generalized Nelson-Siegel model does not need to be cast in state space form – it is *already* in state space form. Subsequently we will discuss the details of specific parameterizations of that state space form, but for now we simply note its immediate existence.

Multi-Country

We now move to an *N*-country framework. We allow global yields to be depend on global yield factors,

$$Y_{t}(\tau) = L_{t} + S_{t}\left(\frac{1-e^{-\lambda\tau}}{\lambda\tau}\right) + V_{t}(\tau), \qquad (4)$$

where the $Y_t(\tau)$ are global yields and L_t and S_t are global yield factors. We endow the global

yield factors with simple autoregressive dynamics,

$$\begin{pmatrix} L_t \\ S_t \end{pmatrix} = \begin{pmatrix} \Phi_{11} & \Phi_{12} \\ \Phi_{21} & \Phi_{22} \end{pmatrix} \begin{pmatrix} L_{t-1} \\ S_{t-1} \end{pmatrix} + \begin{pmatrix} U_t^l \\ U_t^s \end{pmatrix},$$
(5)

where the U_t^n are disturbances such that $EU_t^n U_{t'}^{n'} = (\sigma^n)^2$ if t = t' and n = n', and 0 otherwise, n = l, s.

Each country's yield curve remains characterized by (3), but we now allow the country common factors, l_{it} and s_{it} , to load on the global factors L_t and S_t , as well as country idiosyncratic factors:

$$l_{it} = \alpha_i^l + \beta_i^l L_t + \varepsilon_{it}^l \tag{6a}$$

$$s_{it} = \alpha_i^s + \beta_i^s S_t + \varepsilon_{it}^s \tag{6b}$$

where $\{\alpha_{i}^{l}, \alpha_{i}^{s}\}$ are constant terms, $\{\beta_{i}^{l}, \beta_{i}^{s}\}$ are loadings on global factors, and $\{\varepsilon_{it}^{l}, \varepsilon_{it}^{s}\}$ are country idiosyncratic factors, i=1,...,N. Because we include constant terms in (6), we assume with no loss of generality that the country idiosyncratic factors have zero mean. In addition, we make two sets of identifying assumptions. First, because the magnitudes of global factors and factor loadings are not separately identified, we assume that innovations to global factors have unit standard deviation, that is, $\sigma^{n}=1$, n=l, s.\(^{1}\) Second, to identify the signs of factors and factor loadings, we assume that the U.S. loadings on the global factors are positive; that is, we assume that $\beta_{us}^{n}>0$, n=l, s.

As with the global factors, we allow the county idiosyncratic factors to have first-order autoregressive dynamics,

¹ This follows Sargent and Sims (1977) and Stock and Watson (1989).

$$\begin{pmatrix}
\boldsymbol{\varepsilon}_{it}^{l} \\
\boldsymbol{\varepsilon}_{it}^{s}
\end{pmatrix} = \begin{pmatrix}
\boldsymbol{\varphi}_{i,11} & \boldsymbol{\varphi}_{i,12} \\
\boldsymbol{\varphi}_{i,21} & \boldsymbol{\varphi}_{i,22}
\end{pmatrix} \begin{pmatrix}
\boldsymbol{\varepsilon}_{i,t-1}^{l} \\
\boldsymbol{\varepsilon}_{i,t-1}^{s}
\end{pmatrix} + \begin{pmatrix}
\boldsymbol{u}_{it}^{l} \\
\boldsymbol{u}_{it}^{s}
\end{pmatrix},$$
(7)

where the u_{it}^n are disturbances such that $Eu_{it}^n u_{i't'}^{n'} = (\sigma_i^n)^2$ if i = i', t = t' and n = n', and 0 otherwise, n = l, s. We also assume the shocks to the global factors U_t^n and the shocks to the country-specific factors $u_{it}^{n'}$ are orthogonal: $EU_t^n u_{i,t-s}^{n'} = 0$, for all n, n', i, and s.

Many variations, extensions and specializations of this basic model are of course possible. For example, a useful specialization to facilitate tractable estimation would restrict the dynamic matrices in (5) and (7) to be diagonal. (We shall do this.) As another example, an interesting extension would include not only global factors, but also regional factors, in which case country factors could depend on regional factors, which in turn could depend on global factors. We shall not consider such extensions in this paper; instead, we now implement empirically our basic model sketched thus far.

3. Data Construction, Data Description, and Preliminary Analysis

In this section, prior to fitting the full global yield model, we discuss and describe the data. We perform several preliminary analyses that provide background, motivation and a foundation for the subsequent analysis.

Data Construction

Our data, generously supplied by Michael Brennan and Yihong Xia for 1985.09-2002.05 and extended by us to 2005.08, consist of government bond prices, coupon rates, and coupon structures, as well as issue and redemption dates, in local currency terms for the U.S., Germany, Japan, and the U.K.

We calculate zero-coupon bond yields using the unsmoothed Fama-Bliss (1987) approach.² We measure the bond yields on the second day of each month. We also apply several data filters designed to enhance data quality and focus attention on maturities with good

² Our zero-coupon bond yields are highly correlated with those obtained by Brennan and Xia (2006), who use a cubic spline and maturities of 3, 6, 12, 24, 36, 60, 84, 96, 108 and 120 months.

liquidity. First, we exclude floating rate bonds, callable bonds and bonds extended beyond the original redemption date. Second, we exclude outlying bond prices less than 50 or greater than 130 because their price premium/discounts are too high and imply thin trading, and we exclude yields that differ greatly from yields at nearby maturities. Finally, we use only bonds with maturity greater than one month and less than fifteen years, because other bonds are not actively traded. To simplify our subsequent estimation, using linear interpolation we pool the bond yields into constant maturities of 3, 6, 9, 12, 15, 18, 21, 24, 30, 36, 48, 60, 72, 84, 96, 108 and 120 months, where a month is defined as 30.4375 days.

Data Description

In Figure 1 we show the government bond yield curves across countries and time. It is apparent that each yield curve displays substantial level movements. Cross-country comparison of the yield curves, moreover, reveals clear commonality in level movements. Yield curve slopes vary less, although they do of course vary, and Figure 1 suggests that they may also display some cross-country commonality in movements.

In Table 1 we report summary statistics for bond yields at representative maturities. Japanese yields are lowest on average, typically around two or three percent. All yield curves are upward-sloping, and yield volatility decreases with maturity. In addition, all yields are highly persistent for all countries, with average first-order autocorrelation greater than 0.95; indeed Dickey-Fuller tests fail to reject unit autoregressive roots.³

Preliminary Analysis

Our ultimate goal is to estimate the global yield model (4)-(7), extract the global yield factors, and so forth. To facilitate that goal, we first conduct a preliminary estimation of the Nelson-Siegel factors separately for each country. That is, we estimate the level and slope factors, $\{l_{it}, s_{it}\}$, t = 1, ..., T and i = 1, ..., N, via a series of ordinary least squares regressions for each country, as in Diebold and Li (2006).

In Table 2 we present descriptive statistics for the estimated factors, movement in which

³ However, although the factor roots are not easily distinguished from unity using statistical tests, economic theory strongly suggests that the roots are less than one, because nominal bond yields can not go negative, but they *would* eventually go negative (with probability one) if they contained unit roots.

potentially reflect both global and country-specific influences.⁴ The mean level factor is lowest for Japan, and the mean absolute slope factor is greatest for the U.S.⁵ The comparatively steep average U.S. yield curve slope may reflect comparatively optimistic average U.S. growth expectations during our sample period. The factor autocorrelations reveal that all factors display persistent dynamics, with the level more persistent than the slope. Augmented Dickey-Fuller tests produce mixed results. As argued earlier, however, unit roots in yields are implausible, so we view the factor roots as likely close to, but less than, one.

Of central interest is the possible existence of *commonality* in country level and/or slope factor dynamics, as predicted by our global factor model. Alternatively, the *absence* of such commonality would suggest that our approach was misguided. To investigate this, in Figure 2a we plot superimposed estimated level factors for all the countries, and in Figure 2b we plot the superimposed estimated slope factors. For both sets of factors, there is clear visual evidence of commonality in factor dynamics.

Finally, as an alternative and complementary preliminary assessment of commonality of movements in country yield curves, we conduct a principal components analysis of the estimated level and slope factors. The results, reported in Table 3, suggest the existence of global factors. Specifically, the first principal component for levels explains more than ninety percent of level variation, and the first principal component for slopes explains roughly fifty percent of slope variation. We interpret this as suggesting the existence of one dominant global level factor, and one important (if not completely dominant) global slope factor. Armed with these preliminary and suggestive results, we now proceed to formal econometric estimation of our model, and extraction of the associated global factors.

⁴ In section 4 we will explicitly decompose the country factors into global and country-specific components.

⁵ It is interesting to note that the U.K. has the smallest ratio of mean to variance for both estimated factors. This is consistent with the U.K. yield data plotted in the lower right panel of Figure 1, which appears noticeably noisier than that for the other three countries. We are unsure as to whether the comparatively noisy U.K. data accurately reflect U.K. bond market conditions during our sample period, or whether they are simply of comparatively poor quality.

4. Global Model Estimation

In this section, we estimate the global yield curve factor model, exploiting its state-space structure for both parameter estimation and factor extraction.

4a. State Space Representation

The global yield curve model has a natural state-space representation. The measurement equation is:

$$\begin{pmatrix} y_{1t}(\tau_1) \\ y_{1t}(\tau_2) \\ \dots \\ y_{Nt}(\tau_J) \end{pmatrix} = A \begin{pmatrix} \alpha_1^l \\ \alpha_1^s \\ \dots \\ \alpha_N^s \end{pmatrix} + B \begin{pmatrix} L_t \\ S_t \end{pmatrix} + A \begin{pmatrix} \varepsilon_{1t}^l \\ \varepsilon_{1t}^s \\ \dots \\ \varepsilon_{Nt}^s \end{pmatrix} + \begin{pmatrix} v_{1t}(\tau_1) \\ v_{1t}(\tau_2) \\ \dots \\ v_{Nt}(\tau_J) \end{pmatrix}$$
(8)

where

$$A = \begin{pmatrix} 1 & \left(\frac{1 - e^{-\lambda \tau_1}}{\lambda \tau_1}\right) & 0 & \dots & 0 \\ 1 & \left(\frac{1 - e^{-\lambda \tau_2}}{\lambda \tau_2}\right) & 0 & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & 1 & \left(\frac{1 - e^{-\lambda \tau_J}}{\lambda \tau_J}\right) \end{pmatrix}$$
(9)

$$B = \begin{pmatrix} \beta_1^l & \beta_1^s \left(\frac{1 - e^{-\lambda \tau_1}}{\lambda \tau_1} \right) \\ \beta_1^l & \beta_1^s \left(\frac{1 - e^{-\lambda \tau_2}}{\lambda \tau_2} \right) \\ \dots & \dots \\ \beta_N^l & \beta_N^s \left(\frac{1 - e^{-\lambda \tau_J}}{\lambda \tau_J} \right) \end{pmatrix}$$

$$(10)$$

The transition equations are the union of (5) and (7).

Note that our approach fortunately does not require that we observe global yields or global yield factors. Global yields $Y_t(\tau)$ do not appear at all in the state space representation, the measurement equation of which instead relates observed *country* yields to the latent global yield factors L_t and S_t , which appear in the state vector. Once the model is estimated, L_t and S_t can be immediately extracted via the Kalman smoother. Hence we now turn to estimation.

4b. Model Estimation

Under a normality assumption for the measurement and transition shocks, Gaussian maximum likelihood estimates are readily obtained in principle via application of the Kalman filter to the model in state space form, as in the single-country framework of Diebold, Rudebusch and Aruoba (2006). In practice, however, maximum likelihood is particularly difficult to implement in multi-country environments, because of the large number of parameters to be estimated. Hence we maintain the normality assumption but take a different, Bayesian, approach, using Markov Chain Monte Carlo (MCMC) methods to perform a posterior analysis of the model, in the tradition of recent Bayesian estimation of large-scale dynamic factor models of real economic activity (e.g., Kose, Otrok and Whiteman, 2003; Bernanke, Boivin and Eliasz, 2005).

We use a convenient multi-step estimation method in the tradition of Diebold and Li (2006), but which still exploits the state space structure emphasized by Diebold, Rudebusch and Aruoba (2006). In the first step, we estimate the model (3) separately for each country to obtain the series of level and slope factors, l_{it} and s_{it} . In the second step, we estimate a dynamic latent factor model composed of the country factor decomposition equations (6), the global factor dynamics (5), and the country idiosyncratic factor dynamics (7).

Motivated by the results of single-country analyses, which indicate little cross-factor dynamic interaction, we assume that the VARs given by equations (5) and (7) have diagonal autoregressive coefficient matrices. This drastically simplifies the second-step estimation, because it implies that we can estimate the model factor-by-factor, first estimating the model relating the four country level factors to the global level factor, and then estimating the model

relating the four country slope factors to the global slope factor. For each of the two state-space models there are seventeen parameters to estimate: one autoregressive coefficient for the global factor, four intercepts, four loadings on the global factor, four autoregressive coefficients for the idiosyncratic factors, and four standard deviations for the innovations to the idiosyncratic factors.

Effectively our state space models, whether for levels or slopes, are simply statements that certain "data" Z_t (the set of country level or slope factors estimated in the first step), conditional on a set of parameters φ and a set of latent variables F_t (the global level or slope factor), have a certain normal distribution. We use MCMC methods – effectively just Gibbs sampling – to produce draws from the joint posterior distribution $p(\varphi, F|Z)$ by iterating on the conditionals $p(\varphi|F,Z)$ and $p(F|\varphi,Z)$.

Consider a generic iteration i, and consider first the problem of drawing from $p(\varphi|F^{(i-1)},Z)$. Conditional on F, the state space measurement equations (6) are simply regressions with autoregressive errors, so draws from the conditional posterior $p(\varphi|F^{(i-1)},Z)$ are readily obtained via the Chib-Greenberg (1994) algorithm.

Next consider the second part of iteration i, drawing from $p(F|\varphi^{(i)},Z)$. This is analogous to a standard signal extraction problem, except that we seek not just to know the posterior mean, $E_p(F|\varphi^{(i)},Z)$, but rather to know the entire posterior distribution. The solution is provided by the multi-move Gibbs sampling algorithm of Carter and Kohn (1994), which lets us draw entire realizations of the factor F, governed by $p(F|\varphi^{(i)},Z)$.

4c. Estimated Parameters and Factors

We present the estimation results in Table 4. Consider first the results for the country

⁶ We use *N*(0,1) priors for all intercepts, factor loadings and serial correlation coefficients, and inverse gamma priors for all variances. Given the bounded likelihood and proper priors we use, the joint posterior is well-behaved, and the empirical distribution of draws from the conditional posteriors converges to the joint marginal posterior as the number of iterations goes to infinity. We use chains of length 20,000, discarding the first 10,000 draws as a burn-in, and then using the remaining 10,000 to sample from the marginal posteriors. See the Appendix for details.

⁷ For an insightful exposition of the Carter-Kohn algorithm, and creative application to dynamic factor models, see Kim and Nelson (1999).

level factors, all of which load positively on the global level factor, which is highly serially correlated. The global level factor loadings in the country level factor equations are very precisely estimated, with posterior means much greater than posterior variances. The country-specific level factors are also generally highly persistent. Relative to the middle-of-the-road results for the U.S. and U.K., the German level loading on the global level factor is larger, and the persistence of the German-specific level factor much smaller, implying that the dynamics of the German yield level match closely those of the global level. Conversely, and again relative to the U.S. and U.K., the Japanese level loading on the global level factor is smaller, and the persistence of the Japan-specific level factor larger, implying that the Japanese yield level is comparatively divorced from the global level. The Japanese results are particularly sensible given the very low level of Japanese yields in the second half of our sample.

Now consider the results for the country slope factors. In parallel with the earlier results for the level factors, all slope factors load positively on the global slope factor, which is very highly serially correlated, albeit slightly less so than the global level factor. The country-specific slope factors are also generally highly persistent. A number of novel results are apparent as well. The German-specific slope factor effectively does not load on the global slope factor; instead, its movements appear completely idiosyncratic, just the opposite of the behavior of the German level factor. The Japanese slope results also reverse those for the Japanese level: Japanese slope loads entirely on global slope.

In Figure 3 we plot the posterior means of the global level and slope factors extracted, along with two posterior standard deviation bands. The narrow bands indicate that the factors are estimated with high precision. In Figure 4 we plot the global level and slope factors together with the earlier-discussed first principal components of country levels and country slopes. The global factors and first principal components are highly correlated, which is reassuring. It is important to note, however, that although related, the extracted global factors and first principal components are not at all identical.

The paths of the extracted global level and slope factors reflect the major developments in the global economy over the past twenty years. The temporal decline in the global level factor reflects the reduction of inflation in the industrialized countries; the correlation between our

extracted global level factor and average G-7 inflation during our sample is 0.75.8

Movements in the extracted global slope factor reflect the state of global real economic activity. In particular, the estimated global slope factor peaked in the early 1990s and early 2000s, the two recessionary episodes in our sample. The correlation between our extracted global slope factor and average G-7 GDP growth during our sample is 0.69. The correlation between our extracted global slope factor and average G-7 GDP growth during our sample is 0.69.

All told, the picture that emerges from our results is one of hierarchical linkage: Country yields load off country factors, which in turn load off global factors. This is similar, for example, to standard results in other markets such as equities, in which excess returns on country stocks are driven by country factors, which are in turn driven by global factors, leading to an "international CAPM." Moreover, this hierarchical factor structure of global asset markets mirrors that of macroeconomic fundamentals: Country real activity is typically driven by one real factor (e.g., Stock and Watson, 1989), but country factors load off global factors, consistent with an "international business cycle" (e.g., Kose, Otrok and Whiteman, 2003).

4d. Variance Decompositions

We conduct two sets of variance decompositions. First, we decompose the variation in country level and slope factors into parts driven by global yield variation and country-specific variation. Second, we directly decompose the variation in country yields as opposed to country factors, determining for any given country yield the fraction of its variance due to variation in underlying global factors, whether level or slope.

The global and country-specific factors extracted from a finite sample of data may be correlated even if they are truly uncorrelated in population. Hence we orthogonalize the extracted factors by regressing the country factor on the extracted global factor and updating the global factor loading and country-specific factor variance accordingly. Then from (6) we have:

⁸ We use inflation data from the IMF's *International Financial Statistics*.

⁹ Note that our slope factor actually tracks the negative of yield curve slope, as shown in Diebold and Li (2006), so a large value corresponds to a flat or inverted yield curve.

¹⁰ We use G-7 quarterly GDP data from the IMF's *International Financial Statistics*, and we correlate it with our extracted global slope factor, aggregated to quarterly frequency.

$$var(l_{it}) = (\beta_i^l)^2 var(L_t) + var(\varepsilon_{it}^l)$$
 (11a)

$$var(s_{it}) = (\beta_i^s)^2 var(S_t) + var(\varepsilon_{it}^s), \tag{11b}$$

for i = 1, ..., N. This splits the variation in each country factor into a part driven by the corresponding global factor and a part driven by the corresponding country-specific factor.

We present the results in Table 5, reporting the posterior median as well as the fifth and ninety-fifth posterior percentiles for each variance share. Variation in the global level factor L explains a large fraction of the variation in country level factors, for all countries, typically in the range of sixty to eighty percent. Indeed variation in L explains almost all variation in the German level factor, which is natural because, as discussed earlier, the German level factor loads heavily on L and the Germany-specific level factor is simply white noise with a small variance.

The country-factor variance decomposition results for slopes are more diverse. Variation in the global slope factor accounts for little of the variation in the U.S. slope factor, consistent with indicating independence of the U.S. business cycle. In contrast, variation in the global slope factor accounts for almost *all* of the variation in the Japanese slope factor, consistent with the earlier-discussed fact that the Japanese slope factor loads almost entirely on the global slope factor.

Now we provide variance decompositions for yields, as opposed to yield factors. We regress Nelson-Siegel fitted yields on our extracted global level and slope factors jointly as implied by equations (3) and (6), and we calculate the variance of the bond yield explained by the global level factor and global slope factor jointly in this regression. In Table 6 we present the results for four representative maturities. There are two major results. First, and strikingly, for all countries and maturities, variation in the global factor is responsible for a large share of variation in yields. The global share is never less than a third, and typically more than half (and often much more than half). Second, the global share increases with maturity for all countries

¹¹ We present explicit posterior percentiles, rather than posterior means and standard deviations as elsewhere in the paper, because the posterior distributions of the variance shares are quite highly skewed, whereas the posterior distributions elsewhere in the paper are not.

except Japan.

5. Sub-Sample Analysis

In this section we assess the evidence on the stability (or lack thereof) of the dynamics linking the four countries' yield curves. As mentioned earlier, for example, one might naturally conjecture the enhanced importance of global yield factors in recent decades, due to enhanced global bond market integration.

We split our data sample into two equal sub-samples, 1985:9-1995:8 and 1995:9-2005:8. In Table 7 we report sub-sample summary statistics for the country level and slope factors. The mean levels are lower in the second sub-sample, reflecting the global disinflation of the past twenty years. In contrast, the mean slopes vary less across the sub-samples, reflecting comparatively stable cyclical patterns in real activity.¹²

In Table 8 we report log likelihoods for the full-sample models and sub-sample models, as well as the corresponding log posterior odds. The log posterior odds value (assuming flat priors) is simply the difference between the sum of the sub-sample log likelihoods and the full-sample log likelihood. The evidence strongly suggests instability for both the country level and slope systems.

In an attempt to uncover the sources of instability, we report sub-sample estimation results in Table 9 and sub-sample variance decompositions in Table 10. The results display interesting nuances and are certainly more involved than, for example, a simple uniform increase in importance of the global factor in the second sub-sample.

Consider first the level factors. For three of the four countries, the importance of the global level factor for country yield levels increases across the sub-samples; the exception is Germany. The comparative importance of the German country-specific factor may perhaps be linked to the successful emergence of the Eurozone in the second-subsample, so that in recent years Germany loads less on the global level factor than do Japan, the U.K. and the U.S.

¹² Germany is an exception. Its mean slope is positive in the first sub-sample and negative in the second sub-sample.

The evolving role of the global slope factor is more involved. First, the importance of the global slope factor for country yield slopes decreases across the sub-samples, except for Germany. Second, Japan's slope factor has a negative loading on the global slope factor in the second sub-sample, reflecting the unique characteristics of the Japanese economy post-1995. Similarly, global slope factor variation accounts for only a very small fraction of Japanese slope factor variation in the second sub-sample.

In Table 11 we report the sub-sample variance decompositions of yields, as opposed to factors. Overall the evidence suggests that global factors play a larger and important role in the second sub-sample, but the details are again richly nuanced. Just as the global factors impact the country factors differently across the two sub-samples, so too do they impact the dynamics of yields differently. In the first sub-sample, the importance of global factors decreases with maturity for all countries except Germany, whereas in the second sub-sample the importance of global factors increases with maturity.

6. Summary and Concluding Remarks

We have extended the single-country yield curve model of Nelson-Siegel (1987) and Diebold-Li (2006) to a global setting, and we used the model to study the global factors underlying the yield curve movements of four developed countries: the U.S., Germany, Japan, and the U.K. We develop a hierarchical model in which each country's bond yields may depend on global level and slope factors, as well as country-specific level and slope factors. Using a monthly dataset of the four countries' government bond yields from 1985:9 to 2005:8, we extract global factors and country-specific factors for both the full sample and the 1985:9-1995:8 and 1995:9-2005:8 sub-samples. We find that highly-persistent global factors are indeed responsible for significant fractions of country yields, and that the nature of the relationship has changed in significant and nuanced ways from the first sub-sample to the second. We look forward to future work producing one-step estimates in an environment with many countries, richer country-factor and global-factor dynamics, interactions with macroeconomic fundamentals, and time-varying yield volatility.

Appendix: Details of MCMC Estimation

To be supplied...

References

- Al Awad, M. and Goodwin, B.K. (1998), "Dynamic Linkages among Real Interest Rates in International Capital Markets," *Journal of International Money and Finance*, 17, 881-907.
- Ang, A. and Piazzesi, M. (2003), "A No-Arbitrage Vector Autoregression of Term Structure Dynamics with Macroeconomic and Latent Variables," *Journal of Monetary Economics*, 50, 745-787.
- Andersen, T.G. and Lund, J. (1997), "Stochastic Volatility and Mean Drift in the Short Term Interest Rate Diffusion: Source of Steepness, Level and Curvature in the Yield Curve," Working Paper 214, Department of Finance, Kellogg School, Northwestern University.
- Balduzzi, P., Das, S.R., Foresi, S. and Sundaram, R. (1996), "A Simple Approach to Three-Factor Affine Term Structure Models," *Journal of Fixed Income*, 6, 43-53.
- Bernanke, B., Boivin J. and Eliasz, P. (2005), "Measuring Monetary Policy: A Factor Augmented Vector Autoregressive (FAVAR) Approach," *Quarterly Journal of Economics*, 120, 387-422.
- Bliss, R. (1997a), "Movements in the Term Structure of Interest Rates," *Economic Review*, Federal Reserve Bank of Atlanta, 82, 16-33.
- Bliss, R. (1997b), "Testing Term Structure Estimation Methods," *Advances in Futures and Options Research*, 9, 97–231.
- Brennan, M.J. and Xia, Y. (2006), "International Capital Markets and Foreign Exchange Risk," *Review of Financial Studies*, 19, 753-795.
- Carter, C.K. and Kohn, R. (1994), "On Gibbs Sampling for State Space Models," *Biometrika*, 81, 541-553.
- Chib, S. and E. Greenberg. (1994), "Bayes Inference in Regression Models with ARMA(p,q) Errors," *Journal of Econometrics*, 64, 183-206.
- Dai, Q. and Singleton, K. (2000), "Specification Analysis of Affine Term Structure Models," *Journal of Finance*, 55, 1943-1978.
- Diebold, F.X. and Li., C. (2006), "Forecasting the Term Structure of Government Bond Yields," *Journal of Econometrics*, 130, 337-364.
- Diebold, F.X., Piazzesi, M. and Rudebusch, G.D. (2005), "Modeling Bond Yields in Finance and Macroeconomics," *American Economic Review*, 95, 415-420
- Diebold, F.X., Rudebusch, G.D. and Aruoba, S.B. (2006), "The Macroeconomy and the Yield

- Curve: A Dynamic Latent Factor Approach," Journal of Econometrics, 131, 309-338.
- Dungey, M., Martin, V. and Pagan, A. (2000), "A Multivariate Latent Factor Decomposition of International Bond Spreads" *Journal of Applied Econometrics*, 15, 697-715.
- Fama, E. and Bliss, R. (1987), "The Information in Long-Maturity Forward Rates," *American Economic Review*, 77, 680-692.
- Gregory, A. and Head, A. (1999), "Common and Country-Specific Fluctuations in Productivity, Investment and the Current Account," *Journal of Monetary Economics*, 44, 1999, 423-451.
- Kim, C.-J. And Nelson, C.R. (1998), *State-Space Models with Regime-Switching: Classical and Gibbs-Sampling Approaches with Applications*. Cambridge: MIT Press.
- Kose, M.A., Otrok, C. and Whiteman C.H. (2003), "International Business Cycles: World, Region, and Country-Specific Factors," *American Economic Review*, 93, 1216-1239.
- Litterman R. And Scheinkman, J. (1991), "Common Factors Affecting Bond Returns," *Journal of Fixed Income*, 1, 49-53.
- Lumsdaine, R.L. and Prasad, E.S. (2003), "Identifying the Common Component in International Economic Fluctuations: A New Approach," *Economic Journal*, 113, 101-127.
- Nelson, C.R. and Siegel, A.F. (1987), "Parsimonious Modeling of Yield Curves," *Journal of Business*, 60, 473-489.
- Sargent, T. and Sims, C.A. (1977), "Business Cycle Modeling Without Pretending to Have Too Much A Priori Economic Theory," in C. Sims (ed.), *New Methods of Business Cycle Research*. Minneapolis: Federal Reserve Bank of Minneapolis, 45-110.
- Solnik, B. (1974), "An Equilibrium Model of the International Capital Market," *Journal of Economic Theory*, 8, 500-524
- Solnik, B. (2004), *International Investments* (Fifth Edition). New York: Addison Wesley.
- Stock, J.H. and Watson, M.W. (1989), "New Indexes of Coincident and Leading Economic Indicators," *NBER Macroeconomics Annual*, 351-393.
- Thomas, S.H. and Wickens, M.R. (1993), "An International CAPM for Bonds and Equities," *Journal of International Money and Finance*, 12, 390-412.

Table 1: Descriptive Statistics for Bond Yields

			U.S.					
Maturity (Months)	Mean	Standard Deviation	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
3	4.76	2.07	0.87	9.32	0.95	0.68	0.17	-2.45
12	5.19	2.10	1.03	9.72	0.98	0.71	0.20	-1.82
60	6.02	1.90	1.74	10.05	0.96	0.66	0.40	-2.12
120	6.73	1.59	3.35	10.83	0.91	0.46	0.32	-2.35
			German	y				
Maturity (Months)	Mean	Standard Deviation	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
3	3.38	1.61	1.98	7.98	-	-	-	-
12	5.08	2.06	1.07	9.59	0.98	0.77	0.26	-0.81
60	5.56	1.79	2.20	9.32	0.98	0.77	0.42	-0.57
120	5.57	1.17	3.18	8.42	0.96	0.52	0.17	-1.47
			Japan					
Maturity (Months)	Mean	Standard Deviation	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
3	2.14	2.55	0.01	8.35	-	-	-	-
12	2.36	2.44	0.01	8.41	0.99	0.83	0.57	-1.30
60	2.95	2.15	0.17	8.10	0.98	0.82	0.59	-1.29
120	2.79	1.62	0.16	6.56	0.83	0.59	0.42	-1.90
			U.K.					
Maturity (Months)	Mean	Standard Deviation	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
3	6.92	3.00	3.29	14.77	-	-	-	-
12	7.04	3.02	2.67	14.23	0.94	0.75	0.46	-1.15
60	7.31	2.65	2.30	13.47	0.98	0.80	0.56	-1.16
120	7.12	2.44	3.64	13.34	0.98	0.80	0.67	-1.58

Notes to table: All yield data are monthly, 1985.09-2005.08. $\hat{\rho}(\tau)$ denotes the sample autocorrelation at displacement τ , and ADF denotes the augmented Dickey-Fuller statistic with augmentation lag length selected using the Akaike information criterion. Single and double asterisks denote statistical significance at the ten and five percent levels, respectively. Because of missing data, we do not compute $\rho(\tau)$ and ADF statistics for 3-month bonds for Germany, Japan, and UK. See text for details.

Table 2: Descriptive Statistics for Estimated Country Level and Slope Factors

				U.S.				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
\hat{l}_{it}	6.87	1.72	2.89	11.34	0.94	0.59	0.48	-2.82*
\hat{s}_{it}	-2.39	1.61	-5.90	0.72	0.92	0.37	-0.13	-2.77*
				Germany				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
\hat{l}_{it}	6.20	1.58	2.57	9.39	0.97	0.68	0.42	-1.18
Ŝ _{it}	-1.63	2.10	-5.87	4.51	0.96	0.44	-0.23	-2.36
				Japan				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
\hat{l}_{it}	3.48	1.94	0.41	7.61	0.98	0.82	0.63	-1.23
Ŝ _{it}	-1.63	1.35	-4.32	1.72	0.95	0.63	0.22	-2.06
				U.K.				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
\hat{l}_{it}	7.23	2.38	2.96	12.36	0.97	0.82	0.65	-1.02
\hat{S}_{it}	-0.34	2.18	-5.65	5.56	0.90	0.36	0.02	-2.63*

Notes to table: All yield data are monthly, 1985.09-2005.08. $\hat{\rho}(\tau)$ denotes the sample autocorrelation at displacement τ , and ADF denotes the augmented Dickey-Fuller statistic with augmentation lag length selected using the Akaike information criterion. Single and double asterisks denote statistical significance at the ten and five percent levels, respectively. See text for details.

Table 3: Principal Components Analysis for Estimated Country Level and Slope Factors

Level Factors, \hat{l}_{it} , i = US, GM, JP, UK, t = 1, ..., T

	PC 1	PC 2	PC 3	PC 4
Eigenvalue	3.64	0.27	0.10	0.05
Variance Prop.	0.91	0.05	0.03	0.01
Cumulative Prop.	0.91	0.96	0.99	1.00

Slope Factors, \hat{s}_{it} , i = US, GM, JP, UK, t = 1, ..., T

	PC 1	PC 2	PC 3	PC 4
Eigenvalue	1.99	1.01	0.69	0.30
Variance Prop.	0.50	0.25	0.17	0.08
Cumulative Prop.	0.50	0.75	0.92	1.00

Notes to table: All yield data are monthly, 1985.09-2005.08. For each set of estimated country level factors and slope factors, we report the eigenvalues, variance proportions and cumulative variance proportions associated with the four principal components.

Table 4: Estimates of The Global Yield Curve Model Parameters

Global Level Factor
$$L_{t} = 0.99L_{t-1} + U_{t}^{l}$$

$$(0.01)$$
Global Slope Factor
$$S_{t} = 0.97S_{t-1} + U_{t}^{s}$$

$$(0.01)$$

Country Level Factors

$$\begin{split} l_{US,t} &= 6.77 + 0.18L_t + \varepsilon_{US,t}^l & \varepsilon_{US,t}^l = 0.89 \varepsilon_{US,t-1}^l + 0.43 v_{US,t}^l \\ & (0.29) & (0.03) & (0.02) \end{split}$$

$$l_{GM,t} &= 6.29 + 0.26L_t + \varepsilon_{GM,t}^l & \varepsilon_{GM,t}^l = 0.07 \varepsilon_{GM,t-1}^l + 0.12 v_{GM,t}^l \\ & (0.16) & (0.01) & (0.02) \end{split}$$

$$l_{JP,t} &= 3.18 + 0.11L_t + \varepsilon_{JP,t}^l & \varepsilon_{JP,t}^l = 0.98 \varepsilon_{JP,t-1}^l + 0.28 v_{JP,t}^l \\ & (0.67) & (0.02) & (0.01) & (0.01) \end{split}$$

$$l_{UK,t} &= 7.17 + 0.22L_t + \varepsilon_{UK,t}^l & \varepsilon_{UK,t}^l = 0.69 \varepsilon_{UK,t-1}^l + 0.38 v_{UK,t}^l \\ & (0.56) & (0.03) & (0.03) & (0.03) \end{split}$$

Country Slope Factors

$$\begin{split} s_{US,t} &= -2.24 + 0.09 \, S_t + \epsilon^s_{US,t} & \epsilon^s_{US,t} = 0.93 \, \epsilon^s_{US,t-1} + 0.59 \, \nu^s_{US,t} \\ & (0.53) \quad (0.04) & (0.02) \quad (0.03) \end{split}$$

$$s_{GM,t} &= -1.53 + 0.05 \, S_t + \epsilon^s_{GM,t} & \epsilon^s_{GM,t} = 0.96 \, \epsilon^s_{GM,t-1} + 0.60 \, \nu^s_{GM,t} \\ & (0.70) \quad (0.05) & (0.02) \quad (0.03) \end{split}$$

$$s_{JP,t} &= -1.69 + 0.32 \, S_t + \epsilon^s_{JP,t} & \epsilon^s_{JP,t} = 0.00 \, \epsilon^s_{JP,t-1} + 0.19 \, \nu^s_{JP,t} \\ & (0.28) \quad (0.03) & (0.09) \quad (0.03) \end{split}$$

$$s_{UK,t} &= -0.47 + 0.09 \, S_t + \epsilon^s_{UK,t} & \epsilon^s_{UK,t} = 0.89 \, \epsilon^s_{UK,t-1} + 0.94 \, \nu^s_{UK,t} \\ & (0.54) \quad (0.07) & (0.03) & (0.04) \end{split}$$

Notes to table: We report Bayesian estimates of the global yield curve model (4)-(7), obtained using the Markov chain procedure discussed in the text with monthly yields 1985.09-2005.08. We show posterior means, with posterior standard deviations in parentheses. We define $\mathbf{v}_{i,t} = \mathbf{u}_{i,t}/\sigma_i$, so that $\mathbf{u}_{i,t} = \sigma_i \mathbf{v}_{i,t}$. See text for details.

Table 5: Variance Decompositions of Country Level and Slope Factors

Level Factors

		U.S.	Germany	Japan	U.K.
	5 th Percentile	63.02	99.03	79.8	80.4
Global	Median	63.87	99.4	80.5	81.04
	95 th Percentile	64.92	99.67	81.47	81.81
	5 th Percentile	36.98	0.97	20.2	19.6
Country	Median	36.13	0.6	19.5	18.96
	95 th Percentile	35.08	0.33	18.53	18.19

Slope Factors

		U.S.	Germany	Japan	U.K.
	5 th Percentile	0.49	9.46	96.81	34.82
Global	Median	0.72	10.45	97.8	36.36
	95 th Percentile	1.02	11.39	98.84	38.08
	5 th Percentile	99.51	90.54	3.19	65.18
Country	Median	99.28	89.55	2.2	63.64
	95 th Percentile	98.98	88.61	1.16	61.92

Notes to table: For each country, we decompose country level and slope factor variation into parts coming from global factor variation and country-specific factor variation. We estimate the underlying model using monthly yield data, 1985.09-2005.08. We show posterior medians together with posterior fifth and ninety-fifth percentiles. See text for details.

Table 6: Variance Decompositions of Country Yields

U.S. Germany Japan U.K.			3-Mon	th Yields		
Median 36.78 45.32 90.29 72.1 95th Percentile 37.61 46.27 91.03 73.15 25th Percentile 63.96 55.62 10.44 28.85 Country Median 63.22 54.68 9.71 27.9 95th Percentile 62.39 53.73 8.97 26.85			U.S.	Germany	Japan	U.K.
Sth Percentile		5 th Percentile	36.04	44.38	89.56	71.15
Country Median Median Median (63.22) 54.68 (9.71) 27.9 (27.9) 12-Month Yields 12-Month Yields U.S. Germany Japan U.K. 5th Percentile 43.47 56.02 88.1 75.4 Median 44.22 56.88 88.83 76.25 95th Percentile 45.1 57.78 89.6 77.18 5th Percentile 56.53 43.98 11.9 24.6 Country Median 55.78 43.12 11.17 23.75 95th Percentile 54.9 42.22 10.4 22.82 60-Month Yields U.S. Germany Japan U.K. 5th Percentile 59.64 89.44 84.18 82.46 (Global Median 60.42 89.94 84.88 83.13 95th Percentile 61.4 90.39 85.71 83.86 Country Median 39.58 10.06 15.12 16.87 95th Percentile 40.36 10.56 15.82 17.54 (D.87) 16.14 14.29 16.14 Country Median 39.58 10.06 15.12 16.87 1	Global	Median	36.78	45.32	90.29	72.1
Country Median 95th Percentile 63.22 54.68 9.71 27.9 26.85 12-Month Yields U.S. Germany Japan Ju.K. Sth Percentile 43.47 56.02 88.1 75.4 Global Median 44.22 56.88 88.83 76.25 95th Percentile 45.1 57.78 89.6 77.18 Country Median 55.78 43.12 11.17 23.75 95th Percentile 54.9 42.22 10.4 22.82 Country Median 55.78 49.12 11.17 23.75 95th Percentile Japan U.K. U.S. Germany Go-Month Yields U.S. Germany Japan Ju.K. Global Median 60.42 89.94 84.88 83.13 95th Percentile 61.4 90.39 85.71 83.86 Global Median 39.58 10.06 15.12 16.87 95th Percentile 40.36 10.56 15.82 17.54 Negrow 16.14 16.87 95th Percentile 38.6 9.61 14.29 16.14 Country Median 39.58 10.06 15.12 16.87 95th Percentile 38.6 9.61 14.29 16.14 Sth Percentile 62.61 96.54 82.91 82.79 16.14 Global Median 63.4 96.89 83.59 83.4 95th Percentile 64.4 97.16 84.45 84.11 Sth Percentile 64.4 97.16 84.45 84.11 Sth Percentile 65.6 64.4 97.16 84.45 84.11 Sth Percentile 65.6 65.4 82.91 82.79 83.4 Sth Percentile 64.4 97.16 84.45 84.11		95 th Percentile	37.61	46.27	91.03	73.15
Percentile G2.39 S3.73 R.97 26.85		5 th Percentile	63.96	55.62	10.44	28.85
Sth Percentile 62.39 53.73 8.97 26.85	Country	Median	63.22	54.68	9.71	27.9
U.S. Germany Japan U.K.		95 th Percentile	62.39	53.73	8.97	26.85
Sth Percentile			12-Mor	th Yields		
Median			U.S.	Germany	Japan	U.K.
Sth Percentile		5 th Percentile	43.47	56.02	88.1	75.4
Sth Percentile 56.53	Global	Median	44.22	56.88	88.83	76.25
Country Median 95th Percentile 55.78 43.12 11.17 23.75 60-Month Yields 60-Month Yields U.S. Germany Japan U.K. Global 5th Percentile Median 60.42 89.94 84.88 83.13 95th Percentile 61.4 90.39 85.71 83.86 Country Median 39.58 10.06 15.82 17.54 16.87 95th Percentile 38.6 9.61 14.29 16.14 U.S. Germany Japan U.K. 120-Month Yields U.S. Germany Japan U.K. Sth Percentile 62.61 96.54 82.91 82.79 Global Median 63.4 96.89 83.59 83.4 95th Percentile 64.4 97.16 84.45 84.11 Sth Percentile 64.4 97.16 84.45 84.11 Country Median 36.6 3.11 16.41 16.61		95 th Percentile	45.1	57.78	89.6	77.18
Country Median 95th Percentile 55.78 43.12 11.17 23.75 60-Month Yields 60-Month Yields U.S. Germany Japan U.K. Global 5th Percentile Median 60.42 89.94 84.88 83.13 95th Percentile 61.4 90.39 85.71 83.86 Country Median 39.58 10.06 15.82 17.54 16.87 95th Percentile 38.6 9.61 14.29 16.14 U.S. Germany Japan U.K. 120-Month Yields U.S. Germany Japan U.K. Sth Percentile 62.61 96.54 82.91 82.79 Global Median 63.4 96.89 83.59 83.4 95th Percentile 64.4 97.16 84.45 84.11 Sth Percentile 64.4 97.16 84.45 84.11 Country Median 36.6 3.11 16.41 16.61		5 th Percentile	56 53	43 98	11 9	24.6
Sth Percentile 54.9 42.22 10.4 22.82	Country					
Sth Percentile Sp.64 Sp.44 Sp.44 Sp.46 Sp.46 Sp.44 Sp.46 Sp.46 Sp.46 Sp.46 Sp.47 Sp.	Country					
U.S. Germany Japan U.K.						
Sth Percentile 59.64 89.44 84.18 82.46 Global Median 60.42 89.94 84.88 83.13 95th Percentile 61.4 90.39 85.71 83.86 Country Median 39.58 10.06 15.12 16.87 95th Percentile 38.6 9.61 14.29 16.14			60-Mon	th Yields		
Global Median 95th Percentile 60.42 90.39 89.94 84.88 83.13 85.71 83.86 Country 5th Percentile 40.36 10.56 15.82 17.54 16.87 95th Percentile 38.6 9.61 14.29 16.14 15.12 16.87 16.87 16.14 Global Median 5th Percentile 62.61 96.54 82.91 Median 63.4 96.89 83.59 83.4 95th Percentile 64.4 97.16 84.45 84.11 82.79 83.4 84.11 Country Median 36.6 37.39 3.46 17.09 17.21 Median 36.6 3.11 16.41 16.6 16.61 16.41			U.S.	Germany	Japan	U.K.
95 th Percentile 61.4 90.39 85.71 83.86 Country 5 th Percentile 40.36 10.56 15.82 17.54 Median 39.58 10.06 15.12 16.87 95 th Percentile 38.6 9.61 14.29 16.14 120-Month Yields U.K. 5 th Percentile 62.61 96.54 82.91 82.79 Global Median 63.4 96.89 83.59 83.4 95 th Percentile 64.4 97.16 84.45 84.11 5 th Percentile 37.39 3.46 17.09 17.21 Country Median 36.6 3.11 16.41 16.6		5 th Percentile	59.64	89.44	84.18	82.46
Country Sth Percentile Median 95th Percentile 40.36 39.58 10.06 15.12 16.87 16.14 120-Month Yields U.S. Germany Japan U.K. Sth Percentile Median 63.4 96.89 83.59 83.4 95th Percentile 64.4 97.16 84.45 84.11 Sth Percentile 65.61 37.39 3.46 17.09 17.21 Median 36.6 3.11 16.41 16.6	Global	Median	60.42	89.94	84.88	83.13
Country Median 95 th Percentile 39.58 38.6 10.06 9.61 15.12 16.87 14.29 16.14 120-Month Yields U.S. Germany Japan Ju.K. Sth Percentile 62.61 96.54 82.91 82.79 Global Median 63.4 96.89 83.59 83.4 95 th Percentile 64.4 97.16 84.45 84.11 Sth Percentile 37.39 3.46 17.09 17.21 Country Median 36.6 3.11 16.41 16.6		95 th Percentile	61.4	90.39	85.71	83.86
95 th Percentile 38.6 9.61 14.29 16.14		5 th Percentile	40.36	10.56	15.82	17.54
120-Month Yields U.S. Germany Japan U.K. Sth Percentile 62.61 96.54 82.91 82.79 Global Median 63.4 96.89 83.59 83.4 95th Percentile 64.4 97.16 84.45 84.11 5th Percentile 37.39 3.46 17.09 17.21 Country Median 36.6 3.11 16.41 16.6	Country	Median	39.58	10.06	15.12	16.87
U.S. Germany Japan U.K. Sth Percentile 62.61 96.54 82.91 82.79 Global Median 63.4 96.89 83.59 83.4 95th Percentile 64.4 97.16 84.45 84.11 5th Percentile 37.39 3.46 17.09 17.21 Country Median 36.6 3.11 16.41 16.6		95 th Percentile	38.6	9.61	14.29	16.14
Sth Percentile 62.61 96.54 82.91 82.79 Global Median 63.4 96.89 83.59 83.4 95th Percentile 64.4 97.16 84.45 84.11 5th Percentile 37.39 3.46 17.09 17.21 Country Median 36.6 3.11 16.41 16.6			120-Mo	nth Yields		
Global Median 95 th Percentile 63.4 64.4 96.89 97.16 83.59 83.4 84.11 5 th Percentile 37.39 3.46 17.09 17.21 Country Median 36.6 3.11 16.41 16.6			U.S.	Germany	Japan	U.K.
95th Percentile 64.4 97.16 84.45 84.11 5th Percentile 37.39 3.46 17.09 17.21 Country Median 36.6 3.11 16.41 16.6		5 th Percentile	62.61	96.54	82.91	82.79
5 th Percentile 37.39 3.46 17.09 17.21 Country Median 36.6 3.11 16.41 16.6	Global	Median	63.4	96.89	83.59	83.4
Country Median 36.6 3.11 16.41 16.6		95 th Percentile	64.4	97.16	84.45	84.11
Country Median 36.6 3.11 16.41 16.6		5 th Percentile	37.39	3.46	17.09	17.21
	Country					
		95 th Percentile	35.6	2.84	15.55	15.89

Notes to table: For each country and four maturities, we decompose country yield variation into parts coming from global factor variation and country-specific factor variation. We estimate the underlying model using monthly yield data, 1985.09-2005.08. We show posterior medians together with posterior fifth and ninety-fifth percentiles. See text for details.

Table 7a: First Sub-sample Statistics for Estimated Country Level and Slope Factors, 1985.09-1995.08

				U.S.				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
\hat{l}_{it}	8.18	1.10	5.64	11.34	0.87	0.15	0.09	-3.22**
\hat{s}_{it}	-2.62	1.69	-2.87	0.60	0.94	0.39	-0.34	-1.98
				Germany				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
\hat{l}_{it}	7.37	0.92	5.64	9.39	0.95	-0.36	-0.27	-1.74
ŝ _{it}	1.31	1.97	-5.36	2.97	0.94	0.51	-0.03	-1.42
				Japan				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
\hat{l}_{it}	5.21	0.91	3.04	7.61	0.90	0.33	-0.30	-2.25
ŝ _{it}	-1.11	1.51	-3.89	1.72	0.93	0.48	-0.16	-0.90
				U.K.				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
\hat{l}_{it}	9.32	1.10	6.01	12.36	0.89	0.38	-0.10	-2.39
\hat{S}_{it}	-0.14	2.57	-5.65	5.56	0.91	0.41	-0.14	-2.20

Notes to table: $\hat{\rho}(\tau)$ denotes the sample autocorrelation at displacement τ , and ADF denotes the augmented Dickey-Fuller statistic with augmentation lag length selected using the Akaike information criterion. Single and double asterisks denote statistical significance at the ten and five percent levels, respectively. See text for details.

Table 7b: Second Sub-sample Statistics for Estimated Country Level and Slope Factors, 1995.09-2005.08

				U.S.				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
l_{it}	5.56	1.12	2.89	7.35	0.90	0.34	0.05	-2.31
s _{it}	-2.16	1.49	-5.90	0.72	0.90	0.32	0.16	-1.97
				Germany				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
l_{it}	5.03	1.19	2.57	7.36	0.95	0.28	-0.17	-1.28
s _{it}	-1.95	2.18	-5.87	4.51	0.96	0.29	-0.36	-1.52
				Japan				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
l_{it}	2.50	1.01	0.68	4.77	0.93	0.41	0.15	-1.92
S _{it}	-2.15	0.92	-4.32	-0.54	0.91	0.35	0.11	-1.91
				U.K.				
Factor	Mean	Std. Dev.	Minimum	Maximum	ρ̂(1)	ρ̂(12)	ρ̂(30)	ADF
l_{it}	5.17	1.16	2.96	7.84	0.93	0.44	0.00	-2.47
s_{it}	-0.54	1.49	-4.08	3.49	0.86	0.09	-0.04	-2.87*

Notes to table: $\hat{\rho}(\tau)$ denotes the sample autocorrelation at displacement τ , and ADF denotes the augmented Dickey-Fuller statistic with augmentation lag length selected using the Akaike information criterion. Single and double asterisks denote statistical significance at the ten and five percent levels, respectively. See text for details.

Table 8: Log Posterior Odds and Likelihood Ratio Tests of Structural Stability

	Level Factors		Slope Factors
		Log Likelihoods	
Full-sample: 1985:9 - 2005:8	-320.484		-878.067
Sub-sample: 1985:9 - 1995:8	-195.649		-458.981
Sub-sample: 1995:9 - 2005:8	-99.5121		-406.23
		<u>Log Posterior</u> <u>Odds</u>	
	25.323		12.856
		Likelihood Ratio Statistics	
Likelihood Ratio Statistic	50.646		25.713
p-Value	0.000		0.000

Notes to table: We show Gaussian log likelihoods, posterior odds, and likelihood ratio statistics associated with structural stability analysis of the model (4)-(7). The log posterior odds value (assuming flat priors) is simply the difference between the sum of the sub-sample log likelihoods and the full-sample log likelihood. Under the null hypothesis of structural stability, the likelihood ratio statistics are distributed as chi-squared with seventeen degrees of freedom.

Table 9a: First Sub-sample Estimates of Global Yield Curve Model Parameters, 1985.09-1995.08

Global Level Factor
$$L_{t} = 0.95L_{t-1} + U_{t}^{I}$$

$$(0.03)$$
Global Slope Factor
$$S_{t} = 0.94S_{t-1} + U_{t}^{s}$$

$$(0.03)$$

Country Level Factors

$$\begin{split} l_{US,t} &= 7.96 + 0.14L_{t} + \epsilon_{US,t}^{l} & \epsilon_{US,t}^{l} = 0.87 \epsilon_{US,t-1}^{l} + 0.42 \nu_{US,t}^{l} \\ & (0.35) \quad (0.05) & (0.04) \quad (0.03) \end{split}$$

$$l_{GM,t} &= 7.49 + 0.30L_{t} + \epsilon_{GM,t}^{l} \\ & (0.17) \quad (0.02) & (0.14) \quad (0.03) \end{split}$$

$$l_{JP,t} &= 5.05 + 0.19L_{t} + \epsilon_{JP,t}^{l} \\ & (0.42) \quad (0.04) & (0.05) \quad (0.02) \end{split}$$

$$\epsilon_{JP,t}^{l} &= 0.90 \epsilon_{JP,t-1}^{l} + 0.31 \nu_{JP,t}^{l} \\ & (0.05) \quad (0.02) \end{split}$$

$$l_{UK,t} &= 9.35 + 0.25L_{t} + \epsilon_{UK,t}^{l} \\ & (0.39) \quad (0.05) \quad (0.03) \end{split}$$

Country Slope Factors

$$\begin{split} s_{US,t} &= -2.37 + 0.18 S_t + \epsilon^s_{US,t} \\ &= 0.94 \epsilon^s_{US,t-1} + 0.53 \nu^s_{US,t} \\ &= 0.04 \epsilon^s_{US,t-1} + 0.53 \nu^s_{US,t} \\ &= 0.04 \epsilon^s_{US,t-1} + 0.04 V_{US,t} \\ &= 0.03 V_{US,t} \\ &= 0.04 \epsilon^s_{US,t-1} + 0.04 V_{US,t} \\ &= 0.03 V_{US,t-1} + 0.04 V_{US,t} \\ &= 0.04 \epsilon^s_{US,t-1} + 0.04 V_{US,t-1} \\$$

Notes to table: We report Bayesian sub-sample estimates of the global yield curve model (4)-(7), obtained using the Markov chain procedure discussed in the text. We estimate the underlying model using monthly yield data. We show posterior means, with posterior standard deviations in parentheses. We define $\mathbf{v}_{i,t} = \mathbf{u}_{i,t}/\sigma_i$, so that $\mathbf{u}_{i,t} = \sigma_i \mathbf{v}_{i,t}$. See text for details.

Table 9b: Second Sub-sample Estimates of Global Yield Curve Model Parameters, 1995.09-2005.08

Global Level Factor
$$L_{t} = 0.96L_{t-1} + U_{t}^{l}$$

$$(0.02)$$
Global Slope Factor
$$S_{t} = 0.92S_{t-1} + U_{t}^{s}$$

$$(0.04)$$

Country Level Factors

$$\begin{split} l_{US,t} &= 5.49 + 0.19L_t + \epsilon_{US,t}^l & \epsilon_{US,t}^l = 0.84\epsilon_{US,t-1}^l + 0.42\nu_{US,t}^l \\ & (0.32) \quad (0.04) & (0.05) \quad (0.03) \end{split}$$

$$l_{GM,t} &= 4.63 + 0.13L_t + \epsilon_{GM,t}^l \\ & (0.57) \quad (0.02) & (0.03) \quad (0.02) \end{split}$$

$$l_{JP,t} &= 1.39 + 0.01L_t + \epsilon_{JP,t}^l \\ & (0.54) \quad (0.03) & (0.02) \end{split}$$

$$\epsilon_{JP,t}^l &= 0.95\epsilon_{JP,t-1}^l + 0.23\nu_{JP,t}^l \\ & (0.03) \quad (0.02) \end{split}$$

$$l_{UK,t} &= 5.02 + 0.24L_t + \epsilon_{UK,t}^l \\ & (0.19) \quad (0.02) & (0.03) \end{split}$$

Country Slope Factors

$$\begin{split} s_{US,t} &= -2.18 + 0.09 \, S_t + \epsilon^s_{US,t} & \epsilon^s_{US,t} = 0.90 \, \epsilon^s_{US,t-1} + 0.64 \, v^s_{US,t} \\ & (0.58) \ \, (0.06) & (0.04) \ \, & (0.04) \ \, & (0.04) \ \end{split}$$

$$s_{GM,t} &= -1.82 + 0.11 \, S_t + \epsilon^s_{GM,t} & \epsilon^s_{GM,t} = 0.95 \, \epsilon^s_{GM,t-1} + 0.58 \, v^s_{GM,t} \\ & (0.80) \ \, (0.06) & (0.02) \ \, & (0.04) \ \end{split}$$

$$s_{JP,t} &= -1.85 - 0.03 \, S_t + \epsilon^s_{JP,t} & \epsilon^s_{JP,t} = 0.93 \, \epsilon^s_{JP,t-1} + 0.33 \, v^s_{JP,t} \\ & (0.52) \ \, (0.04) & (0.02) \ \end{split}$$

$$s_{UK,t} &= -0.77 + 0.65 \, S_t + \epsilon^s_{UK,t} & \epsilon^s_{UK,t} = 0.06 \, \epsilon^s_{UK,t-1} + 0.41 \, v^s_{UK,t} \\ & (0.37) \ \, (0.09) & (0.13) & (0.10) \ \end{split}$$

Notes to table: We report Bayesian sub-sample estimates of the global yield curve model (4)-(7), obtained using the Markov chain procedure discussed in the text. We estimate the underlying model using monthly yield data. We show posterior means, with posterior standard deviations in parentheses. We define $\mathbf{v}_{i,t} = \mathbf{u}_{i,t}/\sigma_i$, so that $\mathbf{u}_{i,t} = \sigma_i \mathbf{v}_{i,t}$. See text for details.

Table 10a: First Sub-sample Variance Decompositions of Country Level and Slope Factors, 1985:09-1995:08

Level Factors

		U.S.	Germany	Japan	U.K.
	5 th Percentile	12.06	96.36	54.83	41.43
Global	Median	13.64	97.96	57.06	43.4
	95 th Percentile	15.84	99.23	59.88	45.8
	5 th Percentile	87.94	3.64	45.17	58.57
Country	Median	86.36	2.04	42.94	56.6
	95 th Percentile	84.16	0.77	40.12	54.2

Slope Factors

		U.S.	Germany	Japan	U.K.
	5 th Percentile	21.28	5.29	61.69	93.26
Global	Median	23.64	6.68	64.36	96.51
	95 th Percentile	26.36	8.23	68.18	98.74
	5 th Percentile	78.72	94.71	38.31	6.74
Country	Median	76.36	93.32	35.64	3.49
	95 th Percentile	73.64	91.77	31.82	1.26

Notes to table: For each country, we decompose country level and slope factor variation into parts coming from global factor variation and country-specific factor variation. We estimate the underlying model using monthly yield data. We show posterior medians together with posterior fifth and ninety-fifth percentiles. See text for details.

Table 10b: Second Sub-sample Variance Decompositions of Country Level and Slope Factors, 1995:09-2005:8

Level Factors

		U.S.	Germany	Japan	U.K.
	5 th Percentile	55.00	72.57	72.56	95.34
Global	Median	57.41	74.57	74.76	97.32
	95 th Percentile	60.18	77.13	77.11	98.50
	5 th Percentile	45.00	27.43	27.44	4.66
Country	Median	42.59	25.43	25.24	2.68
	95 th Percentile	39.82	22.87	22.89	1.50

Slope Factors

		Бторе	1 detois		
		U.S.	Germany	Japan	U.K.
	5 th Percentile	12.86	32.8	0.97	87.59
Global	Median	15.52	36.25	1.98	92.90
	95 th Percentile	18.79	41.46	3.49	97.20
	5 th Percentile	87.14	67.2	99.03	12.41
Country	Median	84.48	63.75	98.02	7.10
	95 th Percentile	81.21	58.54	96.51	2.80

Notes to table: For each country, we decompose country level and slope factor variation into parts coming from global factor variation and country-specific factor variation. We estimate the underlying model using monthly yield data. We show posterior medians together with posterior fifth and ninety-fifth percentiles. See text for details.

Table 11a: First Sub-sample Variance Decompositions of Country Yields, 1985:09-1995:08

		3-Mon	th Yields		
		U.S.	Germany	Japan	U.K.
	5 th Percentile	31.14	45.55	78.12	90.53
Global	Median	33.51	47.58	80.2	92.42
	95 th Percentile	36.96	49.63	82.54	93.61
Country	5 th Percentile	68.86	54.45	21.88	9.47
	Median	66.49	52.42	19.8	7.58
	95 th Percentile	63.04	50.37	17.46	6.39
		12-Mor	nth Yields		
		U.S.	Germany	Japan	U.K.
	5 th Percentile	30.9	53.07	77.9	88.3
Global	Median	33.3	55.14	79.98	90.05
	95 th Percentile	36.66	57.14	82.26	91.39
	5 th Percentile	69.1	46.93	22.1	11.7
Country	Median	66.7	44.86	20.02	9.95
-	95 th Percentile	63.34	42.86	17.74	8.61
		60-Mor	nth Yields		
		U.S.	Germany	Japan	U.K.
	5 th Percentile	25.21	81.45	73.2	73.82
Global	Median	27.73	83.29	75.28	75.71
	95 th Percentile	30.65	84.67	77.53	78
Country	5 th Percentile	74.79	18.55	26.8	26.18
	Median	72.27	16.71	24.72	24.29
	95 th Percentile	69.35	15.33	22.47	22
		120-Mo	nth Yields		
		U.S.	Germany	Japan	U.K.
Global	5 th Percentile	21.4	91.53	68.87	63.83
	Median	23.71	93.12	70.97	65.82
	95 th Percentile	26.29	94.21	73.28	68.41
	5 th Percentile	78.6	8.47	31.13	36.17
Country	Median	76.29	6.88	29.03	34.18
•	95 th Percentile	73.71	5.79	26.72	31.59

Notes to table: For each country and four maturities, we decompose country yield variation into parts coming from global factor variation and country-specific factor variation. We estimate the underlying model using monthly yield data. We show posterior medians together with posterior fifth and ninety-fifth percentiles. See text for details.

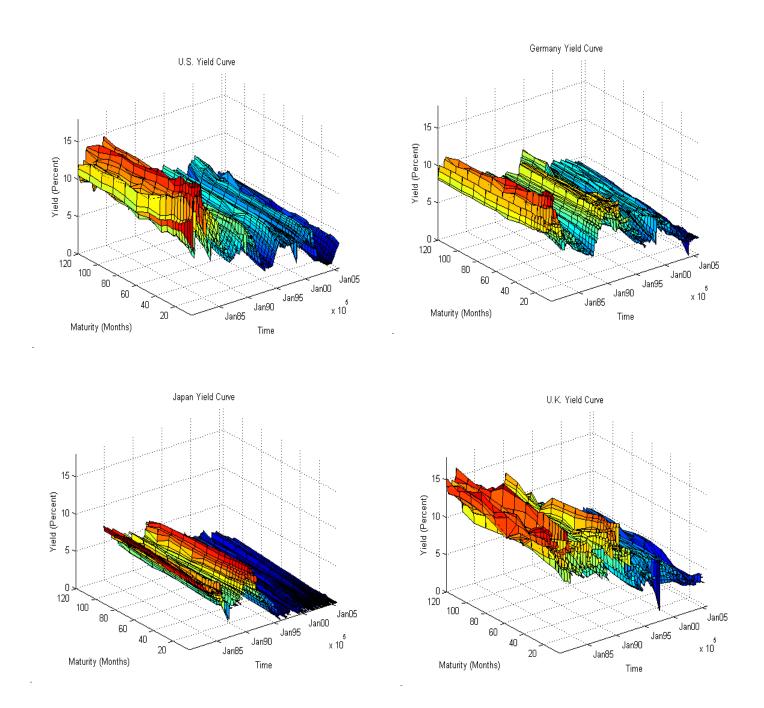
Table 11b: Second Sub-sample Variance Decompositions of Country Yields, 1995:09-2005:08

3-Month Yields

		U.S.	Germany	Japan	U.K.
	5 th Percentile	68.82	46.92	6.5	90.05
Global	Median	72.02	50.94	8.36	94.03
	95 th Percentile	75.39	56.99	11.14	97.16
	5 th Percentile	31.18	53.08	93.5	9.95
Country	Median	27.98	49.06	91.64	5.97
	95 th Percentile	24.61	43.01	88.86	2.84
		12-Mor	nth Yields		
		U.S.	Germany	Japan	U.K.
	5 th Percentile	71.64	54.63	53.45	91.72
Global	Median	74.77	58.9	56.27	94.87
	95 th Percentile	77.98	64.51	59	97.24
	5 th Percentile	28.36	45.37	46.55	8.28
Country	Median	25.23	41.1	43.73	5.13
Country	95 th Percentile	22.02	35.49	41	2.76
		60-Mor	nth Yields		
		U.S.	Germany	Japan	U.K.
	5 th Percentile	73.54	83.44	77.81	95.77
Global	Median	76.55	85.64	80.16	97.32
	95 th Percentile	79.51	87.62	82.22	98.25
	5 th Percentile	26.46	16.56	22.19	4.23
Country	Median	23.45	14.36	19.84	2.68
	95 th Percentile	20.49	12.38	17.78	1.75
		120-Mo	nth Yields		
		U.S.	Germany	Japan	U.K.
Global	5 th Percentile	70.73	79.9	78.01	95.89
	Median	73.68	82.16	80.32	97.58
	95 th Percentile	76.6	84.27	82.39	98.61
	5 th Percentile	29.27	20.1	21.99	4.11
Country	Median	26.32	17.84	19.68	2.42
	95 th Percentile	23.4	15.73	17.61	1.39

Notes to table: For each country and four maturities, we decompose country yield variation into parts coming from global factor variation and country-specific factor variation. We estimate the underlying model using monthly yield data. We show posterior medians together with posterior fifth and ninety-fifth percentiles. See text for details.

Figure 1 Yield Curves Across Countries and Time



Notes to figure: All yield data are monthly, 1985.09 through 2005.08.

Figure 2a
Estimated Country Level Factors

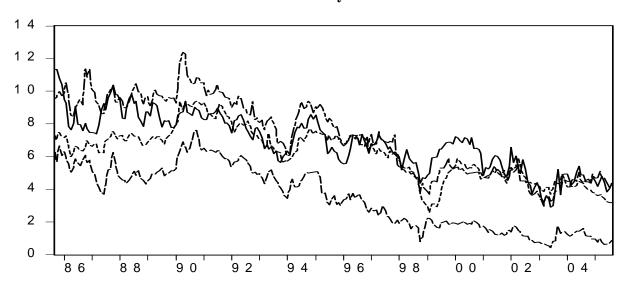
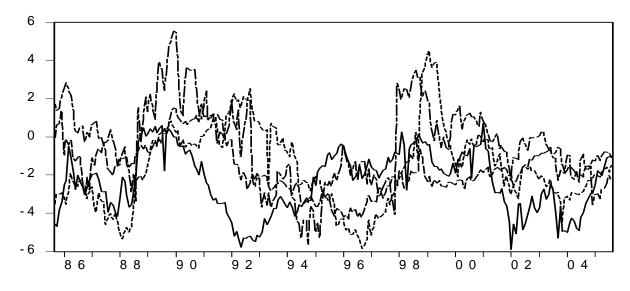


Figure 2b: Estimated Country Slope Factors



Notes to figure: We show estimates of the country level and slope factors, obtained via step one of the Diebold-Li (2006) two-step procedure, for each of four countries. Panel a shows levels, and panel b shows slopes. See text for details.

Figure 3a
Extracted Global Level Factor
Posterior Mean and Two Posterior Standard Deviation Band

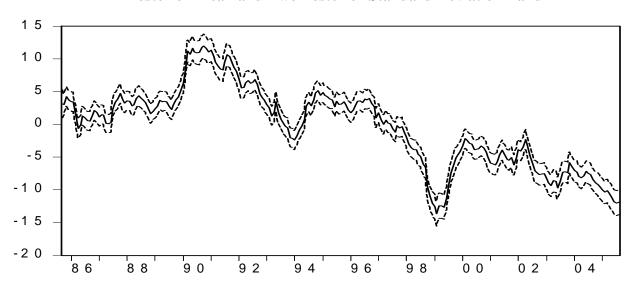
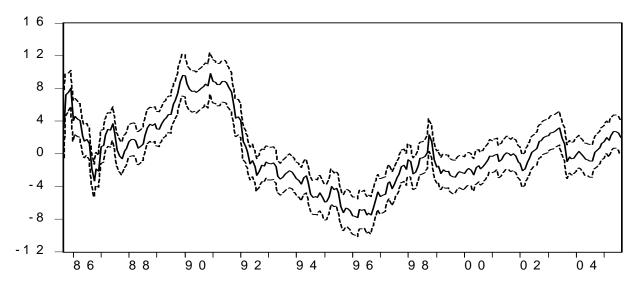


Figure 3b
Extracted Global Slope Factor
Posterior Mean and Two Posterior Standard Deviation Band



Notes to figure: We obtain posterior draws for the time series of global level and slope factors via the Carter-Kohn (1994) algorithm, and we plot the posterior mean and two standard deviation band.

Figure 4a
Posterior Mean of Global Level Factor vs. First Principal Component of Country Yield Levels

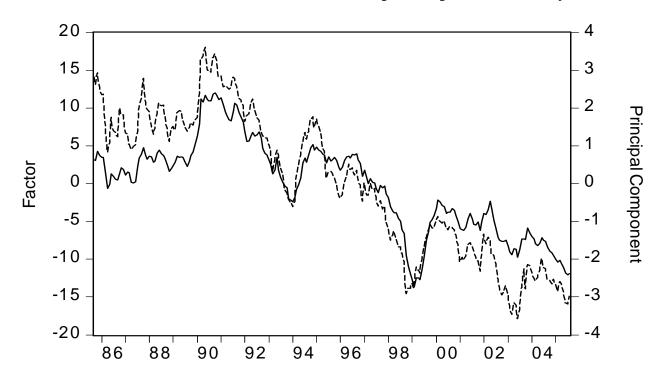
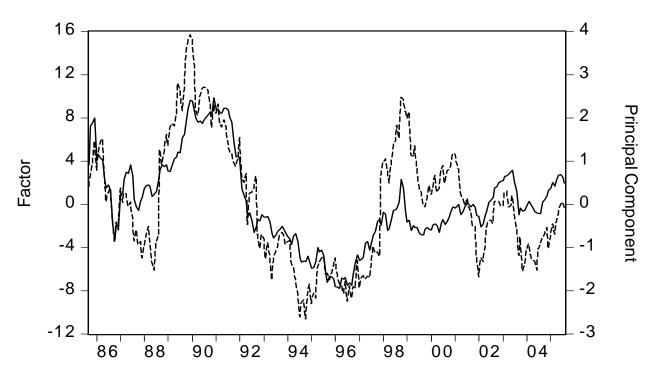


Figure 4b
Posterior Mean of Global Slope Factor vs. First Principal Component of Country Yield Slopes



Notes to figure: We show the posterior mean as a solid line and the first principal component as a dashed line.